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Microstructural study of the deformation zones during cone penetration in silt at variable penetration rates

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Abstract

During conventional cone penetration testing in silt, the soil will normally be partially drained. If the penetration rate varies, time for drainage is altered and therefore the measured cone resistance and pore pressure will change. This paper studies the change in soil microstructure around the probe during cone penetration carried out at different penetration rates to investigate the failure mechanism and the processes controlling drainage in silt. Backscattered electron images of polished thin sections prepared from frozen samples at the end of penetration were used. Making use of advanced image processing techniques, the statistical distribution of particle orientations and the local porosity were investigated for the zones around the cone tip and the shaft. The spatial distribution of the measured microscale parameters in the region near the probe indicates that the soil deformation during CPTU in silt leads to the formation of both contractive and dilative zones. The macro response of the material, presented by the pore pressure and the cone penetration resistance measured during the test, results from the competition between these zones during penetration, which is shown to be dependent on the penetration rate.

Keywords: Silts; Site investigation; Fabric/structure of soils; Microscopy; Cone penetration test

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INTRODUCTION

The cone penetration test (CPT) consists on pushing a cone tip at the end of a cylindrical probe of 35.7 mm diameter (standard size) into the ground at a rate of 20 mm/s while measuring the cone tip resistance \( q_c \) and shaft friction \( f_s \). If in addition the pore water pressure is measured behind the cone shoulder, the test is called CPTU. Key uses of the CPT test include identifying soil layering and determining geotechnical parameters for engineering design. Two extreme modes of behaviour are considered for interpretations of measurements obtained from CPT or CPTU. Drained behaviour is considered for sands and undrained behaviour for clay. When an intermediate soil like silt is tested with CPTU, partially drained behaviour may occur (Lunne et al. 1997).

The partial drainage behaviour of silt during CPTU is further investigated in this paper by studying the failure mechanism around the cone, focusing in particular, to the change in the microstructure (or fabric) of the soil surrounding the probe during penetration at different rates.

Silt response to variable cone penetration rate

Previous studies have shown that drainage during CPTU in silt can be studied by varying the penetration rate, coefficient of consolidation or cone diameter (Randolph and Hope 2004, Chung et al. 2006, Yafrate and DeJong 2007, Schneider et al. 2008, Kim et al. 2008, Jaeger et al. 2010, DeJong and Randolph 2012, Poulsen et al. 2013, DeJong et al. 2013). Laboratory CPTU tests performed on saturated specimens of silt showed two distinct trends of either dilative or contractive behaviour. In the case of dilative
behaviour, an increase in cone resistance and a decrease in pore pressure are observed when penetration rate increases (Silva, 2005; Schneider, et al. 2007; Te Kamp, 1982) and in some cases, negative pore water pressure may occur. Different behaviour was observed in the case of intermediate soils showing contractive behaviour (DeJong and Randolph, 2012). Recent tests performed by the authors confirm that the dilative response dominates for high density and the contractive response dominates for low density, both cases at large strains. For a medium dense silt, increasing the penetration rate from very slow penetration (drained behaviour), was found to result in a reduction of resistance to penetration. However, as the rate increases towards very fast penetration (approaching undrained conditions) the resistance was seen to increase again.

**Cone penetration at the microscale**

Investigation into the deformation around a penetrating object mainly in sand and clay soil has been object for a number of previous studies (Robinsky and Morrison 1964, Muromachi, 1974; Roy et al., 1974; Yasafuku and Hyde, 1995; Broere, 2001; White et al., 2003; Liu, 2010). However, studies focusing on the microscale mechanics during cone penetration are scarce and in most cases limited to numerical analysis using the Discrete Element Method (DEM). For example, Jiang et al. (2008) suggested that the failure mechanisms taking place during cone penetration were derived from a combination of four motions of the grains from the cone. Similar studies using DEM have also been presented by Kilonch and O’Sullivan (2007) and Butlanska et al. (2014).
Experimental work on silt using image-base analysis

Image-based experimental approach to investigate silt behaviour during CPT laboratory test are presented in Paniagua et al. (2012); this includes 1) freezing the sample after cone penetration to preserve deformation patterns for subsequent imaging and 2) using x-ray computed tomography (micro-CT) as penetration takes place. Paniagua et al. (2013) carried out laboratory scale CPTs on Vassfjellet silt combining micro CT and 3D Digital Image Correlation (3D-DIC) to investigate failure mechanics during penetration. The failure pattern observed in this study showed a contracting zone under the tip with a dilating zone further down and outwards. Distinct zones of shear were identified along the shaft with dilation occurring along the cone face. The results suggested that the interaction between the contractive and the dilative zones was likely to influence the pore pressure distribution; i.e., in the case of a saturated soil, water is likely to move locally from a contractive zone to a near dilative zone, creating a short drainage path. Previous work carried out by the authors, on thin sections from zones surrounding the probe following CPTU penetration on the same silt, suggested that the response of the material during cone penetration results from a competition between contraction and dilation phenomena and the extension of the influenced volume is dependent on the initial stresses surrounding the penetrating probe (Paniagua et al., 2014).

The present work explores further these previous studies to improve our understanding of the microscale phenomena underlying the observed macro scale response of CPTU tests in silt. In particular, the drainage condition surrounding the
probe are investigated by examining the interaction between the contractive and dilative zones near the cone during penetration at different rates.

SOIL DESCRIPTION AND CPTU TESTS

Typical silt behaviour and the Vassfjellet silt

The silt investigated in this study is a non-plastic uniform silt from Vassfjellet, Klæbu, Norway. Fig. 1a shows a backscattered electron image from an electron probe microanalysis (EPMA) scan of a reconstituted specimen of Vassfjellet silt. Vassfjellet silt is a medium to fine silt, it has a clay content of 2.5% and 94% of the grains have sizes lower than 74 μm (Fig.1b).

A maximum dry density (ρd-max) of 1.6 g/cm³ was found in a Proctor compaction test at 23% optimum water content and 95% saturation. A minimum dry density was measured by allowing a slurry to settle in a graduated cylinder (method by Bradshaw and Baxter, 2007). Mineralogy x-ray diffraction (XRD) analysis has indicated a composition of: 35% muscovite, 27% quartz, 18% chlorite, 15% feldspar and 5% actinolite. High dilatant behaviour was observed in saturated samples of this material tested in undrained triaxial tests (B-value of approximately 0.95) at its maximum density (Kim, 2012). A friction angle φ' of 32° and an effective cohesion estimated to 4 kPa are also reported by Kim (2012).

Typical failure mechanisms from undrained triaxial tests presented by Ovando-Shelley (1986) and also observed for Vassfjellet silt (Paniagua, 2014), show that silt can exhibit
both contractive and dilative behaviour. A dilative failure mechanism, characterised by a tendency of volume increase, causes a reduction in the pore pressure (towards suction) in a saturated sample; while a contractive failure mechanism, characterised by a reduction in volume, leads to an increase in the pore pressure. The resulting stress paths show that the loose and medium dense silts contract initially before showing dilatant behaviour, while for dense specimens the initial contraction is less obvious (Fig. 1c).

**CPTU at model scale**

Three specimens were prepared by the slurry consolidation method (adapted from Kuerbis and Vaid 1988). The slurry was prepared with 45% water content and consolidated under a top loading of 65 kPa for 12 hours. The load was applied using a load-controlled jack that pushes a movable porous plate on top of the slurry sample (Fig. 2). The porous plate and a filter paper allowed drainage from the top part of the sample. The specimens were built inside a Plexiglas cylinder of 100 mm diameter and 200 mm height padded with two layers of neoprene padding of 6 mm thickness (Fig. 2). The paddings were used to compensate for the effect of the boundary closeness and account for the compressibility of the lacking surrounding soil. The soil cylinder had a diameter of 88 mm and a height of 180 mm. The specimens exhibited water content and density variations with depth inherently related to the sample preparation method. Lower water content and higher density were measured at the top of the specimen, as water content increases and density decreases with depth. After preparation, the samples were preloaded with 80 kPa and this load was kept during
cone penetration. The test was stopped at a penetration depth of 60 mm. Measurements of dry density at the top and bottom of similar specimens indicated a $\rho_d$ of 1.46 g/cm³ and a corresponding experimental void ratio of 6.5 at 60 mm depth (Fig. 2).

The penetrating probe had a diameter of 12 mm and an apex angle at the tip of 60°. The penetration force was measured in all tests at the end of the shaft, therefore, it combines cone penetration resistance and shaft friction measurements. A pore pressure ceramic filter was located at the position $u_2$ (behind the cone tip) and the pore pressure sensor was located at the end of the shaft. The pore pressure filter and sensor were saturated under vacuum and the chamber connecting them was filled with de-aired glycerine before penetration. The samples were penetrated at three different rates: 0.06 mm/s (slow), 6 mm/s (medium) and 50 mm/s (fast). The penetration rates were chosen according to the recommendations of DeJong and Randolph (2012) with the aim of obtaining a combination of drained and undrained conditions.

**IMAGE ACQUISITION**

*Thin sections*

After probe penetration, the samples were rapidly frozen with the cone inside the sample, following the technique proposed by Paniagua et al. (2012). This set-up permitted the cylindrical Plexiglas container and the cone to be subsequently removed and the frozen sample to be cut through its centre. After sample cutting, the frozen blocks were carefully oven dried based on author’s previous experience on drying
techniques. Subsequent resin impregnation was carried out both on carefully carved smaller pieces and directly in the areas around the cone and the shaft (Gylland et al. 2013). A low viscosity epoxy resin was used to avoid disturbance of the soil microstructure. Resin impregnation of soil for fabric inspection was successfully used in previous studies, e.g. Fonseca et al. (2012). Thin sections of 36x22 mm and 30 μm thick, were prepared to study the deformation zones around the cone and shaft. The thin sections were extracted from the zones around the cone tip following 60 mm penetration into a soil specimen 180 mm high. For the subsequent analysis it is assumed that the silt, in this part of the sample, has initially a medium density.

**Electron Probe Microscopy**

The thin sections were first inspected using a polarized light microscope (Nesse, 2011) in order to define specific areas of interest for detailed analysis using backscattered electron images (obtained from Electron Probe Micro Analyser, EPMA, JEOL JXA-8500F). Figure 3 shows the location of the thin sections in the specimens. SDCP stands for Slurry Deposition Cone Penetration. The symbol # seen in Figure 3, was replaced for each test by: S for slow penetration test (i.e. 0.06 mm/s or SDCP-S), M for medium penetration test (6 mm/s or SDCP-M) and F for fast penetration tests (50 mm/s or SDCP-F). The angle α refers to the angle relative to a reference plane (shown as a thicker line) for measuring the particle orientations in the angular histograms. The numbered dots indicate the locations where EPMA images were taken. Those locations were selected based on previously identified deformation zones observed by Paniagua et al. (2013). Each image is defined by 1790x2560 pixels with a pixel size of 0.4 μm.
(image resolution). The high spatial resolution, as well as the good image quality, have allowed a clear identification of the grains and pore spaces. The image processing techniques used in this study are described in the following sections.

**POROSITY ANALYSIS**

**Methodology**

Porosity analysis from an image requires the identification of the voids or pore space, representing air or water, and the solid particles. Binarisation by thresholding is a commonly used technique to separate the solid from the pore space. It consists of defining a threshold value from the bi-modal intensity distribution histogram of the image. The result is a binary image where pixels belonging to the particles are attributed the value 1 and pixels in the pore space are given the value 0. The threshold value that minimizes the intra-class variance between the two classes or peaks, as proposed by Otsu (1979), was used (algorithm implemented in ImageJ 1.48g, Rasband 2013). Measuring the void ratio value from a binary image consists of calculating the ratio between the number of pixels corresponding to pore space and the number of pixels associated with grains in the plane of the thin section. The 2D image-based void ratio values were calculated for the locations presented in Figure 3. Localised artefacts due to irregularities in the specimen surface and grain plucking resulting from thin section preparation were avoided in the selected locations. Comparison between the image-based and laboratory-measured void ratio of 0.65 should be done with some reservation as the latter one is a global value that does not account for local variations within the sample. Also to note are the limitations of using a 2D analysis to measure a
parameters that should consider the three dimensionality of the samples. While the difference between 2D and 3D void ratio measurements have not been established for silts, this is not likely to affect the comparative analysis for the three tests, presented here.

Void ratio contour plots
Figure 4 provides the void ratio distribution presented as contour plots obtained by cubic interpolation of the measured values. The contours show an increase of the void ratio values from the tip of the cone to outwards areas for the slow penetration rate test, while for the fast penetration rate test an inverse trend is observed. Also, there is no clear continuity between the values obtained for the cone and the shaft which indicates the influence of the cone shoulder geometry. The failure zones observed by Paniagua et al. (2013) are shown for comparison in the test with medium penetration rate. This comparison between the void ratio contour plots and the failure zones from Paniagua et al. (2013) can be done, noting that the results obtained in this work are cumulative values (i.e. they are taken at the end of penetration) and the ones from Paniagua et al. (2013) come from an incremental analysis. Besides, a cumulative analysis of the incremental volumetric strains has shown identical results to the incremental observations (Paniagua et al., 2013).

The lower void ratio values observed near the cone face for the slow penetration rate test indicate that dilation along the shaft is less likely to develop at this rate. The high void ratio values attained for the fast rate test is an indication that the dilation zone tends to expand as the rate of penetration increases. For the medium penetration rate,
there is more variation in the porosity values along the cone face. These observations suggest that the rate of penetration is responsible for the mobilisation of either a contractive or dilative response near the tip of the cone with a consequent effect on the cone resistance. In other words, for slow rate, contraction dominates the failure process while for fast rate, dilation dominates. At an intermediate rate, the results indicate the effect of partial drainage.

**Void ratio against distance to cone**

Potential patterns in the variation of void ratio around the cone were investigated. Figure 5 shows the void ratio values for the different locations of the three tests as a function of a normalized distance of \(d/r_c\) and \(x/r_c\) for the cone and shaft regions respectively. In these plots, \(r_c\) is the shaft radius, \(d\) is measured from the cone face, \(x\) is the horizontal distance from the line of symmetry of the probe. For the slow penetration tests, low void ratio values are observed near the cone and they tend to increase as \(d/r_c\) increases. A different pattern can be seen for the test performed at fast penetration rate, i.e. high void ratio values are measured near the cone and they decrease for farther regions. The rate of penetration also influences the porosity along the shaft-shoulder region. Although no clear trend can be found for the void ratio distribution along \(x/r_c\), faster penetration can be seen to lead to higher void ratio values along the shaft and lower near the shoulder.

**Drainage patterns**
The void ratio distribution can be linked to the drainage pattern. At slow penetration rates, drained behaviour is expected (Randolph and Hope 2004) which agrees with a low porosity zone (i.e. contraction dominated) in Figures 5 and 6, as this rate allows the water to drain (i.e. drained contraction). For the medium rate of penetration, the void ratio distribution relates to the partially drained behaviour resulting from contractive and dilative regions. The fast rate of penetration prevents the water from draining and a dilative zone (with high porosity values) is formed, also confirmed by finite element simulations carried out by the authors. The high void ratios observed near the cone face are likely to contribute to the development of negative pore pressures when penetration occurs at fast rates, also observed by Silva (2005). Figure 6 shows schematic diagrams of the void ratio variation around the probe where the arrows represent the potential drainage paths, assuming that the water will travel from the low porosity to the high porosity regions. During slow penetration there will be a side/upward drainage from the cone tip (Figure 6a). While for the fast penetration rate, the drainage paths are essentially upward towards the cone tip (Figure 6c). Again, for the medium penetration rate (Figure 6b) the drainage shows a more complex pattern of paths given the porosity variation along the cone face.

PARTICLE ORIENTATION ANALYSIS

Methodology

While for the porosity analysis the grains are treated as part of a single solid phase, the investigation into the orientation of the grains requires the identification of the individual grains within it, i.e. segmenting the image. This task involves more
sophisticated image processing techniques when compared to thresholding described previously. Watershed techniques have been used for siliceous sands with relatively rounded and convex grains (e.g. Fonseca et al. 2013a). In the case of a silt, the diversity of particle shape ranging from almost spherical to needle-like grains and the wide range of grain sizes, makes the segmentation process more complex. Paniagua et al. (2014) and Fonseca et al. (2013c) describe the use of manual techniques to quantify the characteristics of individual grains for the case of lower quality images where the edges of the grains are difficult to identify and an automated process is not viable. In the present study, the high quality of the EPMA images has enabled the development of an automated process to segment the images. In order to facilitate the image processing, grains defined by less than 30 pixels (approximately diameter of 2 µm) are removed and assumed that their orientation is not relevant for this analysis. Note that this corresponds to the clay fraction and represents less than 2.5% of the total grains. In addition, the different mineralogical composition of the grains originates very distinct intensity values representing the solid phase in the images. The process of segmentation, consisted of 1) filtering the solid phase with similar intensity values and 2) applying a series of morphological operations consisting of eroding and dilating the edges of the grains in order to associate to each grain a unique intensity value or ID. The MATLAB Image Processing Toolbox (Mathworks) was used.

The second task consisted of obtaining the orientation of the major and minor axes for each grain. This was done using the principal component analysis (PCA). PCA is applied to the cloud of points/pixels defining each individual grain given by the x,y
coordinates and ID value (details can be found in Fonseca et al. 2013a). The orientation of each grain (i.e. angle $\theta$) is given by the vector describing the orientation of particle’s major axis (Fig. 7a).

**Size and shape description**

The process used to obtain the size of the grains involved two key steps as developed by Fonseca (2011): 1) orthogonal rotation of the pixel coordinates defining each grain, so that its principal axes (obtained previously) were made parallel to the Cartesian axes and 2) subtracting the corresponding rotated coordinates to obtain the major and minor dimensions of the grain (Fig. 7a). The two principal axes lengths of each particle in $\mu$m were obtained by multiplying the length given in pixels by the size of each pixel (i.e. image resolution). The shape description of each grain was done using the aspect ratio descriptor (AR) or elongation, given by the ratio between the lengths of the minor and the major axes in each grain (e.g., $\text{AR}_{\text{sphere}} = 1$). The statistical distribution of the AR values is presented in Figure 7b for one of the specimens (to note that no significant variation has been found between specimens) compared to a silica sand (Fonseca et al 2012). This silt exhibits AR values ranging from 0,1, i.e. needle-like grains, to approximately circular grains, i.e. $\text{AR} = 1$; while the sand shows a much narrower range of values, i.e. 0,6 - 1. The bias in the re-orientation of the more elongate flaky grains under imposed deformation has been reported in previous studies (e.g. Lupini 1981). For the orientation analysis, the grains were divided into two classes according to their AR value: i.e. bulky grains $\text{AR} > 0,50$ and flaky for $\text{AR} < 0,50$. 
Angular histograms

The statistical distribution of particle orientation was investigated using 2D angular histograms or rose diagrams. Rose diagrams provide an effective way to visualise the distribution of a given set of vectors. In these plots the vectors are “binned” into an interval of selected size and represented as a segment whose length is proportional to the number of vectors orientated within the angle defining the bin limits. The orientation of the vectors is given by the angle $\alpha$ measured relatively to the reference plane shown in Figure 3, i.e. horizontal plane for the shaft and the plane inclined 32° from the horizontal for the cone region. In the histograms, shown in Figure 8, each bin represents an angular interval for angle $\alpha$ and is shaded according to either the major axis length (in $\mu$m) or the AR to provide additional information on the link between grain characteristics and preferential orientation. Only half of the plane is considered in the rose diagrams since each particle has a defined orientation vector without a specific direction, i.e. an orientation of 60° is equivalent to an orientation of 240°. These angular plots correspond to the location SDCP-S-S1-1 and refer to all grains (Figure 8a), flaky grains (Figure 8b) and bulky grains (Figure 8c), respectively. The orientation pattern is similar in the three cases and the key aspect to note is the more explicit preferential orientation of the flaky grains when compared to a more random distribution for the bulky. It is also clear that the directional trend pattern is set by the longer and more elongated grains, depicted by the lighter shading.

Figure 9 illustrates the distribution of particle orientation at selected locations, for all grains after penetration and for the regions near the cone, starting from the top shaft to
the cone tip for the medium rate test, i.e. regions SDCP-M-S1-1, SDCP-M-S1-4, SDCP-M-C1-4, SDCP-M-C1-3, SDCP-M-C1-2, SDCP-M-C1-1. A clear vertical orientation of the grains major axes, i.e. parallel to the shaft, can be observed for the two positions in the shaft region. Similar trend can be observed for the cone region where the grains tend to re-orientate parallel to the cone face and at the tip of the cone at a perpendicular orientation to the cone movement.

**Microscale parameters**

Two parameters are used for the quantitative characterisation of the distribution of particle orientation. The first relates to the preferred orientation of the particle distribution and is called the $\beta$ value and the second parameter describes the anisotropy of the particle distribution ($A$).

**a) $\beta$ value**

This angular parameter is given by the eigenvector associated with the major eigenvalue of the fabric tensor. The fabric tensor of the vectors defining the particle orientations is denoted as follows (Satake, 1982):

$$\Phi_y = \frac{1}{N} \sum_{k=1}^{N} n_i^k n_j^k$$  \hspace{1cm} (1)

where $N$ is the total number of vectors in the system, $n_i^k$ is the unit orientation vector along direction $i$ and $n_j^k$ is the unit orientation vector along direction $j$. 
b) Anisotropy value

The anisotropy of the system is quantified by considering the difference between the major and minor eigenvalues of the fabric tensor, i.e. $\Phi_1 - \Phi_3$ (e.g. Thornton 2000, Fonseca et al. 2013a). An isotropic distribution will have an $A$ value of zero and the correspondent vectors distributed equally in all directions, while the realignment of the vectors along a preferable direction will lead to higher values of $A$. An effective way of graphically representing the degree of anisotropy is to use a Fourier series (Rothenburg and Bathurst 1989, Barreto 2008). The value of $A$ increases with the concentration of the orientation vectors towards a preferable angle. Two extreme anisotropy values are presented here. Figure 10a illustrates the case of $A = 0.06$ (near zero) with the Fourier fitting represented by the dotted lines, exhibiting a near circular shape. The case of $A = 0.53$, illustrated in Figure 10b, shows a clear preferable orientation and an associated ‘more elongated’ fitting curve. Distributions with higher anisotropy values are characterized by a predominant particle alignment which is given by the angle $\beta$. In more isotropic distributions, the particles tend to align in random directions and the angle $\beta$ becomes less meaningful.

Anisotropy against distance to cone

Figure 11 shows the variation of anisotropy with the normalized distance $d/r_c$ for the cone region and $x/r_c$ for the shaft for both flaky and bulky grains. The anisotropy values attained at the end of the test relate to the extent of realignment of the grains. However, when compared to trends observed in Fig. 5 for porosity, it can be seen that there is not always a direct correlation between void ratio and anisotropy values. The
test carried out at medium penetration rate, for SDCP-M in Fig.11a, suggests the development of three areas of distinct anisotropy for the cone region based on the rotation of the grains imposed by the cone movement. In zone 1, near to the cone, the grains realign along the direction of the cone's face: downwards and sideward at the tip. The interaction of these mechanisms leads to grains reorient in distinct directions, resulting therefore, in lower anisotropy values. For zone 2, the grains follow the cone movement but as the distance from the cone increases, a 'strong' realignment and higher anisotropy values are observed. Finally, the zone 3 is likely to be influenced by the friction end effects from the walls.

The anisotropy values do not show much dependency on the rate of penetration. The results suggest that the lower penetration rate imposes more evident reorientation (higher $A$) for zone 2. It can also be observed that the trend of the anisotropy values is the same for both flaky and bulky grains but the flaky grains have much greater values, generally twice, than the bulky grains. This can be explained by the fact that the bulky grains are less prone to rotate when compared to more flaky grains. For the shaft region, low anisotropy values are attained near the shoulder for the slow penetration rate, while for medium and fast penetration rates, higher anisotropy values are observed.

**Contour plots analysis**

The distribution of the $\beta$ values together with the anisotropy field for the three tests is presented in Figure 12. These contour diagrams provide an alternative illustration of
the observations made before. In particular, to note are the lower anisotropy values near the cone tip and higher anisotropy in the middle part of the region investigated, which results from the stronger realignment of the grains. This trend is more pronounced for the medium rate test as shown in Figure 12.

A clear reorientation of the grains towards the vertical direction along the shaft, i.e. $\beta$ close to zero can be observed for the three tests. This trend is more pronounced for the fast test, which also exhibits the lowest void ratio values. The grains near the cone also align parallel to the cone face. At the cone tip the grains rotate towards an orientation perpendicular to the cone pushing direction as a consequence of the deformation mechanism imposed by the movement of the cone. The rate of the test does not seem to affect significantly the final preferred orientation of the grains following penetration.

The extent of the region affected by the movement of the cone cannot be clearly defined. Referring to Paniagua et al. (2013) no significant strains were measured outside the regions defined by the dotted lines in Fig. 5 which would mean that locations 7 to 10 in the cone region and 3 and 6 in the shaft region might not be significantly influenced by penetration. As a result of the slurry deposition used to prepare the initial sample, a near horizontal particle orientation would be expected. The more inclined orientation deviating from the horizontal direction observed for the grains in these outer regions is believed to a result of side friction during sample preparation, also reported by Cetin (2004), what is known as the silo theory effect (Janssen, 1895).

**LINKING MICRO TO MACRO BEHAVIOUR**
The macro response obtained for the three CPTU tests carried out on Vassfjellet silt with a medium density is presented in Table 1. It can be seen that increasing the penetration rate from a slow value (drained behaviour) to a medium value leads to a reduction of the penetration resistance $T_R$; while further increase in the rate to a fast penetration value (approaching undrained conditions) is associated with an increase of the penetration resistance. Regarding the pore pressure ($u_2$), the values are seen to decrease as the penetration rate increases and negative values are measured at both medium and fast rates. The analysis of the local porosity has shown high void ratio values near the cone at fast penetration rate which supports the development of negative pore pressures due to the dilative response. For the slow penetration rate test the lower void ratio values found near the cone tip suggest drained contraction.

Table 1. Measurements of total penetration resistance ($T_R$) and pore pressure ($u_2$) for the three tests carried out a different penetration rates given by the cone velocity ($v$)

<table>
<thead>
<tr>
<th>Test</th>
<th>$v$ (mm/s)</th>
<th>$T_R$ (N)</th>
<th>$u_2$ (kPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Slow SDCP-S</td>
<td>0.06</td>
<td>200</td>
<td>2.5</td>
</tr>
<tr>
<td>Medium SDCP-M</td>
<td>6</td>
<td>190</td>
<td>-10</td>
</tr>
<tr>
<td>Fast SDCP-F</td>
<td>50</td>
<td>225</td>
<td>-40</td>
</tr>
</tbody>
</table>

As discussed previously, the anisotropy of the particle orientation is believed to be largely related to the rotation of the grains imposed by the movement of the cone and these micro scale parameters can also be linked to the dilative response of the soil. Low anisotropy values can be associated with zones of dilation as the grains tend to re-orient in random directions that create a “less organised” system with larger voids and
therefore “less contractive”. Conversely, a system with a strong predominant orientation and higher anisotropy values will be more “more contractive” (Fig. 13).

Figure 14 combines the measured observations for the medium penetration rate test, with EPMA images with the aim of providing a more scientific explanation for the formation of the dilative and compacted systems. It can be observed that the low anisotropy values close to the cone tip and high void ratio agree with the dilative zone denoted by Paniagua et al. (2013). The dilation decreases as the distance from the cone increases making the particle distributions “more organized” and “more contractive” towards the limit between the contractive and dilative zones identified in Paniagua et al. (2013). At larger distances from the cone face, the randomness in the distributions increases as well as the void ratio values. Along the shaft, the zone closer to the cone shoulder show higher anisotropy values perhaps associated with a better alignment of the grains at this location.

CONCLUSIONS

This paper shows that investigating soil fabric following CPTU tests, carried out on silt at different penetration rates, can help understanding the grain-scale mechanisms, induced by the cone penetration, that underlie the measured macroscale response. In particular, the partial drainage behaviour can be linked to the distribution of the void ratio and particle orientation in the regions surrounding the probe during penetration. The analysis of local void ratio measurements allows the identification of areas with distinct density that are, therefore, prone to exhibit distinct behaviour in terms of their
tendency to contract or dilate. Zones more prone to dilate were seen to be associated with low anisotropy values of the vectors defining grain orientation, as the grains tend to create a “less organised” system with larger voids within. Conversely, zones of contraction show strong grain alignment, thus lower anisotropy values of grain orientation and lower void ratio. It is shown that the development of regions of contraction and dilation is influenced by the penetration rate. For higher penetration rate, a dilative area, i.e. high void ratio, was identified near the cone, which is believed to be associated with the generation of negative pore pressure and also leading to an increase of cone resistance. For slow penetration rate, the low porosity values observed near the cone indicate the tendency of this zone to contract and thus, exhibiting drained behaviour. This study suggests that the rate-dependent response of CPTU in silt is not only dependent on the drainage rates but is, above all, a result of the evolution of the soil microstructure in the region surrounding the probe. The findings herein presented show that understanding the mechanisms of grain reorientation following cone penetration is of utmost importance to explain the drainage patterns controlling the cone resistance and the development of pore pressures.

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