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LQR distributed cooperative control of a formation of low-speed experimental UAVs

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Abstract—The paper presents a cooperative scheme for controlling arbitrary formations of low-speed experimental UAVs based on a distributed LQR design methodology. Each UAV acts as an independent agent in the formation and its dynamics are described by a 6-DOF (degrees of freedom) nonlinear model. This is linearized for control design purposes around an operating point corresponding to straight flight conditions and simulated only for longitudinal motion. It is shown that the proposed controller stabilizes the overall formation and can control effectively the nonlinear multi-agent system. Also, it is shown via numerous simulations that the system provides reference tracking and that robustness properties, see e.g. [8]-[10]. Literature tends to favour distributed LQR-based control designs, as centralized solutions become infeasible as the number of subsystems and the distance between them increases [11].

In [12] the framework was extended to the robust formation control method for an arbitrary communication topology and any number of subsystems, whereas previous design methods were adequate only for undirected communication networks. Also, the framework was used later in [13]-[15] to establish different distributed LQR-based control designs for controlling the formation.

In the present work we use the distributed LQR design strategy for uncoupled continuous-time multi-agent systems that has been introduced in [13] for controlling the multi-agent formation. The authors proposed an approach which leads to an elegant and powerful result: the synthesis of stabilizing distributed control laws can be obtained by using a simple local LQR problem whose size depends on the maximum vertex degree of the graph. Compared to [13], where the model with double-integrator dynamics was analyzed, we consider a formation of \( N \) identical low-speed experimental UAVs, known as X-RAE1, that can communicate with each other to achieve the common goal. Individual subsystems are described by 6-DOF (degrees of freedom) nonlinear model, which is linearized at certain operating points for the straight level flight dynamics. The graph-theory framework proposed in [5] is used to model the communication network of the subsystems. It is shown that the proposed controller stabilizes the system. Also, it can be used to control effectively the nonlinear multi-agent system for a standard set of initial conditions. Further, it is shown that both multi-agent systems, linear and nonlinear, are able to provide asymptotic reference tracking and are robust to environmental disturbances such as nonuniform wind profiles for a formation of UAVs and to the loss of communication between any two agents.

The remainder of this paper is organized as follows. In Section II, notation and brief preliminaries on algebraic graph theory are presented. In Section III the nonlinear and linear models of a single X-RAE1 are briefly described. Section IV presents the procedure for modelling the multi-UAV system together with the distributed controller design procedure for this system. The proposed design is able to achieve asymptotic tracking to step height commands and asymptotic rejection of impulsive disturbances modelling wind gusts. Simulation results are presented and discussed in Section V. Finally, the paper’s conclusions appear in Section VI.
A. Nonlinear Model

2) Rotational equations of motion

A. Notation and Definitions

Let $I_n$ denote the identity matrix of dimension $n$, $I_n \in \mathbb{R}^{n \times n}$. Let $M^T$ and $a^T$ denote, respectively, the transpose of matrix $M$ and the transpose of column vector $a = [a_1, \ldots, a_n]^T$. $A \otimes B$ denotes the Kronecker product of $A$ and $B$. Let $A \in \mathbb{R}^{m \times n}$ and $B \in \mathbb{R}^{p \times q}$, then:

$$A \otimes B = \begin{pmatrix}
    a_{11}B & a_{12}B & \ldots & a_{1n}B \\
    \vdots & \vdots & \ddots & \vdots \\
    a_{m1}B & a_{m2}B & \ldots & a_{mn}B
\end{pmatrix} \in \mathbb{R}^{mp \times nq}.$$ 

A matrix $M \in \mathbb{R}^{n \times n}$ is called stable or Hurwitz if all its eigenvalues have negative real part, i.e. $S(M) \subseteq \mathbb{C}_-$.

B. Graph Theory Preliminaries

Let $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ be an undirected graph with the set of nodes (or vertices), $\mathcal{V} = \{1, 2, \ldots, N\}$, and the set of edges $\mathcal{E} \subseteq \mathcal{V} \times \mathcal{V}$, $\mathcal{E} \subseteq \{(i, j) : i, j \in \mathcal{V}, j \neq i\}$. If $i, j \in \mathcal{V}$ and $(i, j) \in \mathcal{E}$, then $i$ and $j$ are said to be adjacent (or neighbors) which is denoted as $i \sim j$. For an undirected graph the communication between two nodes (or agents) is bidirectional and we assume that there is no edge from a node to itself (i.e., no self loops). The number of neighboring nodes, $d_i$ for $i = 1, 2, \ldots, N$, is called the degree or valency of a node. Let $d_{max}(\mathcal{G})$ denote the maximum node degree of the graph $\mathcal{G}$. Any undirected graph can be represented by its adjacency matrix, $A(\mathcal{G})$. Let $A_{i,j} \in \mathbb{R}$ be the $(i, j)$ element of $A(\mathcal{G})$, then $A_{i,i} = 0$, $\forall i = 1, 2, \ldots, N$, and

$$A_{i,j} = \begin{cases} 
    0 & \text{if } (i, j) \notin \mathcal{E} \forall i, j = 1, 2, \ldots, N, \ i \neq j, \\
    1 & \text{if } (i, j) \in \mathcal{E} \forall i, j = 1, 2, \ldots, N, \ i \neq j.
\end{cases}$$

III. DYNAMICAL MODEL OF X-RAE1

A. Nonlinear Model

The 6-DOF equations of motion of X-RAE1 with respect to the body-fixed axes are:

1) Translational equations of motion

$$
\dot{U} = RV - QW - g \sin \Theta + \left[ qS(C_L \sin \alpha - C_D \cos \alpha) + T \right]/m \\
\dot{V} = PW - RU + g \cos \Theta \sin \Phi + (qSC_y)/m \\
\dot{W} = QU - PV + g \cos \Theta \cos \Phi + \left[ qS(-C_L \cos \alpha - C_D \sin \alpha) \right]/m
$$

2) Rotational equations of motion

$$
\dot{\phi}I_x - \dot{P}I_{xz} = QR(I_y - I_z) + PQI_{zx} + qSbC_l \\
\dot{\psi}I_y = PR(I_x - I_z) - (P^2 - R^2)I_{xz} + qScC_m \\
\dot{\phi}I_z = PQ(I_x - I_y) + QRI_{zx} + qScC_n
$$

where

- $U$, $V$, $W$ are forward, side and downward velocities along the $x$, $y$ and $z$ body axes, respectively;
- $P, Q, R$ are roll, pitch and yaw angular velocities around the $x$, $y$ and $z$ body axes, respectively;
- $\Phi, \Theta, \Psi$ are roll, pitch and yaw angles;
- $T$ is the thrust;
- $C_L$, $C_D$, $C_y$ are lift, drag and side force coefficients;
- $\alpha, q$ are the angle of attack and dynamic pressure;
- $m, g, S, \alpha_T$, $h_0$, $b$ and $c$ are known parameters.

B. Linearized Model

In order to design a linear controller, the nonlinear model is linearized and decomposed into two motions, longitudinal and lateral, by assuming small perturbations around the operating point. For a straight, steady, symmetric and horizontal flight at a constant velocity $V_{T_0} = 30$ m/s, the following trimmed values are considered:

$$
U_0 = V_{T_0} \cos \alpha_0, \quad W_0 = V_{T_0} \sin \alpha_0, \\
V_0 = P_0 = Q_0 = R_0 = 0, \\
\alpha_0 = 0, \quad \Phi_0 = \Psi_0 = 0.
$$

Then, the state space longitudinal model

$$
\dot{x}_i = A x_i + B u_i, \quad x_i(0) = x_{i0}
$$

where $x_i = \begin{bmatrix} u_i \ w_i \ q_i \ \theta_i \end{bmatrix}^T$ and $u_i = \begin{bmatrix} \eta_i \ \delta_{iT} \end{bmatrix}^T$ are the state and input vectors of the $i$th system at time $t$, respectively, can be expressed as

$$
\begin{bmatrix}
    u_i \\
    w_i \\
    q_i \\
    \theta_i
\end{bmatrix} = \begin{bmatrix}
    -0.142 & -0.227 & 2.493 & -9.771 \\
    -1.033 & -4.476 & 28.639 & 0.837 \\
    -0.042 & -2.744 & -15.351 & -0.134 \\
    0 & 0 & 1 & 0
\end{bmatrix} \begin{bmatrix}
    u_i \\
    w_i \\
    q_i \\
    \theta_i
\end{bmatrix} + \begin{bmatrix}
    -1.136 & 1.444 \\
    -13.060 & 0 \\
    -137.157 & -2.036 \\
    0 & 0
\end{bmatrix} \begin{bmatrix}
    \eta_i \\
    \delta_{iT}
\end{bmatrix}
$$

where $u_i, w_i, q_i$ and $\theta_i$ denote forward velocity, downward velocity, pitch angular velocity and pitch angle, respectively, while $\eta_i$ and $\delta_{iT}$ are elevator deflection and throttle setting, respectively; the lower case notation denotes the deviation of each motion quantity from the trim value, i.e. $dU_i = u_i$. For more details see [16].

For simulation purposes the disturbance in system (3) is introduced as an arbitrary impulse to the downward velocity...
variable $\dot{w}_i$, which is equivalent to the presence of environmental disturbances such as nonuniform wind for a collection of agents.

IV. FORMATION MODELLING AND CONTROLLER DESIGN

A. Modelling Multi-UAV System with LQR-based Control

The collective dynamics of $N$ identical and decoupled dynamical agents can be described as:

$$\dot{x}(t) = A_n x + B_n u, \quad x(0) = x_0$$

(4)

where $x(t) = [x_1^T(t), \ldots, x_N^T(t)]^T$ and $u(t) = [u_1^T(t), \ldots, u_N^T(t)]^T$ are the vectors which collect the states and inputs of the $N$ systems, while $A_n = I_N \otimes A$ and $B_n = I_N \otimes B$, where $A$ and $B$ are defined as in (3).

The LQR problem for the system (4) is described through the cost function which contains terms for weighting the difference between $i$th and $j$th system states, as well as the $i$th system state and input:

$$J(u(t), x_0) = \int_0^\infty \left( \sum_{i=1}^N \left( x_i(t)^T Q_i x_i(t) + u_i(t)^T R_i u_i(t) \right) + \sum_{i=1}^N \sum_{j=1}^N \left( (x_i(t) - x_j(t))^T Q_{ij} (x_i(t) - x_j(t)) \right) \right) dt,$$

which can be rewritten using the more compact notation:

$$J(u(t), x_0) = \int_0^\infty \left( x(t)^T Q x(t) + u(t)^T R u(t) \right) dt$$

(5)

where the matrices $Q$ and $R$ have the following structure:

$$Q_n = \begin{pmatrix} Q_{11} & Q_{12} & \cdots & Q_{1N} \\ Q_{21} & Q_{22} & \cdots & Q_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ Q_{N1} & Q_{N2} & \cdots & Q_{NN} \end{pmatrix}, \quad R = I_N \otimes R, \quad (6)$$

with $Q_{ij} = \sum_{k=1}^N Q_{ik}$ for $i = 1, \ldots, N$, $Q_{ij} = -Q_{ji}$ for $i, j = 1, \ldots, N$, $i \neq j$, and $R_{ij} = R_{ji}^T > 0$, $\forall i$. Further, $Q_{ii} = Q_i^T \geq 0$, $\forall i$ and $Q_{ij} = Q_{ji} = 0$, $\forall i \neq j$.

We are assuming that the pairs $(A, B)$, $(A_n, B_n)$ are stabilizable and the pairs $(A, C)$, $(A_n, C_n)$ are observable for any $Q = Q^T \geq 0$ and $Q_n$ as in (6) (where $CTC = Q$, $C_n^T C_n = Q_n$).

Then, for the given initial conditions, $x_0$, the control input $u = -R_n^{-1} B_n^T P_a x$ minimizes the cost function in (5) subject to $\dot{x}(t) = A_n x + B_n u$, $x(0) = x_0$. Also, $P_n$ is the symmetric positive definite stabilizing solution of the following (large-scale) Algebraic Riccati Equation (ARE):

$$A_n^T P_n + P_n A_n - P_n B_n R_n^{-1} B_n^T P_n + Q_n = 0.$$  

(7)

For $Q_{a_{ii}} = Q_1$, $\forall i = 1, \ldots, N$, and $Q_{a_{ij}} = Q_2$, $\forall i = 1, \ldots, N$, $i \neq j$ $P_a$ has the structure:

$$P_a = \begin{pmatrix} P_{a_{11}} & P_{a_{12}} & \cdots & P_{a_{1N}} \\ P_{a_{21}} & P_{a_{22}} & \cdots & P_{a_{2N}} \\ \vdots & \vdots & \ddots & \vdots \\ P_{a_{N1}} & P_{a_{N2}} & \cdots & P_{a_{NN}} \end{pmatrix} \quad (8)$$

with $P_{a_{11}} = P - (N - 1) P_{a_{12}}$, where $P \in \mathbb{R}^{n \times n}$ is the symmetric positive definite definite solution of the ARE:

$$A^T P + PA - PBR^{-1}BT P + Q_1 = 0.$$  

(9)

Further, the same structure of diagonal and off-diagonal blocks will be preserved in the gain matrix $K_n$, as $K_n = R_n^{-1} B_n P_n$.

For more details and proofs see [13].

B. Distributed Controller Design Approach

Consider the multi-agent system composed of $N_d$ identical and decoupled agents described as:

$$\dot{x}(t) = A \dot{x} + B \dot{u}, \quad \dot{x}(0) = \dot{x}_0$$

(10)

where $x(t)$ and $\dot{u}(t)$ are the states and inputs of the $N_d$ systems, while $A = I_{N_d} \otimes A$ and $B = I_{N_d} \otimes B$, where $A$ and $B$ are defined as in (3). Systems (4) and (10) differ only in the number of subsystems. The distributed optimal control problem is given in [13], but instead of solving NP-hard problem, the suboptimal distributed design procedure is given next.

Theorem 4.1: [13] For the system in (10), with cost function:

$$J(\dot{u}(t), \dot{x}_0) = \int_0^\infty \left( x(t)^T Q \dot{x}(t) + u(t)^T R \dot{u}(t) \right) dt$$

(11)

where $\dot{Q} = \dot{Q}^T \geq 0$, $\dot{R} = \dot{R}^T > 0$ and $\dot{Q}$ is structured as: $\dot{Q}_{ii} = \dot{Q}_i$ for all $i = 1, \ldots, N$ and $\dot{Q}_{ij} = \dot{Q}_2$ for all $j = 1, \ldots, N$, $i \neq j$, the gain matrix can be constructed as:

$$\dot{K} = I_{N_d} \otimes R^{-1} B^T P - M \otimes R^{-1} B P_{a_{12}}$$

(12)

where $P$ is the symmetric positive definite definite solution to the single agent LQR problem in (9) and $P_{a_{12}}$ represents the off-diagonal blocks of the solution $P_a$ in (7) for $N_{min} = d_{max}(\mathcal{G}) + 1$ agents.

Matrix $M$ reflects the structure of the graph $\mathcal{G}$ and is given by $M = aI_{N_d} - bA(\mathcal{G})$, $b \geq 0$ where $A(\mathcal{G})$ is the adjacency matrix. Also, $a$ and $b$ have to satisfy $a - bd_{max} \geq 0$ which follows from the gain margin properties of the proposed design. Then, the closed loop system:

$$\dot{A}_{cl} = A - B \dot{K} = I_{N_d} \otimes A + (I_{N_d} \otimes B) \dot{K}$$

(13)

will be asymptotically stable and $\dot{P}$ is the unique solution of the following Lyapunov equation:

$$\dot{A}_{cl}^T \dot{P} + \dot{P} A_{cl} + \dot{Q} + \dot{K}^T \dot{R} \dot{K} = 0.$$  

(14)

Proof 4.1.1: See [13]

C. Reference tracking with LQR

In order to show that the distributed LQR controller proposed in Section IV-B provides the asymptotic tracking of step references the state-space system in (10) is augmented by an error vector $e_h = h - h_a$, where $h$ is the vector that collects heights of each agent while $h_a$ is the vector of desired heights for each agent (step inputs). Then, the augmented distributed system is given by

$$\hat{x}_I = \hat{A}_I \hat{x}_I + \hat{B}_I \hat{u}_I, \quad \hat{x}_I(0) = \hat{x}_I_0$$

(15)
where $\ddot{x}_I = \begin{bmatrix} \ddot{x} & e_h \end{bmatrix}^T$, $\tilde{A}_I = \begin{bmatrix} \tilde{A} & 0 \\ \tilde{C} & 0 \end{bmatrix}$ and $\tilde{B}_I = \begin{bmatrix} \tilde{B} \\ 0 \end{bmatrix}$. Matrix $\tilde{C}$ is used to construct individual agent heights according to the equation $\tilde{h}_i = -0.087 u_i - 0.996 w_i + 30 \ell_i$. By solving the (large-scale) ARE:

$$\tilde{A}_I^T \tilde{P}_I + \tilde{P}_I \tilde{A}_I - \tilde{P}_I \tilde{B}_I \tilde{R}_I^{-1} \tilde{B}_I^T \tilde{P}_I + \tilde{Q}_I = 0$$  \hfill (16)

for $\tilde{Q}_I = \begin{bmatrix} \tilde{Q} & 0 \\ 0 & \gamma I \end{bmatrix}$ and $\tilde{R}_I = \rho I$, we get the stabilizing solution $\tilde{P}_I$ ($\gamma$ and $\rho$ are given positive constants). Furthermore, by using the gain matrix $\tilde{K}_{IC} = \tilde{R}_I^{-1} \tilde{B}_I^T \tilde{P}_I$ we define the control input as

$$\tilde{u}_I = -\tilde{K}_{IC} \tilde{x}_I = \begin{bmatrix} -K_P & -K_I \end{bmatrix} \begin{bmatrix} \tilde{x} \\ e_h \end{bmatrix}$$  \hfill (17)

where the matrices $K_P$ and $K_I$ are the proportional state feedback gain and the integral output gain, respectively.

The block diagram of the augmented closed-loop LQR system that provides reference tracking is given in Figure 1.

![Fig. 1. Closed-loop distributed LQR system that provides reference tracking](image)

V. SIMULATION RESULTS

Consider a network of four dynamically decoupled X-RAEIs moving in a plane, whose individual dynamics is linear and described in (3). The interconnection structure is depicted in Figure 2.

![Fig. 2. The interconnection structure](image)

The maximum vertex degree of the interconnection graph is 2, thus the size of LQR problem in (7) that has to be solved to design a stabilizing distributed controller is $N_{\text{min}} = 3$. Then, we define the distributed LQR problem for a formation in Figure 2 as

$$\min_{\tilde{K}} \tilde{J}(\tilde{u}(t), \tilde{x}_0) \quad \text{subj. to} \quad \dot{\tilde{x}} = \tilde{A} \tilde{x} + \tilde{B} \tilde{u}, \quad \tilde{x}(0) = \tilde{x}_0$$

where $\tilde{A} = I_3 \otimes A$ and $\tilde{B} = I_3 \otimes B$, and $A$ and $B$ are as in (3). The cost function $\tilde{J}(\tilde{u}(t), \tilde{x}_0)$ is as in (11) with the weighting matrices $\tilde{Q}$ and $\tilde{R}$, which are structured as: $\tilde{Q}_{ii} = \text{diag}(0.3, 3, 0.15, 3)$ for $i = 1, \ldots, N_{\text{min}}$, $\tilde{Q}_{ij} = \text{diag}(-0.1, -1, -0.05, -1)$ for $i, j = 1, \ldots, N_{\text{min}}$, and $i \neq j$, and $\tilde{R} = I_3 \otimes R$ with $R = 10I_2$.

The solution of the above minimum size LQR problem is of the following structure:

$$P_n = \begin{bmatrix} P_{11} & P_{12} & P_{13} \\ P_{21} & P_{22} & P_{23} \\ P_{31} & P_{32} & P_{33} \end{bmatrix}.$$

Our control objective is to stabilize each individual agent moving on a plane by using the distributed gain matrix

$$\tilde{K} = I_4 \otimes R^{-1} B^T P - M \otimes R^{-1} B^T P_{12}$$

where $P = P_{11} + 2P_{12}$ and $M = 2I_4 - A(G)$. Further, the adjacency matrix representing the graph is given by

$$A(G) = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}.$$  \hfill (20)

In order to validate that the distributed controller in (19) is able to accommodate the reference tracking we use the augmented model described in Section IV-C with $\tilde{Q}_I = \begin{bmatrix} \tilde{Q} & 0 \\ 0 & I_4 \end{bmatrix}$ and $\tilde{R}_I = 10I_8$.

A simulation environment is created for both models, linear and nonlinear, by using Matlab® and Simulink® [17]. Agents’ movement is illustrated by examining the deviation from nominal velocity $V_{T_0} = 30 \text{ m/s}$, which is the horizontal speed at which the model has been linearized. Further, the individual agents’ vertical positions (i.e. heights) are depicted for both controllers.

The first simulation illustrates the height responses (i.e. deviation from the nominal height) of the each agent in Figure 2 in the presence of environmental disturbances for the case of linear dynamics. The disturbances are introduced as arbitrary impulses to the downward velocities of the four agents. Results are depicted in Figure 3. Similarly, Figure 4 depicts the deviation of each agent’s velocity from the nominal velocity of 30 m/s in the presence of environmental disturbances for the case of linear dynamics.

Figure 3 and Figure 4 demonstrate that in the case of linear model the distributed LQR controller stabilizes the formation and agents are able to recover their vertical positions. Note that the formation structure is lost with respect to the horizontal agents’ positions. This can be prevented, if required, by introducing an additional state variable for horizontal regulation. Results are omitted due to space restrictions. Further, the proposed controller is able to provide asymptotic reference tracking to step commands which is depicted in Figure 5 for the case of linear LQR system and unit step reference for each of the agents.

Next, the same set of results are reproduced for the nonlinear system using identical simulation parameters. These are given in Figure 6, Figure 7 and Figure 8. Despite strong nonlinearity...
in the model, the controller was able to reproduce results that are closely related to those obtained in the linear case.

Finally, we considered the case when the communication between two agents is lost shortly after a disturbance impulse was applied. We assume the impulse disturbance to agent 1 at $t = 9\, s$ which is followed by the failure of link communication between agent 1 and agent 2 (in both directions) at $t = 9.2\, s$. Results are produced only for agent 1 for the nonlinear dynamics case where the distributed LQR controller in (15) is used as this can be considered as the most critical case for the stability of the formation. Thus, the height and velocity responses of agent 1 are depicted in Figure 9.

It can be seen that system stabilizes even in the case of link failure in the presence of disturbance as long as connectivity of network is preserved. These can be considered as the preliminary results that can be extended along various directions. Future work will investigate the size of disturbances that can be rejected, as well as the minimum time that system needs to recover from a communications failure before the next disturbance happens.

VI. CONCLUSIONS

The paper has described a cooperative scheme for controlling a formation of low speed experimental UAVs based on distributed LQR control. The simulation results presented demonstrate the effectiveness of the method in dealing with nonlinear model dynamics, partial loss of communication between agents, rejection of external disturbances and asymptotic tracking requirements to step hight demands.
Fig. 7. Velocity response of the nonlinear LQR system controlled by the distributed controller in the presence of the impulse disturbance

Fig. 8. Step height response of the nonlinear LQR system controlled by the distributed controller in the presence of the impulse disturbance

Fig. 9. Height and velocity responses of the nonlinear LQR system controlled by the distributed controller in the presence of an impulsive disturbance to agent 1 followed by the communication failure between agent 1 and agent 2

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