I. INTRODUCTION

One of the most challenging issues of recent years is presented by the overwhelming mass of available data. While this abundance of information and the extreme accessibility to it represents an important cultural advance, it raises on the other hand the problem of retrieving relevant information. Imagine entering the largest library in the world, seeking all relevant documents on your favorite topic. Without the help of an efficient librarian this would be a difficult, perhaps hopeless, task. The desired references would likely remain buried under tons of irrelevancies. Clearly the need for effective tools for information retrieval and analysis is becoming more urgent as the databases continue to grow.

First of all let us consider some among the possible sources of information. In nature many systems and phenomena are often represented in terms of sequences or strings of characters. In experimental investigations of physical processes, for instance, one typically has access to the system only through a measuring device which produces a time record of a certain observable, i.e. a sequence of data. On the other hand other systems are intrinsically described by string of characters, e.g. DNA and protein sequences, language.

When analyzing a string of characters the main question is to extract the information it brings. For a DNA sequence this would correspond, for instance, to the identification of the subsequences codifying the genes and their specific functions. On the other hand for a written text one is interested in questions like recognizing the language in which the text is written, its author or the subject treated.

In this paper we exploit concepts of information theory to address the fundamental problem of identifying and defining the most suitable tools to extract, in a automatic and agnostic way, information from a generic string of characters. We introduce in particular a class of methods which use in a crucial way data compression techniques in order to define a measure of remoteness and distance between pairs of sequences of characters (e.g. texts) based on their relative information content. We also discuss in detail how specific features of data compression techniques could be used to introduce the notion of \textit{dictionary} of a given sequence and of \textit{Artificial Text} and we show how these new tools can be used for information extraction purposes. We point out the versatility and generality of our method that applies to any kind of corpora of character strings independently of the type of coding behind them. We consider as a case study linguistic motivated problems and we present results for automatic language recognition, authorship attribution and self consistent-classification.

One of the main approach to this problems, the one we address in this paper, is that of information theory (IT) \cite{1,2} and in particular the theory of data compression.

In a recent letter \cite{3} a method for context recognition and context classification of strings of characters or other equivalent coded information has been proposed. The remoteness between two sequences $A$ and $B$ was estimated by zipping a sequence $A + B$ obtained by appending the sequence $B$ after the sequence $A$ and exploiting the features of data compression schemes like \texttt{gzip} (whose core is provided by the Lempel-Ziv 77 (LZ77) algorithm \cite{4}). This idea was used for authorship attribution and, by defining a suitable distance between sequences, for languages phylogeny.

The idea of appending two files and zipping the resulting file in order to measure the remoteness between them had been previously proposed by Loewenstein et al. \cite{5} (using \texttt{zdiff} routines) who applied it to the analysis of DNA sequences, and by Khmelev \cite{6} who applied the method to authorship attribution. Similar methods have been proposed by Juola \cite{7}, Teahan \cite{8} and Thaper \cite{9}.

In this paper we extend the analysis of \cite{3} and we describe in details the methods to define and measure the remoteness (or similarity) between pairs of sequences based on their relative informatic content. We devise in particular, without loss of generality with respect to the nature of the strings of characters, a method to measure this distance based on data-compression techniques.

The principal tool for the application of these methods is the LZ77 algorithm, which, roughly speaking, achieves the compression of a file exploiting the presence of repeated subsequences. We introduce (see also \cite{10}) the notion of \textit{dictionary} of a sequence, defined as the set of all the repeated substrings found by LZ77 in a sequential parsing of a file, and we refer to these substrings as dictionary’s \textit{words}. Besides being of great intrinsic interest, every dictionary allows for the creation of \textit{Artificial texts} (AT) obtained by the concatenation of random ex-
In this paper we discuss how comparing AT, instead of the original sequences, could represent a valuable and coherent tool for information extraction to be used in very different domains. We then propose a general AT comparison scheme (ATC) and show that it yields to remarkable results in experiments.

We have chosen for our tests some textual corpora and we have evaluated our method on the basis of the results obtained on some linguistic motivated problems. Is it possible to automatically recognize the language in which a given text is written? Is it possible to automatically guess the author and the subject of a given text? And finally is it possible to define methods for the automatic classification of the texts of a given corpus?

The choice of the linguistic framework is justified by the fact that this is a field where anybody could be able to judge, at least partially, about the validity and the relevance of the results. Since we are introducing techniques for which a benchmark does not exist it is important to check their validity with known and controlled examples. This does not mean that the range of applicability is reduced to linguistics. On the contrary the ambition is to provide physicists with tools which could parallel other standard tools to analyze strings of characters.

In this perspective it is worthwhile recalling here some of the last developments of sequence analysis in physics related problems. A first field of activity is that of segmentation problems, i.e. cases in which a unique string must be partitioned into subsequences according to some criteria to identify discontinuities in its statistical properties. A classical example is that of the separation of coding and non-coding portions in the DNA but the analysis of genetic sequences in general represents a very rich source of segmentation problems (see, for instance, [10, 13, 14, 15]).

A more recent area is represented by the use of data compression techniques to test specific properties of symbolic sequences. In [11], the technology behind adaptive dictionary data compression algorithms is used in a suitable way (which is very close to our approach) as an estimate of reversibility of time series, as well as a statistical likelihood test. Another interesting field is related to the problem of the generation of random numbers. In [12] it is outlined the importance of suitable measures of conditional entropies in order to check the real level of randomness of random numbers, and an entropic approach is used to discuss some random number generator shortcomings (see also [13]).

Finally, another area of interest is represented by the use of data compression techniques to estimate entropic quantities (e.g. Shannon entropy, Algorithmic Complexity, Kullback-Leibler divergence etc.). Even though not new this area is still topical [14, 15]. A specific application that has generated an interesting debate has been drawn about the analysis of electroencephalograms of epilepsy patients [21, 22, 23]. In particular in these papers it is argued that measures like the Kullback-Leibler divergence could be used to spot information in medical data. The debate is wide open.

The outline of the paper is as follows. In section II, after a short theoretical introduction, we recall how data compression techniques could be used to evaluate entropic quantities. In particular we recall the definition of the LZ77 [4] compression algorithm and we address the problem of using it to evaluate quantities like the relative entropy between two generic sequences as well as to define a suitable distance between them. In section III we introduce the concept of Artificial Text (AT) and present a method for information extraction based on Artificial Text comparison. Sections IV and V are devoted to the results obtained with our method in two different contexts: the recognition and extraction of linguistic features (see also [18]) and the self-consistent classification of large corpora (sect. IV) and the self-consistent classification of large corpora (sect. V). Finally section VI is devoted to the conclusions and to a short discussion about possible perspectives.

II. COMPLEXITY MEASURES AND DATA COMPRESSION

Before entering in the details of our method let us briefly recall the definition of entropy of a string. Shannon’s definition of information entropy is indeed a probabilistic concept referring to the source emitting strings of characters.

Consider a symbolic sequence \(\{\sigma_1, \sigma_2, \ldots\}\), where \(\sigma_i\) is the symbol emitted at time \(t\) and each \(\sigma_i\) can assume one of \(m\) different values. Assuming that the sequence is stationary we introduce the \(N\)-block entropy:

\[
H_N = - \sum_{W_N} p(W_N) \ln p(W_N)
\]

where \(p(W_N)\) is the probability of the \(N\)-word \(W_N = (\sigma_1, \sigma_{t+1}, \ldots, \sigma_{t+N-1})\), and \(\ln = \log_e\). The differential entropies

\[
h_N = H_{N+1} - H_N
\]

have a rather obvious meaning: \(h_N\) is the average information supplied by the \((N+1)\)-th symbol, provided the \(N\) previous ones are known. Noting that the knowledge of a longer past history cannot increase the uncertainty on the next outcome, one has that \(h_N\) cannot increase with \(N\) i.e. \(h_{N+1} \leq h_N\). With these definitions the Shannon entropy for an ergodic stationary process is defined as:

\[
h = \lim_{N \to \infty} h_N = \lim_{N \to \infty} \frac{H_N}{N}.
\]
The Shannon entropy \( h \) measures the average amount of information per symbol and it is an estimate of the “surprise” the source emitting the sequence reserves to us. It is remarkable the fact that, under rather natural assumptions, the entropy \( H_N \) apart from a multiplicative factor, is the unique quantity which characterizes the “surprise” of the \( N \)-words. Let’s try to explain in which sense entropy can be considered as a measure of a surprise. Suppose that the surprise one feels upon learning that an event \( E \) has occurred depends only on the probability of \( E \). If the event occurs with probability 1 (sure) our surprise in its occurring will be zero. On the other hand if the probability of occurrence of the event \( E \) is quite small our surprise will be proportionally large. For a single event occurring with probability \( p \) the surprise is proportional to \( \ln p \). Let’s consider now a random variable \( X \), which can take \( N \) possible values \( x_1, \ldots, x_N \) with probabilities \( p_1, \ldots, p_N \), the expected amount of surprise we shall receive upon learning the value of \( X \) is given precisely by the entropy of the source emitting the random variable \( X \), i.e. \( -\sum p_i \ln p_i \).

The definition of entropy is closely related to a very old problem, that of transmitting a message without losing information, i.e. the problem of the efficient encoding.

A good example is the Morse code. In the Morse code a text is encoded with two characters: line and dot. What is the best way to encode the characters of the English language (provided one can define a source for English) with sequences of dots and lines? The idea of Morse was to encode the more frequent characters with the minimum numbers of characters. Therefore the \( e \) which is the most frequent English letter is encoded with one dot (·), while the letter \( q \) is encoded with three lines and one dot (− − ·).

The problem of the optimal coding for a text (or an image or any other kind of information) has been enormously studied. In particular Shannon showed that there is a limit to the possibility to encode a given sequence. This limit is the entropy of the sequence.

This result is particularly important when the aim is the measure of the information content of a single finite sequence, without any reference to the source that emitted it. In this case the reference framework is the Algorithmic Complexity Theory and the basic concept is Chaitin - Kolmogorov entropy or Algorithmic Complexity (AC): the entropy of a string of characters is the length (in bits) of the smallest program which produces as output the string and stops afterwords. This definition is really abstract. In particular it is impossible, even in principle, to find such a program and as a consequence the algorithmic complexity is a non computable quantity. This impossibility is related to the halting problem and to Godel’s theorem.

It is important to recall how it exists a rather important relation between the Algorithmic Complexity Theory and the basic concept emitted it. In this case the reference framework is the finite sequence, without any reference to the source that emitted it. This limit is the entropy of the sequence.

A great improvement in the field of data compression has been represented by the Lempel and Ziv algorithm (LZ77) (used for instance by gzip and zip). It is interesting to briefly recall how it works (see fig. 1). Let \( x = x_1, \ldots, x_N \), the sequence to be zipped, where \( x_i \) represents a generic character of sequence’s alphabet. The LZ77 algorithm finds duplicated strings in the input data. The second occurrence of a string is replaced by a pointer to the previous string given by two numbers: a distance, representing how far back into the window the sequence starts, and a length, representing the number of characters for which the sequence is identical. More specifically the algorithm proceeds sequentially along the sequence. Let us suppose that the first \( n \) characters have been codified. Then the zipper looks for the largest integer \( m \) such that the string \( x_{n+1}, \ldots, x_{n+m} \) already appeared in

**Original sequence**

qwhhABCDhhABCDhzABCDhhz...

**Zipped sequence**

qwhhABCDhh(6,4)z(11,6)z...

FIG. 1: Scheme of the LZ77 algorithm: The LZ77 algorithm works sequentially and at a generic step looks in the look-ahead buffer for substrings already encountered in the buffer already scanned. These substrings are substituted by a pointer \((d,n)\) where \( d \) is the distance of the previous occurrence of the same substring and \( n \) is its length. Only strings longer than two characters are substituted in the example.

\[ K_N(W_N) \text{ of a sequence } W_N \text{ of } N \text{ characters and } H_N: \]

\[
\frac{1}{N}(K_N) = \frac{1}{N} \sum_{W_N} K_N(W_N)P(W_N) \xrightarrow{N \to \infty} \frac{h}{\ln 2}
\]

where \( K_N \) is the binary length of the shorter program needed to specify the sequence \( W_N \).

As a consequence it exists a relation between the maximum compression rate of a sequence \((\sigma_1 \sigma_2 \ldots)\) expressed in an alphabet with \( m \) symbols, and \( h \). If the length \( N \) of the sequence is large enough, then it is not possible to compress it into another sequence (with an alphabet with \( m \) symbols) whose size is smaller than \( Nh / \ln m \). Therefore, noting that the number of bits needed for a symbol in an alphabet with \( m \) symbols is \( \ln m \), one has that the maximum allowed compression rate is \( h / \ln m \).

Though the maximal theoretical limit of the Algorithmic Complexity is not achievable, there are nevertheless algorithms explicitly conceived to approach it. These are the file compressors or zippers. A zipper takes a file and tries to transform it in the shortest possible file. Obviously this is not the best way to encode the file but it represents a good approximation of it.

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for instance already described, a compression algorithm like LZ77 applied to a sequence emitted by \( A \) will be asymptotically (i.e. in the limit of an available infinite sequence) able to encode the sequence almost optimally, i.e. coding on average every character with \(-p \log_2 p - (1 - p) \log_2 (1 - p)\) bits (the Shannon entropy of the source). This optimal coding will not be the optimal one for the sequence emitted by \( B \). In particular the entropy per character of the sequence emitted by \( B \) in the coding optimal for \( A \) (i.e. the cross-entropy per character) will be \(-q \log_2 q - (1 - q) \log_2 (1 - q)\) while the entropy per character of the sequence emitted by \( B \) in its optimal coding is \(-q \log_2 q - (1 - q) \log_2 (1 - q)\). The number of bits per character waisted to encode the sequence emitted by \( B \) with the coding optimal for \( A \) is the relative entropy of \( A \) and \( B \).

\[
d(A||B) = -q \log_2 p - (1 - q) \log_2 \frac{1 - p}{1 - q} 
\]

A linguistic example will help to clarify the situation: transmitting an Italian text with a Morse code optimized for English will result in the need of transmitting an extra number of bits with respect to another coding optimized for Italian: the difference is a measure of the relative entropy between, in this case, Italian and English (supposing the two texts are each one archetypal representations of their Language, which is not).

We should remark that the relative entropy is not a distance (metric) in the mathematical sense: it is neither symmetric, nor does it satisfy the triangle inequality. As we shall see below, in many applications, such as phylogenesis, it is crucial to define a true metric that measures the actual distance between sequences.

There exist several ways to measure the relative entropy (see for instance [33, 36, 37]). One possibility is of course to follow the recipe described in the previous example: using the optimal coding for a given source to encode the messages of another source.

Here we follow the approach recently proposed in [51] which is similar to the approach by Ziv and Merhav [39]. In particular in order to define the relative entropy between two sources \( A \) and \( B \) we consider a sequence \( A \) from the source \( A \) and a sequence \( B \) from the source \( B \). We now perform the following procedure. We create a new sequence \( A + B \) by appending \( B \) after \( A \) and use the LZ77 algorithm or, as we shall see below, a modified version of it.

In [11] it has been studied in detail what happens when a compression algorithm tries to optimize its features at the interface between two different sequences \( A \) and \( B \) while zipping the sequence \( A + B \) obtained by simply appending \( B \) after \( A \). It has been shown in particular the existence of a scaling function ruling the way the compression algorithm learns a sequence \( B \) after having compressed a sequence \( A \). In particular it turns out that it exists a crossover length for the sequence \( B \), given by

\[
L_B^* \simeq L_A^* 
\]
with \( \alpha = \frac{A(B)}{A(B)+A(B')} \). This is the length below which the compression algorithm does not learn the sequence \( B \) (measuring in this way the cross entropy between \( A \) and \( B \)) and above which it learns \( B \), i.e. optimizes the compression using the specific features of \( B \).

This means that if \( B \) is short enough (shorter than the crossover length) one can measure the relative entropy by zipping the sequence \( A + B \) (using gzip or an equivalent sequential compression program); the measure of the length of \( B \) in the coding optimized for \( A \) will be \( \Delta_{AB} = L_{A+B} - L_A \), where \( L_X \) indicates the length in bits of the zipped file \( X \). The cross entropy per character between \( A \) and \( B \) will be estimated by

\[
C(A|B) = \frac{\Delta_{AB}}{|B|},
\]

where \( |B| \) is the length in bits of the uncompressed file \( B \). The relative entropy \( d(A||B) \) per character between \( A \) and \( B \) will be estimated by

\[
d(A||B) = \frac{\Delta_{AB} - \Delta_{B'B}}{|B'|},
\]

where \( B' \) is a second sequence extracted from the source \( B \) with \( |B'| \) characters and \( \Delta_{B'B}/|B'| = (L_{B+B'} - L_B)/|B'| \) is an estimate of the entropy of the source \( B \).

If, on the other hand, \( B \) is longer than the crossover length we must change our strategy and implement an algorithm which does not zip the \( B \) part but simply “reads” it with the (almost) optimal coding of part \( A \). In this case we start reading sequentially file \( B \) and search in the look-ahead buffer of \( B \) for the longest sub-sequence already occurred only in the \( A \) part. This means that we do not allow for searching matches inside \( B \) itself. As in the usual LZ77, every matching found is substituted with a pointer indicating where, in \( A \), the matching subsequence appears and its length. This method allows us to measure (or at least to estimate) the cross-entropy between \( B \) and \( A \), i.e. \( C(A|B) \).

Before proceeding let us briefly discuss which difficulties one could experiment in the practical implementation of the methods described in this section. First of all in practical applications the sequences to be analyzed can be very long and their direct comparison can then be problematic due to finiteness of the window over which matching can be found. Moreover in some applications one is interested in estimating the self-entropy of a source, i.e. \( C(A|A) \) in a more coherent framework. The estimation of this quantity is necessary to calculate the relative-entropy between two sources. In fact, as we shall see in the next section, even though in practical applications the simple cross-entropy is often used, there are cases in which relative entropy is more suitable. The most typical case is when we need to build a symmetrical distance between two sequences. One could think to estimate self-entropy comparing, with the modified LZ77, two portions of a given sequence. This method is not very reliable since many bias could afflict the results obtained in this way. For example if we split a book in two parts and try to measure the cross-entropy between these two parts, the result we would obtain could be heavily affected by the names of the characters present in both parts. More importantly, defining the position of the cut would be completely arbitrary, and this arbitrariness would matter a lot especially for very short sequences. We shall address this problem in section III.

### B. On the definition of a distance

In this section we address the problem of defining a distance between two generic sequences \( A \) and \( B \). A distance \( D \) is an application that must satisfy three requirements:

1. positivity: \( D_{AB} \geq 0 \) (\( D_{AB} = 0 \) iff \( A = B \));
2. symmetry: \( D_{AB} = D_{BA} \);
3. triangular inequality: \( D_{AB} \leq D_{AC} + D_{CB} \ \forall C \);

As it is evident the relative entropy \( d(A||B) \) does not satisfy the last two properties while it is never negative. Nevertheless one can define a symmetric quantity as follows:

\[
P_{AB} = P_{BA} = \frac{C(A|B) - C(B|B)}{C(B|B)} + \frac{C(B|A) - C(A|A)}{C(A|A)}
\]

We now have a symmetric quantity, but \( P_{AB} \) does not satisfies, in general, the triangular inequality. In order to obtain a real mathematical distance we give a prescription according to which this last property is met. For every pair \( A \) and \( B \) of sequences, the prescription writes as:

\[
\text{if } P_{AB} > \min_C[P_{AC} + P_{CB}] \text{ then } P_{AB} = \min_C[P_{AC} + P_{CB}].
\]

By iterating this procedure until for any \( A,B,C \) \( P_{AB} \leq P_{AC} + P_{CB} \), we obtain a true distance \( D_{AB} \). In particular the distance obtained in this way is simply the minimum over all the paths connecting \( A \) and \( B \) of the total cost of the path (according to \( P_{AB} \)) i.e.

\[
D_{AB} = \min_{\{N \geq 2\}} \min_{\{X_1,\ldots,X_N: X_1 = A, X_N = B\}} \sum_{k=0}^{N-1} P_{X_k X_{k+1}}.
\]

Also it is easy to see that \( D_{AB} \) is the maximal distance not larger than \( P_{A,B} \) for any \( A,B \), where we have considered the partial ordering on the set of distances: \( P \geq P' \) if \( P_{AB} \geq P_{AB}' \) for all pairs \( A,B \).

Obviously this is not an a-priori distance. The distance between \( A \) and \( B \) depends, in principle, on the set of files we are considering.

In all our tests with linguistic texts the triangle condition was always satisfied without the need to have recourse to the above mentioned prescription. However
there are cases in other contexts, like, for instance, genetic sequences, in which could be necessary to force the triangularization procedure described above.

An alternative definition of distance can be given considering

\[ R_{AB} = \sqrt{P_{AB}}, \]  

where the square root must be taken before forcing the triangularization. The idea of using \( R_{AB} \) is suggested by the fact that as \( A \) and \( B \) are very close sources then \( P_{AB} \) is of the order of the square of their “difference”. Let us see this in a concrete example where the distance between the two sources is very small. Suppose having two sources \( A \) and \( B \) which can emit sequences of 0 and 1. Let \( A \) emit a 0 with a probability \( p \) and 1 with the complementary probability \( 1 - p \). Now let the source \( B \) emit a 0 with a probability \( p + \epsilon \) and a 1 with a probability \( 1 - (p + \epsilon) \), where \( \epsilon \) is an infinitesimal quantity. In this situation it can be easily shown that the relative entropy between \( A \) and \( B \) is proportional to \( \epsilon^2 \) and, of course, \( P_{AB} \) is then proportional to the same quantity. Taking the square root of \( P_{AB} \) is then simply requiring that, if two sources have a distribution of probability that differs for a small \( \epsilon \), their distance must be of the order of \( \epsilon \) instead of being reduced to the \( \epsilon^2 \) order.

It is important to recall that an earlier and rigorous definition of an unnormalized distance between two generic strings of characters has been proposed in [55] in terms of the Kolmogorov Complexity and of the Conditional Kolmogorov Complexity [30] (see below for the definition).

A normalized version of this distance has been proposed in [52, 50]. In particular Li et al. define

\[ d_K(x, y) = \frac{\max(K(x|y), K(y|x))}{\max(K(x), K(y))} \]  

where the subscript \( K \) refers to its definition in terms of the Kolmogorov complexity. \( K(x|y) \) is the conditional Kolmogorov Complexity defined as the length of the shortest program to compute \( x \) if \( y \) is furnished as auxiliary input to the computation, and \( K(x) \) and \( K(y) \) are the Kolmogorov complexities of strings \( x \) and \( y \), respectively. The distance \( d_K(x, y) \) is symmetrical and it is shown to satisfy the identity axiom up to a precision \( d_K(x, x) = O(1/K(x)) \) and the triangular inequality \( d_K(x, y) \leq d_K(y, z) + d_K(z, y) \) up to an additive term \( O(1/\max(K(x), K(y), K(z))) \).

The problem with this distance is the fact that it is defined in terms of the Conditional Kolmogorov Complexity which is an uncomputable quantity and its computation is performed in an approximate way.

In particular what is important is that the specific procedure (algorithm) used to approximate this quantity, which is indeed a well defined mathematical operation, defines a true distance. In the specific case of the distance \( d_K(x, y) \) defined in [52] the authors approximate this distance by the so-called Normalized Compression Distance

\[ NCD(x, y) = \frac{C(xy) - \min(C(x), C(y))}{\max(C(x), C(y))} \]  

where \( C(xy) \) is the compressed size of the concatenation of \( x \) and \( y \), and \( C(x) \) and \( C(y) \) denote the compressed size of \( x \) and \( y \), respectively. Then this quantities are approximated in a suitable way by using real world compressors.

It is important to remark how it exists a discrepancy between the definition [13] and its actual approximate computation [14].

We discuss here in some details the case of the LZ77 compressor. Using the results presented in Sect.IIA, one obtains that, if the length of \( y \) is small enough (see expression [10], \( NCD(x, y) \) is actually estimating the cross-entropy between \( x \) and \( y \). The cross-entropy is not a distance since it does not satisfy the identity axiom, it is not symmetrical nor it satisfies the triangular inequality. In the general case of \( y \) being not small, again following the discussion of Sect.IIA (presented in more details in [11]), one can show that \( NCD(x, y) \) is given roughly (for \( L_x \) large enough) by:

\[ 1 + \frac{L_x d(x|y)}{L_y C(y)}, \]

where \( L_x \) and \( L_y \) are the lengths of the \( x \) and \( y \) files (with \( L_y \gg L_x^2 \)) and \( d(x|y) \) is the relative entropy rate between \( x \) and \( y \). Again this estimate does not define a metric. Moreover, since \( \alpha \leq 1 \) one can see that \( NCD(x, y) \to 1 \), independently of the choice of \( x \) and \( y \) when \( L_x \) and \( L_y \) tends to infinity.

The discrepancy between the definition of a mathematical distance based on the Conditional Kolmogorov Complexity and its actual approximate computation in [52] has also been pointed out in [60].

Finally it is important to notice that recently Otu and Sayood [61] have proposed an alternative definition of distance between two string of characters, which is rigorous and computable. Their approach is based on the LZ complexity [62] of a sequence \( S \) which can be defined in terms of the number of steps required by a suitable production process to generate \( S \). In their very interesting paper they also give a review on this and correlated problems. We do not enter here on the details and we refer the reader to [61].

III. DICTIONARIES AND ARTIFICIAL TEXTS

As we have seen LZ77 substitutes sequences of characters with a pointer to their previous appearance in the text. We now need some definitions before proceeding. We call dictionary of a sequence the whole set of subsequences substituted with a pointer by LZ77, and we
refer to these sequences as dictionary’s words. As it is evident from these definitions, a particular word can be present many times in the dictionary. Finally, we call root of a dictionary the sequence it has been extracted from. It is important to stress how this dictionary has in principle nothing to do with the ordinary dictionary of a given language. On the other hand there could be important similarities between the LZ77-dictionary of a written text and the dictionary of the Language in which the text is written. As an example we report in Table I and Table II the most frequent and the longest words found by LZ77 while zipping Melville’s Moby Dick text. Figure 2 reports an example of the frequency-length distribution of the LZ77-words as a function of their length (for a very similar figure and similar but less complete dictionary analysis see [10]).

Beyond their utility for zipping purposes, the dictionaries present an intrinsic interest since one can consider them as a source for the principal and more important syntactic structures present in the sequence/text from which the dictionary originates.

A straightforward application is the possibility to construct Artificial Texts. With this name we mean sequences of characters build by concatenating words randomly extracted from a specific dictionary.

Each word has a probability of being extracted proportional to the number of its occurrences in the dictionary. Since typically LZ77 words already contains spaces, we do not include further spaces separating them. It should be stressed as the structure of a dictionary is affected by the size of LZ77 sliding window. In our case we have typically adopted windows of 32768 characters, and, in a few cases, of 65536 characters.

Below we present an excerpt of 400 characters taken from an artificial text (AT) having Melville’s Moby Dick text as root.

<table>
<thead>
<tr>
<th>Frequency</th>
<th>Length</th>
<th>Word</th>
</tr>
</thead>
<tbody>
<tr>
<td>110</td>
<td>6</td>
<td><del>-The</del></td>
</tr>
<tr>
<td>107</td>
<td>7</td>
<td>in-the~</td>
</tr>
<tr>
<td>98</td>
<td>4</td>
<td>you~</td>
</tr>
<tr>
<td>94</td>
<td>6</td>
<td><del>-But</del></td>
</tr>
<tr>
<td>92</td>
<td>9</td>
<td>from-the~</td>
</tr>
<tr>
<td>92</td>
<td>5</td>
<td><del>-very</del></td>
</tr>
<tr>
<td>91</td>
<td>4</td>
<td>one~</td>
</tr>
</tbody>
</table>

Table I: Most frequent LZ77-words found in Moby Dick’s text: Here we present the most represented word in the dictionary of Moby Dick. The ~ represents the space character.

<table>
<thead>
<tr>
<th>Frequency</th>
<th>Length</th>
<th>Word</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>80</td>
<td><del>-Such</del>-a-funny,-sporty,-gamy,<del>-jesty,-joky,-hoky-poky-lad,-is</del>-the-Ocean,-oh!~-Th</td>
</tr>
<tr>
<td>1</td>
<td>78</td>
<td><del>-Such</del>-a-funny,-sporty,-gamy,<del>-jesty,-joky,-hoky-poky-lad,-is</del>-the-Ocean,-oh!~-Th</td>
</tr>
<tr>
<td>1</td>
<td>63</td>
<td>&quot;<del>-&quot;!-look,</del>-you~-look,-he~-looks;<del>-we</del>-look,-ye~-look,-they~-look.&quot;~-&quot;W</td>
</tr>
<tr>
<td>1</td>
<td>63</td>
<td>&quot;<del>-&quot;I</del>-&quot;&quot;look,<del>-you</del>-look,-he~-looks;<del>-we</del>-look,-ye~-look,-they~-look.&quot;~-&quot;W</td>
</tr>
<tr>
<td>1</td>
<td>54</td>
<td>repeated~-in~-this~-book,-<del>that</del>-the~-skeleton~-of~-the~-whale</td>
</tr>
<tr>
<td>1</td>
<td>46</td>
<td><del>-THIS</del>-TABLET~-is~-erected~-to~-his~-Memory~-BY~-HIS~-</td>
</tr>
<tr>
<td>1</td>
<td>43</td>
<td>s-a<del>mild,-mild</del>-wind,-and-a<del>mild</del>-looking~-sky</td>
</tr>
</tbody>
</table>

Table II: Longest words in Moby Dick: Here we present the longest words in the dictionary of Moby Dick. Each of these words appears only one time in the dictionary. The dictionary was extracted using a 32768 sliding window in LZ77.
string can be well represented by a number of AT pro-
certain “reasonable” AT size has been established, any
analyzed. In fact it seems very plausible that, once a
the previous section, related to the length of the strings
it is possible to overcome all the difficulties, discussed in
resentative of the same original root text. In this way
analysis by comparing the features of many AT all rep-
sequence), one can construct an
for texts). Moreover for each original text (or original

DNA sequences are analyzed. The log-normal curve fits well
to define typical AT. This figure illustrates
of all AT present several positive features. They allow
between the root strings is obtained as the average < C >
of all the C(i,j). This method has the advantage of allowing
of AT created (for fixed length of the AT).
portional to its length. On the other hand one can con-
struct AT by merging dictionaries coming from different
original texts: merging dictionaries extracted from differ-
texts all about the same subject or all written by the
same author. In this way the AT would play the role of
an archetypal text of that specific subject or that specific

FIG. 2: LZ77-Word Distribution This figure illustrates
the distribution of the LZ77-words found in different strings of
characters. Above: results for the dictionary of Moby Dick are
shown. In the upper curve several findings of the same word
are considered separately; in the lower curve each different
word is counted only once. It can be shown that the peaks are
well fitted by a log-normal distribution, while there are large
deviations from it for large lengths. Below: words extracted
from Mesorhizobium loti bacterium’s original and reshuffled
dNA sequences are analyzed. The log-normal curve fits well
the whole distribution of words extracted from the reshuffled
string, but is unable to describe the presence of the long words
of the true one.

FIG. 3: Artificial Text Comparison (ATC) method:
This is the scheme of the Artificial Text Comparison method.
Instead of comparing two original strings, several AT (two
in figure) are created starting from the dictionaries extracted
from the original strings, and the comparison is between pairs
of AT. For each pair of AT coming from different roots a
cross-entropy value C(i,j) is measured and the cross-entropy
between the root strings is obtained as the average < C >
of all the C(i,j). This method has the advantage of allowing
for an estimation of an error, σ, on the obtained value of
the cross-entropy < C >, as the standard deviation of the
C(i,j). From the point of view of the ATC computational
demand, point 1) simply consists in the procedure of zipping
the original files, that usually requires few seconds, points
2) and 4) are of course negligible, while point 3) is crucial.
Obviously, in fact, the machine time requested for the cross-
entropy estimation grows as the square power of the number
of AT created (for fixed length of the AT).
In Figure 3 comparing many AT coming from the same two roots (or single root), we can estimate a statistical error on the value of the cross-entropy between the two roots.

With the help of AT we can then build a comparison scheme (Artificial Text Comparison or ATC) (see figure 4) between sequences whose validity will be checked in the following sections. This scheme is very general since it can be applied to any kind of sequence independently of the coding behind it. Moreover the generality of the scheme comes from the fact that, by means of a re-definition of the concept of word, we are able to extract subsequences from a generic sequence using a deterministic algorithm (for instance LZ77) which eliminates every arbitrariness (at least once the algorithm for the minimalistic algorithm (for instance LZ77) which eliminates every arbitrariness (at least once the algorithm for the dictionary extraction has been chosen). In the following sections we shall discuss in detail how one can use AT for recognition and classification purposes.

IV. RECOGNITION OF LINGUISTIC FEATURES

Our first experiments are concerned with recognition of linguistic features. Here we consider those situations in which we have a corpus of known texts and one unknown text X. We are interested here in identifying the known text A closest (according to some rule) to the X one. We then say that X, being similar to A, belongs to the same group of A. This group can, for instance, be formed by all the works of an author, and in that case we say that our method attributed X to that author. We now present results obtained in experiments of language recognition and authorship attribution. After having explained our experiments we will be able to make some more comments on the criterion we adopted to set recognition and/or attribution.

A. Language recognition

Suppose we are interested in the automatic recognition of the language in which a given text X is written. This case can be seen as a first benchmark for our recognition technique. The procedure we use considers a collection (a corpus), as large as possible, of texts in different (known) languages: English, French, Italian, Tagalog . . . . We take an X text to play the role of the unknown text whose language has to be recognized, and the remaining A_i texts of our collection to form our background. We then measure the cross entropy between our X text and every A_i with the procedure discussed in section II. The text, among the A_i group, with the smallest cross entropy with the X one, selects the language closest to the one of the X file, or exactly its language, if the collection of languages contains this language. In our experiment we have considered in particular a corpus of texts in 10 official languages of the European Union (UE): Danish, Dutch, English, Finnish, French, German, Italian, Portuguese, Spanish and Swedish. Using 10 texts for each language we had a collection of 100 texts. We have obtained that for any single text the method has recognized the language. This means that the text A_i for which the cross entropy with the unknown X text was the smallest was a text written in the same language. We found out also that if we ranked for each X text all the texts A_i as a function of the cross entropy, all the texts written in the same language of the unknown text were in the first positions. This means that the recall, defined in the framework of information retrieval as the ratio between the number of relevant documents retrieved (independently of the position in the ranking) and the total number of existing relevant documents, is maximal, i.e. equal to one. The recognition of language works quite well for length of the X file as small as a few tens of characters.

B. Authorship attribution

Suppose now to be interested in the automatic recognition of the author of a given text X. We shall consider, as before, a collection, as large as possible, of texts of several (known) authors all written in the same language of the unknown text and we shall look for the text A_i for which the cross entropy with the X text is minimum. In order to collect a certain statistics we have performed the experiment using a corpus of 87 different texts of 11 Italian authors, using for each run one of the texts in the corpus as the unknown X text. In a first step we proceeded exactly as for language recognition, using the actual texts. The results, shown in Table III feature a rate of success of roughly 93%. This rate is the ratio between the number of texts whose author has been recognized (another text of the same author was ranked as first) and the total number of texts considered. There are of course fluctuations in the success rate for each author and this has to be expected since the writing style is something difficult to grasp and define; moreover it can vary a lot in the production of a single author.

We then proceeded analyzing the same corpus with the ATC method we have discussed in the previous section. We extracted the dictionary from each text, and built up our 87 artificial texts (each one 30000 characters long). In each run of our experiment we chose one artificial text to play the role of the text whose author was unknown and the other 86 to be our background. The result is significant. We found that 86 times on 87 trials the author was indeed recognized, i.e. the cross entropy between our unknown text and at least another text of the right author was the smallest. This means that the rate of success using artificial texts was of 98.8%. The unrecognized text was L’Asino by Machiavelli, which was attributed to Dante (La Divina Commedia), and, in fact, these are both poetic texts; so it does not appear so strange thinking that L’Asino is found to be in some way closer to the
To these remaining 430 A Ts, we first joined all the rankings relative to the 5 cross-entropies between an AT created from X text and an AT extracted from that A.

In this way we obtained 86 cross-entropy values, and we set authorship attribution using the usual minimum-criterion. We found again that 86 texts over 87 were well attributed, L’Asino being again mis-attributed.

This result shows that ATC is a robust method since it does not seem to be strongly influenced by the particular set of artificial texts. In particular, as we have discussed before, ATC allows for a quantification of the error committed on the cross entropy estimation. Defined as \( \sigma_m \) the standard deviation estimated for the \( m \)th cross-entropy, in a ranking in which the smallest cross-entropy value is the first one, we empirically observed these relations:

\[
\frac{\sigma_1}{C_1} \approx \frac{\sigma_2}{C_2} \approx \frac{\sigma_3}{C_3} \approx 0.5\%
\]

\[
(C_2 - C_1) \approx \sigma_1 \approx \sigma_2.
\]

The difference \( C_2 - C_1 \) gives an indication of the level of confidence of the results. When this difference is of the order of the standard deviation of \( C_1 \) and \( C_2 \), this is an indication that the result for the attribution has an high level of confidence (at least inside the corpus of reference files/texts considered).

Finally, in order to explore the possibility of using natural words, we performed experiments with natural artificial texts. We call this method Natural ATC or NATC. We built up 5 artificial texts for each actual one using Italian words instead of words extracted by LZ77. Having these natural artificial texts we proceeded exactly as before. We obtained that 85 over 87 texts where recognized. Besides L’Asino, the other mismatch was the Storie Fiorentine by Machiavelli that was set closest to Storie Fiorentine del 1378 al 1509 by Guicciardini. It seems clear that the closeness of the subjects treated in the two texts played a fundamental role in the attribution.

It is interesting trying some conjectures on why artificial texts made up by LZ77 extracted dictionary worked better in our experiment. Probably the main reason is that LZ77 very often puts some correlation between characters and actual words by grouping them into a single word, while clearly this correlation does not exist using natural words. In a text written to be read, words and/or characters are correlated in a precise way, especially in some cases (one of the most strict, but probably less significant, is “,” followed by a capital letter). These observations could maybe suggest that LZ77 is able to capture correlations that are in some sense a signature of an author, this signature being stronger (up to a certain point, of course) than that of the subject of a particular text. On the other hand this ability of keeping memory of correlations, combined with the specificity of poetic register, could also explain the apparent strength of poetic pattern that seems to emerge from our experiments.
We have also performed some additional experiments on a corpus of English texts. Results are shown in Table IV. In this corpus there were a few poetic texts which, as we could expect, afflicted in some cases ATC. It is worth noting, in fact, that the number of ATC failures is 7, and in this case it’s higher than that of actual text comparisons, which is 4. However, if we look carefully we note that 4 of this 7 mismatches come from the 5 Marlowe works present in our corpus. Among Marlowe’s works only 1 is mis-attributed by actual text comparison, too. This peculiarity of Marlowe roused our interest and we analyzed carefully Marlowe’s results. We found that one of the 4 bad attributions was a poetic text, Hero, and was attributed to Shakespeare, while the remaining 3 unrecognized texts were all attributed to Shakespeare. Similar results were obtained using the NATC method which also does not allow for a clear distinction between Marlowe and Shakespeare. Just as a matter of curiosity, and without entering in the debate, we report here that, among the many thesis on the real identity of Shakespeare, there is one who claims Shakespeare was just a pseudonym used by Marlowe to sign some of its works. The Marlowe Society embraces this cause and has presented many works which should prove this theory, or at least make it plausible (starting of course by confuting the official date of death of Marlowe, 1593).

Before concluding this section several remarks are in order concerning our minimum cross-entropy method used to perform authorship attribution. Our criterion has been that of saying that the X should be attributed to a given author if another work of this author is the closest (in the cross-entropy ranking) to X. It can happen, and sometimes this is the case, that the second-closest text to X belongs to another author, different from the first. Said in other words, in the ranking of relative entropies between the X text and all the other text of our corpus, works belonging to a given author are far from clustering in the same zone of the ranking. This fact can be easily explained with the large variety of features that can be present in the production of an author. Dante, for instance, wrote both poetry and prose, this latter both in Italian and Latin. In order to take into account this non-homogeneity we decided to set authorship by watching only at the closest text to the unknown one. In fact, for what we have said, averaging or taking into account all the texts of every author could introduce biases given to the heterogeneity in each author’s production. Our choice is then perfectly coherent with the purpose of authorship attribution which is not to determine an average author of the unknown text, but who wrote that particular text. The limit of this method is the assumption that if an author wrote a text, then he is likely to have written a similar text, at least with regard to structural or syntactic aspects. From our experiments we can say, a posteriori, that this assumption does not seem to be unrealistic.

A further remark concerns the fact that our results for authorship attribution could only provide with some hints about the real paternity of a text. One cannot, in fact, never be sure that the reference corpus contains at least one text of the unknown author. If this is not the case we can only say that some works of a given author resembles to the unknown text. On the other hand the method could be highly effective when one has to decide among a limited and predefined set of candidate authors: see for instance the Wright-Wright problem \[67\] and the Grunberg-Van der Jagt problem in The Netherlands \[67\].

From a general point of view, finally, it is important to remark that the ATC method is of much greater interest than the NATC one. In fact, even though in linguistic related problem the two methods give comparable results, ATC can be used with every set of generic sequences, while the NATC requires a precise definition of words in the original strings.

### V. SELF-CONSISTENT CLASSIFICATION

In this section we are interested in the classification of large corpora in situations where no a priori knowledge of corpora’s structure is given. Our method, mutated by the phylogenetic analysis of biological sequences \[68, 69, 70\], considers the construction of a distance matrix, i.e. a matrix whose elements are the distances between pairs of texts. Starting from the distance matrix one can build a tree representation: phylogenetic trees \[70\], spanning trees etc. With these trees a classification is achieved by observing clusters that are supposed to be formed by similar elements. The definition of a distance between two sequences of characters has been discussed in section II.b.

<table>
<thead>
<tr>
<th>AUTHOR</th>
<th>Number of texts</th>
<th>Successes: ATC</th>
<th>Successes: NATC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bacon</td>
<td>6</td>
<td>6</td>
<td>6</td>
</tr>
<tr>
<td>Brown</td>
<td>3</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>Chaucer</td>
<td>6</td>
<td>6</td>
<td>6</td>
</tr>
<tr>
<td>Marlowe</td>
<td>5</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>Milton</td>
<td>8</td>
<td>8</td>
<td>7</td>
</tr>
<tr>
<td>Shakespeare</td>
<td>37</td>
<td>37</td>
<td>37</td>
</tr>
<tr>
<td>Spencer</td>
<td>7</td>
<td>5</td>
<td>6</td>
</tr>
<tr>
<td>TOTALS</td>
<td>72</td>
<td>68</td>
<td>65</td>
</tr>
</tbody>
</table>

TABLE IV: Author recognition: This table illustrates the results for the experiments of author recognition. In this case ATC results were afflicted by the presence in the corpus of a few poetic texts that, as we have discussed, tend to recognize each others.
Suppose to have a collection of texts written in different contexts: that of relationships between languages and the distances between nodes and leaves.

For the sake of clarity in the representation, we have chosen a constant length for the distances between nodes and between nodes and leaves.

A. Author trees

In our applications, we used the Fitch-Margoliash method of the package PhylIP (Phylogeny Inference Package) which basically constructs a tree by minimizing the net disagreement between the matrix pairwise distances and the distances measured on the tree. Similar results have been obtained with the Neighbor algorithm. The first test for our method consisted in analyzing with the Fitch-Margoliash procedure the distance matrix obtained by the corpus of Italian texts used before for authorship attribution. Results are presented in Figure 4. As it can be seen, works by the same author tend to cluster quite well in the presented tree.

B. Language trees

The next step was applying our method in a less obvious context: that of relationships between languages. Suppose to have a collection of texts written in different languages. More precisely, imagine to have a corpus containing several versions of the same text in different languages, and to be interested in a classification of this corpus. In order to have the largest possible corpus of texts in different languages, we have used: “The Universal Declaration of Human Rights” which sets the Guinness World Record for the most translated document.

We proceeded here for our analysis exactly as for author trees. We analyzed with the Fitch-Margoliash method the distance matrix obtained using the Artificial Text Comparison method with 5 artificial texts for each real text. After averaging on the Artificial Texts sharing the same root, we have built up the distance matrix as discussed in section II.b. In Figure 5, we show the tree obtained with the Fitch-Margoliash algorithm for over 50 languages widespread on the Euro-Asiatic continent. We can notice that essentially all the main linguistic groups (Ethnologue source) are recognized: Romance, Celtic, Germanic, Ugro-Finnic, Slavic, Baltic, Altaic. On the other hand, one has isolated languages as well as few isolated languages as the Maltese, typically considered non-Indo-European languages and whose origins and relationships with other languages are uncertain. The tree is unrooted, i.e., it does not require any hypothesis about common ancestors for the languages and it cannot be used to infer information about common ancestors of the languages. For more details see the text. The lengths of the paths between pairs of documents measured along the tree branches are not proportional to the actual distance between the documents.

FIG. 4: Italian Authors’ tree: Tree obtained with Fitch-Margoliash algorithm using the P pseudo-distance built from ATC method for the corpus of Italian texts considered in sect.IV.b. For sake of clarity in the representation, we have chosen a constant length for the distances between nodes and between nodes and leaves.

FIG. 5: Indo-European family language tree: This figure illustrates the phylogenetic-like tree constructed on the basis of more than 50 different versions of the “The Universal Declaration of Human Rights”. The tree is obtained using the Fitch-Margoliash method applied to the symmetrical distance matrix based on the R distance defined in sect. II.b built from ATC method. This tree features essentially all the main linguistic groups of the Euro-Asiatic continent (Romance, Celtic, Germanic, Ugro-Finnic, Slavic, Baltic, Altaic), as well as few isolated languages as the Maltese, typically considered an Afro-Asiatic language, and the Basque, classified as a non-Indo-European language and whose origins and relationships with other languages are uncertain. The tree is unrooted, i.e., it does not require any hypothesis about common ancestors for the languages and it cannot be used to infer information about common ancestors of the languages. For more details see the text. The lengths of the paths between pairs of documents measured along the tree branches are not proportional to the actual distance between the documents.
as the Maltese, typically considered a Semitic language because of its Arabic base, and the Basque, a non-Indo-European language whose origins and relationships with other languages are uncertain. The results are also in good agreement with those obtained by true sequences comparison reported in \[52\] with a remarkable difference concerning the Ugro-Finnic group here fully recognized, while with true texts Hungarian was put a little apart.

After the publication of our tree in \[83\] a similar tree, using the same dataset, has been proposed in \[52\] using $NCD(x, y)$ (see Sect. IIB) estimated with gzip.

It is important to stress how these trees are not intended to reproduce the current trends in the reconstruction of genetic relations among languages. They are clearly biased by the fact of using entire modern texts for their construction. In the reconstruction of genetic relationships among languages one is typically faced with the problem of distinguishing vertical (i.e. the passage of information from parent languages to child languages) from horizontal transmission (i.e. which includes all the other pathways in which two languages interact). This is the main problem of lexicostatistics and glottochronology \[83\] and the most widely used method is that of the so-called Swadesh 100-words lists \[77\]. The main idea is that of comparing languages by comparing lists of so-called basic words. These lists only include the so-called cognate words ignoring as much as possible horizontal borrowings of words between languages. It is clear now how an obvious source of bias in our results is represented by the fact of non-having performed any selection of words to be compared. It turns out then that in our trees English is closer to Romance languages simply because almost 50% of English vocabulary has been borrowed from French. These borrowings should be expunged if one is interested in reconstructing the actual genetic relationships between languages. Work is presently in progress in order to merge Swadesh list techniques with our methods \[77\].

\section{VI. DISCUSSION AND CONCLUSIONS}

We have presented here a class of methods, based on the LZ77 compression algorithm, for information extraction and automatic categorization of generic sequences of characters. The essential ingredient of these methods is the definition and the measure of a remoteness and of a distance between pairs of sequences of characters. In this context we have introduced in particular the notion of dictionary of a sequence and of Artificial Text (or Artificial Sequence) and we have implemented these new tools in an information extraction scheme (ATC) that allows to overcome several difficulties arising in the comparison of sequences.

With these tools in our hands, we have focused our attention on several applications to textual corpora in several languages, since in this context it is particularly easy to judge experimental results. We have at first shown that dictionaries are intrinsically interesting and that they contain relevant signatures of the texts they are extracted from. Then in a first series of experiments we have shown how we can determine, and then extract, some semantic attributes of an unknown text (its language, author or subject). We have also shown that comparing artificial texts, instead of actual sequences, gives better results in most of these situations. In the linguistic context, moreover, we have been able to define natural artificial texts (NAT) exploiting the presence of natural language words in the analyzed texts. Results from experiments indicate that this additional information does not produce any advantage, i.e. the NAT comparison (NATC) and ATC yield to the same results. However, the question is not whether NATC performs better than ATC. From a general point of view, in fact, the ATC method is of much greater interest with respect to the NATC one. In fact, while in linguistic related problems the two methods equally perform, in many cases NATC are impossible to construct because outside linguistics there is no precise definition of word. On the other hand the fact that ATC and NATC perform at least equally well in linguistics motivated problems, is a good news because one can reasonably infer that the situation will not change drastically in situations where NATC will not be available anymore.

A slightly different application of our method is that of the self-consistent classification of a corpus of sequences. In this case we do not need any information about the corpus, but we are interested in observing the self-organization that arises from the knowledge of a matrix of distances between pairs of elements. A good way to represent this structure can be obtained using phylogenetic algorithms to build a tree representation of the considered corpus. In this paper we have shown how the self-organized structures observed in these trees are related to the semantic attributes of the considered texts.

Finally, it is worth stressing once again the high versatility and generality of our method that applies to any kind of corpora of character strings independently of the type of coding behind them: texts, symbolic dynamics of dynamical systems, time series, genetic sequences, etc. These features could be potentially very important for fields where the human intuition can fail: genomics, geological time series, stock market data, medical monitoring, etc.

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