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Extending the Role of Computational Fluid Dynamics in Screw Machines

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ABSTRACT

Previous publications show that Computational Fluid Dynamics (CFD) can be readily used for the flow prediction and analysis of screw compressors. Several case studies are presented in this paper to show the scope and applicability of such methods. These include solid-fluid interaction in screw compressors, prediction of flow generated noise in screw machines, cavitation modelling in gear pumps, and flow in multiphase pumps for oil and gas industry. Numerical grids for all these cases were generated by us of an in-house grid generator, while the CFD calculations were performed with a variety of commercially available CFD codes.

In order to validate the accuracy of the CFD calculations, an extended test programme was carried out using Laser Dopler Velocimetry (LDV) to measure the mean and fluctuating velocity distribution in screw compressor flow domains. The measurement results are then compared with the CFD simulations. The results confirm the viability of the developed techniques.

It is shown in this publication that the flexibility of the developed method creates further opportunities for a broader use of Computational Fluid Dynamics for analysis of twin screw machines in a range of new applications.

1 INTRODUCTION

Screw compressors are today the most common type of positive displacement compressors used in industry. Due to their compactness, efficiency and reliability the operating range of these machines is continually being increased [21]. Consequently similar machines are used as liquid and gas expanders, multiphase pumps, vacuum pumps, superchargers, fuel pumps etc. There is a continual demand for performance improvements in screw machines such as increased flow rates and operating pressures and also alterations to meet new environmental protection legislation which require reduced pollution and increased efficiency. Thus, more refined analytical procedures are required to help the designers of such machines to meet these requirements. Three dimensional computational Fluid Dynamics (CFD) permits detailed analyses which may help in achieving the required goals. In the past, this technique has attracted the interest of many investigators and it is now used in a wide range of applications. CFD is based on the numerical solution of the conservation laws of mass, momentum and energy, derived for a given quantity of matter, called a control mass. Early developments in CFD were facilitated mainly by the automotive and aero industries for the
prediction of external flows. A comprehensive overview of available methods for the utilization of CFD is given by Ferziger and Perić [6].

The calculation of internal unsteady flows was for a long time regarded of secondary importance. However, with increased demands for accurate prediction of flows in internal combustion engines, compressors and other types of machines, CFD analysis became particularly interesting for internal flows within moving boundaries. In the last decade it was shown that ability to accurately predict flows in screw machines gives competitive advantage to manufacturers of such machinery. There are two basic issues which make such calculation difficult. Firstly, due to the complex geometry of its internal passages, the flow regimes inside a screw displacement machine can vary significantly within different flow domains. Secondly, it can be very difficult to replace such domains with a computational grid of sufficient quality for accurate and reliable calculation. A pioneering approach, published in the works of Demirdžić, Perić and Muzaferija, [4], [18] enabled the calculation of such flows with a variety of grid topologies by use of finite volume methods of discretisation.

Initially, many attempts to model screw machines by CFD methods were unsuccessful due to inability to generate an appropriate numerical grid for complex moving domains. The breakthrough was made when an analytical transfinite interpolation method with adaptive meshing was used to establish an automatic numerical mapping method for arbitrary screw compressor geometry. It is explained in detail by Kovacevic, [11]. This method follows the procedure for rotor generation, fully elaborated in detail in [20], and was later regularly used for grid generation in analysis of the processes in screw compressors. The interface grid generation program is called SCORG - Screw COmpressor Rotor Geometry Grid generator. This software suite enables numerical mapping of both, moving and stationary parts of the machine and direct integration in commercial CFD or CCM codes. Thus, Kovačević, Stošić and Smith published a number of papers between 1999 and 2008, [9], [10], [12], [14] presenting feasible 3-D numerical analysis of fluid flow and stress analysis in screw compressors by use of Computational Continuum Mechanics (CCM). A monograph on CFD in screw machines [12], published by the same authors, gives a more comprehensive

Figure 1 Numerical mesh for CFD calculation of screw compressor
overview of the methods and tools used. These are applicable to the majority of commercial CFD software packages and can accommodate use of a variety of CAD systems [14]. A typical arrangement of a numerical mesh for the CFD calculation of screw compressors is shown in

Figure 1. The moving parts of the flow domain are mapped with a hexahedral block structured numerical mesh while the remaining stationary parts are modelled by an unstructured polyhedral mesh, produced directly from a CAD system [18], by the proprietary commercial grid generators suitable for non moving geometries. Although mainly used for CFD in screw machines, the same concept may be utilized for a variety of other applications, for example, in the grid generation of the flow paths in a rotary heat exchanger [1].

The first experimental verification of the numerical results was obtained in 2002 and reported in [9]. This study was performed on an oil injected screw compressor of a 5/6 lobe configuration with a male rotor outer diameter of 128 mm of 'N' type profile. The numerical mesh used, contained just over half a million grid cells, of which about 200,000 were used to map the moving parts of the grid, the rotors and space between them. A converged solution was obtained on an office PC after 120 time steps each requiring approximately 15 minutes of computing time.

The results were compared with measurements obtained from a laboratory air screw compressor. Four piezo-resistive transducers were positioned in the housing to measure pressure fluctuations across the compressor. The numerical and experimental results were compared for discharge pressures of 6, 7, 8 and 9 bar. Good agreement was obtained both for the integral performance parameters, as well as for the instantaneous pressure values, as shown in Figure 2. The report [9] also discussed the effects of various factors that influenced the calculation accuracy. These included variations in the mesh size, different turbulence models and differencing schemes. It was concluded that these variations did not affect the overall calculation accuracy significantly. Therefore the method was recommended as a reliable procedure for performance calculations in industry.
However it was also shown that use of different differencing schemes and turbulence methods significantly influences predictions for local velocity and pressure values in certain machine regions. Although these differences have a low impact upon the overall performance, their influence upon flow development needs further investigation. Very few authors have analysed local effects in screw compressors. Examples are the work of Vimmr [22], following Kauder et al [8], who analysed the flow of a single leakage path through a static mesh at the male rotor tip to conclude that the rotor relative velocity does not affect flow velocities significantly and that none of the turbulence models used change the modelling outcome significantly. This agreed with the findings of Kovacevic et al [12], but also confirmed that further validation of full 3-D CFD calculation results could not be obtained by the use of simplified numerical or experimental methods. For this, a full understanding of the local velocities in the machine suction, compression and discharge chambers was needed.

2 FLOW MEASUREMENTS IN A SCREW COMPRESSOR BY USE OF LASER DOPPLER VELOCIMETRY

The instrumentation for measuring complex flows in a screw compressor must be robust to withstand the unsteady aerodynamic forces and oil drag, must have a high spatial and temporal resolution and most importantly may not disturb the flow. Point optical diagnostics, such as Laser Doppler Velocimetry [3], [2], [5], can fulfil these requirements [15]. In order to measure flow velocities inside a screw compressor, an experiment, using this technique, was set up at City University and an extensive study was performed to measure velocities in the compression domain and in the discharge chamber of an air screw compressor, as reported by Guerrato et al, [7].
A transparent window for optical access into the rotor chamber of the test compressor was machined from acrylic to the exact internal profile of the rotor casing and was positioned on the pressure side of the compressor near the discharge port, as shown in Figure 3. After machining, the internal and external surfaces of the window were fully polished to allow optical access. Optical access to the discharge chamber was arranged through a transparent plate, 20 mm thick, installed on the upper part of the exhaust pipe. The optical compressor was then installed in a standard laboratory air compressor test rig, modified to accommodate the transmission of a laser beam and its traverses, as shown to the right of Figure 3. The laser Doppler Velocimeter operated in a dual-beam near backscatter mode. It comprised a 700 mW argon-ion laser, a diffraction-grating unit, to divide the light beam into two and provide frequency shift, and collimating and focusing lenses to form the control volume. A Fibre optic cable was used to direct the laser beam from the laser to the transmitting optical system, and a mirror was used to direct the beams from the transmitting optics into the compressor through one of the transparent windows. The collecting optics were positioned around 25° of the rotor chamber and 15° of the discharge chamber to the full backscatter position and comprised collimating and focusing lenses, a 100 μm pin hole and a photomultiplier equipped with an amplifier. The signal from the photomultiplier was processed by a processor interfaced to a PC and led to angle-averaged values of the mean and RMS velocities. In order to synchronise the velocity measurements with respect to the location of the rotors a shaft encoder that provides one pulse per revolution and 3600 train pulses, with an angular resolution of 0.1°, was used and fixed at the end of the drive shaft. Instantaneous velocity measurements were made over thousands of shaft rotations to provide a sufficient number of samples. In the study described, the average sample density was 1350 data per shaft degree. Since the processing software enables use of 4 external channels, one of them was used to collect the pressure signal coming from the high data rate pressure transducer via an amplifier.

Figure 3  Optical compressor (left), LDV optical set for discharge chamber (right)

2.1  Flow measurements within the compression chamber
Two coordinate systems were defined within the rotor chamber of the compressor, one for the male and the other for the female rotor. The female rotor coordinate system is shown in Figure 4. Each of them was applied to one of the rotors where $\alpha_p$ and $R_p$ are, respectively, the angular and radial position of the control volume and $H_p$ is the distance from the discharge port centre. Taking the
appropriate coordinate system, measurements were obtained at \( R_p = 48, 56, 63.2 \) mm, \( \alpha_p = 27^\circ \) and \( H_p = 20 \) mm for the male rotor, and at \( R_p = 42, 46, 50 \) mm, \( \alpha_p = 27^\circ \) and \( H_p = 20 \) for the female rotor.

Figure 4 (a) Coordinate system and the window; (b) Axial plane view
Figure 5: LDV measurements of the axial velocity in the working chamber (top), Schematic representation of zones in the compressor interlobe domain (bottom)

Typical velocity values measured in the working chamber are shown in Figure 5. Three zones were identified in the working chamber near the discharge port. Zone (1) covers most of the main trapped working domain with fairly uniform velocities. Zone (2) is associated with the opening of the discharge port. The velocities and turbulence in this zone are much higher than in Zone (1). In this zone the flow is driven by the pressure difference between rotors and the discharge chamber, which is especially visible in this case as the pressure in the discharge system was maintained at practically atmospheric conditions. Zone (3) is associated with the leakage flows between the rotors and the casing, where velocities increase to values higher than in Zone (1) but are not as chaotic as in Zone (2).

Conclusions derived from the measurements are explained in more detail in [7], and are summarised as follows: (1) Chamber-to-chamber velocity variations were
up to 10% more pronounced near the leading edge of the rotor. (2) The mean axial flow within the working chamber decreases from the trailing to the leading edge with velocity values up to 1.75 times larger than the rotor surface velocity near the trailing edge region (3). The effect on velocities of the opening of the discharge port is significant near the leading edge of the rotors and causes a complex and unstable flow with very steep velocity gradients. The highest impact of the port opening on the flow is experienced near the tip of the rotor with values decreasing towards the rotor root.

2.2 Flow measurements within the discharge chamber

Figure 6 (a) shows a schematic arrangement of the discharge chamber divided into the discharge port domain and the discharge cavity. Figure 6 (b) and (c) show the measurement locations for two characteristic cross sections called the W and V sections. The coordinate system, drawn in all of the sketches in Figure 6, identifies the location of the measured CV. Measurements were made at $X_p=5.5\text{mm}$, $Z_p=13\text{mm}$ and $Y_p=-8$ to $13\text{mm}$.

Typical measured results obtained by LDV in the discharge chamber are shown in Figure 7. The axial mean flow velocities are obtained at a rotational speed of 1000 rpm and a pressure ratio of 1.0. The most important findings are as follows.

1. Velocities are higher than in the compression chamber due to fluid expansion in the port between sections W and V.
2. The axial velocity distribution within the discharge chamber is strongly related to the rotor angular position since the rotors periodically cover and expose the discharge port through which, at some point, more then one working chamber is connected. The left diagram in Figure 8 shows the case when only one compression chamber is connected to the discharge port and the flow is relatively stable. This corresponds to the domains to the left of the port opening line in diagrams in Figure 7. As another chamber with high pressure flow connects to the discharge chamber, in the right diagram in Figure 8, jet like flows occur near the sides of the discharge chamber passage. These are rendered with high velocities in the domain to the right of the thick port.
opening line in Figure 7. (3) The jet flows create velocity peaks making the flow in that region highly turbulent.

Figure 7 LDV measured axial velocity component inside the discharge chamber: male rotor side (left), female rotor side (right)

Figure 8 Schematic view of the periodic exposure of working domains to the discharge port
3 VALIDATION OF CFD RESULTS BY LDV MEASUREMENTS

The numerical mesh used for CFD calculation is shown in Figure 1. The flow paths around the rotating machine parts are generated using the in-house developed software package SCORG. The pre-processing script generated in SCORG is then used to connect the mesh for the rotating parts with the stationary numerical mesh of the compressor ports and other housing elements, generated directly from a CAD system. They are then transferred together to the commercial CFD solver.

For the purpose of obtaining the grid independent solution, three different meshes were generated, the smallest consisting of 600000 numerical cells, the mid sized mesh consisting of 935000 numerical cells and the largest with 2.7 million cells. Results used for comparison with LDV measurements in this paper are obtained on the mid sized mesh. One full rotation of the male rotor that consisting of 300 time steps was sufficient to obtain a converged solution. Each time step took approximately 25 minutes of computer time.

3.1 Compression Chamber
The compressor working conditions and the position of the control volumes are identical for the CFD calculation and the LDV measurements. Figure 9 shows a comparison of the axial mean velocities in the compression chamber close to the discharge port. This figure shows a very good agreement throughout Zone (1) and Zone (2), as specified in Figure 5. In Zone (3), both the measured and calculated velocities increase but the increase in calculated velocities is larger than in the measured ones. It is believed that this difference is due to the inability of the k-e turbulence model to cope with near wall flows in the large numerical cells existing there. Such a configuration of the numerical mesh is a consequence of the methodology used for the generation and movement of the numerical mesh, as explained in more detail in [12].

Figure 9 Comparison of the LDV and CFD axial velocities in the compression domain

The circumferential velocities in the measured cross section are shown in Figure 10. Since the compression chamber closes very quickly in that area and the flow is mainly driven towards the axial discharge port, the circumferential velocities...
are low. Moreover, since the numerical mesh in each cross section contains 2640 cells, while there are only 240 numerical cells in the axial direction, it is necessary to interpolate velocities between neighbouring numerical cells. That inevitably leads to decreased accuracy, especially for low velocity flows with high local pressure gradients. Therefore, the difference between the measured and calculated circumferential velocity values is larger. Despite this, the calculation results show fairly good agreement with the measured values. Since the predicted integral parameters and pressure correlate well with the measured values, it is reasonable to assume that the small difference between the velocities in the circumferential direction does not play a significant role overall.

![Velocity Profile for the Male rotor at Hp=22mm, θ=27°](image1)

**Figure 10** Comparison of the LDV and CFD circumferential velocities inside the compression chamber

### 3.2 Discharge Port

Figure 11 shows a comparison of the axial velocities in the discharge port. The differences appear to be rather large at locations where velocities are measured, although the trends and mean values are similar. It was confirmed by calculation that the highest values of axial velocity are in the middle section through the discharge port, which corresponds to the period of time when only one working chamber is connected to the discharge chamber.
Figure 11 Comparison of the measured and calculated axial velocities in the discharge chamber

On both the male rotor side of the discharge port, as shown in the left diagram of Figure 11, and on the female rotor side of the port, shown in the right diagram, the velocities during that process decrease towards the walls. However during the phase when another working chamber is connected to the discharge port, the velocities near the walls increase due to the jet like flows induced by the higher pressure differences on the outside of the rotors.

Moreover the leakage flows between the compression and discharge chambers, just prior to the opening of the discharge port, are large as presented in Figure 12. These cause an increase in velocity in the central region of the discharge chamber.

Figure 12 Axial velocities in three characteristic cross sections in the discharge region of the compressor

The measurements suggest that turbulence plays a significant role in the narrow passage which connects the compression chamber with the large discharge domain. The lack of an existing turbulence model to calculate the near wall velocity values properly is probably the main reason why the CFD results do not replicate the measured values better. Therefore further research into turbulence models for internal flow in the compressor ports may be needed. Since it seems that the flow turbulence on both sides of that region is not so intensive, and since the internal energy in positive displacement machines is significantly higher than the flow kinetic energy, this discrepancy obviously does not greatly affect the overall performance estimation. However, despite this, further development and improvement of the CFD codes are necessary.
4 CASE STUDIES

The following four case studies are presented to demonstrate the flexibility of the method:

1) Calculation of fluid-solid interaction in screw compressors.
2) Estimation of pressure oscillations for noise prediction in a screw compressor discharge port
3) Investigation of cavitation in a helical gear pump
4) CFD modelling of a multiphase screw pump.

A numerical mesh was obtained in all cases, by the in-house grid generator described earlier in this paper. However, the CFD calculations were performed by a different CFD numerical solver in each case.

4.1 Fluid solid interaction
Fluid solid interaction in screw compressors was investigated in three common applications of screw compressors, namely an oil-injected air compressor of moderate pressure ratio, a dry air compressor, of low pressure ratio, and a high pressure oil flooded compressor. In all cases the rotors were of the 'N' type with a 5/6 lobe configuration.

Rotor deformation in an ordinary oil injected air screw compressor is caused mainly by pressure forces. The compressor in this analysis was working between 1 bar suction and 8 bar discharge pressure. Rotor deformation increases the clearance gaps between the rotors but by an order of magnitude smaller than the rotor clearances. Therefore this does not greatly affect compressor performance. In order to make the results visible, the deformations in Figure 13 are enlarged 20000 times and presented on the deformed numerical mesh.

In the oil free air compressor, due to the lack of cooling, the air temperature rise is much higher. For 3 bar discharge pressure the exit temperature has an average value of 180°C. The rotor deformation is presented in the left of Figure 14. The fluid temperature in the immediate vicinity of the solid boundary changes rapidly,
as shown in the right diagram of the same figure. However, the temperature of the rotor pair is lower due to the continuous temperature averaging as shown in the right diagram of Figure 14. Deformation tends to reduce the clearance between the rotors. To be visible on the deformed mesh, these are magnified 5000 times.

![Figure 14](image1.png)

**Figure 14** Rotor displacement vectors and temperature distribution for an oil free compressor

![Figure 15](image2.png)

**Figure 15** Deformation of high pressure oil injected compressor rotors

The oil injected high pressure application of a CO₂ refrigeration compressor with suction at 30 bar and 0°C and discharge at 90 bar and 40°C is shown in Figure 15. In this case, the large pressure difference is the main cause of the rotor deflection. The highest deformation is in excess of 15μm. The deformation pattern of the rotors is similar to the low pressure case but with slight enlargement at discharge.

Figure 16 shows the temperature distribution and rotor deformation in a combined compressor-expander intended for fuel cell application. The deformation of the rotors is substantially smaller than in the case of the compressor or expander alone. The nature of the deformation suggests that the design of the compressor-expander needs special attention specially in selecting the material for the rotors and casings. More details can be found in [10].

![Figure 16](image3.png)
4.2 Use of CFD for Noise Prediction

Identification of sources of noise and noise attenuation has become an important issue for the majority of screw compressor applications. Pressure fluctuations in the discharge port not only generate aeroacoustics in that domain but also induce mechanical noise due to rotor rattling. It was confirmed in previous studies that adequate porting can decrease the noise level and improve the machine performance. A thermodynamic model was set up to estimate pressure oscillations as a function of the discharge port shape and the cross sectional area of the connecting flange. These predictions are convenient for the estimation of the main noise harmonics. However, this model does not take into account the shape of the discharge chamber which probably plays an important role in the generation of higher harmonics. Therefore further steps were undertaken to analyse pressure fluctuations in the discharge port by use of a full 3-D CFD code, Figure 17.
The results obtained by the 3-D model agree very well with measurements, [16] but the model is too computation intensive for everyday industrial use. Therefore a combined model was developed which combines the accuracy of the full 3D model and the speed of a thermodynamic chamber model [13]. A comparison of these three models is presented in Figure 18. More details are given in [17] and [14].

4.3 Cavitation in gear pumps

Gear pumps are often used in the automotive and aero industries to supply fuel to an engine. A fuel gear pump geometry of is very similar to that of a screw compressor. It has two rotors with either straight or helical lobes which are contained in a housing and connected to other flow paths of the system through the suction and discharge chambers. The left side of Figure 19 shows a numerical mesh of such a gear pump. The hexahedral numerical mesh of rotors and flow around them was generated by SCORG, while the stationary parts were meshed by ANSYS CFX and ICEM tools into a tetrahedral mesh. These two domains were connected through transient sliding interfaces, readily available in the CFX solver.

Erosion damage, caused by cavitation, was noticed on the running pump at the rotor shafts and within the gaps. The results presented here have been previously
given in [19]. The authors demonstrated the capability to generate the numerical mesh in such machines by the use of the SCORG software. The CFD calculation showed that cavitation occurred in the flow through the interlobe gaps in the direction towards the suction chamber. It was outlined in [19] that the main challenge for a successful computation is a relatively complex geometry of the moving and deforming grids, as well as the transient interface. This was fully overcome by use of the SCORG software.

![Figure 19 Numerical mesh of the gear pump and the occurrence of cavitation](image)

**4.4 CFD analysis of a multiphase screw pump**

Multiphase screw pumps are regularly used in the oil and gas industry. A CFD analysis of the leakage flow and pressure distribution in these pumps has been calculated by Star CCM+. As an example, the pressure distribution on the first layer of cells of the 3/3 lobe combination rotors of a down hole pump passage flows for 1-10 bar pressure rise is presented in Figure 20. The leakage flow through the clearances and blow hole area is shown in the same figure.

![Figure 20 Pressure distribution and leakage flow on multiphase down hole pump](image)
The numerical grid was similarly generated by the SCORG grid generator, developed for screw compressors. In addition to the standard twin-screw arrangements, this grid generation software can generate multi-rotor arrangements as shown in Figure 21. The pressure distribution for the multi-rotor applications was calculated by StarCCM+. The machine with three female rotors shown in Figure 21 achieves a smaller pressure drop between its interlobes than in the pump with two female rotors. This means that lower leakage flows are achieved in the machine with more female rotors. The integration of pressure force over the rotor surfaces shows that the load on the female rotors is more or less independent of their number.

**CONCLUSIONS**

Comparison of estimated and measured velocities within a test optical screw compressor has confirmed the validity of CFD methods as a means of calculating both local and bulk velocities within twin screw machines. It has been shown that the modelling accuracy may be further improved by local tuning of the CFD model, including the use of turbulence models suitable for complex pressure driven internal flows.

It has also been shown that CFD modelling can be used not only for estimation of the screw compressor performance, but also for capturing of phenomena not possible by the use of other, simplified models. Case studies confirm that a number of available CFD and CCM software packages can be used for this purpose if combined with the SCORG mesh generator. These applications include prediction of multiphase flows in screw and gear pumps, even in configurations that differ from classical twin screw arrangements.

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