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### Vibration-based structural performance assessment via output-only sub-Nyquist/compressive wireless sensor data

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ABSTRACT: This paper assesses two different approaches for efficient output-only Vibrationbased Structural Health Monitoring (V-SHM) in large-scale civil engineering structures, promoting the use of dense arrays of low-power wireless sensors. Firstly, a non-uniform deterministic sub-Nyquist multi-coset sampling scheme is considered to acquire ambient stationary structural response signals. This sampling scheme is coupled with a power spectrum blind sampling technique along with the frequency domain decomposition algorithm of operational modal analysis to obtain structural modal properties. This is accomplished without necessitating either signal reconstruction in the time-domain or signal sparsity assumption. Secondly, a spectro-temporal compressive sensing approach is considered applicable to cases where signal reconstruction in time-domain is desired , . The latter approach considers nonuniform in time random sampling at sub-Nyquist average rates informed by prior knowledge of signal sparsity gained through smart on-sensor operations and sensor/server communication. The usefulness and applicability of two approaches is numerically demonstrated by considering field recorded data pertaining to the monitoring of an overpass open to the traffic and of an operating on-shore wind turbine.

#### 1 INTRODUCTION

Vibration-based structural health monitoring (V-SHM) is widely used for structural assessment, design verification, and damage detection in civil engineering structures. In most field applications, V-SHM relies on output-only linear system identification techniques to extract the dynamic properties (e.g., natural frequencies and mode shapes) of vibrating structures subject to low-amplitude operational loads (e.g., due to wind traffic, etc.) (Brincker and Ventura (2015)). Such techniques consider acquiring and processing of *only* structural response signals recorded by relatively dense arrays of sensors. The excitation loads are not measured and are assumed to have a flat spectrum over a wide range of frequencies (i.e., white noise excitation assumption).

From a practical viewpoint, the use of wireless sensor networks (WSNs) offers low-cost and rapid V-SHM implementations compared to tethered sensors, especially in densely instrumented and geometrically complex structures (Lynch (2007)). However, the widespread adoption of WSNs in practical applications is hindered by limitations to the available wireless transmission bandwidth and by maintenance costs related to frequent sensor battery replacement requiring



(Lynch (2007)). To this end,, it has been recently recognized that WSNs operating on sub-Nyquist data acquisition schemes can provide low-power wireless sensors, while minimizing the onsensor data storage and local processing requirements prior to wireless transmission. Such considerations reduce WSNs' upfront and maintenance costs as well as increase WSNs' reliability for quality and robust V-SHM.

In this context,, advances in the field of compressive sensing (CS) have been recently considered by various researchers to facilitate cost-effective V-SHM using WSNs (O'Connor et al. (2014), Klis and Chatzi (2015; 2017), Yang and Nagarajaiah (2015), Park et al. (2014)). Specifically, CS considers random non-uniform in time response acceleration signal sampling to acquire a relatively small number of measurements, below the Nyquist rate. Then, the unknown full-length (Nyquist-sampled) signals are recovered, with high probability, from the acquired sub-Nyquist/compressed measurements by solving an underdetermined system of linear equations assuming a certain level of signal sparsity. Sparsity is a signal attribute related to the number of non-zero coefficients required to capture the signal energy on a given basis (see e.g. Donoho 2006). In this regard, all algorithms for sparse signal recovery necessitate an assumption of signal sparsity (Vaswani and Zhan 2016) which is unknown and is adversely affected by signal noise. To circumvent heuristically assumed sparsity signal levels in practical V-SHM settings, a spectro-temporal CS-based approach was developed by Klis and Chatzi (2015; 2017), which employs a re-weighted Basis Pursuit De-Noising algorithm (rwBPDN) (Becker et al. 2011) together with local on-sensor data processing and two-way wireless communication between sensor and server. The latter consideration allows for determining the underlying signal sparsity level prior to CS-based data acquisition, leading to improved time-domain signal recovery from the compressed measurements, at the cost of an increase wireless data transmission payload demands and communication protocols compared to the standard CS-based V-SHM (O'Connor et al. 2014). The recovered structural response acceleration signals can next be treated by any standard output-only V-SHM algorithm. Alternatively to the above CS-based approaches, Gkoktsi et al. (2016) adopted a *deterministic* multi-coset sub-Nyquist data acquisition (Venkataramani and Bresler 2001, Tausiesakul and Gonzalez-Prelcic 2013) in conjunction with a Power Spectrum Blind Sampling (PSBS) technique (Ariananda and Leus 2012, Tausiesakul and Gonzalez-Prelcic 2013) to support V-SHM without requiring signal sparsity knowledge. The considered PSBS-based method treats response acceleration signals as stochastic processes (in alignment with the theory of output-only V-SHM (Brincker and Ventura 2015), aiming to retrieve the second order statistics of structural responses (i.e., covariance/power spectrum density estimates) by solving an *overdetermined* system of linear equations free from the sparse signal assumption.. This signal-agnostic approach is coupled with the standard frequency domain decomposition algorithm (Brincker and Ventura 2015) to estimate structural modal properties from the compressed/sub-Nyquist measurements without signal reconstruction in time. In this manner, data processing and memory requirements at both sensor and server level are minimized.

In this paper, the efficiency of the PSBS-based method (Gkoktsi et al. 2016) and of the spectrotemporal *rwBPDN* approach (Klis and Chatzi 2015 and 2017), is numerically assessed in support of low-power WSNs that operate on sub-Nyquist data acquisition rates for output-only V-SHM. In this respect, the efficacy of the two adopted methods in extracting quality modal estimates is assessed vis-à-vis, using field recorded acceleration response data from a highway overpass under operational conditions. The performance of the two approaches is further evaluated for different data compression ratios, based on sub-Nyquist sampled data from an operating on-shore wind turbine. The remainder of the paper is organized as follows. Section 2 outlines the theoretical background of the two considered approaches. Sections 3 and 4 furnish numerical results



associated with the overpass and the with the wind turbine, respectively. Finally, Section 5 summarizes concluding remarks.

#### 2 THEORETICAL BACKGROUND

#### 2.1 Power Spectrum Blind Sampling (PSBS) approach

Let x(t) be a continuous in time t real-valued wide-sense-stationary stochastic process characterized in the frequency domain by the power spectrum  $P_x(\omega)$  band-limited by  $2\pi/T$ . It is desired to sample x(t) at a rate lower than the Nyquist sampling rate 1/T (in Hz), while maintaining a sufficiently accurate estimate of the power spectrum  $P_x(\omega)$ . To this end, the multi-coset sampling strategy is herein adopted (Ariananda and Leus 2012) according to which the grid of Nyquist samples x(nT) is divided into blocks of  $\overline{N}$  consecutive samples and from each block only  $\overline{M}$  ( $<\overline{N}$ ) samples are selected. The resulting sampling is periodic with period  $\overline{N}$ ; non-uniform since any subset of  $\overline{M}$  samples may be selected from a total of  $\overline{N}$  Nyquist-rate samples within each block; and deterministic since the position of the  $\overline{M}$  samples on the Nyquist grid of samples x(nT) is defined *a priori* and applies to all considered blocks. The above sampling strategy can be implemented by utilizing  $\overline{M}$  interleaved ADC units operating at a sampling rate of  $1/(\overline{NT})$ . At the *m-th* ( $m=0, 1, ..., \overline{M}$ -1) unit, the discrete-time signal x[n]=x(n/T) is first shifted by  $n_m$  samples and then uniformly sampled at  $1/\overline{NT}$  (in Hz). In this respect, an average sampling rate of  $\overline{M}/(\overline{NT})$ (in Hz) is defined, which is associated with the compression ratio  $\overline{M}/\overline{N}$ , with  $0 \le \overline{M}/\overline{N} \le 1$ , corresponding to lower values at stronger signal compression. Notably, the limiting case of  $\overline{M}=N$ (i.e.,  $\overline{M}/\overline{N}=1$ ) pertains to the Nyquist rate. Finally, the shifting values  $n_m$  are collected in the sequence  $\mathbf{n} = [n_0, n_1, \dots, n_{\overline{M}-1}]$  which defines the multi-coset sampling pattern.

Consider, next, an array of *D* sensors and  $\overline{M}$  cosets. The cross-correlation function of the acquired measurements  $y_{m_i}^{d_a}[l]$ ,  $y_{m_i}^{d_b}[l]$  can be computed for all  $m_i$ ,  $m_j = 0, 1, ..., \overline{M}$ -*l* cosets and  $d_a$ ,  $d_b=1$ , 2,..., *D* sensors as in  $r_{y_i^a, y_j^b}[k] = E_y \left\{ y_{m_i}^{d_a}[l] y_{m_j}^{d_b}[l-k] \right\}$ , where  $E_a\{\cdot\}$  is the mathematical expectation operator with respect to a. Further, the following relation holds (Gkoktsi et al. 2016)

$$\mathbf{r}_{\mathbf{y}^{a}\mathbf{y}^{b}} = \mathbf{R}_{c}\mathbf{r}_{\mathbf{x}^{a}\mathbf{x}^{b}},\tag{1}$$

where  $\mathbf{r}_{y^a y^b} \in \mathbb{R}^{\overline{M}^2(2L+1) \times D}$  is a matrix collecting the output cross-correlation sequences  $r_{y^a, y^b}[k]$  computed within the range (support)  $-L \leq k \leq L$ . Similarly,  $\mathbf{r}_{x^a x^b} \in \mathbb{R}^{\overline{N}(2L+1) \times D}$  is a matrix collecting the input cross-correlation sequences of the traditionally sampled signals (at Nyquist rate or above), given in  $r_{x^a x^b}[k] = \mathbf{E}_x \left\{ x^{d_a}[n] x^{d_b}[n-k] \right\}$ , and computed for all  $d_a$  and  $d_b$  sensors in the above range. Further,  $\mathbf{R}_c \in \mathbb{R}^{M^2(2L+1) \times \overline{N}(2L+1)}$  is a sparse pattern correlation matrix populated with the pattern cross-correlations (Ariananda and Leus 2012)  $r_{c_i,c_j}[n] = \delta[n - (n_{m_i} - n_{m_j})]$ , where  $\delta[n] = 1$  for n = 0 and  $\delta[n] = 0$  for  $n \neq 0$ . Note that Eq. (1) defines an overdetermined system of linear equations which can be solved for  $\mathbf{r}_{y^a y^b}$  without any sparsity assumptions, provided that  $\mathbf{R}_c$  is full column rank. The latter is satisfied for  $\overline{M}^2 \geq \overline{N}$  (Tausiesakul and Gonzalez-Prelcic 2013, Ariananda and Leus 2012). An unbiased estimator of the output cross-correlation sequence  $r_{y^a, y^b_i}[k]$  is then adopted (Gkoktsi et al. 2016) and used together with the DFT matrix,  $\mathbf{F}_{(2L+1)\overline{N}} \in \mathbb{C}^{\overline{N}(2L+1) \times \overline{N}(2L+1)}$  to obtain an estimate of the input cross-spectra  $\mathbf{s}_{x^a x^b}$  at the discrete frequencies  $\omega = [0, 2\pi/(2L+1)\overline{N}, \dots, 2\pi((2L+1)\overline{N}-1)/(2L+1)\overline{N}]$  (Tausiesakul and Gonzalez-Prelcic 2013)

$$\hat{\mathbf{s}}_{x^{a}x^{b}} = \mathbf{F}_{(2L+1)\bar{N}} \left( \mathbf{R}_{c}^{\mathrm{T}} \tilde{\mathbf{W}}^{-1} \mathbf{R}_{c} \right)^{-1} \mathbf{R}_{c}^{\mathrm{T}} \tilde{\mathbf{W}}^{-1} \hat{\mathbf{r}}_{y^{a}y^{b}}.$$
(2)



In the above equation,  $\tilde{\mathbf{W}}$  is a weighting matrix, the symbol "^" denotes matrix estimation, and the superscript "-1" denotes matrix inversion. The solution of Eq. (2) relies on the weighted least square criterion  $\hat{\mathbf{r}}_{x^{a_{x^{b}}}} = \arg \min_{\mathbf{r}_{x^{a_{x^{b}}}}} \|\hat{\mathbf{r}}_{y^{a_{y^{b}}}} - \mathbf{R}_{c}\mathbf{r}_{x^{a_{x^{b}}}}\|_{\tilde{\mathbf{W}}}^{2}$ , where  $\|\mathbf{a}\|_{\tilde{\mathbf{W}}}^{2} = \mathbf{a}^{T}\tilde{\mathbf{W}}\mathbf{a}$  is the weighted version of the Euclidean norm.

#### 2.2 Spectro-Temporal Compressive Sensing via rwBPDN

Spectro-Temporal Compressive Sensing (*STCS*) is based on the formulation of the missing data problem investigated by a number of authors (Candes 2007 and 2011, Becker 2011). Let  $\mathbf{x}_i = [x_{1i}, x_{2i}, ..., x_{Ni}]^T \in \mathbb{R}^N$  designate the complete *i*<sup>th</sup> signal recorded by the *i*<sup>th</sup> sensor of *N* data samples. The missing data estimation problem can be expressed as:

$$\mathbf{y}_i = \mathbf{S}\mathbf{x}_i \,. \tag{3}$$

The problem may be formulated as the task of inferring the full response time-series  $\mathbf{x}_i \in \mathbb{R}^N$  given the incomplete observation vector  $\mathbf{y}_i \in \mathbb{R}^M$  ( $M \ll N$ ), and the selection matrix  $\mathbf{S} \in \mathbb{C}^{M \times N}$ , so that (3) holds. A spectral representation of the complete response signal  $\mathbf{x}_i$  is accomplished using the orthonormal basis  $\mathbf{A} \in \mathbb{C}^{N \times N}$  of the Discrete Fourier Transform (DFT) as:

$$\mathbf{x}_{i} = \mathbf{A}\mathbf{c}_{i}, \text{ where } \mathbf{A}_{i,l} = \frac{1}{\sqrt{N}} e^{-j2\pi i \frac{l}{N}},$$
 (4)

where  $\mathbf{c}_i = [c_{1i}, c_{2i}, ..., c_{Ni}]^T \in \mathbb{R}^N$  is a sparse vector of coefficients. From the above equations, the observed vector  $\mathbf{y}_i$  can be cast in the form

$$\mathbf{y}_i = \mathbf{SAc}_i \,. \tag{5}$$

As demonstrated in previous work of the authors (Klis and Chatzi 2015 and 2017) the former representations allow to reconstruct the original (i.e, complete) response signal  $\mathbf{x}_i$ , by solving (5) for  $\mathbf{c}_i$  and inverting the transformation in (4). The sought solution for  $\mathbf{c}_i$  may be obtained via the following optimization problem, known as the *reweighed Basis Pursuit De-Noising problem* (*rwBPDN*) (Becker 2011)

$$\hat{\mathbf{c}}_{i} = \underset{\mathbf{c}_{i}}{\operatorname{arg minl}} \| \mathbf{W} \mathbf{c}_{i} \|_{1} \text{ subject to } \| \mathbf{y}_{i} - \mathbf{S} \mathbf{A} \mathbf{c}_{i} \|_{2} \leq \epsilon , \qquad (6)$$

where  $\mathbf{W} = diag([w_1, w_2, ..., w_N])$ , indicating the salient spectral elements. These weighting coefficients are the key feature of the Spectro-Temporal Compressive Sensing formulation. The weighting matrix  $\mathbf{W}$  is defined upon selection of a suitable threshold  $\epsilon_i$ , which defines the elements to be included in the so-called support vector  $\mathbf{U}$ . The support components are defined locally at the node level, and eventually transmitted to the server, where the weighting matrix is formed and the level of sparsity is decided upon. Sparsity *k* is defined as the ratio of the number of harmonic components, *K*, in the signal over its full dimension, *N*. The original signal is then reconstructed using the coefficient vector  $\hat{\mathbf{c}}_i$  defined in equation (6), via projection back to the time domain as in

$$\hat{\mathbf{x}}_i = \mathbf{A}\hat{\mathbf{c}}_i \,. \tag{7}$$

For further details on the steps involved, as well as the exchange of operations between the server and the nodes, the interested reader is referred to the work of Klis and Chatzi (2015, 2017).



#### 3 ASSESSMENT FOR OPERATIONAL MODAL ANALYSIS

The effectiveness of the PSBS-based approach for structural modal properties extraction is herein numerically assessed vis-à-vis the spectro-temporal *rwPBDR* method by considering response acceleration signals recorded in the Bärenbohlstrasse overpass in Zürich, Switzerland (Klis *et al* 2016). Specifically, a dataset of D=18 vertical bridge acceleration responses of 107460 samples each is considered, acquired under operational conditions at a uniform sampling rate of 200Hz. The raw data are first pre-processed (baseline adjustment and 4<sup>th</sup>-order Butterworth band-pass filtering within the frequency range of [0.15, 50] in Hz) to remove the mean value and any potential low-frequency trend within each acceleration response. The PSBS-based approach is applied assuming compression ratios (CRs) at 31% ( $\overline{M}=5$ ,  $\overline{N}=16$ ,  $\mathbf{n} = [0, 1, 2, 5, 8]^{T}$ ), and at 11% ( $\overline{M}=14$ ,  $\overline{N}=128$ ,  $\mathbf{n}=[0, 1, 2, 6, 8, 20, 29, 38, 47, 50, 53, 60, 63, 64]^{T}$ ) below the Nyquist frequency to retrieve the sub-Nyquist sampled measurements  $y_m^d[l]$  (d=1,2,...,18, m=1,2,...,M). The latter are next collectively considered to obtain the output cross-correlation sequences,  $\hat{r}_{y_a,y_b}^a[k]$ , which

are further used in Eq. (2) to estimate the power spectral density (PSD) response matrix,  $\hat{\mathbf{s}}_{x^ax^b}$ , from the 18 devices. The *PSD* matrix is subsequently fused within the standard FDD algorithm (Brincker and Ventura 2015) to extract the modal properties of the monitored bridge, which are reported in Table 1 for the first four modes of vibration.

Table 1. Bridge modal estimates obtained from a conventional approach applied to the full-length dataset (*CR*=100%), the PSBS-based FDD *CR*= $\{31\%, 11\%\}$ , and the rwPBDR NeXT-ERA at *CR*= $\{36\%, 11\%\}$ 

	Conventional	PSBS				rwPBDR			
	CR=100%	<i>CR</i> =31%		<i>CR</i> =11%		<i>CR</i> =36%		<i>CR</i> =11%	
Mode	<i>F</i> [Hz]	d <i>F/F</i> [%]	MAC						
1	7.617	0.37	1.000	1.02	0.997	0.63	0.997	0.52	0.983
2	10.352	0.44	0.998	0.31	0.987	0.18	0.981	0.32	0.976
3	11.719	0.84	1.000	0.46	0.998	0.19	0.992	0.14	0.990
4	12.598	0.47	0.972	0.50	0.960	1.22	0.960	0.78	0.943

The STCS-rwPBDN approach is further applied to a dataset of 18 two-minute long measurements  $\mathbf{x}_i \in \mathbb{R}^{N \times 1}, (i = 1...18, N = 11776)$ , down-sampled at 100 Hz. The considered dataset is first partitioned into R=29 windows (frames) of  $N_R=400$  samples, and each window is projected into the spectral domain (see also left panel in Figure 1). Following the methodology in Section 2.2, the spectral coefficients per data frame are then thresholded with a value  $\epsilon_{ij} = \epsilon \| \mathbf{\hat{c}}_{ij} \|_1 / N_R$ , j = 1...R, which pertains to  $\epsilon_l = 1.5$ , yielding the spectral domain elements illustrated in the left panel of Figure 1. The selected support elements are further used to form a weighting matrix  $\mathbf{W}_{ii}$  per data frame. Considering next two different *CRs* at {36%,11%}, the compressed samples  $y_i$  (denoted with a cross in Figure 1) are selected and used to retrieve the reconstructed time-domain sequence plotted in Figure 1 by a broken line. The Natural eXcitation Technique (NeXT) combined with the Eigensystem Realization Algorithm (ERA) are then used to extract the bridge modal propertied presented in Table 1. This table also reports the modal estimates obtained from a conventional approach applied to the full-length dataset (i.e. CR=100%), hereafter referred to as the "exact solution". In this respect, the percentage difference error, dF/F, and the Modal Assurance Criterion (MAC) (Brincker and Ventura (2015)) are used to quantify the accuracy of the modal estimates extracted from the two alternative sub-Nyquist approaches with respect to the exact solution. From Table 1, it is readily observed that the two alternative approaches perform equally well in extracting quality modal estimates even from the



processing of 89% fewer measurements compared to conventional approaches (i.e., at CR=11%), yielding natural frequencies with small errors (below 1.3%), and mode shapes of high MAC values (close to unity) in all cases considered.



Figure 1. Spectral domain projection (left) and time-domain recovery (right) of data-frame #4, channel #1 at CR=36%. Crosses indicate transmitted samples used in the recovery process.

### 4 ASSESSMENT FOR SIGNAL RECOVERY IN TIME AND IN FREQUENCY DOMAIN

Arguably, the accuracy of the two considered approaches strongly depends on the efficiency of the associated recovery operation (i.e., power spectral recovery in the PSBS-based approach, and time-domain signal reconstruction in the *STCS-rwPBDN* method) applied on the acquired compressed measurements. For both approaches, the pertinent recovery performance is numerically assessed herein as a function of the signal compression level achieved by the adopted sub-Nyquist sampling schemes, using field-recorded acceleration responses from an operational Wind Turbine (WT) in Lübbenau, Germany (Klis and Chatzi 2015). The recorded WT data were conventionally acquired at a uniform sampling rate of 200 Hz.

#### 4.1 PSBS approach for frequency domain signal recovery

For the numerical evaluation of the power spectral recovery in the PSBS-based approach (subsection 2.1), a WT pre-processed (i.e., baseline adjusted and filtered) acceleration time-series is employed herein, in which the stationarity hypothesis is confirmed at the 95% confidence level. Thus, the accuracy of the recovered PSD estimate in Eq. (2) is assessed at two different CRs of approximately 11% (for  $\overline{M}=14$ ,  $\overline{N}=128$ , and  $\mathbf{n}=[0,1,2,6,8,20,29,38,47,50,53,60,63,64]^{T}$ ), and 31% (for  $\overline{M}=5$ ,  $\overline{N}=16$ , and  $\mathbf{n}=[0,1,2,5,8]^{\mathrm{T}}$ ), which pertain to 89% and 69% fewer data compared to the uniformly-sampled full-length signal. For the two adopted CRs, the obtained PSD estimates are presented in Figure 2 (solid gray curve), and plotted against the standard Welch periodogram (broken black curve), which is computed for the full-length signal of 172420 samples, assuming  $4096 (=2^{12})$  FFT points, eight overlapping segments with 50% overlap, windowed with a Hanning function (Marple 1987). Notably, the PSD curves in Figure 2 are normalized to their maximum amplitude to facilitate comparison. For CR=11%, the left panel of Figure 2 shows that the recovered PSD curve can closely approximate the Welch periodogram in the frequency range below 5 Hz, where the important WT modal information lies. However, the retrieved PSD estimate deviates significantly from the Welch periodogram at higher frequencies (i.e., above 5 Hz), and especially in the anti-resonance ranges. These discrepancies are considerably reduced at the higher CRs and the PSD recovery from an increased number of measurements, as clearly indicated in right panel of Figure 2 for the *PSBS*-based approach operating at CR=31%.

SMAR 2017 – Fourth Conference on Smart Monitoring, Assessment and Rehabilitation of Civil Structures





Figure 2. PSD estimates: Which periodogram at Nyquist rate compared with PSBS approach for CR=11% (left), and CR=31% (right)

#### 4.2 STCS-rwBPDN approach for time domain signal recovery

The reconstruction performance of the *STCS-rwBPDN* framework is next assessed for two compression ratios at  $CR = \{30\%, 45\%\}$ . For a given WT acceleration response, the underlying signal support **U** is first computed to define the signal's sparsity level, *k* (i.e., number of components in the spectral domain), as well as the variance of the noisy component, i.e., the complementary set of the support (remaining part of the spectral representation). As elaborated upon in the work of Klis and Chatzi (2015; 2017), this is used to prescribe error bounds on the reconstructed signal. For the two considered *CRs*, the obtained signal reconstruction estimates are illustrated in Figure 3 for an acceleration time-window of 400 samples. Comparing the two panels in Figure 3, it becomes evident that the increase in the number of transmitted samples results in narrowing the estimated maximal error bounds. Figure 3 also demonstrates the potential of the proposed framework, when applied in windows of non-stationary response signals, albeit necessitating higher compression rates than the conventional stationary case. The delivered error bounds allow for attributing some level of confidence on the undertaken signal reconstruction operation, which offers a benefit over the alternative (plain) *BPDN* approach adopted by O'Connor et al. (2014).



Figure 3. Effect of the increase of transmission level *CR* on the estimated error bounds: *CR*=30% (left), *CR*=45% (right). Figure reused from (Klis and Chatzi (2015)).

#### 5 CONCLUDING REMARKS

The performance of a PSBS-based method and a spectro-temporal *rwBPDN*-based approach has been numerically assessed in undertaking output-only V-SHM using WSNs. Both the approaches aim to reduce wireless data transmission payloads by considering compressed structural acceleration responses acquired at sub-Nyquist rates. The PSBS method recovers power spectral estimates directly in the compressed domain while the *STCS-rwBPDN* approach provides



reconstructed signals in time-domain. The validation of the two approaches is carried out on fieldrecorded data obtained from an overpass, and from an operating wind turbine. It is shown that both considered approaches can accurately identify the underlying structural modal properties for compression ratios (CRs) as low as 11% yielding modal estimates of similar accuracy. It is further shown that the efficacy of the two approaches relies on the pertinent recovery operations applied on compressed data, which are significantly affected by the adopted CR.

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