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1	Neural-latency noise places limits on human sensitivity to the					
2	timing of events					
3						
4	Abbreviated Title: Neural-latency noise limits timing sensitivity					
5						
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24 Abstract

25	The brain-time account posits that the <i>physical</i> timing of sensory-evoked neural activity determines
26	the <i>perceived</i> timing of corresponding sensory events. A canonical model formalises this account for
27	tasks such as simultaneity and order judgements: Signals arrive at a decision centre in an order, and
28	at a temporal offset, shaped by neural propagation times. This model assumes that the noise
29	affecting people's temporal judgements is primarily neural-latency noise, i.e. variation in
30	propagation times across trials, but this assumption has received little scrutiny. Here, we recorded
31	EEG alongside simultaneity judgements from 50 participants in response to combinations of visual,
32	auditory and tactile stimuli. Bootstrapping of ERP components was used to estimate neural-latency
33	noise, and simultaneity judgements were modelled to estimate the precision of timing judgements.
34	We obtained the predicted correlation between neural and behavioural measures of latency noise,
35	supporting a fundamental feature of the canonical model of perceived timing.
36	
37	Keywords
38	Time perception, timing, simultaneity, synchrony, order, intersensory.

40 1. Introduction

41 The temporal sequencing of events provides narrative structure for our experiences, and likely 42 supports important cognitive operations such as inferring causal relationships (Michotte, 1954) and 43 perceptually binding or segregating sensory representations (Fujisaki & Nishida, 2010; Holmes & 44 Spence, 2005). However, we don't yet know how the brain determines synchrony and order. Indeed, 45 even basic premises, such as the idea that the timing of the neural activity that represents an event 46 is causal for the experience of subjective timing – which we refer to as the brain-time account – 47 remain controversial (Dennett & Kinsbourne, 1992; Moutoussis & Zeki, 1997; Nishida & Johnston, 48 2002; Paillard, 1949; Whitney & Murakami, 1998; Yarrow & Arnold, 2016). 49 The brain-time account has inspired several formal models of temporal sequencing. The canonical 50 model (Sternberg & Knoll, 1973) represents a special case of signal detection theory (Green & Swets, 51 1966). Behaviourally, tasks assessing perceived event timing, such as temporal order and synchrony 52 judgements, reveal variation in judgements even across trials presenting the exact same physical 53 stimuli, yielding gently sloped psychometric functions as responses gradually transition from 54 predominance of one judgement category to another (e.g. asynchronous to synchronous). This 55 implies that some kind of *internal noise* limits performance. A key assumption of the canonical 56 model is that this internal noise reflects *latency* noise, i.e. trial-to-trial differences in the latencies 57 with which the signals representing events propagate through the nervous system toward a central 58 decision centre. Modern variants of the canonical model retain the notion that latency noise is a key 59 determinant of the psychometric function (García-Pérez & Alcalá-Quintana, 2012a), even when they 60 allow for other contributory sources, such as instability in decision criteria from trial to trial (Ulrich, 61 1987; Yarrow, Jahn, Durant, & Arnold, 2011). 62 Discussions of the brain-time account often focus on the average subjective ordering of events, 63 which could reflect neural propagation latencies. For example, participants are biased to tap earlier

64 when synchronising tap responses with an auditory metronome, and this bias is exacerbated for foot

65 tapping compared to hand tapping (Fraisse, 1980). This is consistent with an attempt to synchronise 66 reafferent tactile and exafferent auditory signals in the brain, given generally longer somatosensory 67 relative to auditory latencies, with the resulting bias exaggerated by lengthened neural pathways 68 from the foot relative to the hand. A similar focus on subjective order is evident in more direct 69 assays of timing in the human brain. For example, studies have related the average timing of neural 70 activity, in the form of event-related potential (ERP) components, to attention-dependent changes in 71 average perceived temporal order, known as prior entry effects (McDonald, Teder-Salejarvi, Di 72 Russo, & Hillyard, 2005; Vibell, Klinge, Zampini, Spence, & Nobre, 2007).

73 A focus on average subjective order, with less scrutiny applied to the predicted consequences of 74 latency variation, is understandable, as estimating a bias seems conceptually more straightforward 75 than measuring and making predictions about noise (but see Yarrow, et al., 2011). Yet the impact of 76 latency noise on the precision of timing judgements is a key diagnostic for the canonical model of 77 event timing, which has not been thoroughly tested. Furthermore, the primacy of latency noise is by 78 no means a given. In addition to conceptual criticisms (Dennett & Kinsbourne, 1992; Nishida & 79 Johnston, 2002), several models exist which could imply primacy for other forms of noise. These 80 include population-code models, formulated to explain aftereffects of event timing (Roach, Heron, 81 Whitaker, & McGraw, 2011; Yarrow, Minaei, & Arnold, 2015), where noise is thought to reflect 82 variation in the spiking activity of units tuned to specific timing relationships, and models that imply 83 a series of linear operations on temporally filtered inputs (Burr, Silva, Cicchini, Banks, & Morrone, 84 2009; Parise & Ernst, 2016), where noise has been modelled as an add on at a decision stage. 85 Here, we test whether neural-latency variation across trials predicts (and thus may limit) the 86 precision of timing judgements. We present auditory, visual, and tactile stimulations, in order to

88 the canonical model (GLINC – Gaussian Latency Independent Noisy Criteria; Yarrow et al., 2011) to

estimate latency variation from inter-trial changes in ERP components. We then apply a variant of

87

89 estimate the precision of synchrony judgements concerning audio-visual (AV), audio-tactile (AT), and

- visuo-tactile (VT) stimulus pairs. Our analytic approach is schematised in Figure 1. We find that the
 precision of subjective timing judgements can be predicted from formally near-equivalent measures
- 92 of inter-trial latency variation consistent with the hypothesis that temporally noisy brains promote
- 93 temporal imprecision in perception.



96	Fig. 1. Overview of the analysis workflow used to establish correlations between behavioural and
97	neural estimates of latency variation. Top Panel: Participants completed unimodal and bimodal
98	judgement trials. Left Panels: Bimodal-trial (here, AT) performance was estimated using the GLINC
99	model (expanded in Figure 2) with the steeper of the two slopes from the resulting psychometric
100	function inversely related to a behavioural estimate of latency variation (σ_{min}). Right Panels: EEG data
101	associated with unimodal, i.e. single stimulus, trials (here, A trials and T trials) were used to compute
102	event-related latency variation profiles (see Figure 3 for further details). These profiles were then
103	combined to create an AT' profile, representing a neural estimate of latency variation. Bottom Panel:
104	The behavioural and neural estimates of latency variation were then tested for correlation using
105	cluster permutation tests (see Figure 5).
106	
107	2. Materials & Methods
108	
109	2.1 Participants
110	The combination of an unknown effect size and a complex familywise correction applied across a
111	spatiotemporally correlated neural signal (via cluster tests; see below) made a priori power
112	calculations challenging. We opted to target a sample size of 50. This provides >80% power to detect
113	an (uncorrected) correlation of 0.35 (with p < 0.05 under our one-tailed hypothesis). Data were
114	successfully collected from 57 predominantly female ¹ participants, but for six, SJ data were
115	insufficient to properly constrain behavioural model parameters in one or more modality pairings
116	(see data analysis, below) and for one, poor EEG data quality led to rejection of >50% of trials. The
	(see data analysis, below) and for one, poor LEG data quality led to rejection of >50% of thats. The

118 reported normal or corrected to normal vision and hearing, and were reimbursed, either with course

¹ A loss of data regarding the gender of the final 17 participants means we cannot provide an exact proportion, but we estimate that our sample was 80% female.

credits (for undergraduate psychology students) or at a rate of £8 per hour. They provided informed
 consent following procedures approved by the City, University of London Psychology Department
 ethics committee.

122

123 2.2 Apparatus & Stimuli

124 The experiment was controlled by a PC running Matlab (The MathWorks, Nattick, U.S.A.) under 125 Windows OS, utilising the Cogent toolbox (Wellcome Department of Imaging Neuroscience) and 126 communicating with both the stimulus peripherals and a second PC hosting the EEG recording 127 software via a pair of parallel ports. These ports were accessed via the inpoutx64.dll freeware driver 128 (http://www.highrez.co.uk/) made accessible in Matlab via the IO64 mex file 129 (http://apps.usd.edu/coglab/psyc770/IO64.html). EEG was recorded using a BrainAmp amplifier 130 (BrainProducts; sampling rate: 1000 Hz; filter pass band 0.1-500 Hz) with 64 active electrodes placed 131 equidistantly on the scalp (EasyCap, M10 Montage) and referenced to the right mastoid. Stimuli 132 were delivered as a 10 ms on-off pulse via either a yellow LED for visual stimuli (located centrally, 133 just beneath instructions on an LCD flat-screen monitor) or solenoid stimulators (tactors; Dancer 134 Design, St. Helen's, U.K.) for auditory and tactile stimuli. The tactile tactor was pinched gently 135 between left forefinger and thumb. The auditory tactor struck a metal surface (a badge) pinned to 136 the participant near their left ear in order to produce a sharp click. Throughout the experiment, a 137 white-noise machine (Wellcare model SC1752) masked the subtle sounds associated with tactile 138 stimuli.

139

140 2.3 Design & Procedure

Following EEG preparation, participants sat comfortably in a dark, electromagnetically shielded room
to complete the experiment (which took around 90 minutes). Each trial of the experiment contained

143 either one or two events. Events could be central LED flashes, taps to the left hand, or left-lateralised 144 audible clicks. Initially, participants received 35 practice trials, in which they used their right hand to 145 judge stimuli "not simultaneous" or "simultaneous" using left/right keyboard arrow keys, 146 respectively. Participants were instructed to also use the non-simultaneous response if they 147 detected only a single stimulus. During practice they received feedback about the correctness of 148 each response. Trials could contain a single visual (V), auditory (A) or tactile (T) stimulus (each with 149 probability 10/90), a bimodal AV, AT or VT pair with stimulus onset asynchrony (SOA) of 0 ms (each 150 with probability 8/90), or an asynchronous bimodal AV, AT, or VT pair with SOAs of -500, -300, 300 151 or 500 ms (each of these 12 possible combinations presented with probability 3/90). The practice 152 sequence was random with replacement.

Participants next completed an experimental block of 900 trials (with breaks offered every 35 trials).
They now received no feedback. Trial types remained the same as during practice except that a
wider range of bimodal asynchronous trials was presented, consisting of AV, AT, or VT pairs with 12
possible SOAs (+/-500 ms, +/-300 ms, +/-200 ms, +/-150 ms, +/-100 ms, +/-50 ms) and each of these
36 possible combinations occurred with a probability of 1/90. The sequence was now random
without replacement and hence yielded exactly 100 unimodal, 80 bimodal synchronous, and 120
bimodal asynchronous trials per modality or modality pairing.

Each trial began with the on-screen instruction "Look down at LED". After one second the LED flashed five times across a 500 ms period (with a 50% duty cycle) to ensure attention was directed correctly. A random (800-1200 ms) fore-period preceded the onset of the first stimulus (or both stimuli in synchronous trials). For non-synchronous bimodal trials, the SOA determined the further delay to the second stimulus. After another 500 ms, the on-screen instruction changed to display the response options. Once the response was registered, 500 ms of feedback (on practice trials only) and/or a 500 ms blank response-stimulus interval completed the trial.

168 2.4 Data Analysis

173

169 2.4.1 Observer Model

- 170 A variant of the canonical model for relative timing judgements was applied to behavioural data
- 171 from bimodal trials, separately for each participant, and in the AV, AT and VT pairs (200 trials per
- 172 modality pairing). This "GLINC" observer model is schematised in Figure 2.



174 Fig. 2. Schematic of GLINC observer model. Each signal must traverse a neural pathway to a decision centre, which receives both signals, and thus has access to their subjective difference in arrival times 175 176 (Δt). (a) Each stimulus onset asynchrony (SOA) value (e.g. -50 ms) is presented many times during an 177 experiment. Each presentation yields a noisy internal response (Δt). The relationship between 178 objective and subjective asynchronies has unit slope and an intercept reflecting the average 179 difference in transmission times between signals. However, the relationship is stochastic: Slicing for 180 any given objective SOA yields the Gaussian distribution of resulting Δt values across trials, reflecting 181 the signals' combined latency noise. (b) This probability density function (PDF) is shown for a -50 ms 182 SOA. Participants judge the trial synchronous when Δt falls between two decision criteria (solid 183 greyed region). As the area under a PDF (to the left of any given point) is captured in the cumulative 184 density function, the shaded region can be estimated as the difference of two cumulative Gaussians,

185 one integrating all the way to the rightmost criterion, the other integrating only to the leftmost one. 186 Variable shading around the criteria indicates additional criterion noise; each criterion is most likely 187 to be placed where the shading is darkest, but varies across trials. (c) Resulting psychometric 188 function, with the point calculated in part b highlighted. Other points on the function are obtained in 189 the same way. Precision is reflected in the slopes of the psychometric function. Under this observer 190 model, both slopes combine latency noise and criterion noise, but the criterion noise is permitted to 191 differ for each. Hence the steeper slope (σ_{min}) will align with the more stable of the two criteria, and 192 thus better reflect (i.e. be more dominated by) latency noise (see main text for further details).

193

Data were summarised as proportion judged simultaneous at each SOA. They were fitted with a
 four-parameter observer model which typically predicts a psychometric function representing the
 difference of two cumulative Gaussians:

197 (1)
$$P(Simultaneous) \sim \Phi\left(\frac{SOA - C_{Low}}{\sigma_{Low}}\right) - \Phi\left(\frac{SOA - C_{High}}{\sigma_{High}}\right)$$

198 In Equation 1, ϕ is the standard normal cumulative distribution function. Under this model, the c 199 parameters are the mean positions of two decision criteria (low and high) used to demarcate 200 successive judgements from simultaneous judgements (i.e. the observer judges two stimuli 201 simultaneous when the internal signals they generate arrive at a decision centre with a subjective 202 SOA, Δt , that is both above the low criterion and below the high criterion). The associated σ values 203 quantify (inversely) the slope on each side of the psychometric function. These are composite noise 204 variables, used because they are formally identifiable in a model fit, whereas the various 205 psychological constructs that feed into them are not. Each σ , when squared, represents the sum of 206 two sources of variance. The first, the variance of Δt , is itself the sum of the (Gaussian) latency 207 variance associated with each stimulus. This source contributes to the slope on both sides of the 208 psychometric function (low and high). The second, the trial-by-trial (Gaussian) variance in a decision criterion, is unique on each side of the function, thus allowing the slopes to vary. Note that Equation
1 is an approximation, with simulation required in rare cases when the approximation breaks down.

211 Custom Matlab functions were used to find maximum-likelihood fits (assuming binomially 212 distributed data). The Nelder-Mead simplex algorithm was used to find the best fit, with simplex 213 searches initiated from the factorial combination of several positions per parameter (i.e. a grid 214 search seeding a set of simplex searches). Observer models incorporated a fixed 1% keyboard 215 error/lapse rate, to model occasional errors without increasing parametric complexity (and also 216 simplify the calculation of log likelihood). In order to determine if participants had produced data of 217 sufficient quality to incorporate into our main analysis, we assessed whether (for each bimodal 218 condition) the four-parameter model provided a significantly better fit than a two-parameter 219 cumulative Gaussian (deviance improvement, $\chi^2_{[2]}$ < 0.01, where deviance is -2 times the shortfall in 220 log-likelihood relative to a saturated model). This represents the lab's standard approach to 221 participant exclusion (Yarrow, 2018) with this null model used in place of a simpler guessing model, 222 as it can capture both guessing, and cases where the range of stimuli is only sufficient to capture the 223 decision boundary on one, but not both, sides of zero. For participants passing this test, we recorded 224 their four best-fitting model parameters in each stimulus pairing, but in particular noted the smaller 225 of the two σ values (i.e. the one associated with the steeper slope). This choice was guided by the 226 particulars of the model – because both σ values contain the noise we are interested in (latency 227 noise), but each overestimates it, as a results of also containing an additional nuisance source 228 (criterion noise), the lower σ parameter should be the one less contaminated by this decision-level 229 source.

230

231 2.4.2 EEG pre-processing

EEG data were pre-processed using custom Matlab scripts incorporating functions from EEGLAB
(Delorme & Makeig, 2004). Data were initially band-pass filtered (0.1-45 Hz) before identifying bad

234 channels (all channels were assessed via channel spectra, and electrode traces outlying from the 235 norm or with extreme irregularities were removed). Next, data were re-referenced to an average 236 reference, and data recorded during breaks were rejected by eye before running an independent 237 component analysis (ICA) targeting blink components for removal. A second artefact rejection by eye 238 was conducted to remove any remaining irregularities in the data, such as excessive muscular noise, 239 electrode drifts and miscellaneous peaks. Finally, the missing (bad) channels were spherically 240 interpolated from the new, clean dataset. Epochs (-200 to +800 ms relative to stimulus onset) were 241 extracted for each unimodal (i.e. single-event) condition, with summary ERPs created following 242 baseline correction to the mean of the first 200 ms. The artefact rejection steps left a median 243 average of 91, 94 and 92 (range 56-99, 66-100, 58-99) unimodal trials for the auditory, visual, and 244 tactile modalities respectively.

245 Note that by design our EEG analysis focussed on unimodal trials, which were included in the 246 experiment specifically for the purpose of estimating neural latency variation. Bimodal trials were 247 not utilised for our derived EEG measure, because they contain/conflate the brain's response to two 248 signals in a way that makes these responses difficult to separate, and we wanted to obtain an 249 independent ERP for each individual modality, in order to properly equate neural and behavioural 250 noise under the GLINC model (as described in the next section). Hence, because unisensory ERPs 251 provide the bedrock for subsequent estimates of latency variation, we confirmed their information 252 content via trial-by-trial decoding based on a 300 ms post-stimulus segment, using a nearest 253 neighbour classifier with jack-knifed cross validation. Trials were classified as A, V or T based on 254 similarities between measures of brain activity on a given trial, and average neural activation 255 patterns elicited by each type of stimulus (individually for each participant) on training trials (all trials 256 for that participant, bar the trial to be decoded on that iteration of the decoding process). On 257 average, stimulus modality could be decoded correctly on 64.7% of trials (95% CI 61.9-67.3), i.e. 258 around twice the chance expectation.

259

260 2.4.3 Event-related latency variation

261 In order to provide a time-varying measure of latency variation for the brain's response to isolated 262 unimodal stimuli, we first calculated, for each participant and electrode, standard sensory ERPs, as 263 the mean of all acceptable trials in a given condition, but with additional 20 Hz bi-directional (3rd 264 order Butterworth) low-pass filtering to minimise small oscillations and emphasize more substantial 265 components. Within each ERP, local maxima and minima were identified out to 500 ms post 266 stimulus, and their times recorded. Conceptually, the next step was to generate 1000 bootstrap 267 resamples of the ERP (Efron & Tibshirani, 1994). A bootstrap resample is generated by resampling 268 with replacement from the original sample, to create a new data set of equal size. The "with 269 replacement" aspect of this procedure means that each resample is likely to contain some trials 270 more than once, with some trials being entirely absent. Hence each resampled ERP was derived from 271 a slightly different mixture of trials compared to the original ERP, and thus differed from it. For each 272 such bootstrap ERP, we attempted to find the most sensible matches between its maxima/minima 273 and those of the original signal, in order to build up bootstrap latency distributions for each turning 274 point (see Figure 3). In practice, such a match is quite challenging, because a given bootstrap 275 resample (calculated out to 600 ms to capture any delayed components) can generate more or less 276 turning points than the original ERP, including some that are a poor match. Hence our bespoke 277 Matlab function implemented a preliminary bootstrap (in order to identify likely time points where 278 bootstrapping would generate spurious turning points) prior to the final bootstrap, where matching 279 was achieved. Matching was based largely on correspondence of sign (i.e. being a 280 maximum/minimum) and timing, but with some additional checks to try and ensure unique and 281 sensible matches (specifically, a match was rejected where it better matched a spurious locus than 282 an original ERP turning point, or where, despite being the closest match for a particular turning 283 point, it was closer still to a different turning point). Where a convincing match could not be

determined, none was recorded, such that the bootstrap latency distribution for any given turning



point could contain fewer than 1000 values.



301

302 The standard deviation of each resulting bootstrap distribution (i.e. the bootstrap standard error) 303 was multiplied by the square root of the number of trials contributing to a condition in order to 304 recover a value approximating the standard deviation of the latency of each ERP component across 305 trials. In a final step, these scores (one for each component, and representing neural-latency 306 variation at the time of that component) were linearly interpolated, so as to give a time-varying 307 measure that respected the sampling rate of the original EEG signal. These event-related variation 308 profiles were derived by interpolating between a median average of 11 turning points 309 (minimum/maximum of 4 and 25 respectively across all electrodes/modalities/participants). We 310 confirmed through simulation (using a tri-peaked difference of Gaussian to mimic underlying signal, 311 and adding varying levels of latency, amplitude, and general 1/f noise) that our method generates 312 estimates of latency noise that increase monotonically (albeit non-linearly) with simulated latency 313 noise.

314

315 2.4.4 Cluster-based correlations

316 Visual, auditory, and tactile event-related latency variation profiles were combined in order to 317 correlate them with behavioural measures that should (under the canonical model) also reflect 318 latency variation. Because behavioural measures represent the standard deviation of Δt , which is 319 formed from a combination of latency variation within each contributing modality, we created AV, 320 AT and VT event-related latency variation profiles by squaring, summing, and square-rooting the two 321 relevant profiles in each case (at each electrode). Correlating the resulting brain-based bimodal 322 variation profiles (comprising 300 time points x 60 electrodes for each participant) with the relevant 323 behavioural measure (e.g. σ_{min} from the relevant psychometric function; one per participant) 324 presents a substantial multiple comparison problem, which we addressed via cluster-based 325 permutation testing (Blair & Karniski, 1993; Groppe, Urbach, & Kutas, 2011) using functions from the

Fieldtrip toolbox (Oostenveld, Fries, Maris, & Schoffelen, 2011) (<u>http://fieldtriptoolbox.org</u>) to control familywise error (for each modality pairing) at a one-tailed alpha of 0.05, reflecting our *a priori* directional hypothesis. Tests were based on 9,999 permutations, with a minimum of two neighbours forming a cluster and a cluster threshold set to two-tailed p < 0.05.

330

331 3. Results

332 3.1 People differ in their ability to perform synchrony judgements

333 Fits of the GLINC model (schematised in Figure 2) to AV synchrony judgements are shown for two 334 representative participants in Figure 4a. As expected, judgements of synchrony were more likely 335 when events were physically synchronous, or separated by only a brief interval. However, slopes on 336 either side of the psychometric function suggest the presence of judgement noise, with different decisions reached on repeated trials with the same physical stimulation. GLINC ascribes this noise to 337 338 a combination of neural-latency variation across trials, and to criterion (i.e. decision-level) noise. For 339 example, the less-precise observer illustrated in Figure 4a (on the right of the panel) has a steeper 340 slope (and thus a lower σ parameter) for the low than for the high criterion. The interpretation of this based on GLINC would be that this observer is better able to maintain a consistent internal 341 demarcation between auditory-leading and synchronous AV stimuli, compared to the demarcation 342 343 of synchronous from visual-leading stimuli. This pattern has been observed before (e.g. Yarrow et al., 344 2011) and indeed was found for the majority of participants in the current sample (33/50, binomial p $= 0.033).^{2}$ 345

² A similar tendency was evident in AT data, with 37/50 participants having less noise at the low criterion associated with the categorisation of auditory-leading AT stimuli. No such tendency emerged for VT data (23/50 participants with less noise at the criterion associated with visual-leading VT stimuli).



Figure 4. Behavioural data. Error bars show 95% confidence intervals. **(a)** Example audio-visual SJ data for two participants (one relatively precise, one relatively imprecise). **(b)** Mean latency noise (σ_{min}) in each sensory combination from the complete sample of participants. Surrounding shape widths denote kernel probability density estimates. AV = audio-visual, VT = visuo-tactile, AT = audiotactile.

Under the GLINC model, the steeper of the two slopes (σ_{min}) will better isolate neural-latency 353 354 variation, so this is used here to estimate this quantity (see Figure 2, especially legend to part c, and 355 section 2.4.1). These behavioural estimates of latency noise are illustrated for the full sample of 356 participants, and all three simultaneity-judgement (SJ) tasks, in Figure 4b. We also conducted split-357 half correlations on behavioural estimates of latency noise, with data split into odd and even-358 numbered subsets of trials for each stimulus onset asynchrony (SOA) category before fitting. These 359 tests indicated reliable individual differences in behavioural noise for all three SJ tasks (r values of 0.534, 0.335 and 0.785; p values of <0.001, =0.0173, and <0.001; for AV, VT and AT SJ tasks 360 361 respectively). This establishes that it is reasonable for us to investigate what neural processes might 362 explain our reliable individual differences in the precision of behavioural timing judgements. 363 364 3.2 Behavioural differences are associated with changes in neural-latency variation 365 The canonical model predicts correlations between behavioural and neural estimates of latency

variation. For our neural estimates, we used bootstrapping of ERPs recorded in response to isolated

367 stimuli from each modality to estimate latency noise at each time point (out to 300 ms post 368 stimulus) and each electrode (see Figure 3). Having estimated visual, auditory, and tactile event-369 related latency variation profiles at each time point and electrode, we combined estimates from 370 each pair of modalities (see Figure 1 and sections 2.4.3 and 2.4.4) to form three bimodal neural-371 variation profiles. Like our behavioural measures, these composite neural-variation profiles provided 372 evidence for reliable individual differences across participants (with mean split-half r values of 0.616, 373 0.611 and 0.627 for AV, VT and AT SJ tasks respectively, and r significant following permutation rmax 374 correction (Blair & Karniski, 1993) at 82% of electrodes and time points). Given robust individual 375 differences in both behavioural and neural estimates of inter-trial latency variation, we proceeded to 376 perform correlations between them as a direct test of our hypothesis. Each composite neural-377 variation profile was correlated with the corresponding behavioural measure that should (under the 378 canonical model) reflect the exact same latency variation (e.g. audio and tactile profiles were 379 combined for correlation with the behavioural measure AT σ_{min} , see Figure 1). To achieve a non-380 parametric whole-brain control of familywise error, we used cluster permutation tests. Results are 381 illustrated in Figure 5.



382

Figure 5. Summary of results from cluster-permutation tests of correlations between behavioural and neural estimates of latency variation, for **(a)** audio-visual, **(b)** visuo-tactile and **(c)** audio-tactile synchrony judgement tasks. Within each panel, the lower row contains topoplots of average correlations, including all 25 ms epochs where a cluster remains significant throughout. Electrodes

387 contributing continuously to the significant cluster are highlighted by red asterisks. One such

388 electrode is further highlighted (black ring) for detailed illustration in the top row. Here, to the left,

389 the correlation is plotted across time at this electrode. Correlations exceeding cluster thresholds are

390 *highlighted (red background region). One time point (yellow vertical line) is picked out for illustration*

in a scatterplot, shown on the right. Here, the line of equality is shown in dashed black, and the line

392 of best fit in yellow (with 95% Cls in solid black).

393

394	Figure 5a shows correlations between audio-visual SJ precision and neural-latency noise, estimated
395	from isolated audio and visual ERPs. The cluster permutation test revealed a single significant cluster
396	(p = 0.0245). Topoplots illustrate the strength of correlation across the scalp at all epochs spanned
397	by this cluster. This cluster seems to emerge at central electrodes (consistent with electrodes where
398	strong auditory ERPs are observed) around 50 ms after stimulus onset, then spreads to occipital
399	electrodes (suggestive of visual system involvement), and persists until around 200 ms post
400	stimulation. ³
401	Figure 5b shows correlations in the visuo-tactile case. The permutation test again revealed a single
402	significant cluster (p = 0.0328), this time emerging at right-central electrodes from around 150 ms

403 post stimulation, spreading to occipital electrodes, before disappearing around 225 ms post

404 stimulation.

³ We verified that the portions of contributing latency variation profiles which were coincident with this cluster contained many values estimated directly from ERP turning points (as opposed to being based entirely on interpolated values falling between ERP turning points). For the AV cluster, which spanned 17 channels, each for a duration ranging from 7 to 116 ms, across participants a median average 18 (minimum 10) turning points intersected coincident portions of visual variation profiles, while a median average 17 (minimum 12) turning points intersected coincident portions of auditory variation profiles. We went on to make similar calculations for the VT and AT clusters that are described next in the main text. For the VT cluster, which spanned 22 channels, each for a duration ranging from 1 to 80 ms, across participants a median average 17 (minimum 8) turning points intersected coincident portions of visual variation profiles, while a median average 14 (minimum 7) turning points intersected coincident portions of tactile variation profiles. For the AT cluster, which spanned 28 channels, each for a duration ranging from 1 to 107 ms, across participants a median average 26 (minimum 14) turning points intersected coincident portions of auditory variation profiles, while a median average 29 (minimum 20) turning points intersected coincident portions of auditory variation profiles.

In Figure 5c, correlations involving audio-tactile timing precision are plotted, once again highlighting
a single significant cluster (p = 0.0242). In line with the contributing left-lateralised unisensory
signals, this is largely right lateralised, and spreads from central to parietal electrodes. The cluster
lasts until around 100 ms, and emerges very early at 0 ms, probably as an artefact of our
interpolation process used to estimate latency variation, which assigns the noise estimate from the
first ERP turning point to all earlier time points (Figure 3).

411 Based on a model-derived hypothesis, we have so far correlated neural-latency variability estimated 412 from contributing unisensory stimulations with behavioural estimates of timing precision from 413 bimodal stimulations (e.g. A and V variation profiles were combined and then correlated with estimates of the precision of AV synchrony judgements).⁴ In principle, one might expect no such 414 415 correlation between behavioural estimates and non-contributing unisensory signals (e.g. between 416 AV behaviour and tactile ERPs). However, it is also plausible that some peoples' brains have a 417 generally high temporal fidelity, and others a generally poor temporal fidelity, sharing this property 418 across all sensory modalities, in which case correlations would still emerge. Testing for these 419 relationships, we found no significant clusters for two of three tests (VT-A: smallest p = 0.0949; AT-V: 420 no positive clusters to assess), but found a significant cluster for the final such test (AV-T; p = 0.0074) 421 with an early (0-125 ms) occipito-parietal locus.

422

423 3.3 Average neural latency variability is higher for visual compared to tactile and auditory stimuli

424 Temporal acuity may vary between the senses. Our behavioural data are suggestive of greater

425 variability for synchrony judgements involving visual stimuli (see Figure 4b – variability trend

⁴ Our analysis followed, in a principled manner, from the model we have assumed as the basis for generating psychometric functions (i.e. the GLINC model). For this reason, we used the steeper slope of the psychometric function to estimate behavioural noise (see methods). However, in response to an anonymous reviewer request, we re-ran our three correlation analyses using the average of the two slopes to estimate behavioural noise instead. Headline results were very similar, with a single significant cluster emerging for all three modality pairs (AV p = 0.0461; VT p = 0.0299; AT, p = 0.0332).

426 suggests AV > VT > AT). Repeated-measures permutation tests with a tmax familywise correction for 427 the three possible pairwise contrasts indicated that of these, just the outer contrast (AV>AT) was 428 significant (p = 0.013). We sought a similar pattern in our neural data, calculating a crude measure of 429 neural variability in each modality by averaging latency variability profiles across the full 300 ms x 60 430 electrodes included in our main correlation analysis. This measure showed a V > T > A pattern (with 431 variability of 60, 55 and 54 ms respectively) that is somewhat consistent with our behavioural result. 432 Tmax corrected permutation tests indicated significantly greater neural variability in response to 433 visual stimuli, compared to both tactile and auditory stimuli (p < 0.001).

434

435 4. Discussion

436

437 The canonical model of multisensory timing perception formalises the brain-time account, i.e. the 438 idea that the timing of particular operations in the human brain determines the perceived timing of sensory events.⁵ Because the canonical model is a formal (if simple) process model, it makes clear 439 440 predictions about the sources of noise that limit the precision of timing judgements. Specifically, the 441 fidelity of timing judgements should be determined, to a substantial degree, by inter-trial differences 442 in the speed at which contributing signals propagate through the central nervous system (measured 443 as latency variation). Here, we tested this idea using synchrony judgements, completed alongside 444 EEG recordings. Because it would be very difficult to estimate the latency noise affecting individual

⁵ The brain-time account is usually invoked in discussions of event ordering. Event ordering can be seen as a prequel to other forms of time perception such as interval timing, although no clear consensus exists regarding the degree of neurocognitive interrelation between different forms of time perception (we use *timing* perception here to focus our discussion specifically on issues of relative order). In general, the brain-time account should probably be considered agnostic regarding the necessity of forming higher-order representations about time, such as of intervals, but specific formal accounts derived from it are required to be more specific. For example, our GLINC model implies that arrival order gives rise to a representation of intervening time (to which criteria can be applied to form judgements). Many formal models of interval timing go a step further, by acknowledging neural latency variability as a constant source of noise for interval judgements, but one that is typically dwarfed by interval-dependent "scalar" noise (Wearden & Lejeune, 2008). Such scalar noise is generally omitted in accounts of relative timing, because they focus on such tiny intervals.

trials (either behaviourally from SJs, or in the brain from the corresponding single-trial bimodal ERPs,
somehow decomposed into their unimodal constituents) we have not attempted any withinparticipant, trial-by-trial correlations of neural and behavioural noise. Rather, we used responses
across multiple trials to provide a model-based estimate of behavioural noise for each participant,
and have correlated these with bootstrap-based estimates of neural noise derived from EEG. For all
three modality pairs (AV, VT, and AT), we observed the predicted positive relationship between
individual-difference measures, supporting a key assumption of the canonical model.

452 Inter-trial latency variation is likely to have a variety of physiological causes. Even operations as 453 seemingly deterministic as propagations of action potentials show latency variance, at least for thin, 454 unmyelinated axons (Faisal & Laughlin, 2007). Such latency noise is likely exaggerated greatly by 455 stochasticity in the thresholding that occurs at synapses (e.g. Paraskevopouloua, Coon, Brunner, 456 Miller & Schalk, 2021). The canonical model embraces such noise. However, several promising 457 models of relative timing do not explicitly incorporate sensory latency noise (Parise & Ernst, 2016; 458 Roach et al., 2011). Our data suggest that such noise may be an important feature that should be 459 incorporated in modelling of time perception.

460 We estimated inter-trial latency variation based on a bootstrapping approach. Our overall approach 461 is novel, although bootstrapping itself is well established, having become a textbook method for 462 estimating standard errors. There are, of course, other ways to estimate neural latency noise from 463 EEG data. Possibilities include attempting to clean the data sufficiently to enable estimations of ERP 464 latencies on individual trials, which would also provide an estimate of latency variance across trials. 465 However, the noise levels associated with EEG data makes this approach challenging. Another 466 approach would be to use the variance of the EEG signal across trials at each time point (cf. Arazi, 467 Yeshurun & Dinstein, 2019). Finally, for a non-time-varying estimate, one might select a temporal 468 window of interest and compute cross correlations between all possible pairs of trials within that 469 time window. The time delay that maximises each such correlation could then be calculated, with a

summary statistic of these measures taken as an estimate of implied delays. We do not claim that
our particular approach is a gold standard, but we do think it has some important strengths relative
to these other possibilities. For example, the variance of EEG signals across trials, while
straightforward to compute, would reflect both variability in the timing of ERP components, and
variability in their magnitude, with each source contributing to an unknown extent. By contrast, our
bootstrapping measure specifically targets latency noise (while still tracking changes in variability
across time).

477 It is worth acknowledging that any method that derives an aggregate measure of (bimodal) neural 478 noise by combining estimates based on unimodal trials is blind to possible early interactions 479 between sensory channels. Such interactions might affect latency noise, or even act as an entirely 480 separate cue for the detection of synchrony (Arnold, Hohaia, & Yarrow, 2020). Ignoring this putative 481 issue is true to the assumptions of the canonical model, which Sternberg and Knoll (1973) explicitly 482 labelled the "independent channels" model on this account, but the existence/importance of early 483 interactions between bimodal signals is of course an empirical question that might be addressed in 484 future work. For this investigation, we chose a particular variant of the canonical model (GLINC) to fit 485 behavioural data and generate predictions – one we have outlined and used in previous publications 486 (Yarrow et al., 2011; Yarrow, Sverdrup-Stueland, Roseboom, & Arnold, 2013; Yarrow et al., 2015; 487 Yarrow, Martin, Di Costa, Solomon, & Arnold, 2016; Yarrow, 2018). Other variants exist, with some 488 important differences (García-Pérez & Alcalá-Quintana, 2012a; García-Pérez & Alcalá-Quintana, 489 2012b; Sternberg & Knoll, 1973; Ulrich, 1987), but all assume latency noise is reflected in the slope 490 of psychometric functions that describe subjective timing, and so all variants derive some support 491 from our findings. We invite other authors to use our publicly available data (Yarrow, Kohl, Arnold & 492 Rowe, 2021) to further test the predictions of different models.

We recognise that our focus on noise in sensory processes invites comparison with Bayesian models
(e.g. Knill & Pouget, 2004), which have become popular when modelling various kinds of time

perception (e.g. Jazayeri & Shadlen, 2010) including judgements of relative time (Ley, Haggard &
Yarrow 2009; Miyazaki, Yamamoto, Uchida & Kitazawa, 2006; Roseboom, 2019). GLINC does not
incorporate Bayesian information-processing stages, such as the integration of a current sensory
estimate with a prior derived from past experience, but the model architecture could be elaborated
to incorporate this. Bayesian model predictions are generally tested by estimating noise from
behaviour, and such tests might usefully be supplemented by approaches like ours, which
additionally estimate noise from brain recordings.

502 Our spatiotemporal illustrations should be considered, at best, suggestive. Caveats limit any 503 inference regarding the spatial origins of neural signals from EEG scalp topography, and cluster 504 significance does not imply significance for all contributing spatiotemporal points. Furthermore, ours 505 are not classic contrasts, but rather correlations across participants. While some ERP components 506 likely represent processing at regions critical for synchrony judgements, any ERP component 507 correlated with these components would also emerge. For example, left-lateralised components 508 evoked by a central visual stimulus might have a temporal fidelity limited by similar physiologically-509 imposed noise compared to right-lateralised components. The same applies to components 510 preceding and following a critical component in time. Moreover, our method sums variance 511 estimated from two contributing unimodal sensory signals, using spatiotemporal correspondence at 512 the scalp, and it is not clear that this summation should accurately index a temporal comparator of 513 different sensory modalities. Given these considerations, we feel the spatiotemporal loci of our 514 correlations are surprisingly well matched to expectations, being most clearly right lateralised when 515 both stimuli originated from the left (i.e. for audio-tactile stimuli), and broadly in line with regions of 516 cortex relevant for each sensory pairing, and with expectations regarding processing latencies for 517 different sensory modalities (e.g. central electrodes consistent with audio activations emerged early, 518 right-central electrodes consistent with tactile activations slightly later, and occipital activations 519 consistent with visual activation emerged last).

Although we observed the predicted correlations, they were modest, accounting at best for around 25% of the variance in behavioural performance. Several factors may be relevant. First, correlations are limited by the reliability of contributing measures. These reliabilities are unknown in the absence of a retest session, but split-half analyses of both behavioural and neural data generated r values of around 0.5, suggesting test-retest correlations would likely fall well short of a perfect correlation. Hence, we have imperfect but moderately reliable measures of behaviour and neural activity, reflecting practical trade-offs when determining the length of experimental sessions.

527 Second, only austere versions of the canonical model (e.g. Gibbon & Rutschmann, 1969) assume 528 trial-by-trial latency variation is the only source of noise affecting timing judgements. Any additional 529 sources of noise would suppress the correlations we have sought here. The GLINC model we have 530 used, for instance, assumes criterion noise, i.e. an inability to make the same decisions about inputs, 531 even if sensory coding and experiences are held constant across trials (Ulrich, 1987). Other variants 532 assume participants cannot resolve relative timing when two signals arrive within some limited temporal window (Sternberg & Knoll, 1973). This refractory "moment" might be triggered by the 533 534 arrival of the first stimulus (e.g. García-Pérez & Alcalá-Quintana, 2012a; Venables, 1960), but in this case it would not influence the *slope* of the SJ function, and thus should not act as an additional 535 536 source of noise under our analysis. Indeed, this consideration informed our choice of task - we 537 opted not to use temporal order judgements (TOJs), because TOJs seem more profoundly affected 538 by additional sources of noise relative to SJs (Yarrow et al., 2016) perhaps including a flattening of 539 the slope of the psychometric function resulting from something formally akin to a triggered 540 moment (García-Pérez & Alcalá-Quintana, 2012a). We have previously concluded (via a very 541 different kind of analysis) that variation in evoked responses does not have an easily detectable role 542 in AV TOJ performance (Arnold, Hohaia, & Yarrow, 2020).

Another variant of the canonical model proposes a moving (i.e. non stimulus-locked) perceptual
moment (Stroud, 1956). This has been linked to the alpha rhythm, for example when explaining

545 individual differences in the double-flash illusion (Cecere, Rees, & Romei, 2015) and changes in 546 visual-visual TOJ sensitivity across an entrained alpha cycle (Chota, Margue, & VanRullen, 2021). 547 Perhaps of greatest relevance here, individual alpha frequencies have also been linked with the 548 width of synchrony functions for visuo-tactile SJs (Migliorati et al., 2019), albeit without recourse to 549 a formal observer model. A moving moment would increase noise in SJs much like criterion 550 noise/variance under the GLINC model, because the time period within which the ordering of stimuli 551 could not be resolved would vary from trial to trial, depending on where in the ongoing cycle the 552 first stimulus happened to arrive. Hence, the modest degree of correlation in our data may provide 553 some support for both criterion-noise and moving-moment variants of the canonical model. 554 In supporting the canonical model of relative timing, our data also support the broader brain-time 555 account which it formalises. We recognise that our approach to testing the brain-time account is 556 somewhat indirect, compared to the more common tactic of introducing experimental 557 manipulations designed to vary mean transmission times while measuring corresponding changes in 558 average timing perception and/or neural latencies (e.g. Fraisse, 1980; McDonald et al., 2005; Vibell 559 et al., 2007). However, we believe our method makes a novel contribution to the wider debate. Of 560 course, there are other findings that cast doubt on the brain-time account as a complete and 561 sufficient theory. For example, the existence of contextual influences on perceived event timing (e.g. 562 Bechlivanidis & Lagnado, 2016; Miyazaki et al., 2006; Yarrow, Whiteley, Haggard & Rothwell, 2006) 563 suggests a softening of the brain-time account, to admit that some degree of (likely post-hoc) biasing 564 or rationalisation can occur. However, as we have argued elsewhere (Yarrow & Arnold 2016), brain 565 time remains viable as the fundamental basis for perceived temporal order, even if it is unlikely to be 566 a complete account under all circumstances.

Other results may appear challenging to the brain-time account, but often bear closer examination.
For example, the canonical model implies that neural latencies inform the point of subjective
simultaneity (PSS), such that relative latency is one reasonable explanation on offer for non-zero or

570 altered PSS values (e.g. Freeman et al., 2013; Grabot & van Wassenhove, 2017). However, most 571 variants of this model also provide equally valid alternative explanations (e.g. differences in the 572 positioning of decision criteria) such that PSS results that appear to refute the brain-time account 573 (e.g. apparent dissociations between tasks; Love, Petrini, Chen & Pollick, 2013) may be less 574 challenging when viewed through the lens of a formal model (Yarrow et al., 2016). Indeed, many 575 such "dissociations" seem to result from comparing measures believed to be comparable on some 576 intuitive basis (e.g. the width of an SJ function and the just noticeable difference derived from a TOJ 577 function) but for which formal modelling reveals no such equivalence.

578 Returning to the current results: We have already noted limitations stemming from our correlational 579 approach, and urge due caution when interpreting our findings. For example, the correlations we 580 observe may be driven by an unmeasured third variable with putative effects on both our neural and 581 behavioural measures, such as levels of arousal, focussed attention and so forth. We tried to make 582 our measure of neural latency variability as specific as possible, but of course it is likely that this 583 measure is itself related to more general forms of neural variability. However, although unmeasured 584 variables might underlie the correlations observed here, we sought these correlations only because 585 they are implied by the causal steps of a formal process model. This makes a causal attribution at 586 least plausible.

As a final issue, we note that we have incorporated three tests of our one-tailed hypothesis into our design. Although each was subjected to appropriate statistical control of familywise alpha levels, one might argue that the experiment-wise alpha is higher. However, there is considerable overlap between measures informing the three cluster tests, so their independence is unclear. Furthermore, the average p value across the three tests still implies significance. Hence, while our inference is less robust than if we had *independently* verified the hypothesis in three separate data sets, we consider the degree of protection against false positives to be reasonable. We note, however, that a pilot for

- this project, with only AV stimuli and a less fully developed analysis, failed to detect the correlations
- 595 we report here (Keane, 2019). As such, our findings would certainly bear replication.
- 596 To summarise: Our data suggest that better performers on cross-modal SJ tasks exhibit lower levels
- 597 of neural-latency noise compared to worse performers, exactly as predicted by the canonical model
- 598 of relative time perception. We therefore argue that viable models of relative timing should
- 599 incorporate latency variability in neural transmission times as an explicit feature of human time
- 600 perception.

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- 603
- 604 Author contributions
- 605 KY and DHA conceived and designed the experiment. CK, PR, RKB and TS collected the data. KY and
- 606 CK performed the analysis. KY drafted the manuscript, which all authors edited and approved.
- 607
- 608 Data Availability
- 609 The datasets analysed during the current study are available in the City University of London figshare
- 610 repository [https://doi.org/10.25383/city.11843274].
- 611
- 612 Competing Interests
- 613 The authors declare no competing interests.

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