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Numerical Analysis of Second Harmonic Generation in Soft Glass Equiangular Spiral Photonic Crystal Fibers

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Abstract: In this study, the accurate and numerically efficient Finite Element (FE) based Beam Propagation Method (BPM) has been employed to investigate Second Harmonic Generation (SHG) in highly nonlinear soft glass (SF57) Equiangular Spiral Photonic Crystal Fibers (ES-PCF) for the first time. It is shown here that the SHG output power in highly nonlinear SF57 soft glass PCF exploiting the ES design is significantly higher compared to that of Silica PCF with hexagonal air-hole arrangements. The effects of fabrication tolerances on the coherence length and the modal properties of ES-PCF are also illustrated. Moreover, phase matching between the fundamental and the second harmonic modes is discussed through the use of the quasi-phase matching technique. Furthermore, the ultra low bending loss in the SF57 ES-PCF design has been successfully analyzed.

Index Terms: Second Harmonic Generation (SHG), Photonic Crystal Fibers (PCF), Finite Element Method (FEM).

1. Introduction

Recently, considerable interest has been shown in guided wave Second Harmonic Generation (SHG) devices implementing compact short wavelength coherent light sources which would be useful across a range of applications such as optical data storage, xerography, spectroscopy and telecommunication [1]. SHG is a nonlinear effect that comes into play with the use of sufficiently intense electromagnetic fields. The nonlinear response of a medium is related to the anharmonic motion of bound electrons under the influence of the applied electromagnetic field [2] and nonlinear processes such as SHG are a result of the second order susceptibility denoted by χ^2 . The requirements for efficient SHG include a medium with large second order susceptibility and phase matching between the optical modes at the fundamental and second order frequencies.

1.1 Choice of Structure

Photonic Crystal Fibers (PCFs) can improve the power conversion efficiency by enhancing the overlap integral between the fundamental and second harmonic modes, which is a result of unique air-hole orientation of the PCF structure [3]. These fibers have been responsible for a renaissance in the field of optical fiber devices since they were first reported in the late 1990s [4]. Generally, an index guided PCF consists of a solid central core surrounded by an array of microscopic air holes extending along the entire length of the fiber. The structure of a PCF allows the guidance of light in the solid core by the mechanism of modified total internal reflection, which arises due to the lower equivalent index of the micro-structured air-filled cladding region. Appropriate design of the microstructure of air-holes allows significant flexibility in tailoring the modal and dispersion properties of a PCF, for example, in achieving small mode area (for high non-linearity), and/or low and flat dispersion. The Equiangular Spiral PCF (ES-PCF) [5] provides several design parameters by which the modal properties as well as the dispersion can be controlled more easily. The ES-PCF provides better confinement of the fundamental mode in the core area than conventional PCF does. For a given material, ES-PCF achieves better overlap between the optical fields of the fundamental mode at the frequencies of interest (i.e. of the pump and second harmonic) than in conventional PCF. Hence an ES-PCF is an excellent choice for nonlinear applications such as SHG, Four Wave Mixing (FWM) and Supercontinuum Generation.

1.2 Choice of Material

Traditionally, Silica has been the material of choice for the fabrication of PCF due to its superior optical and material properties. However, the inversion symmetry of the Silica glass implies that its second order nonlinear susceptibility (χ^2) is zero. So far, various thermal poling techniques have been implemented to overcome this problem [6-9] which can bring the second order susceptibility of Silica glass to $d_{33} \sim 0.22 \text{ pm/V}$ [10]. Alternatively, commercially available lead Silicate glass (also called soft glass) of type SF57 (manufactured by Schott) can achieve a much higher second order susceptibility tensor value (of $d_{33} \sim 0.35 \text{ pm/V}$) when the electron-beam irradiation technique is applied¹ [11], [12]. Therefore, SF57 which is the

¹ Note that electron-beam irradiation cannot be applied to pure Silica.

earliest available single mode non-Silica glass PCF is a promising candidate material for SHG. Further, SF57-based PCF has been reported to have the highest nonlinearity in optical fibers ($640 \text{ W}^{-1} \text{ km}^{-1}$) [13]. Also, challenging structures such as nano-wires have been fabricated using SF57 glass [14]. This glass also possesses a higher thermal expansion coefficient ($9.2 \times 10^{-6} \text{ K}^{-1}$ [15]) compared to that of Silica ($\sim 5 \times 10^{-7} \text{ K}^{-1}$ [16]) which may allow for higher flexibility in adjusting the coherence length of the fiber.

1.3 Layout of the Paper

This paper is organized as follows: Section 2 details the numerical methods used while Section 3 provides a description of the ES-PCF structure considered. Section 4 presents detailed results and is divided into sub-sections: sub-section 4.1 discusses the effective indices and overlap integral of the fundamental and second harmonic modes; sub-section 4.2 contains results and discussion on the coherence length and quasi-phase matching; sub-section 4.3 discusses the error tolerance in the coherence length; Sub-section 4.4 discusses the power comparison between ES-PCF and PCF for fundamental and second harmonic frequencies and Sub-section 4.5 presents a comparison of bending loss between ES-PCF and conventional PCF. Finally, Section 5 presents the conclusions of the study.

2. Numerical Method

Initially, the Finite Element Method (FEM) was used for modal analysis. The FEM has been used to obtain the optimum ES-PCF structural parameters for SHG, following which the propagation constant (β) and the generated modal fields are used in the Finite Element Beam Propagation Method (FE-BPM) to analyze the evolution of the fundamental and second harmonic waves [17-20].

For modal analysis using the FEM, the cross-section of a waveguide is discretized into a number of triangular elements using an irregular mesh. The FEM, based on the vector H-field formulation, is used to obtain the modal field solutions and propagation constants of the fundamental and higher order quasi-Transverse Electric (TE) and quasi-Transverse Magnetic (TM) modes [21]. The full vector H-field formulation can be written as:

$$\omega^2 = \frac{\left(\int (\nabla \times \vec{H})^* \cdot \hat{\epsilon}^{-1} (\nabla \times \vec{H}) d\Omega \right) + \left(\int (\eta / \epsilon_0) (\nabla \cdot \vec{H})^* (\nabla \cdot \vec{H}) d\Omega \right)}{\int \vec{H}^* \cdot \hat{\mu} \vec{H} d\Omega} \quad (1)$$

where \vec{H} is the full-vectorial magnetic field, $\hat{\epsilon}$ and $\hat{\mu}$ are the permittivity and permeability, respectively, of the waveguide, ϵ_0 is the permittivity of the free space, and ω^2 is the eigenvalue where ω is the angular frequency of the wave. The dimensionless parameter η is used to impose the divergence-free condition of the magnetic field in a least squares sense to eliminate spurious solutions.

3. Equiangular Spiral PCF Design

The structure of the Equiangular Spiral Photonics Crystal Fiber (ES-PCF) is shown in Fig. 1. The air-hole arrangement of the ES-PCF structure mimics the "spira mirabilis" (Equiangular Spiral) which is seen in nature in nautilus shells and sunflower heads [5]. This ES pattern of the sunflower head produces the most efficient packing of seeds within the flower head without altering the angle or the shape of the curve and thus the air-holes in the ES-PCF are arranged in a similar pattern.

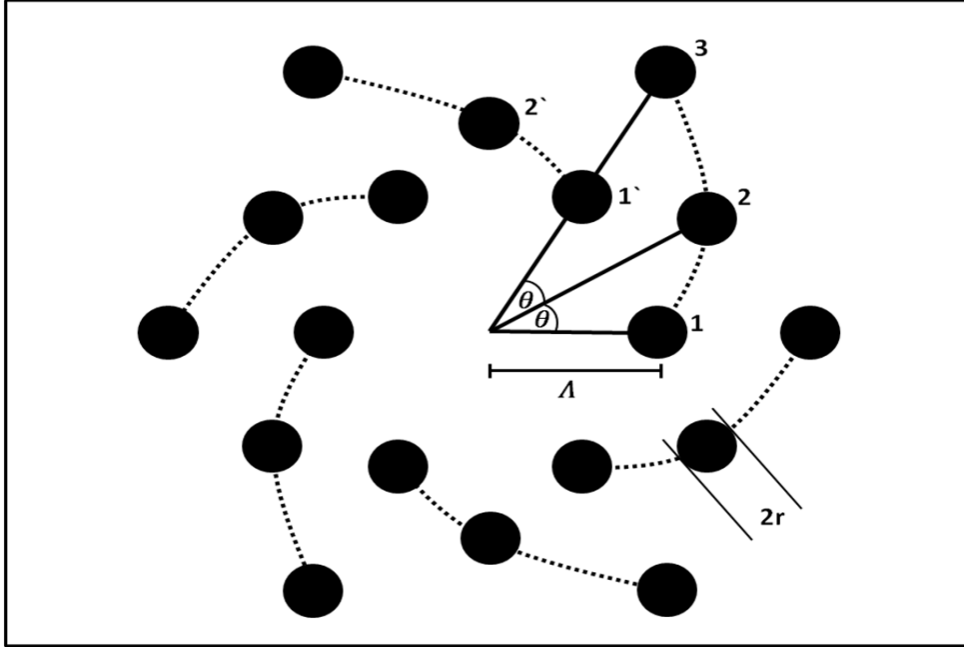


Fig. 1. Structure of the Equiangular Spiral-Photonic Crystal Fiber.

In the ES-PCF, each arm of air-holes forms a single ES where the angle from the centre of the core to adjacent holes of a given arm or ES differs by θ (e.g. the angular increment from hole 1 to hole 2 is θ and hole 2 to hole 3 is also θ). The diameter (d) of each air-hole is fixed at $2r$ where r is the air-hole radius. It should be noted that the equivalent holes of each arm can be considered to form a ring, e.g. the first holes of all the arms form the first ring and the second holes of all the arms form the second ring and so on. The radius (Λ) of the ES-PCF is defined as the distance between the centre of the core and the centre of an air-hole in the first ring. The radii drawn to the centre of air-holes on subsequent rings of the same ES, i.e. at intervals of θ , form a geometric progression. The distance between the air-holes within a ring increases with the ring number (e.g. the distance between holes 2 and 2' is larger than the distance between holes 1 and 1').

The main advantage of the ES-PCF is the improved field confinement in comparison to that of conventional PCF. This is due to the hole-orientation of the ES-PCF, where the outer air-holes block the field escaping through the material (i.e. inter-hole region) of the previous ring. The results presented in this paper show that the SH output power of SF57 ES-PCF is considerably higher than that of conventional PCF, e.g. $\sim 2.1W$ in ES-PCF as opposed to $\sim 1.6W$ in conventional PCF after the propagation of $250\mu m$ with a fundamental pump power of $1kW$ (continuous wave), operating fundamental wavelength of $1.064\mu m$, corresponding second harmonic wavelength of $0.532\mu m$, $d/\Lambda = 0.5$ and $\Lambda = 1.0\mu m$, while the ES-PCF design consisted of 6 arms, 4 rings and $\theta = 30^\circ$.

The ES-PCF structure with air-holes arranged in a spiral lattice in the cladding is represented in the simulation by an irregular mesh of 28800 triangular elements. In this paper, the H_{mn}^x (quasi-TM) and H_{mn}^y (quasi-TE) mode notations are used: the equivalent LP_{mn} notation has been indicated where appropriate.

4. Results

4.1 Modal Properties and SHG in the ES-PCF

The variation of the effective index (n_{eff}) with pitch (Λ) has been studied for the first order mode at the two frequencies ω and 2ω , and this is shown in Fig. 2. The dispersion properties of SF57 have been considered by using the refractive indices for SF57 and the Sellmeier coefficients of SF57 [15]. Here, $n_{eff} = \beta/k_0$ where β is the propagation constant and k_0 is the wavenumber ($k_0 = 2\pi/\lambda$ where λ denotes the wavelength). The first order mode H_{11}^x (i.e. HE_{11} or LP_{01}) of the fundamental frequency ω is indicated by H_{11}^x, ω .

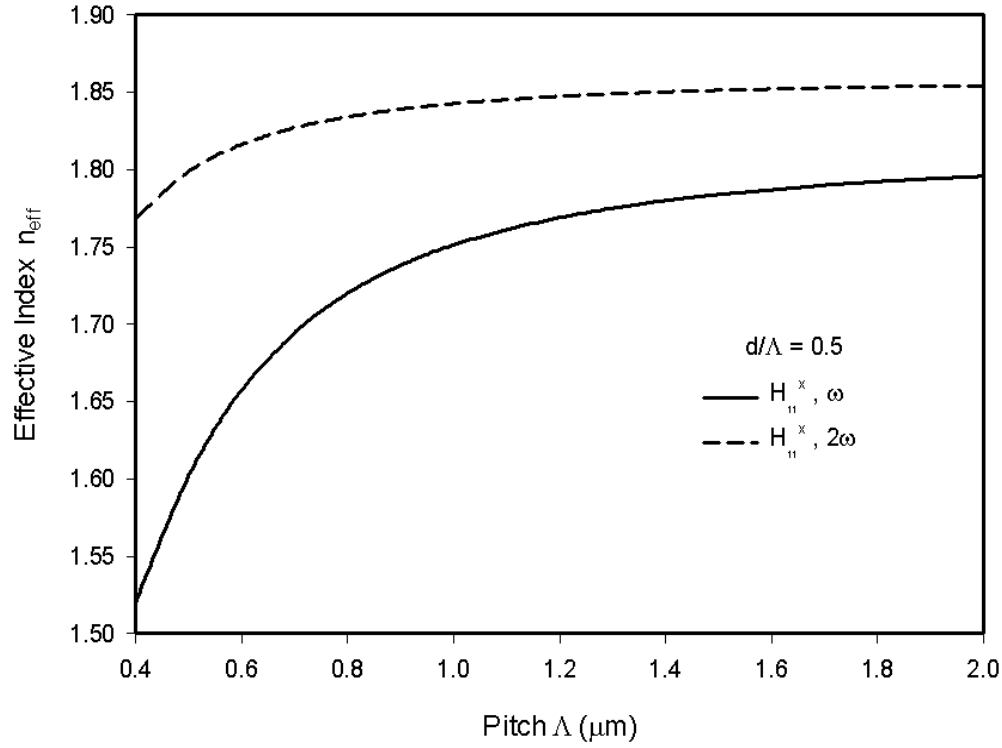


Fig. 2. Variation of the effective indices with the pitch for the first order mode at ω and 2ω .

As can be seen in Fig. 2, a reduction of the pitch results in a reduction of n_{eff} as the confined mode gets exposed to the first ring of air-holes. Initially the effective indices of the modes reduce slowly, but these decrease rapidly as the modes approach their cut-off conditions. Moreover the effective index of $H_{11}^x, 2\omega$ (i.e. H_{11}^x of the second harmonic frequency) is shown to move towards the cut-off condition at a lower rate than of H_{11}^x, ω . This is because the first order mode of the higher frequency (i.e. of second harmonic) is more confined in the centre than that of the lower frequency. Furthermore, as the pitch is increased, the mode becomes more confined to the core, resulting in n_{eff} asymptotically approaching the refractive index of SF57 (i.e. $n_{\omega}=1.81173$ and $n_{2\omega}=1.85841$).

The overlap integral (Γ) between the interacting fundamental and second harmonic first order modes (H_{11}^x) directly relates to the efficiency of power transfer between these modes, i.e. a higher value of the overlap integral results in a higher conversion efficiency and vice versa [2]. The definition of the overlap integral is given by:

$$\Gamma = \frac{\left| \iint E_{\omega}^2 \cdot E_{2\omega} \cdot dx \cdot dy \right|}{\left(\iint E_{\omega}^2 \cdot dx \cdot dy \right) \cdot \left(\iint E_{2\omega}^2 \cdot dx \cdot dy \right)^{1/2}} \quad (2)$$

where E_{ω} and $E_{2\omega}$ are the electric field distribution of the fundamental and second harmonic waves respectively [22]. Figure 3 illustrates how the overlap integral of the first order modes (H_{11}^x) for ω and 2ω vary with the pitch (Λ) over a range of d/Λ values.

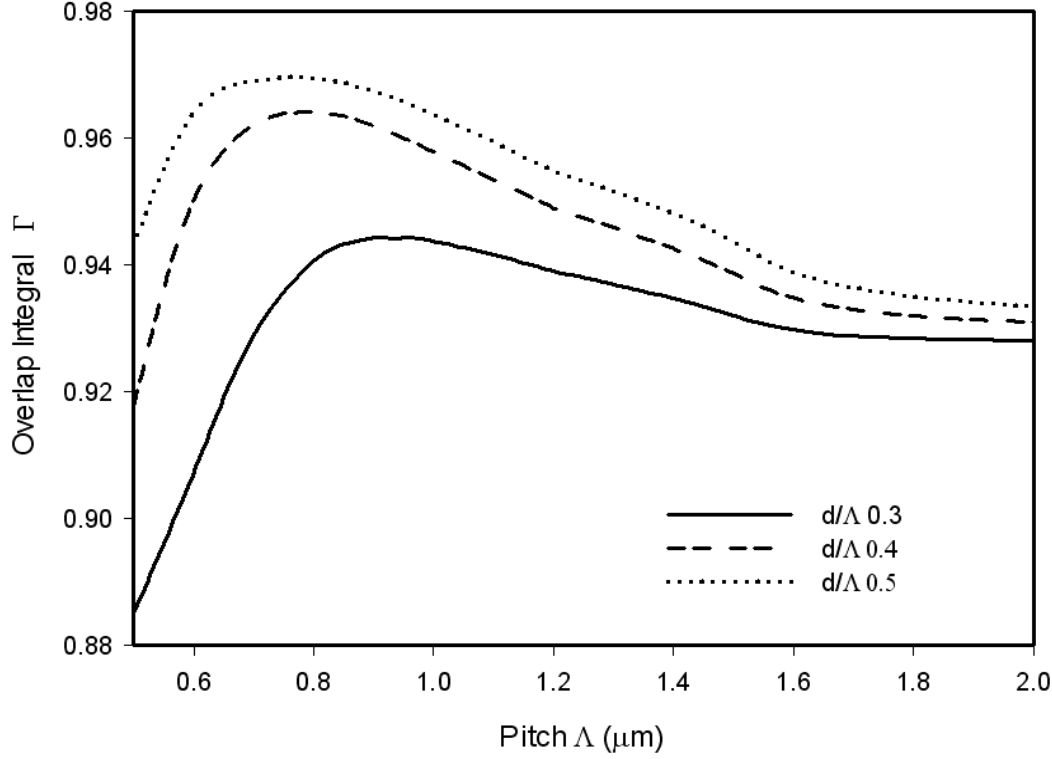


Fig. 3. Variation of the overlap integral with the pitch, Λ .

For a given pitch, the overlap integral increases as d increases. This arises because, as d increases, the equivalent index of the cladding decreases, increasing the index contrast between core and cladding, which in turn increases the confinement of the mode in the ES-PCF. Further, as the pitch decreases for a given value of d/Λ , the overlap integral increases reaching a maximum value (in the region $0.7\mu\text{m} \leq \Lambda \leq 1\mu\text{m}$) then starts to decrease: this can be explained as follows. Reducing the pitch makes H_{11}^x, ω and $H_{11}^x, 2\omega$ more confined which reduces the mismatch of their effective areas leading to an increase in the overlap integral. However, at very small pitch values the fundamental field reaches its cut-off region faster than the second harmonic field. Therefore, even though the second harmonic field becomes more confined to the core, the mismatch between fundamental and second harmonic fields becomes significant and the overlap integral starts to reduce at very small Λ values.

The overlap integral (Γ) and the Second Harmonic susceptibility tensor values (d_{ij}) are key parameters in determining the rate of power conversion. High SH power can be gained by d_{ij} values which are material properties; indeed the d_{ij} values of SF57 (i.e. $d_{33} \sim 0.35 \text{ pm/V}$) are high in comparison with that of Silica (i.e. $d_{33} \sim 0.22 \text{ pm/V}$). On the other hand, the overlap between the interacting modes depends on the fiber design. When the fundamental and second harmonic waves are not phase matched, the second harmonic power increases until the waves are out of phase and SH power starts depleting. Figure 4 shows the variation of the maximum output power (P_{L_c}) with the pitch (Λ), for different d/Λ values, where P_{L_c} is the power after the propagation of one coherence length (L_c) (which is explained in Section 4.2). This value is obtained by FE-BPM which takes into account all factors including phase matching.

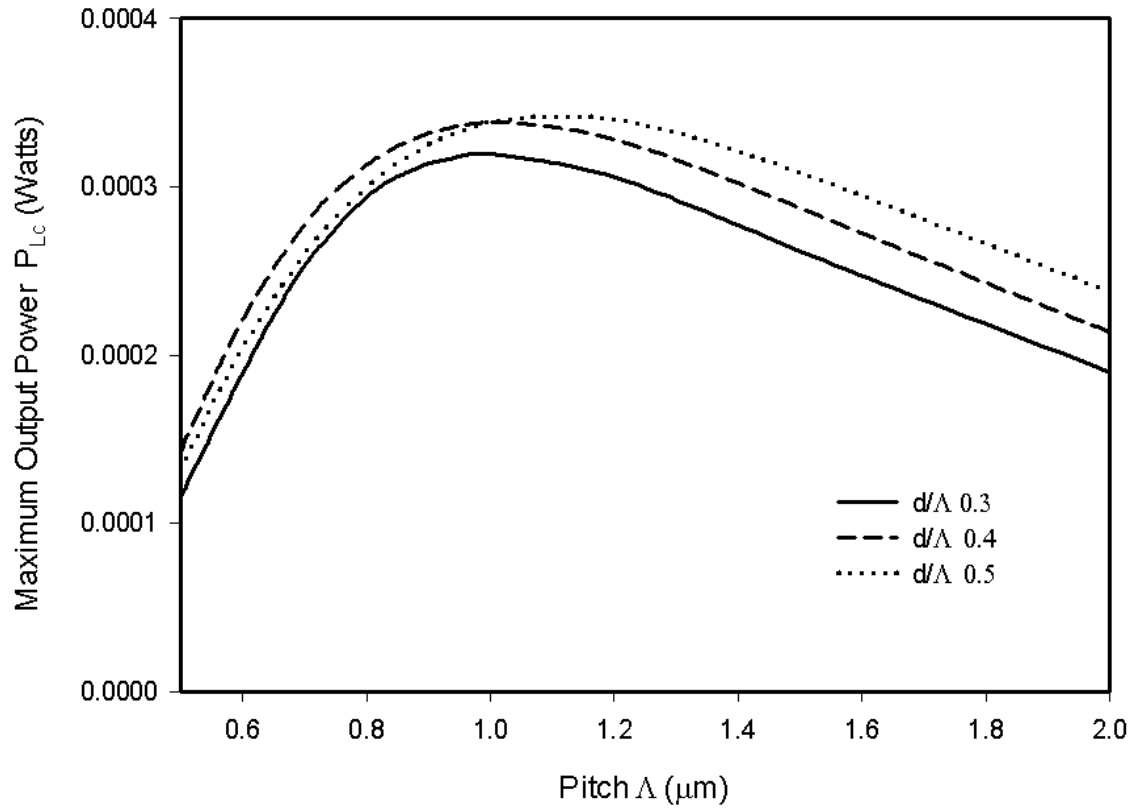


Fig. 4. Variation of the maximum Second Harmonic output power with the pitch.

It can be observed that a higher d/Λ value yields a higher value of P_{Lc} : this is because as d/Λ increases, the fraction of air increases in the ES-PCF, and the power intensity is more confined in the core. Even though the decreasing of the pitch causes the power to be further confined into the core, once it reaches its threshold, the power spreads into the air region and dissipates, reducing P_{Lc} and hence creating the peak values (in the region $0.9\mu\text{m} \leq \Lambda \leq 1.1\mu\text{m}$). Further, since the air filling fraction is higher for larger d/Λ values (e.g. $d/\Lambda = 0.5$), the cut-off region is reached faster than in the case of lower d/Λ values (e.g. $d/\Lambda = 0.3$).

4.2 Coherence Length and Quasi Phase Matching

The fundamental and second harmonic waves accumulate a phase shift of π over a distance known as the coherence length (L_c). Here $L_c = \pi/\Delta\beta$ and $\Delta\beta = \beta_{2\omega} - 2\beta_\omega$, where β_ω and $\beta_{2\omega}$ are the propagation constants of the fundamental and second harmonic waves respectively. The variation of L_c with respect to the pitch is plotted in Fig. 5.

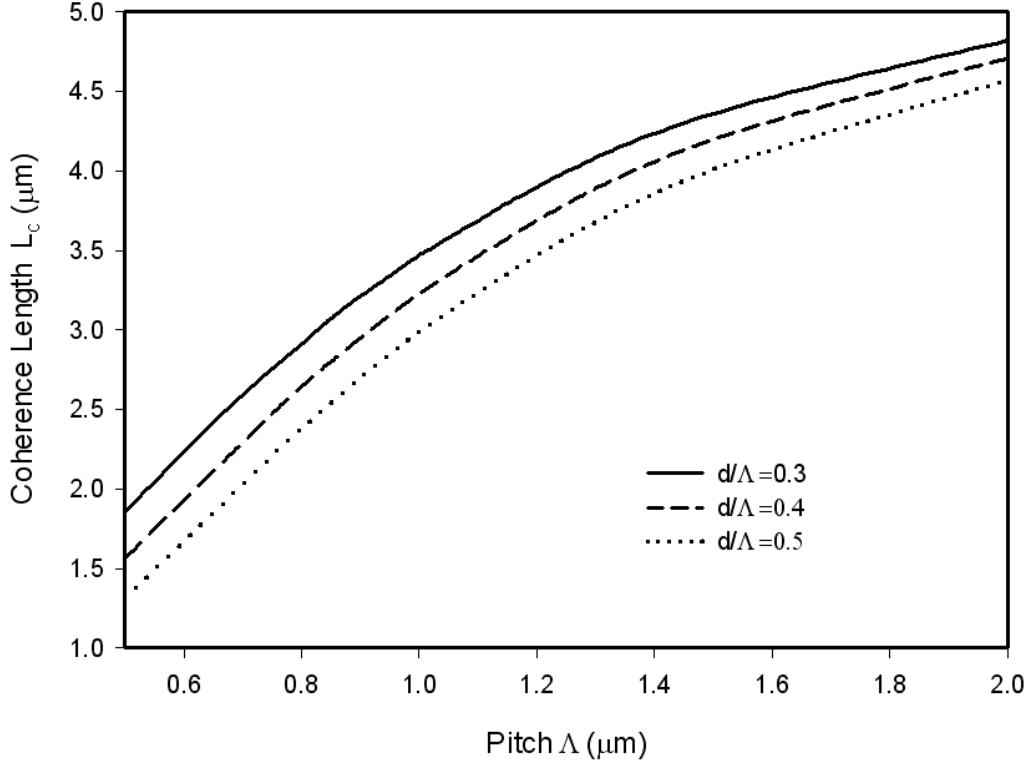


Fig. 5. Variation of the coherence length (L_c) with the pitch (Λ).

As d/Λ decreases for a given pitch (Λ), the effective index (n_{eff}) increases due to the increased area of the solid SF57 bridges between the air-holes: this results in an increase of L_c . Moreover, as the pitch is increased, the SF57 area is further increased and L_c asymptotically approaches the value for bulk SF57 ($\sim 5.69\mu\text{m}$). As the effective index increases, the propagation constant (β) also increases. As seen in Fig. 2, for higher Λ values, β_ω increases faster than $\beta_{2\omega}$ bringing $2\beta_\omega$ close to $\beta_{2\omega}$ (i.e. $2\beta_\omega \approx \beta_{2\omega}$) which results in a higher value of L_c . Further, the ideal condition occurs when $n^\omega = n^{2\omega}$ (where n^ω and $n^{2\omega}$ are the fundamental and second harmonic refractive indices respectively) which cannot be realized in practice due to the chromatic dispersion of the material.

The direction of power flow between the fundamental and second harmonic waves depends on their relative phase of the fundamental and second harmonic waves and hence this changes sign for a distance equal to every coherence length. To overcome this problem, a technique called Quasi Phase Matching (QPM) can be applied, i.e. by changing the sign of the nonlinear susceptibility (χ^2) at every L_c , the phase of the polarization wave is shifted by π , effectively re-phasing the interaction and leading to monotonic power flow into the second harmonic wave [23]. Changing the sign of χ^2 can be achieved by using poling techniques.

The most rapid growth of the second harmonic output power can be achieved by changing the sign of χ^2 for every L_c (which is known as first order QPM) as shown in Fig. 6 (for $d/\Lambda = 0.5$ and $\Lambda = 1.0\mu\text{m}$).

Changing the sign of χ^2 at every value of L_c (i.e. $\sim 2.9\mu\text{m}$) along the fiber length is challenging in practice. Hence, higher order QPM can be considered instead, i.e. n^{th} order phase matching can be achieved by poling with a period of nL_c . The QPM for the first, third and fifth order modulations are shown in Fig. 6. Note that higher order QPMs need a longer propagation distance to reach a given level of SH output power within the fiber when compared to lower order ones. However, this difference in the micro-meter range does not cause any problems given the length of a fiber in practice and in fact, higher order QPMs make the fabrication process easier especially in the case of short coherence lengths.

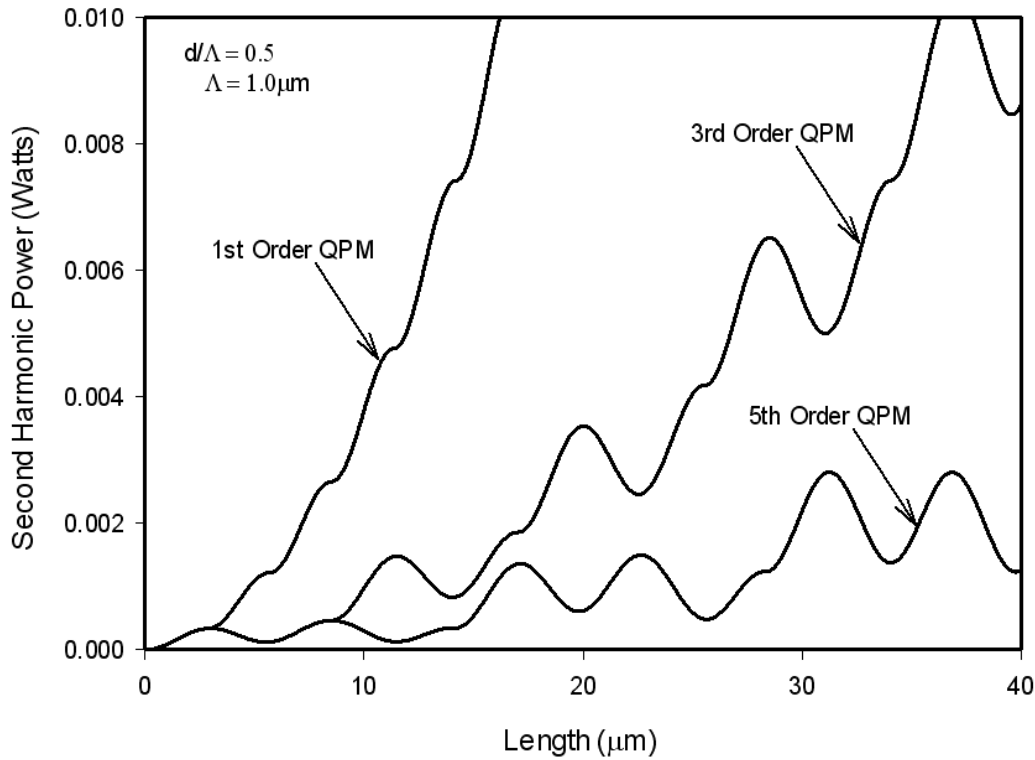


Fig. 6. Generated Second Harmonic power with first, third and fifth order Quasi Phase Matching.

4.3 Error Tolerance in Quasi Phase Matching

During the fabrication process, an error denoted by ΔL_c can occur, which is defined as the difference between the desired coherence length and the actual coherence length achieved after the fabrication. Assuming that the fundamental frequency propagates through N periodically poled regions, and the second harmonic output power builds up along the length of the ES-PCF, the accumulated error in length after propagating a distance NL_c is given by $N\Delta L_c$. After a distance of propagation during which the accumulated length error becomes equal to the coherence length, the phase mismatch is equal to π and the power starts to reduce [18]. This behavior can be observed in Fig. 7 and Fig. 8 for first order and fifth order QPM respectively.

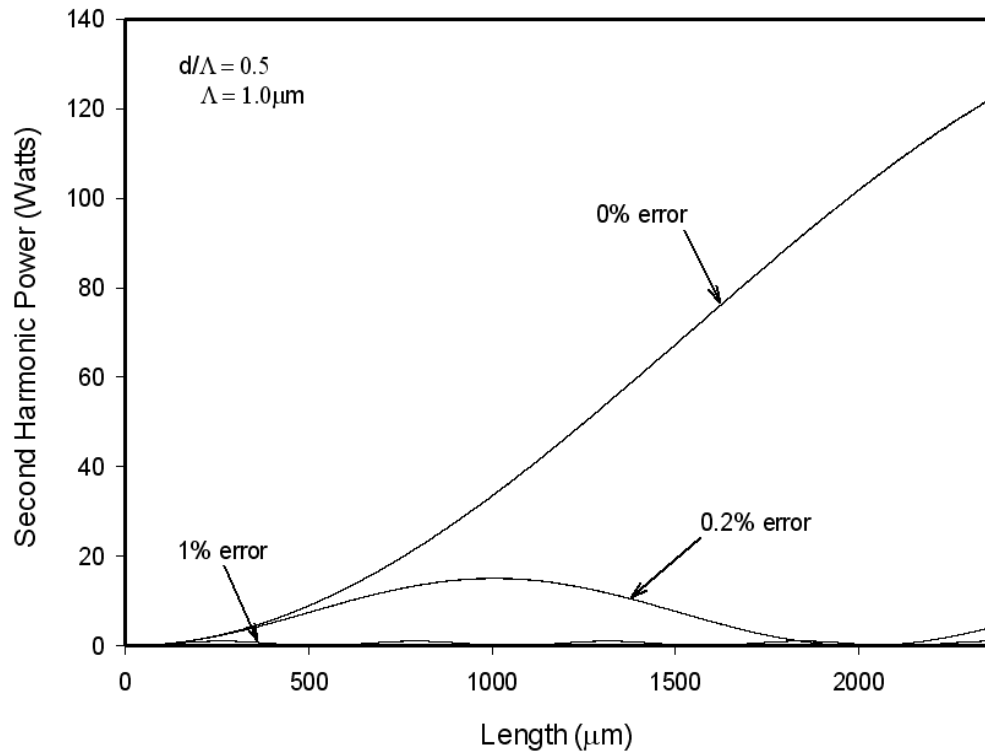


Fig. 7. Effect of fabrication tolerance on Second Harmonic output power with first order Quasi Phase Matching.

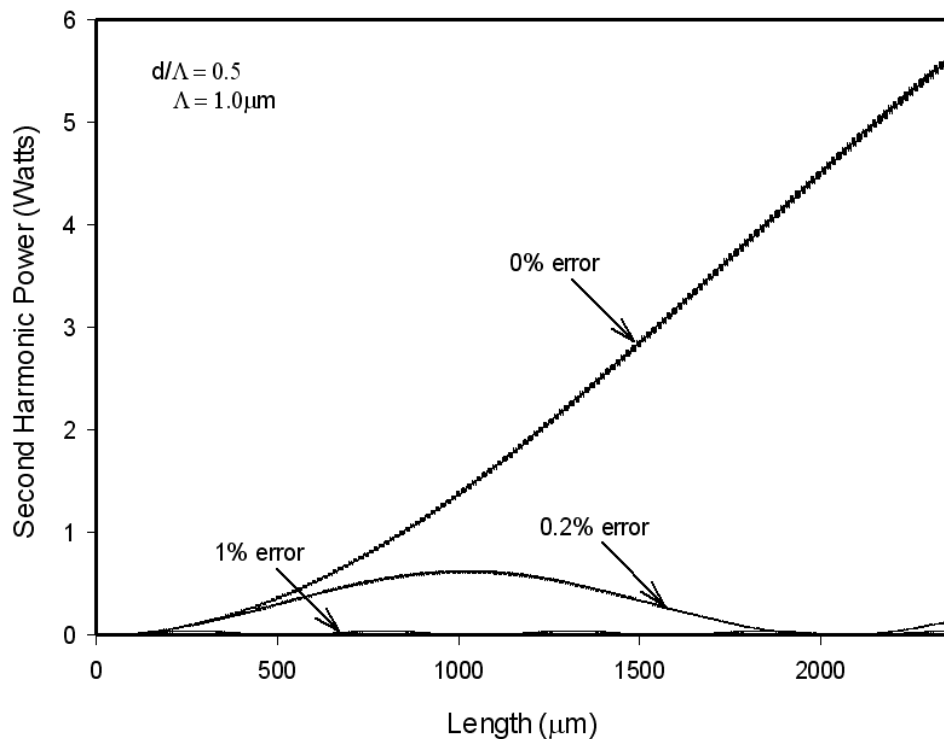


Fig. 8. Effect of fabrication tolerance on Second Harmonic output power with fifth order Quasi Phase Matching.

It can be seen that with the first order QPM, the maximum SH output power for the 0% error case (i.e. no fabrication error) reaches a value of $\sim 120\text{W}$ (and $\sim 5.6\text{W}$ with fifth order QPM) over a distance of $\sim 2350\mu\text{m}$ while a 0.2% error reduces the maximum power to $\sim 15\text{W}$ (and $\sim 0.7\text{W}$ with fifth order QPM) for the same distance. Therefore, once a reasonable coherence length is achieved by using poling techniques, it is important to fine-tune by employing techniques such as temperature tuning period of the Bragg Grating [24] or strain period of a long period grating [25] in order to minimize the error.

4.4 Second Harmonic Power Comparison

Figure 9 shows the first order quasi-phase matched SH output power for ES-PCF (SF57) and PCF (Silica and SF57) with varied numbers of air-holes. In all the cases $d/\Lambda = 0.5$ and $\Lambda = 1.0\mu\text{m}$.

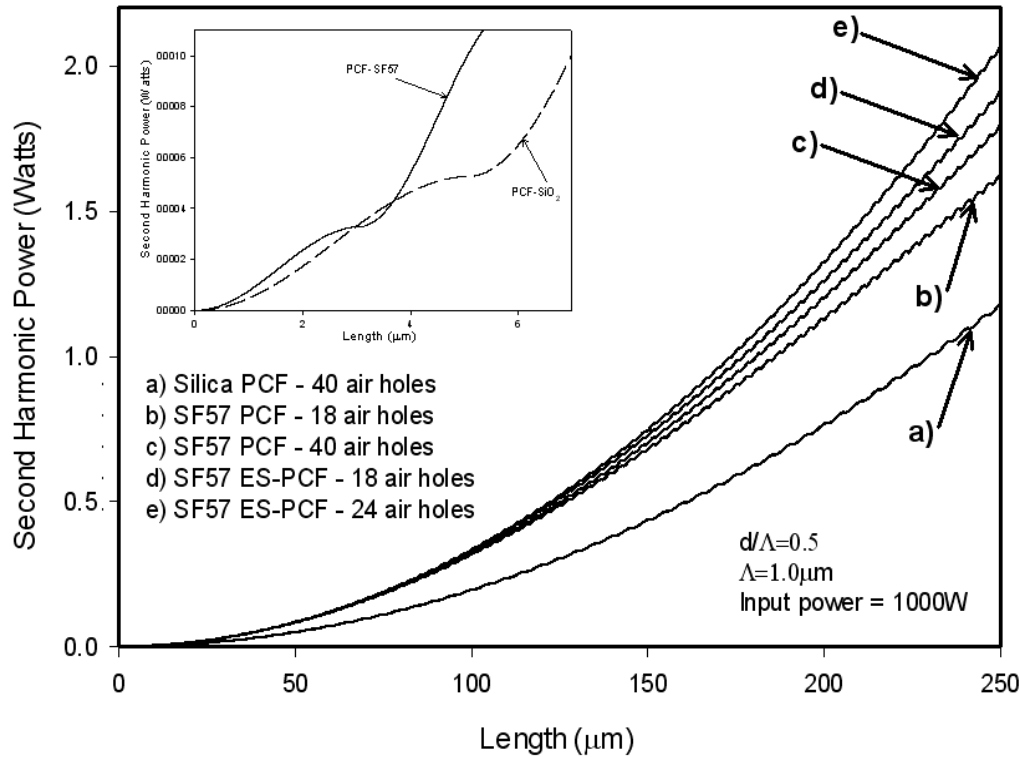


Fig. 9. Comparison of Quasi Phase Matched Second Harmonic output power with length, for different PCF structures and different materials. The inset graph shows an enlarged version of curves a) and c) for the propagation of a single coherence length.

It is clear that as the number of air-holes is increased, the SH power improves for both conventional PCF and ES-PCF. The SH power can be further improved by employing the ES-PCF structure (instead of conventional PCF) and the SF57 material (instead of Silica). Considering curves a) and c), i.e. conventional PCF with Silica and SF57 respectively, both with 40 air-holes it can be seen clearly that the SH output power of curve c) is much higher, which is due to the high d_{33} value of the SF57 material. The superiority of the ES-PCF structure is clearly illustrated by curve d), i.e. ES-PCF with 18 air-holes, which has a considerably higher output power ($\sim 1.9\text{W}$) than that of curve b) ($\sim 1.6\text{W}$), i.e. PCF with the same number of air-holes (and same material); and still higher compared with that of curve c) ($\sim 1.8\text{W}$), i.e. PCF with almost twice the number of air-holes (i.e. 40). Moreover, curve e) shows that the SH output power ($\sim 2.1\text{W}$) can be further improved by increasing the number of air-holes (i.e. 24 air-holes) in the ES-PCF. This improvement is already seen at a propagation length of $250\mu\text{m}$ and will be much more significant with further propagation. The difference between the two structures is a result of the superior confinement of the mode in the core region in ES-PCF which results in a better overlap integral compared to that of the conventional PCF structure.

The inset graph shows an enlarged version of curves a) and c) for the propagation over a single coherence length. The value of L_c of Silica is higher than that of SF57 which is due to the lower material refractive index difference between the fundamental and the SH waves (i.e. for SF57 $\Delta n = 0.0467$, for SiO_2 $\Delta n = 0.0097$). The inset graph shows clearly that the SH output power is higher in Silica after the propagation of a distance equal to one L_c . Nevertheless, as mentioned above, observations made at further propagation lengths show that SF57 leads to a higher level of power compared to Silica while the ES-PCF structure helps further increase the power.

4.5. Bending Loss

Bending and leakage losses are important factors to consider when determining performance and practical implementation of the PCF/ES-PCFs. The modal properties of the bending loss have been analyzed by full vectorial complex FEM with Perfectly Matching Layer (PML). Both types of structures suffer from bending loss due to the bend curvature creating an angle that is too sharp for the field to be reflected back into the core, causing some of the field to radiate from the fiber cladding. Further, it is well known that an optical fiber suffers from increased bending loss as it reaches its critical bending radius. However, bending can also be exploited to fine tune the modal properties of a PCF, and in this case the phase matching of the fundamental and second harmonic waves. The effect of bending can be modeled by converting a bent fiber to its equivalent straight fiber with a modified refractive index profile. The coordinate transformation allows a bent optical

waveguide in the x plane to be represented by an equivalent straight waveguide with a modified refractive index distribution, $n_{eq}(x, y)$ and thus:

$$n_{eq}(x, y) = n(x, y) \left(1 + \frac{x}{R} \right) \quad (3)$$

where $n(x, y)$ is the original refractive index profile of the bent waveguide, $n_{eq}(x, y)$ is the equivalent refractive index profile of a straight guide, R is the radius of the curvature and x is the distance from the centre of the waveguide [26]. It was observed that coherence length can be adjusted up to 3% by introducing a bending in these PCFs (results are not shown here). However, bending a PCF also introduces a resulting bending loss. Bending and leakage losses can be reduced by increasing the number of air-holes, although this generally adds to the fabrication costs. Previously, it has been shown that ES-PCF suffers from lower leakage and bending losses, as the second ring of air-holes can be placed more effectively [27]. Figure 10 shows the comparison of the bending loss as a function of the bending radius in ES-PCF and PCF designs in SF57 for both the fundamental and second harmonic waves.

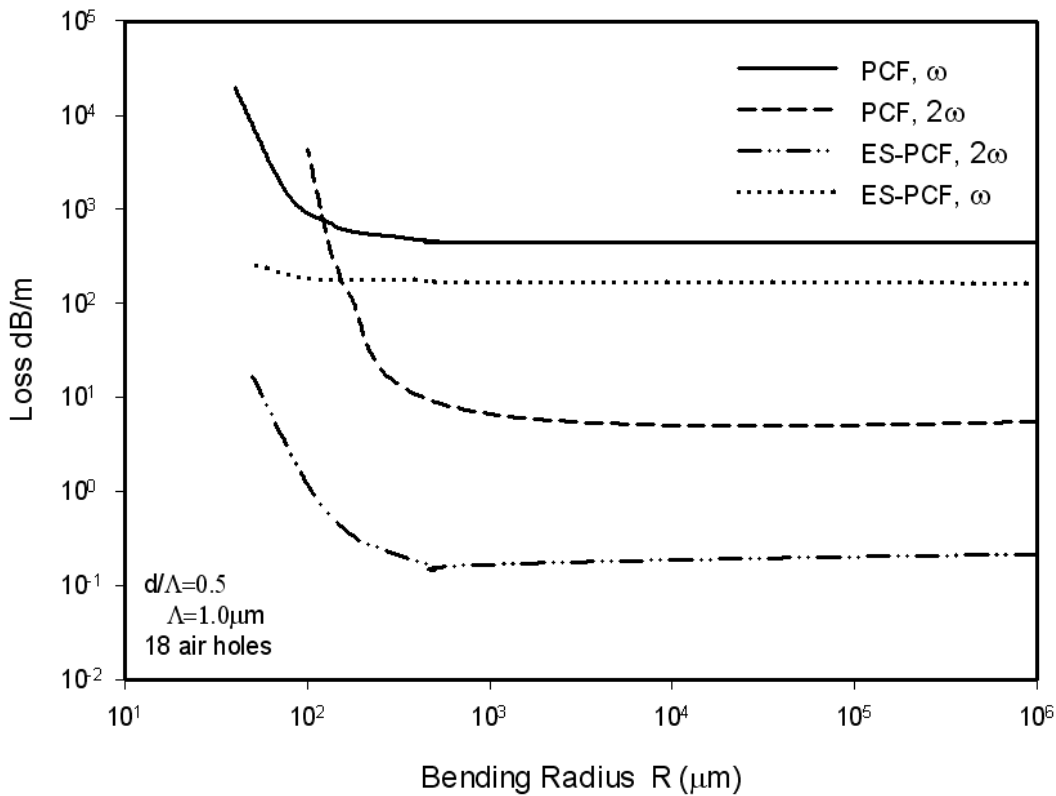


Fig. 10. Comparison of the bending loss as a function of the bending radius for ES-PCF and PCF with fundamental and Second Harmonic frequencies.

In this case, the number of air-holes is taken to be 18 for both ES-PCF and PCF. As seen in Fig. 10, the bending loss in ES-PCF is significantly lower than that of PCF for the fundamental frequency. A similar behavior can be observed in ES-PCF and PCF for the SH frequency but with lower loss as the modes are well confined. The low confinement loss occurs due to the unique orientation of the air-holes of the ES-PCF structure [28]. When the bending radius is decreased, the air-holes in the outer rings in ES-PCF (which are positioned between the air-holes of the inner rings) prevent the mode escaping through the SF57 bridges. However, both bending and leakage losses can be further reduced by increasing the number of air-holes. For a given number of air-holes, ES-PCF suffers lower bending and leakage loss than the conventional PCF, particularly when the number of air-holes is modest, which reduces fabrication costs while also making such ES-PCF easy to handle for practical applications.

5. Conclusions

In this paper, numerically simulated results show that a significantly higher level of SH output power can be achieved by employing the ES-PCF design in SF57 soft glass rather than conventional Silica PCF. For example, a power increase of 31% was numerically demonstrated from conventional PCF ($\sim 1.6W$) to ES-PCF ($\sim 2.1W$) for a propagation length of $250\mu m$. The higher output power is a result of the higher overlap integral due to the better modal properties in ES-PCF. The Quasi Phase Matching technique has been applied in order to achieve maximum SH output power. It has been shown that potential fabrication tolerances lead to errors in the coherence length which could result in a substantial reduction in the generated Quasi Phase Matched SH power. However, it is possible to minimize fabrication errors by temperature or strain tuning. Moreover, the ability of the ES-PCF structure to effectively control the modal field gives rise to ultra-low bending loss which would be easy to handle: this is a significant advantage over conventional PCF and furthermore, bending can also be exploited in the adjustment of phase matching.

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