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**Title: Some mistakes go unpunished: the evolution of “all or nothing”
signalling**

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24 **Running title:** evolution of “all or nothing” signalling

25

26 **Abstract**

27 Many models of honest signalling, based on Zahavi’s handicap principle, predict that
28 if receivers are interested in a quality that shows continuous variation across the

29 population of signallers, then the distribution of signal intensities will also be

30 continuous. However, it has previously been noted that this prediction does not agree

31 with empirical observation in many signalling systems, where signals are limited to a
32 small number of levels despite continuous variation in the trait being signalled.

33 Typically, there is a critical value of the trait, with all individuals with trait values on

34 one side of the threshold using the same cheap signal, and all those with trait values

35 on the other side of the threshold using the same expensive signal. It has already been

36 demonstrated that these classical models naturally predict such “all-or-nothing

37 signalling” if it is additionally assumed that receivers suffer from perceptual error in

38 evaluating signal strength. We show that such all-or-nothing signalling is also

39 predicted if receivers are limited to responding to the signals in one of two ways. We

40 suggest that many ecological situations (such as the decision to attack the signaller or

41 not, or mate with the signaller or not) involve such binary choices.

42

43 **Keywords:** signaling, signal honesty, Zahavi’s handicap principle, communication,

44 cost of signalling

45

46 **Introduction**

47 Game theoretical models based on Zahavi's handicap principle have been very
48 influential in offering an explanation for how signalling can remain (on average)
49 honest when there is conflict of interest between signaller and receiver (Maynard
50 Smith & Harper 2003; Searcy & Nowicki 2005) . Johnstone (1994) raised an
51 interesting comparison between the predictions of still-influential models and
52 empirical observation. Models generally predict that the intensity of the signal will
53 vary continuously in relation to the quantity being signalled. For example, in a
54 situation where potential prey individuals vary continuously in the strength of their
55 chemical defences, these models would predict a similar continuous distribution of
56 warning signal intensities to potential predators. To express this another way, these
57 models predict that the signals should provide exact quantitative information about the
58 specific defensive capability of each signaller. In contrast, Johnstone (1994) provides
59 numerous empirical examples of signals where observed variation in signal strength is
60 much less: being confined to a small number (often two) of discrete signal strengths.
61 In the context of our example above, this would suggest that even if there is strong
62 and continuously-distributed between-individual variation in the strength of the
63 defences being signalled, the potential prey only adopt one of two signal intensities.
64 All those individuals with defence levels below some threshold value produce
65 essentially identical signals of the same low intensity; all those with defence values
66 above the threshold signal at the same characteristic high intensity. In comparison to
67 the model predictions then, real signals often seem less quantitatively informative.
68 They inform the receiver not about the specific quality of an individual signaller but
69 only about the range of qualities (either above or below the threshold in the example
70 above) in which the individual falls.

71 Johnstone (1994) not only drew attention to this apparent tension between
72 model predictions and empirical observations, he also offered a plausible solution. He
73 demonstrated that previous models had assumed that the receiver identifies the
74 intensity of the signal with perfect fidelity. If, however, perceptual errors are
75 introduced into these models, such that the receiver can make errors in their
76 evaluation of the signal intensity, then the predictions of the models change to being
77 much more in line with the “all or nothing” displays often seen in nature. Such
78 perceptual errors are very plausible (Dusenbury 1992; Hailman 2008).

79 Here we make no criticism of Johnstone’s (or any other previous) work but
80 present another modification to previous models which we argue is biologically
81 realistic, very widely applicable and again leads to a prediction of “all of nothing”
82 displays even when no perceptual errors are assumed in the model. Essentially our
83 key modification rests in the evaluation of optimal predator behaviour. Like previous
84 works, Johnstone assumed that the optimal strategy for the receiver was that which
85 minimized the least-square estimate of signaller quality for each perceived advertising
86 level. That is, the receiver is expected to be selected to evaluate the underlying quality
87 of all individuals as accurately as possible, and all deviations from accurate estimation
88 are in some way costly to the receiver. We suggest that there are many biological
89 situations where the challenge facing the receiver is less strict and some mis-
90 evaluations produce no fitness cost.

91 Consider again the predator that encounters individuals from a prey population
92 that vary continuously in their level of chemical defence. On encountering a potential
93 prey individual, the predator must make a binary decision: to eat the individual or not.
94 If the predator somehow had complete and perfect knowledge of the level of chemical
95 defence in each prey individual then the most rational strategy is to identify the

96 minimum level of defence that makes a prey individual unattractive, then eat all
97 individuals with levels below this threshold and reject all those with levels above it
98 (Skelhorn & Rowe 2007). The problem for most real predators is that they do not
99 have this perfect knowledge, rather they must make their decisions based on each
100 individual's level of signalling (Mappes et al 2005). Let us imagine that the level of
101 defence can vary between zero and one and the threshold value discussed above is
102 denoted by T . The challenge facing the predator is not to evaluate the defence level of
103 each encountered individual as accurately as possible, but rather to make as few
104 misclassifications as possible as it attempts to classify each individual as having a
105 defence level either above or below T . Another way to look at this is that (unlike the
106 formulation of Johnstone 1994 and other models) not all mistakes in the estimation of
107 a prey individual's level of defense incur fitness costs for the predator. If the true level
108 of defence is D and the predator estimates the defence as a different value d , then this
109 error only has fitness consequences for the predator (it only changes its behaviour) if
110 D and d bracket the threshold value T , otherwise the inaccuracy of estimation has no
111 effect. Further, it may be that the cost of a misclassification to the predator depends
112 upon the value of D , but the value of d has no effect on the size of this cost, except in
113 influencing whether or not misclassification occurs (and thus whether or not the cost
114 is paid). Thus, we suggest that models where receivers can only produce a discrete
115 number of responses to the signal might reasonably involve the assumption that
116 fitness is affected not by accurate estimation of the qualitative value of the underlying
117 quality of signallers, but by the less onerous task of correctly classifying prey into a
118 number of distinct categories. We expect that this situation will occur commonly,
119 where a receiver must make a simple binary choice (e.g. to attack or not, to mate or

120 not, to abandon a nest or not). Here we will explore the consequences of this change
121 of fitness function for model predictions.

122

123

124 **Model description**

125 For ease of comparison we have attempted to keep our model definition and structure
126 as close to that of Johnstone (1994) as possible.

127

128 We suppose that signallers vary in some quantity that is of interest to receivers, but
129 which they cannot directly observe. We denote the value of this quantity held by a
130 specific individual as q (for quality). Signallers can vary in the intensity of some
131 signal that can be directly observed by receivers, with the signal given by a specific
132 individual being denoted a (for advertising). We denote the function $A(q)$ as the
133 signalling strategy, which specifies the signal intensity (the value of a) given by
134 individuals of different qualities (different values of q).

135

136 On receipt of the signal from a specific signaller, the receiver can act in one of only
137 two distinct ways (we denote these alternatives “choice 0” and “choice 1”). The
138 receiver strategy is described by $g(a)$, which is the probability of making choice 1 on
139 receipt of a signal of intensity a . By definition, an individual which does not make
140 choice 1 must make choice 0, and vice versa. Unlike Johnstone (1994), we assume
141 perfect fidelity of signal transmission, so if the signaller sends a value a , the receiver
142 receives exactly that same value.

143

144 The reward U that a signaller gets from an interaction with the receiver depends on its
145 quality q , the signal strength it used a , and the response of the receiver (either 0 or 1).
146 Thus the reward to the signaller is $U(a,i,q)$, where i is the response of the receiver: i
147 $\in \{0,1\}$.

148

149 We assume that choice 1 by the receiver is always more beneficial to the signaller
150 than choice 0. That is $U(a,0,q) < U(a,1,q)$ for all combinations of a and q values. Thus
151 in our previous example, choice 1 is rejection of the signalling prey by the predator.

152 We also assume that the advantage of choice 1 over choice 0 to the receiver does not
153 decrease with q , i.e.

154

$$155 \frac{\partial(U(a,1,q) - U(a,0,q))}{\partial q} \geq 0. \quad (1)$$

156 For example, a high-quality male will have at least as large a gain from mating over
157 not mating as a lower-quality male. This seems generally likely to be true for mating
158 systems. For our predator-prey example, the difference between choice 1 and choice 0
159 is between persuading the predator not to attack versus being attacked. In this case,
160 condition (1) means that even very highly defended prey benefit from persuading the
161 predator not to attack at least as much as weakly defended prey do. Whilst it may be
162 that very highly defended prey can survive attacks because the predator discovers the
163 level of defence during the attack and thus aborts the attack, even such abortive
164 attacks can be costly to prey in terms of risk of injury and/or time and energy wasted.
165 Further, in some situations the predator may have already killed the prey before
166 aborting the attack when realizing that the particular prey item is too defended to be
167 eaten. Thus condition (1) seems plausible in a predator-prey context too.

168

169 We further assume that signals are expensive to the signaller, and that this expense
170 increases (and so the net reward from an interaction decreases) with increasing
171 signalling intensity. Thus we assume that for all combinations of (a,i,q) ,

172

173
$$\frac{\partial U(i,q)}{\partial a} < 0. \tag{2}$$

174 We also assume that the cost of higher signal intensity is proportionately greater for a
175 lower quality individual:

176

177
$$\frac{\partial^2 U(i,q)}{\partial q \partial a} > 0. \tag{3}$$

178 These assumptions about the costs of signalling are those generally considered as
179 requirements for honest signalling via the handicap model (Grafen 1990, Bradbury &
180 Vehrencamp 1998, Searcy & Nowak 2005; but see Lachman et al 2001 for an
181 exception).

182

183 The reward to a signaller of quality q that signals with intensity a is given by

184

185
$$S_q = g(U(1,q)) - g(U(0,q)) \tag{4}$$

186

187 We assume that there is only a single type of receiver in our model, so that for
188 instance receivers do not vary in quality and hence in their reward functions. We also
189 assume the reward to the receiver from an encounter is a function of the quality of the

190 signaller q and the receiver's decision i , which we shall denote by $V(q,i)$, and that the
 191 higher the quality of the signaller (the higher q is) the better it is for the receiver to
 192 make choice 1. That is $V(q,1) - V(q,0)$ increases with q . In our example, the more
 193 defended the prey individual the more advantageous it is for the predator to reject the
 194 opportunity to eat it.

195

196 Let $f(q)$ describe the frequency distribution of signallers of different qualities in the
 197 local population (which the receiver encounters randomly). The expected receiver
 198 reward is a function of its strategy (g) and is given by

199

$$\begin{aligned}
 R(g) &= \int f(q) V(q,0) (1-g) dq + \int f(q) V(q,1) g dq \\
 &= \int f(q) V(q,0) dq + \int f(q) [V(q,1) - V(q,0)] g dq
 \end{aligned}
 \tag{5}$$

201

202 where integrals are evaluated over all possible values of signaller quality. We shall
 203 assume that in the absence of any signal the receiver will always make choice 0 (e.g.
 204 predators must always attack some prey to survive, so in the absence of a signal they
 205 will attack all prey rather than none), i.e.

206

$$\int f(q) V(q,0) dq > \int f(q) V(q,1) dq
 \tag{6}$$

208

209 **Model evaluation**

210 We know that $V(q,1) - V(q,0)$ increases with q ; let us suppose in particular that

211 $V(q,1) - V(q,0) < 0$ if and only if the quality of the signaller is below some critical

212 value q_{crit} , so we have

213

214 $V(q_{crit}, 0) \geq V(q_{crit}, 1)$. (7)

215

216 Thus the receiver would benefit from making choice 0 if and only if $q < q_{crit}$.

217

218 Any strategy of the receiver must specify how it responds to every possible signal.

219 Denote the set of all signals a for which the receiver actually makes choice 1 as A_1 ,

220 and the set of all signals for which the receiver makes choice 0 as A_0 . A_1 and A_0 are

221 disjoint sets (no possible signal appears in both sets), and all possible signals are a

222 member of either A_0 or A_1 .

223

224 Since receivers respond to all signals in A_1 identically, but signals are increasingly

225 costly (inequality (2)) to senders as signal intensity increases, the only rational signal

226 in the set A_1 for a signaller to give is the lowest intensity (cheapest) signal in that set:

227 which we denote $\min(A_1)$. Similarly since receivers respond to all signals in A_0

228 identically, but signals are increasingly costly to senders as signal intensity increases,

229 the only rational signal in the set A_0 for a signaller to give is the lowest intensity

230 (cheapest) signal in that set: which we denote $\min(A_0)$.

231

232 Since $U(a, 0, q) < U(a, 1, q)$ for all combinations of a and q values, for $\min(A_0)$ to be

233 optimal for any q , this implies that $\min(A_0) < \min(A_1)$; that is that the signal associated

234 with the less favourable receiver choice 0 must be of lower cost, and so at a lower

235 intensity, than that associated with the more favourable choice 1. Since all possible

236 signals are in either A_0 or A_1 , the signal associated with 0 will be the cheapest signal

237 of all the possible signals that are open to those individuals ($A_1 \cup A_0$). Thus if the

238 lowest cost signal is $a = 0$, then $\min(A_0) = 0$. Let us further define $a_1 \equiv \min(A_1)$.

239 Clearly a_1 must be greater than zero. Thus there are at most two distinct signals in any
240 evolutionarily stable signalling system. A necessary qualification at this point is that
241 this is only true when receivers do not vary in quality to a sufficient degree that
242 different receivers would ideally like to respond to many different signallers in
243 different ways. If there is wide receiver variation, our results would no longer be
244 valid. For instance Johnstone & Grafen (1992) consider the Sir Philip Sidney game
245 where the choice to receivers is to donate food to a relative or not. All receivers
246 survive if they do not donate (and all signallers survive if they receive a donation), but
247 some receivers (signallers) are almost guaranteed to survive if they donate (do not
248 receive), and others are almost guaranteed to die. Under such circumstances,
249 assuming high relatedness, different receivers would “want” to make different
250 decisions to a wide range of signallers (equivalent to having very different values of
251 q_{crit} in our model), and consequently their model has a continuous signalling solution.

252

253 It should be noted that our argument about the number of distinct signals generalizes
254 to a system where the receiver has any finite number of decisions n . If we denoted the
255 set of all signals for which the receiver would respond with choice i by A_i , then the
256 only potentially consistent signal choices by the signallers would be $\min(A_i)$, and so
257 the maximum number of distinct signals would be n .

258

259 Now let us suppose that we have an “honest” signal, namely one that distinguishes the
260 signallers for which the receiver would want to make choice 0, from those for which
261 choice 1 would be best. This would yield

262

263
$$g(q) = \begin{cases} 1, & q > q_{crit} \quad (q \in A_1) \\ 0, & q < q_{crit} \quad (q \in A_0) \end{cases} \quad (8)$$

264

265 When the receiver plays this strategy then the reward to the signaller simplifies to

266

267
$$S_q(q) = \begin{cases} U(0,0,q) & a \in A_0 \quad (q < q_{crit}) \\ U(a_1,1,q) & a \in A_1 \quad (q > q_{crit}) \end{cases} \quad (9)$$

268

269 Thus the optimal signalling strategy associated with an honest signal should be

270

271
$$A(q) = \begin{cases} \min(A_0) = 0, & q < q_{crit} \\ \min(A_1) = a_1 > 0, & q > q_{crit} \end{cases} \quad (10)$$

272

273 For there to be a stable signalling strategy where all $q < q_{crit}$ individuals pick 0 and all

274 $q > q_{crit}$ individuals pick a_1 , for some positive a_1 , we need both choices to offer the

275 same reward to the signaller when $q = q_{crit}$ (otherwise individuals of quality either just

276 above or below q_{crit} could do better by switching signal). Thus we need

277

278
$$U(a_1,1,q_{crit}) = U(0,0,q_{crit}). \quad (11)$$

279

280 Since $U(a_1,1,q)$ decreases with increasing a_1 , there is at most one value of a_1 that

281 satisfies (11). Such a value will exist provided there is such a critical quality value q_{crit}

282 where the receiver would want to change their strategy, and that the largest signals are

283 sufficiently costly, so that $U(\infty,1,q_{crit}) < U(0,0,q_{crit})$. Thus $[0, a_1) \subseteq A_0$ and $a_1 \in A_1$. In

284 fact we shall assume the natural solution of $A_0 = [0, a_1)$ and $A_1 = [a_1, \infty)$.

285

286 Inequalities (1) and (2) ensure that for lower quality individuals the relative costs of
287 signalling compared to the benefits of receiving choice 1 are higher, and consequently
288 any individual of quality $q < q_{crit}$ would do worse by changing its signal to a_I or any
289 other value in A_I , and any individual of quality $q > q_{crit}$ would also do worse by
290 switching signal. Note that the combination of (1) and (2) are sufficient but not
291 necessary, so that the relative costs compared to benefits may decrease with quality
292 even if only one of the two conditions hold.

293

294 Note that the exact composition of the sets A_0 and A_I in such a system depends upon
295 how rogue signals not equal to 0 or a_I come about. Any individual that uses such a
296 signal is behaving sub-optimally, so we would expect such situations to be rare. The
297 exact solution in these rare cases would depend upon assumptions about the
298 underlying causes of such irrational behaviour (see Discussion).

299

300 It should also be noted that only two signals are used at equilibrium, and that if there
301 are no rogue signals as described above, every receiver strategy that responds to these
302 two signals in the same way thus performs equally well at the equilibrium, regardless
303 of how they respond to other signals. We assume that there will be a low level of such
304 “mistakes” which means that all receivers have to play optimally against the “non-
305 played” strategies themselves. This idea is often used in game theoretical modelling,
306 and is known as the “trembling hand” (Selten, 1975).

307

308 It is possible to envisage a signalling system that is not entirely honest. For stability
309 all low-quality individuals must play 0, and all high quality individuals must play

310 $\min(A_1)$; but perhaps there can be a cut-off point q^* that is different to q_{crit} . If we
311 replace q_{crit} by q^* in (8-11), we would obtain a different equilibrium signalling system
312 with a new level a^* for the higher signal. In the case where $q^* > q_{crit}$, so that
313 $a^* = \min(A_1) > a_1$, such a system could be destabilized by the introduction of a signaller
314 that included $a_1 \in A_1$, which would enable individuals with qualities $q^* > q > q_{crit}$ to
315 signal honestly to the benefit of themselves and the receiver. There will also be a
316 value q_{min} so that if $q^* \leq q_{min}$, (i.e. if q^* is sufficiently small), then (due to inequality 6)
317 the expected reward to the receiver will be at least as high if it changes to make choice
318 0 against all signals, and so again the system is not stable. This leaves a family of
319 possible “semi-honest” signalling systems with cutoff q^* such that $q_{min} < q^* \leq q_{crit}$ that
320 might be stable in some circumstances (when the “honest” solution also exists). Note
321 that such alternative solutions are “semi-honest” in the sense that every individual
322 giving the higher signal is of better quality than every individual giving the lower
323 signal. However, some individuals with qualities near to (and on one side of) the
324 critical value will gain advantage by using the “wrong” signal from the receiver’s
325 viewpoint. Thus it is important to note that we do not claim that the fully honest signal
326 is the one that the population will evolve to. We have shown, however, that such a
327 system is a possible solution, and that all of the other potential solutions have the
328 same all-or-nothing property.

329

330 The general solution for our model is that signallers below a defined quality threshold
331 all signal using the lowest-cost signal that is possible, and receivers respond to this
332 signal with the choice that least benefits signallers; signals with quality above this
333 threshold all signal using the same signal, this is a higher cost signal than that used by
334 low-quality individuals and is the signal that leads to the same payoff to individuals of

335 the critical quality regardless of what the receivers do. Receivers respond to the
336 higher-cost signal by adopting the behaviour (from a choice of two) that is more
337 beneficial to signallers.

338

339 Thus, although signallers vary continuously in quality, they do not show continuous
340 variation in signal strength at this equilibrium. Rather, the discrete nature of the
341 behavioural responses to signals available to the receiver causes the receiver to be
342 interested in categorizing signallers rather than fully evaluating their quality, and this
343 in turn leads to signalling being restricted to a number of discrete levels, less than or
344 equal in number to the number of behavioural options open to the receiver.

345

346 **An example**

347 Let us consider a simple example where males of quality q signal to females, who can
348 choose either to mate with a specific male or not.

349

350 For the female, there is no reward (or cost) for declining to mate $V(q,0) = 0$. Mating
351 requires a fixed cost (α) and benefits increase linearly with the quality of the male.

352 Thus, at its simplest $V(q,1) = q - \alpha$.

353

354 For the male, there is a cost for an individual of quality q to produce a signal of
355 strength a given by a/q . There is an additional payoff of unity if the female chooses to
356 mate and zero otherwise. Thus,

357

$$358 \quad U(q,0,q) = -\frac{a}{q}, \quad U(q,1,q) = 1 - \frac{a}{q}.$$

359

360 Substituting these into (7) and (11) yields the solution $a_1 = q_{crit} = \alpha$.

361

362 Thus under fully honest signalling we predict that males with quality lower than $q = \alpha$
363 will signal using the lowest-cost signal available and will always be rejected by
364 females; whereas males with a higher quality than this will signal at level α and will
365 always be mated with by females.

366

367 It is easy to see the rationality of this in the very simple case considered. At the
368 equilibrium females always mate with males that offer a net benefit to them, and
369 never mate with males that offer a net loss to them. Given this behaviour by receivers,
370 the minimal-cost signalling of low quality males also seems easy to understand. Since
371 these individuals are destined to be rejected by females, their signal can bring them no
372 rewards and so the best strategy is to minimize the costs of signalling. However,
373 investment in more expensive signalling is rational for the high quality individuals
374 since they can convert this advertising into rewards (mating opportunities). Still they
375 should be selected to invest just enough in advertising to both produce the desired
376 behaviour in the receiver, and to prevent the best of the poor males from cheating. The
377 payoff to low-quality, minimum-cost signallers is zero, the signal level adopted by the
378 high-quality individuals is the cheapest signal that yields a net positive payoff to all
379 individuals that use this signal (except any right on the threshold, who also receive
380 zero).

381

382 **Discussion**

383 In this paper we have considered a model of signalling behaviour where the receivers
384 have only a discrete number of possible responses to the signal. Our model predicts
385 that even if signallers vary continuously in quality, and signals are received with
386 perfect fidelity, these signals need not show continuous variation in signal strength.
387 Rather, the discrete nature of the behavioural responses to signals available to the
388 receiver causes the receiver to be interested in categorizing signallers rather than fully
389 evaluating their quality, and this in turn leads to signalling being restricted to a
390 number of discrete levels (at most equal in number to the number of behavioural
391 options open to the receiver). Thus we predict that such signals will be commonplace
392 when the behavioural responses of receivers are constrained to take a discrete number
393 of values. Examples of this could include signalling of prey toxicity to predators,
394 where predators can respond either by eating an individual signaller or rejecting the
395 opportunity to eat it. Another example may be mate choice where the choice is again
396 binary: mating with or rejecting the signaller. We thus expect such situations and such
397 all-or-nothing signalling to be commonplace. However, there are other cases where
398 the responses of signal receivers may be more continuously distributed. For example,
399 in response to signal quality of a long-term social partner, a female bird may vary the
400 investment that she makes in the eggs that will become their joint-offspring (Clutton-
401 Brock 1991; Blount et al. 2000). This investment (say in levels of anti-oxidants
402 committed to the eggs) is best seen as a continuously varying response, and so we
403 would predict that the signalling behaviour of the males would not be well represented
404 by the model considered here and (in the absence of perceptual errors) we would
405 consider a continuously distributed signal by the males to be more likely.

406 Bergstrom & Lachman (1998) present a model that they use to suggest that
407 honest signaling between relatives can be maintained in the absence of substantial

408 costs to signal production. The type of equilibrium that they consider are of the all-or-
409 nothing type discussed here, where signallers of a range of qualities are grouped into a
410 finite number of what the authors term “pools” with all individuals in the same pool
411 producing the same signal. However, a very important difference between our
412 approach and theirs is that a finite number of signal levels is a prediction of our
413 model, whereas the signal being constrained such that only a finite number of signal
414 types are possible is a fundamental assumption of their model. Our methodology does
415 not involve any such constraint on signal production.

416 The all-or-nothing signalling predicted here may not be seen in situations where there
417 is strong between-individual variation in the receivers in the value of the signallers to
418 them. Consider the example of predators and chemically defended prey. Previously
419 we have considered a critical value of toxins above which the prey becomes
420 unattractive to the predators. There may be some circumstances where individual
421 predators essentially agree on this critical value, in which case we would expect our
422 model to hold. However, there may be other circumstances where there is
423 considerable variation in this value between individual predators. This could be driven
424 by variation between individuals in the need for the nutritional benefits of the prey
425 (with hungrier individuals being prepared to accept higher toxin loads to avoid the
426 risk of starvation) or variation in their ability to cope with the toxins (perhaps through
427 variation in their current toxin burden): see Endler & Mappes (2004) for examples. If
428 this variation in threshold of defence is large then this may cause the all-or-nothing
429 type of signal predicted here to break down and be replaced by a more continuously-
430 varying signal, as in [10].

431

432 Johnstone (1994) cited a number of influential papers that predict (in contrast to our
433 model) that signal intensity should vary continuously in relation to the quality or need
434 of the signaller: (Grafen 1990, Godfray 1991, Johnstone & Grafen 1992, Pagel 1993).
435 In each case, it is possible to explain why these models make different predictions to
436 ours. As already discussed, in Johnstone & Grafen (1992) wide receiver variation
437 causes different receivers to wish to respond to many different signallers in different
438 ways, making variation in signalling level viable. In Grafen (1990) and Pagel (1993)
439 this difference is due to the cost function, which they make an explicit function of the
440 error in perception of underlying signaller quality, so that there is a cost which
441 continuously increases as a function to the size of the perceptual error. This is the
442 situation we discussed in the introduction where all errors are considered to be costly.
443 The exact mechanism underlying these costs is not defined in these papers, and
444 choices available to the receivers (on receipt of a particular signal value) are not
445 explicitly given. In Godfray (1991) the choices are explicitly given; these are the
446 possible levels of provisioning by a parent to its offspring. This provisioning effort is
447 considered to vary continuously, so there is a continuum of choices (rather than the
448 binary choice considered here), and thus the scenario is different to ours, and (in the
449 absence of perceptual errors) a continuously varying signal intensity is certainly
450 plausible here.

451

452 Notice that the receiver strategy as we have defined it only describes responses to the
453 two types of signal that are expected in the equilibrium situation. There may be
454 occasional aberrant individuals that produce signals that are different from either of
455 the two signals that form the equilibrium. It is likely that the receivers will treat such a
456 signal in a way similar to whichever of the two equilibrium signals it most resembles,

457 with the similarity of response getting stronger as the similarity between aberrant and
458 nearest-equilibrium signals increases. Such generalization across similar signal types
459 is commonly observed empirically (Bradbury & Vehrencamp 1998). However if
460 signals just below the higher signalling level are always treated as the higher signal,
461 the signalling system will be destabilized, so there must be at least some probability of
462 such signals being treated as a low signal for any system to be stable (this would only
463 need to be small for small discrepancies, since the benefit from using a lower-cost
464 signal is greatly outweighed by the cost of being interpreted as a low signal). Overall,
465 the optimal strategy for receivers to deal with aberrant signals will depend on the
466 exact biological mechanism that leads to the production of aberrant signals, since the
467 fine detail of this mechanism will influence the probability distribution of individual
468 signaller qualities (q values) associated with a particular aberrant signal strength.
469 However, we might not expect to see natural receivers closely following this
470 theoretical optimum strategy, since aberrant signals will be rare and so selection
471 pressure shaping responses to such signals will be less than selection on responses to
472 more commonly encountered signals. Rather we might expect to find between-
473 receiver variation in response to aberrant signals (Arak & Enquist 1993), but with all
474 receivers generally showing the rational behaviour of generalization across similar
475 signals such that they treat aberrant signals (in particular high signals) in a way that is
476 like their treatment of the most similar of the signals that makes up the equilibrium
477 set.

478

479 In this paper we have been particularly interested in how an honest signalling system
480 could work in our chosen scenario, and this has been our main focus. However, we
481 found that we could not discount the possibility of what we called a semi-honest

482 system, where higher signals mean a better quality individual than lower ones, but
483 where the cut-off is not that of the totally honest signalling system. It may be that such
484 systems can be destabilized through the introduction of signalling errors, as in
485 Johnstone (1994), or alternatively through receiver variation, and this would certainly
486 be worth further investigation.
487

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