Tests on R/C Beams Strengthened at the Span with Externally-bonded Polymers,
Reinforced with Carbon or Steel Fibers

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Abstract
The main objective of the experimental work reported herein is the comparative evaluation of Steel-Reinforced (SRP) and Carbon-Reinforced (CFRP) Polymers used as externally-bonded reinforcement in strengthening of reinforced concrete (R/C) members. Tensile stress-strain, as well as bond constitutive laws for these materials were first derived from sixteen tests and are summarized here. Results are then reported from four-point bending tests of five full-scale R/C beams strengthened at their span using SRP and CFRP strips. The bond tests have shown that by providing a bond length greater than the effective one, neither the bond strength nor the deformation capacity are increased, whereas by increasing the width of the strip the bond strength is increased. From the bending tests of beams it was found that the use of both SRP and CFRP strips resulted in a significant increase in strength (up to 92%) with respect to the strength of the initial specimen. The experimentally measured strengths were estimated analytically, using both the experimental measurements of the specimen deformations and the pertinent provisions of ACI 440 and Eurocode 8-Part 3.

Keywords: SRP; CFRP; R/C beams; flexural strengthening; testing

Introduction
The use of carbon fiber-reinforced polymers (CFRP) for strengthening R/C beams has been the subject of several investigations in the last decades, and the efficiency of this material in increasing the flexural strength of beams has been shown. During the last decade, research has also focused on strengthening of R/C members using steel-reinforced polymers (SRP). Relevant tests carried out so far addressed the strength of the SRP material (typically in the form of strips), bond with concrete, and means of improving their anchorage conditions.

Among the researchers that investigated experimentally the mechanical properties of SRP materials, Kim et al. (2005) tested SRP type 3X2 cords (made by twisting 5 individual wires together) and reported data on their modulus of elasticity, tensile strength, Poisson ratio, and ultimate strain. Huang et al. (2005) studied experimentally the properties of SRP type 12X cords (made by twisting three 0.22 mm wires and nine 0.20 mm wires together) and compared them with theoretical predictions from micromechanics equations, to evaluate the reliability of these equations; they found

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that the mechanical properties of SRP cords can be predicted with reasonable accuracy with the aid of micromechanics models. Barton et al. (2005) tested dog bone shaped strips, consisting of 3X2 cords embedded either in polymeric resin (SRP) or in cementitious grout (SRG). It was found that SRP’s have a higher modulus of elasticity and shear modulus than SRG’s. Among the researchers that studied bond between SRP (and/or SRG) and concrete surfaces, Matana et al (2005), conducted direct shear tests on specimens including 3X2 and 3SX cords (three identical wires twisted together at a longer than usual lay length and then over-wrapped with a single wire) embedded in polymeric resin or cementitious grout. It was found that SRP strips separated from the concrete substrate attracting the outer surface of concrete, while in SRG specimens debonding occurred at the interface between the SRG strip and the concrete surface. The required bond length for SRG was found to be almost double that for SRP. Figeys et al. (2005) studied the bond mechanism between SRP and concrete by means of direct tension tests. Test results were compared with predictions of models originally developed for CFRP (the average ratio of experimental/analytical values was 1.16) with predictions of models proposed by the authors (average ratio of 1.02). Cancelli et al. (2007), also studied bond between SRP and SRG, and the concrete substrate. They found that maximum strength, load transfer mechanism, and ultimate failure mode are all influenced by the type of the matrix (polymeric resin of grout). More specifically, in specimens where epoxy resin was used peeling of concrete took place, whereas in specimens with cementitious grout debonding occurred at the interface between SRG and concrete, and bond resistance was lower than for the SRP. Toutanji et al. (2007), studied the effect of the number of FRP layers on bond strength. An increase of 15 to 20% (depending on concrete grade) in bond strength was found when an extra layer was added. Among studies that involved strengthening of R/C beams with externally-bonded polymers those by Wobbe et al. (2004), Prota et al (2004), Kim et al. (2005), Huang et al. (2005), Casadei et al. (2005), Figeys et al. (2005), Lopez et al. (2007), Saber et al. (2008) involved comparative evaluation of the relative efficiency of SRP, SRG and CFRP. These studies also included proposals for improving the anchorage (bond) conditions for the materials used. It was found that externally-bonded SRP and SRG strips constitute an effective means for strengthening R/C members. More specifically, flexural strengthening provided by SRP/SRG was found to be equally effective as that provided by CFRP. Specimens strengthened with SRP or SRG developed a higher deformation capacity than similar CFRP-strengthened specimens, while their failure modes were similar to those of CFRP-strengthened specimens. The most common failure mode was a rather brittle debonding (peeling) of the concrete surface, that initiates at the ends of the anchorage zones. The use of either anchors or U-shaped strips perpendicular to the beam axis, was found to delay debonding of the composite strips, leading to an improved flexural behavior of the strengthened specimen. Lopez et al. (2007), strengthened with SRP’s the beams of an actual bridge for both flexure (at the span) and shear (at the supports). The results of their tests indicate that SRP’s can be applied for the strengthening of structures, without limitations additional to those that normally apply for FRP’s. It
was also found that, although the design method prescribed in ACI 440.2R-02 (ACI 2002) does not implicitly apply to SRP’s, it can nevertheless be used for the design of structural interventions involving these materials.

In the present paper, results are first reported from tests aiming at the determination of the mechanical properties of SRP and CFRP strips, as well as the characteristics of bond between these materials and concrete. Then, the experimental set-up and the results from five tests involving full-scale reinforced concrete (R/C) beams are reported; three of these beams were strengthened with SRP or CFRP strips, with a view to increasing their flexural strength. A detailed description of test results involving the materials used for strengthening can be found in previous papers by Mitolidis et al. (2008 a, b) and they are also summarized in this paper, whenever needed.

**Research Significance**

While a fair number of experimental studies exists dealing with issues related to strengthening of R/C members with CFRP and (to a lesser extent) SRP materials, a review of the existing literature indicates that there are still some issues that require further research. Hence the present study supplements the existing state-of-the-art mainly in the following respects:

- Bond tests are carried out using an experimental set-up that is different from those used so far, and addresses in a uniform way CFRP strips, and SRP strips with different types of steel cords (3X2 and 12X); moreover, bond tests are carried out for two different concrete grades.

- A key objective was to study the effectiveness of SRP strengthening of ‘old-type’ members, since such members are the ones that typically need strengthening. Hence, the ‘prototype’ beams were designed according to old code provisions, and are characterized by the use of smooth reinforcing bars, and relatively low-strength concrete. Bending tests reported here involve a total of five full-scale beams, two of them without strengthening (one critical in flexure and one critical in shear) and three nominally identical beams strengthened against flexure using CFRP, SRP-3X2, and SRP-12X.

- In previous studies on reinforced polymer-strengthened beams the anchorage of the composite materials was done in the usual way i.e. they extended one development length beyond the section wherein they were required for flexural resistance, which means that they terminated in an area that is still in tension; moreover, in these areas shear cracks are often present that adversely affect bond conditions. In some of the beams of the present study, anchorage of composite strips extends further towards the support, reaching areas without tensile stresses but also unaffected (due to test set-up) by the compression resulting from an actual support, hence providing more insight into the factors affecting this critical region of the strengthened members.
Another objective was to assess the reliability of international codes/guidelines for strengthening with externally bonded reinforced polymers, which were developed for FRP reinforcement and are not necessarily adequate for SRP strengthening. Hence, in the analytical part of the study the flexural, as well as the shear, strength of the beams are estimated using the two leading international documents, i.e. the ACI 440R-08 Guidelines and Eurocode 8-Part 3, leading to conclusions particularly relevant to design practice.

Tests for the Estimation of the Mechanical Properties of the Fiber-Reinforced Polymers

For the estimation of the flexural and/or shear strength of R/C elements strengthened with externally-bonded FRPs the strain capacity of the reinforced polymer is used. In these cases either the fracture, or the debonding, strain is used, while for design purposes a lower value is introduced, typically through an appropriate safety factor. It is recalled here that for these materials the fracture strain is significantly higher than the debonding strain, Mitolidis et al (2008b). In the case of SRP strips with ample width and proper anchorage, and also of strips with coarsely spaced wires, the fracture strain becomes critical as found by simplified calculations using models available in the literature, see Toutanji et al (2007). In view of these considerations, direct tension, as well as bond, tests were carried out for the composite materials used herein. SRP strips were of two types, SRP 3X2-23-12 and SRP 12X-23-12; the difference in the twisted wire cords used in each type were explained in the Introduction, while more details can be found in Mitolidis et al (2008b). The CFRP strips were Sika® Carbodur® (type S512). On the basis of direct tension tests (see insert of Fig. 1), stress – strain diagrams were derived for the various strips, and are shown in Figure 1 together with the corresponding diagram for ordinary steel reinforcement; again, more details of the test set-up can be found in Mitolidis et al. (2008b).

Also as part of the present experimental program, 16 bond tests were carried out to estimate the strength of reinforced polymer strips bonded through epoxy on concrete. The main parameters explored were the type of fiber-reinforced polymer (CFRP, SRP3X2, SRP12X), the width of the strip (50 mm, 80 mm), its bond (development) length (150 mm, 300 mm), the compressive strength of concrete used for preparing the prisms on which the reinforced polymers were bonded, and the degree of treatment of the outer surface of the concrete prisms (removal of the cement skin). The experimental set-up used (which is different from those used in past studies) is shown in Fig. 2a. From the above tests, summarized in Fig. 2b, it was found that the debonding strength of the CFRP laminates was (on average) 30% higher than the debonding strength of the corresponding SRP laminates, which is consistent with the higher elasticity modulus of the CFRPs, compared to the SRPs (see Fig. 1). For the two types of SRP and for CFRP used here the moduli of elasticity given by manufacturers were 77900, 67600 and 160000 MPa respectively. In some of the models found in the literature, and summarized in Toutanji et al (2007), debonding strength is related to the square root of...
the modulus of elasticity of the reinforced polymer. The debonding load was affected, as expected, by the width of the strips. For SRP laminates with 80 mm width the debonding load was 45% higher than the debonding load of the SRP laminates with 50 mm width. It is pointed out that both bond lengths used for the specimens (150 mm and 300 mm) were higher than the effective length in all cases, hence no noticeable effect of the bond length was observed in the bond tests. On the other hand, a small increase was observed in the debonding strength of the reinforced polymers when concrete strength was increased from 20.0 MPa to 36.9 MPa. The tensile strength of the concrete prisms was estimated to be 2.2 MPa and 3.3 MPa, respectively; however, it is known that the increase in the debonding strength is not related to the (conventionally derived) tensile strength of concrete but rather to its surface (skin) tensile strength. In cases where the concrete surface is not properly roughened, as purposely done in the high-strength concrete prisms of this work, the expected debonding strength increase is not reached. Results from these tests are summarized in Table 1. The name of each specimen denotes the reinforced polymer type (first letters), the strip width in cm (the first number), the strip length in cm (the second number), and the concrete grade (normal strength “NS” or high strength “HS”). The thickness of all specimens is almost the same, 1.23 mm for CFRP laminates and 1.20 mm for SRP laminates. For this reason the ratio of the debonding strengths between the specimens of table 1, is proportional to the square root of their moduli of elasticity. This is valid for specimens with the same width. The last column of table 1 lists the values of the ratio:

\[ \frac{\sqrt{E_i}}{\sqrt{E_{SRP12X}}} \frac{P_{SRP12X}}{P_i} \]

where \( E_i \) are the moduli of elasticity for SRP12X, SRP3X and CFRP respectively, and \( P_i \) the debonding strengths of SRP12X, SRP3X and CFRP respectively, given separately for each considered width value.

The debonding strengths of the aforementioned specimens were then estimated using the analytical models of Chen & Teng (2001), Neubauer & Rostasy (1997), Yang et al. (2001), and Yuan & Wu (1999), all of them reported by Toutanji et al. (2007). The measured debonding strengths were better predicted by the analytical model of Chen and Teng. The analytical model of Neubauer and Rostasy overestimated the experimentally measured strengths, while the models of Yang et al. and Yuan & Wu underestimated them. Comparisons of experimentally measured debonding strengths with the analytically calculated values predicted from the models of Chen & Teng and Yang et al. are presented in Figures 3a and 3b. More details on the experimental set-up (Fig. 2a) devised for the tests, and the direct tension and bond test results are given in Mitolidis et al. (2008a, 2008b).

**Design and Description of Strengthened Specimens**

The part of the experimental work on which this paper focuses included five full-scale R/C beam specimens. Two of them, intended as reference specimens, did not embody any interventions, while
the remaining three were strengthened against flexure with externally-bonded reinforced polymers. Among the unstrengthened beams, one (SVM) was designed as flexure-critical, and the other (SVS) as shear–critical. The other three specimens were strengthened utilizing SRP 3X2, SRP 12X and CFRP laminates.

The nomenclature of the specimens is as follows: The first letter denotes that the specimen represents the “Span” (S) of a continuous beam; the entire program included eight more beam specimens, not reported herein, that represent the support region of a continuous beam. The last letter denotes the expected failure mode of the specimen, “S” for shear failure, “M” for bending moment (flexural) failure. The middle letters refer to the intervention scheme (or absence of it), i.e. “V” for virgin (unstrengthened) specimens, “C” for the specimen strengthened in flexure using CFRP, while for the specimens strengthened with SRP the letters in the middle are “S3X2” and “S12X” denoting the type of steel-reinforced polymer used.

The three strengthened specimens SCM, SS12XM and SS3X2M were nominally identical (prior to strengthening) to virgin specimen SVM, and were all designed to fail in a flexural mode. Reinforcing scheme and construction details for all specimens are given in Figure 4, and it is recalled here that the reference beams were designed according to prevailing European practices in the 1970’s. As is common in laboratory testing, the specimens were loaded in four-point flexure, unlike beams in real structures which are subjected to distributed loading. To accommodate the constant shear force in the test beam end regions, bent-up bars (Ø12/25) were added along the first and the last thirds of the length of the specimens. Smooth bars were used both as longitudinal flexural reinforcement and as shear reinforcement (bent-up bars and stirrups) in the four flexure-dominated specimens; smooth bars were typically used in pre-1970 R/C construction in Europe and elsewhere. In the shear-critical specimen (SVS) ribbed bars were used as longitudinal reinforcement (the main reason for this was the higher strength of these bars, see Fig. 1, which ensured that the flexural strength was well above the shear strength), while smooth bars were used for the stirrups.

The 28-day compressive strength of concrete used 3 to 4 decades ago typically had a specified mean value of 22.5 MPa, referring to 200 mm cube specimens. The concrete used for the specimens of this study had a mean cylinder strength value of 22.0 MPa, corresponding to a cube strength of 26.4 MPa, and tensile strength 2.4 MPa. It was estimated that the 28-day cube strength of 22.5 MPa increases to about 26.9 MPa after 30 to 40 years; hence the concrete grade used in the tests was representative of the prevailing grade in the 1970’s, as initially envisaged.

For the flexural strengthening of the beam specimens, the previously described CFRP and SRP strips were used. The epoxy resin used for bonding the carbon laminates was Sikadur® 30, with modulus of elasticity 12.8 GPa and tensile strength 27 to 32 MPa (manufacturer’s specifications). The epoxy resin used for bonding the SRPs was Sikadur® 330 with modulus of elasticity 4.8 GPa and tensile strength 30 MPa. The process according to which these materials were applied on the beam
specimens was that specified by the manufacturer. Details of the specimens are given in Figure 4 and a close-up at the support of the specimens is given in Figure 5.

**Description of Experimental Set-up and Instrumentation**

The hydraulic actuator needed for applying the vertical loading (four-point bending) on the beam specimens was mounted on the reaction frame of the Laboratory of Concrete and Masonry Structures of the Aristotle University as shown in Figure 6; a strong steel beam was used to distribute the actuator force into two point loads. Since the evaluation of the behavior of the specimens well into the inelastic range was a key objective of the study, the loading history consisted of a displacement ‘ramp’, applied at a rate of 1mm/min. The control of the loading rate was made by a digital controller, by comparing the measurements of the sensors of the actuator with the load command several times at each loading step.

The displacement and deformation of the specimen were measured by eight externally-mounted displacement sensors (LVDTs). The arrangement of the LVDTs used on the specimen and their nomenclature are given in Figure 7. On the basis of the measurements of these instruments and the records of the actuator’s load shell, load – displacement (or deformation) diagrams were drawn.

**Description of Specimen Behavior**

The cracking patterns of all specimens after completion of the tests are shown in Figures 8a to 8e. **SVM:** This reference specimen failed, as anticipated, in a flexural mode. At an applied load of 50 kN (shear force of 25 kN at each end) the first flexural cracks formed at the bottom of the beam specimen, distributed along the middle 1 m of the specimen. This occurred because this was the length along which the maximum bending moment was applied (cf. Fig. 4). As the imposed displacement was increased, for a shear force of 57 kN and a mid-span deflection of 9 mm, opening of one flexural crack in the middle of the specimen started. At this location the flexural reinforcement consisting of smooth bars developed significant inelastic deformations. Since these bars were smooth, practically all inelastic deformation concentrated in this critical crack, while the other flexural cracks remained hairline throughout the test. The large deformation at the critical crack was accompanied by detachment of steel bars from the surrounding concrete; this loss of local bond prevented the smooth bars from developing their full flexural capacity, as also verified by comparing the measured strength with the theoretical one calculated on the basis of the ultimate stress in the reinforcement. Hence, at the end of the test all inelastic deformation was concentrated in the critical crack region, while shear deformations were negligible and no visible shear cracks were detected. The latter was attributed to the intentional over-design of the beam in shear (as evident from the shear reinforcement shown at the top of Fig. 4).
**SVS:** This specimen, which was designed with adequate flexural reinforcement and inadequate stirrups, failed subsequent to the formation of a major shear crack at the left support. Hairline shear cracks appeared at an applied load of 180 kN (shear force 90 kN). These cracks initiated next to the point of the application of the load (see Fig. 8b). By increasing the imposed displacements, shear cracks opened further, until shear failure of the specimen occurred. The maximum shear force resisted by the beam was 131 kN. At the top of the beam, spalling of concrete and kinking of steel bars occurred, attributed to the inadequate transverse reinforcement (sparsely-spaced stirrups).

**SS3X2M, SS12XM, SCM:** These specimens, prior to strengthening, were nominally identical to specimen SVM, and were strengthened using SRP and CFRP strips (Fig. 4) with a view to obtaining a response dominated by flexure. The key response parameters studied were the failure mode and the deformation at failure of the specimens strengthened using different techniques. For the specimens strengthened with SRP strips, higher deformation capacity was expected than for specimens strengthened with CFRP strips, due to the higher deformability of the former (Fig. 1).

During the tests, the first flexural cracks formed at an imposed displacement of about 5 mm. These cracks were distributed along the middle two meters of the length of the specimens. It is known that the width of such cracks increases from the neutral axis to the tension fiber of the specimen’s section. However, in the strengthened beams the width of flexural cracks at the outer face of the section, where the reinforced polymer strip was applied, was very small and the cracks showed no visible opening. This is attributed to the much stiffer nature (much higher modulus of elasticity than concrete) of the composite strips used (see also Fig. 1). As the applied displacement (and load) increased, flexural cracks kept opening, but still remained almost closed at the lower face of the specimen. This flexural crack configuration (i.e. cracks closed at their lower tip), hints to the fact that Bernoulli’s principle does not apply in the case of beams strengthened at their span with externally-bonded FRPs or SRPs. This has the repercussion that the tensile force (due to bending) resisted by steel reinforcement (located at the bottom of the beam, very close to the reinforced polymer layers) is lower than the corresponding force in specimen SVM, for the same level of beam displacement. It was also noted that the flexural cracks in the strengthened beams were distributed along a significantly longer length than in the reference specimen. The stiffness of the strengthened specimens decreased when these flexural cracks formed, and further reduction was noted when loss of bond between concrete and the reinforced polymer started; this loss of bond was perceived by characteristic cracking noises. The reduced stiffness remained almost constant up to debonding of the reinforced polymers from the concrete surface. In all three strengthened specimens, the reinforced polymer strips debonded at approximately the same load (about 220 kN). Debonding of the strips initiated at a flexural crack in the middle region of the beam. Right after debonding, the strength of the specimens was reduced to a value lower than the strength of the unstrengthened specimen (117.6 kN), indicating that, apparently due to the different cracking pattern, steel bars did not develop (at that stage) the stress developed in the bars of the
unstrengthened beam. By further increasing the applied displacement, the strength of the specimen increased up to a value close to the strength level of the initial specimen, while all inelastic deformation concentrated in the longitudinal (smooth) reinforcement at one main flexural crack. After that point, the response of the specimen was almost identical to the one of the unstrengthened specimen. Finally, in the strengthened specimens no visible shear deformations and shear cracks were detected, as expected due to the high shear strength provided (see top of Fig. 4).

8 Load – Displacement Characteristics of the Specimens

The measured load vs. displacement diagrams for all specimens are given in Figures 9 to 13. The arrangement of the sensors (LVDTs) and their nomenclature are shown in Figure 7 and those plotted in Figures 9 to 13 are summarized below:

“Mid-span Deflection” – MD
“Horizontal Mid-span Tension-side Displacement” – HMT
“Horizontal Right-span Displacement” – HR
“Horizontal Mid-span Compression-side Displacement” – HMC
“Diagonal Left-side Displacement” – DL

From the recorded load – deflection curve for the unstrengthened specimen SVM (Fig. 9) it is seen that it has an inelastic deformation capacity of at least 30 mm (which is 1/100 of its span). As mentioned in the previous section, only one major flexural crack formed at the mid-span of the specimen (Fig. 8a). As will be shown analytically later on, bond of the smooth bars of this beam was destroyed when the elongation of the bars was lower than the value corresponding to the development of the maximum strength of the reinforcement. The gradual deterioration of bond should be the reason why this specimen maintained a practically constant strength for a broad range of applied displacements, from 9 mm to 30 mm, despite the fact that the stress – strain diagram of smooth reinforcement has a rather short yield plateau, as shown in Figure 1.

The shear-critical specimen SVS, that failed in diagonal tension, reached a mid-span deflection of 22 mm, but with a noticeable drop in strength; it is pointed out that strength begun to deteriorate at about half the previous deflection. Although fracture of two stirrups was observed, the residual strength of this specimen was rather high; this was attributed to the contribution of the arch mechanism (inclined compression with the longitudinal reinforcement acting as a tie) of shear resistance, since the longitudinal reinforcement was well anchored in the length of the specimens beyond the supports (600 mm on the left and 600 mm on the right, see Figs. 4 and 5), hence more effective in contributing to this mechanism. It is worth noting here that no previous work was found in the literature, on shear failure of beams with longitudinal reinforcement anchored well beyond the supports.
In all strengthened specimens the reinforced polymer strip bonded at the bottom was detached at almost the same load. This is justified by noting that debonding occurred by detachment of a layer of the outer concrete cover, and concrete strength was the same in all beams. Since the elastic modulus of SRP strips is lower than that of CFRP, a larger elongation (hence a larger curvature) was required at the bottom of the beam to achieve the same contribution to the flexural resistance. As a result, for specimens strengthened with SRP the strip was found to detach at a displacement 15% higher than that in the specimen strengthened with a CFRP strip.

From the recorded force vs. horizontal elongation diagrams at the tension (bottom) side of the central one meter of the beams (HMT), Fig. 10, the most noticeable, yet anticipated, difference is that between the two unstrengthened specimens; in the flexure-dominated SVM significant elongation of the flexural reinforcement took place for a practically constant force, whereas in the shear-dominated specimen SVS after peak strength was reached, elongation not only stopped but also tended to decrease, implying that for this specimen inelastic deformations developed primarily close to the supports where diagonal tension failure occurred, as discussed in the previous section. Diagrams for the three strengthened specimens lie in-between those for the unstrengthened ones, as far as maximum elongation is concerned, but clearly closer to that of SVM, which was anticipated since these specimens were also flexure-dominated. Among the strengthened specimens, elongation of the strips was higher for the specimens (SS3X2M, SS12XM) strengthened with SPR than for the specimen (SCM) strengthened with CFRP.

From the recorded force vs. horizontal elongation diagrams at the tension side of the right third of the beam’s length (HR), Fig. 11, it is seen that elongation of this region is very small in the case of specimen SVM; in fact no elongation was recorded subsequent to the formation of the major flexural crack at midspan, where all deformation concentrated. The elongation was larger in specimen SVS but ceased after the formation of the diagonal tension crack. For the strengthened specimens the elongation of the tension side increased at the end regions, apparently due to the fact that cracking in these regions was much more pronounced than in the unstrengthened specimens (see Fig. 8); the largest value was recorded for the SRP-strengthened specimen SS3X2M.

Referring now to the compression (upper) side of the beams, from the diagrams of Fig. 12 (recorded from LVDT ‘HMC’ in Fig. 7) it is seen that the only specimen wherein a typical flexural behavior was observed (i.e. continuous shortening of the top side with increasing imposed deflection) was specimen SVM. In all other specimens subsequent to the application of the maximum loading, ‘unloading’ occurred in the compression zone (i.e. reduced shortening with increasing imposed vertical deflection), indicating a different inelastic deformation pattern. In the case of the strengthened beams, it was observed that in the post-peak range (after debonding of the strips started) an elongation of almost the entire specimen (including most of its top part) took place due to crack opening, which resulted in recovering a rather substantial part (up to about 50%) of the shortening developed previously in the upper part; recall that LVDT ‘HMC’ does not measure the deformation of the top
fiber, but that at a location a short distance (about 30 mm) from it, as shown in Fig. 7. This reduction in the compression strain can also be explained by the smaller neutral axis depth required to balance the reduced tensile force offered by steel reinforcement alone, compared to the stage prior to failure of the strip.

Finally, from the recorded force vs. diagonal elongation diagrams at the outer third of the beam’s length (DL) shown in Fig. 13, it is clear that the only specimen that developed significant shear (diagonal tension) deformation was the shear-dominated SVS. In the flexure-dominated specimen SVM shear deformation was negligible, and in the three strengthened specimens it was very small and tended to stabilize, or even reduce, in the post-peak range. The diagrams in Fig. 13 confirm previous remarks that all reinforced polymer-strengthened beams were flexure-dominated.

Analytical Estimation of the Specimen Strength

The measurements obtained during the tests were used to estimate analytically the flexural and shear strength of both the initial (unstrengthened) and the strengthened beams, as reported in the following.

Flexural Strength Estimation based on Measurements and First Principles

On the basis of the discussions presented in the previous sections, it is clear that in all strengthened specimens, while the elongation of the reinforced polymer strips was significantly lower than the limit strain $\varepsilon_{f, \text{lim}}$ the strip was detached from the concrete surface; this detachment initiated at a flexural crack at mid-span.

For this well-known failure mechanism, the bending moment $M_R$ resisted by the beam, can be estimated from the following relationship (Triantafillou 2003):

$$M_R = A_{s1} \cdot f_y \cdot (d - \delta_G \cdot x) + A_f \cdot E_f \cdot \varepsilon_f \cdot (h - \delta_G \cdot x) + A_{s2} \cdot E_s \cdot \varepsilon_{s2} \cdot (\delta_G \cdot x - d)$$

(1)

where $A_{s1}$ = area of tension reinforcement

$A_{s2}$ = area of compression reinforcement

$f_y$ = yield stress of steel reinforcement

$E_f$ = modulus of elasticity of the reinforced polymer (parallel to the direction of the fibers)

$E_s$ = modulus of elasticity of steel reinforcement

$\varepsilon_f$ = strain of the reinforced polymer strip

$\varepsilon_{s2}$ = strain of compression steel reinforcement

$d$ = distance between the center of tension reinforcement and the top fiber of the section (effective depth)

$h$ = height of specimen section

$d_2$ = distance between the center of compression reinforcement and the top fiber of the section

$x$ = depth of the compression zone of the section
and

\[ \delta_G = \text{height coefficient for the resultant of the internal compressive forces} \]

\[ \delta_G = \begin{cases} 
\frac{8 - 1000 \cdot \varepsilon_c}{4 \cdot (6 - 1000 \cdot \varepsilon_c)} & \text{for } \varepsilon_c \leq 0.002 \\
1000 \cdot \varepsilon_c \cdot (3000 \cdot \varepsilon_c - 4) + 2 & \text{for } 0.002 \leq \varepsilon_c \leq 0.0035 \\
2000 \cdot \varepsilon_c \cdot (3000 \cdot \varepsilon_c - 2) & \text{for } \varepsilon_c > 0.0035
\end{cases} \]  

(2)

The strain (\(\varepsilon_c\)) at the compressed part of the section of the specimens is estimated from the measured shortening (LVDT ‘HMC’), while the strain (\(\varepsilon_f\)) of the reinforced polymer strip is estimated from the measured elongation (LVDT ‘HMT’). Using the measured values of \(\varepsilon_c\) and \(\varepsilon_f\) into equations (2) and Bernoulli’s principle, the coefficient \(\delta_G\) and the depth of the compassion zone of the section \(x\) can be found. The flexural capacity of the specimens can then be estimated from equation (1). From the moment capacity, the maximum shear in the specimens can be found from equilibrium.

The bending moment carried by the reinforced polymers (\(M_{R,f}\)) is given by the second term of equation (1) and the corresponding shear (\(V_{R,f}\)) resisted by the SRP or CFRP strips can be found from equilibrium.

It is known from the literature (e.g. Teng et al. 2002), that in regions of beams where flexural cracking exists the effective strain (\(\varepsilon_f\)) of the reinforced polymer, and hence the force that causes debonding, are increased. This increase was estimated for the beams of the present study by taking the average value of \((V_{\text{deb,exp}} - V_{\text{crit,SVM}})/V_{R,f}\), where \(V_{\text{deb,exp}}\) is the shear at debonding (estimated from measured values) and \(V_{\text{crit,SVM}}\) is the shear carried by the reference specimen SVM at yielding of the flexural reinforcement. The average value of this ratio was found to be 1.40, which is higher than the value 1.30 suggested by Teng et al. (2002), hence the maximum shear (corresponding to debonding) for the strengthened beams was subsequently estimated from

\[ V_{\text{deb}} = V_{\text{crit,SVM}} + 1.40 \cdot V_{R,f} \]  

(3)

and \(V_{\text{deb}} = P_{\text{deb}}/2\) where \(P_{\text{deb}}\) the load applied at the time of debonding (see Fig. 14). For the estimation of the effective elongation of the strips, just prior to detachment, the constant moment in the middle third of the length of the specimen was used. Results from the equations given in this section, along with the pertinent experimental measurements, are reported in Table 2.

Table 3 summarizes the analytically calculated strengths of the strengthened specimens, according to ACI 440R-08, and the Greek Code for Interventions (which is compatible with Eurocode 8 – Part 3), as well as the corresponding measured strengths. Predictions of the Greek version of EC8-3 are quite close to the test results, while those from ACI 440 provide conservative estimates (up to 13% lower than the measured values). The reason for the latter conservatism was found to be eqn. 10-2 of ACI 440, which gives much lower effective strain values for the FRP than its 2002 edition, especially
for low concrete strengths, as was the case here. It is worth noting that the strengths found using the 2002 edition varied from 95% to 101% the measured values.

Shear strength estimation for specimen SVS by the use of measurements

Among the tested specimen reported herein, only SVS was shear-dominated, hence an attempt to predict its shear strength using existing relationships in combination with measured test quantities was made. Most of current codes (but not Eurocode 2) specify that the shear strength $V_R$ can be determined as the sum of the ‘concrete contribution’ $V_c$ and the contribution of shear reinforcement (through the truss mechanism) $V_w$. Introducing the measured stress of the stirrups in the equation for $V_w$ and adding the concrete contribution from the Prestandard version of Eurocode 2 (which is also adopted in the Greek Concrete Code), the estimated shear strength of beam SVS was found to be 136.85 kN, which corresponds to an applied load of 273.7 kN; as shown in Table 2, this is very close to the value measured during the test (263.6 kN).

Relative Efficiency of Strengthening Techniques

Given the fact that SRP is generally less expensive than CFRP, it is important for practical application to have some quantitative information regarding the relative efficiency of each composite material in strengthening the specimens of the present study. Table 4 shows the strength increase (ratio of measured ultimate load of strengthened specimen to that of the unstrengthened specimen SVM), and the ratio of deflection at midspan corresponding to the maximum measured load ($P_{max}$) to that of the CFRP-strengthened specimen SCM; the latter provides a relative measure of the deformability of the strengthened members. It is seen that as far as strength is concerned all three composite strips had a similar efficiency, i.e. increases in strength varied between 86% and 92%. The ratio $E_fA_f$ of SRP to CFRP strips used for strengthening the beams was very close to unity, hence the percentage increases are directly comparable; it should also be recalled that strength of these specimens was controlled by the debonding failure mode. It is noted here that although strength increases up to 160% are possible, much lower percentages are advisable for practical design (ACI 2008) due to additional requirements such as ductility, serviceability, and possible failure of the FRP system due to damage or vandalism.

Unlike strength, differences in deformability are more noticeable between CFRP and SRP strengthening, the latter leading to deflections up to 17% higher than that of the CFRP-strengthened beam. Among the two types of SRP used, that with a large number of twisted wires (12X) was clearly more efficient with respect to deformability, but slightly less efficient with respect to strength increase. Finally, comparison of the axial deformation of the reinforced polymer strip corresponding to the maximum load has shown that in specimens SS3X2M and SS12XM, this was 15% and 50% higher, respectively, than that of the CFRP-strengthened specimen, which indicates an increased axial flexibility of the SRP-strengthened members. The amount of energy dissipated by each specimen that
failed in a flexural way is given in figure 15. It is clear that, among the considered specimens, SRP12X dissipated the highest amount of energy. By considering also the highest deformation capacity that SRP12X developed, this material seems to be more suitable for strengthening of reinforced concrete beams than SRP3X2.

Conclusions

From the first part of the study, involving tension tests of reinforced polymer materials, it was confirmed that the stress – strain curves of SRP strips have a small inelastic branch prior to fracture, in contrast with CFRP for which the stress – strain curve is linear up to fracture. On the other hand, fracture strain had similar values for both materials.

Bond tests showed that the CFRP strips had higher debonding strength than SRP strips, which is in line with previous findings that bond strength of strips is proportional to the square root of their modulus of elasticity. The width of the strip was found to affect the bond strength between the reinforced polymer and the concrete; however, the increase in bond strength was not directly proportional to the width of the reinforced polymer. The two different anchorage lengths used for the tested strips (300 mm and 150 mm), were not found to have any noticeable effect on the debonding strength. This is not surprising if one notes that the effective anchorage length for the tested strips was lower than 150 mm. From the analytical models used for predicting the experimentally measured bond strengths, the model proposed by Chen and Teng (2001) was found to better match the test values.

The main part of the study, involving testing of full-scale beam specimens, showed that proper use of SRP strips as externally-bonded tensile reinforcement can increase the flexural strength up to 92%, which is substantially higher than that required in practice; it is recalled here that current codes place limits on the amount of strengthening, so that in the event that the reinforced polymer system is damaged (e.g. due to damage or vandalism), the structure will still be capable of resisting a reasonable level of load without collapse (ACI 2008). These materials can be deemed equally effective as CFRPs in increasing the flexural strength of R/C beams. After debonding of the strips, the strength of the specimen was found to be slightly lower than the strength of the corresponding unstrengthened specimen; this was attributed to the different cracking pattern, due to which the steel bars did not develop (at that stage) their full strength as in the unstrengthened beam. Higher deformation capacity (up to 17%) was found for the specimens strengthened with SRP, compared to the specimen strengthened with CFRP. Providing additional anchorage length (600 mm beyond the support) to the strips of the SRP and CFRP strengthened specimens, was not found to lead to increased strength or deformation capacity, with respect to that of the specimen where the strip was anchored close to the support in an area subjected to tension. As expected, all strengthened specimens failed by debonding of the strip; debonding initiated close to a flexural crack at mid-span.

From the analytical part of the study, the most interesting finding was that the increase in the effective strain (hence the strength) of reinforced polymer-strengthened beams attributed to the
presence of flexural cracks was 40%, which is slightly higher than the value reported in previous studies (Teng et al. 2002); of course this 40% cannot be claimed to be a value of general validity.

Finally, comparisons of analytically predicted strengths with experimentally measured values has shown that the equations developed for FRP-strengthened beams can also be used for SRP-strengthened members.

Acknowledgements

The research project, results of which are present in this paper, was jointly funded by EU-European Social Fund, the Greek Ministry of Development-GSRT, and Sika – Hellas.

References


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4. Table 4. Ratios of measured strengths (ultimate loads) and deflections of strengthened beams to that of the reference specimen (SVM)

**Figure Captions**

5. Fig. 1. Tensile stress-strain diagrams for unidirectional CFRP and SRP strips, and for steel reinforcement.
6. Fig. 2. Bond tests of 50 mm ×150 mm SRP and CFRP strips: (a) Test set-up; (b) Load vs. slip diagrams (detachment force is equal to 0.5P_{tot}).
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16. Fig. 12. Load vs. mid-span horizontal compression (LVDT ‘HMC’) curves
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Table 1. Specimen data and results from bond tests

<table>
<thead>
<tr>
<th>Specimen</th>
<th>Concrete Grade</th>
<th>$t_1 \times b_1 \times L$ mm</th>
<th>Type of Strip</th>
<th>$0.5P_{\text{tot}}$ kN</th>
<th>$s_{\text{tot}}/s_{\text{tot,u}}$</th>
<th>$\sqrt{E_i}/\sqrt{E_{\text{SRP12X}}}$</th>
<th>$P_{\text{SRP12X}}/P_i$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CFRP-5X15NS</td>
<td>C20/25</td>
<td>1.20 x 50 x 150</td>
<td>CFRP</td>
<td>19.0</td>
<td>0.38/0.52</td>
<td>1.13</td>
<td></td>
</tr>
<tr>
<td>CFRP-5X30NS</td>
<td>C20/25</td>
<td>1.20 x 50 x 300</td>
<td>CFRP</td>
<td>18.5</td>
<td>0.50/0.70</td>
<td>1.16</td>
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<td>SRP12-5X15NS</td>
<td>C20/25</td>
<td>1.23 x 50 x 150</td>
<td>SRP12X</td>
<td>13.7</td>
<td>1.09/1.25</td>
<td>1.01</td>
<td></td>
</tr>
<tr>
<td>SRP12-5X30NS</td>
<td>C20/25</td>
<td>1.23 x 50 x 300</td>
<td>SRP12X</td>
<td>13.5</td>
<td>0.55/1.11</td>
<td>1.02</td>
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</tr>
<tr>
<td>SRP12-8X15NS</td>
<td>C20/25</td>
<td>1.23 x 80 x 150</td>
<td>SRP12X</td>
<td>19.0</td>
<td>0.55/ -</td>
<td>1.05</td>
<td></td>
</tr>
<tr>
<td>SRP12-8X30NS</td>
<td>C20/25</td>
<td>1.23 x 80 x 300</td>
<td>SRP12X</td>
<td>21.0</td>
<td>0.58/0.99</td>
<td>0.95</td>
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</tr>
<tr>
<td>SRP3X2-5X15NS</td>
<td>C20/25</td>
<td>1.23 x 50 x 150</td>
<td>SRP3X2</td>
<td>15.0</td>
<td>0.45/0.56</td>
<td>0.99</td>
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</tr>
<tr>
<td>SRP3X2-5X30NS</td>
<td>C20/25</td>
<td>1.23 x 50 x 300</td>
<td>SRP3X2</td>
<td>14.0</td>
<td>- /0.60</td>
<td>1.07</td>
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</tr>
<tr>
<td>SRP3X2-8X15NS</td>
<td>C20/25</td>
<td>1.23 x 80 x 150</td>
<td>SRP3X2</td>
<td>20.3</td>
<td>0.37/0.79</td>
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<td>SRP3X2-8X30NS</td>
<td>C20/25</td>
<td>1.23 x 80 x 300</td>
<td>SRP3X2</td>
<td>22.0</td>
<td>1.29/1.28</td>
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<tr>
<td>CFRP-5X15HS</td>
<td>C35/45</td>
<td>1.20 x 50 x 150</td>
<td>CFRP</td>
<td>18.7</td>
<td>0.21/0.25</td>
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<td>CFRP-5X30HS</td>
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<td>1.20 x 50 x 300</td>
<td>CFRP</td>
<td>18.8</td>
<td>0.23/0.60</td>
<td>1.14</td>
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<td>SRP12-5X15HS</td>
<td>C35/45</td>
<td>1.23 x 50 x 150</td>
<td>SRP12X</td>
<td>13.8</td>
<td>0.23/0.51</td>
<td>1.00</td>
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<tr>
<td>SRP12-5X30HS</td>
<td>C35/45</td>
<td>1.23 x 50 x 300</td>
<td>SRP12X</td>
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<td>0.51/1.29</td>
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<td>SRP3X2-5X15HS</td>
<td>C35/45</td>
<td>1.23 x 50 x 150</td>
<td>SRP3X2</td>
<td>13.8</td>
<td>- /0.50</td>
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<tr>
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<td>C35/45</td>
<td>1.23 x 50 x 300</td>
<td>SRP3X2</td>
<td>15.3</td>
<td>0.28/0.54</td>
<td>0.98</td>
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* measured displacement between the outer points of the bonded lengths.
Table 2. Comparison between calculated and measured strength (ultimate load) for the tested beams

<table>
<thead>
<tr>
<th>Specimen</th>
<th>Calculated strength</th>
<th>Measured Strength</th>
<th>$P_{deb,calc} / P_{u,meas}$</th>
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<tr>
<td></td>
<td>$P_{deb}$</td>
<td>$P_{crit}$</td>
<td>$P_{fin}$</td>
</tr>
<tr>
<td></td>
<td>kN</td>
<td>kN</td>
<td>kN</td>
</tr>
<tr>
<td>SVS</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>SVM</td>
<td>-</td>
<td>-</td>
<td>113.24</td>
</tr>
<tr>
<td>SS3X2M</td>
<td>231.01</td>
<td>95.56</td>
<td>113.24</td>
</tr>
<tr>
<td>SS12XM</td>
<td>216.45</td>
<td>95.56</td>
<td>113.24</td>
</tr>
<tr>
<td>SCM</td>
<td>203.36</td>
<td>95.56</td>
<td>113.24</td>
</tr>
</tbody>
</table>

Note: $P_{deb}$, $P_{crit}$, and $P_{fin}$ are defined in Fig. 14.
Table 3. Comparison of the measured experimental strength with predictions according to ACI-440R-02, and EC8-3 and Greek Code for Interventions

<table>
<thead>
<tr>
<th>Specimen</th>
<th>Flexural Strength $M_u$</th>
<th>Ultimate Load $P_u$</th>
<th>$P_{u,\text{theor}} / P_{u,exp}$</th>
<th>Flexural Strength $M_u$</th>
<th>Ultimate Load $P_u$</th>
<th>$P_{u,\text{theor}} / P_{u,exp}$</th>
<th>Measured Strength</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>SS12XM</strong></td>
<td>105.95 kNm</td>
<td>192.63 kN</td>
<td>0.88</td>
<td>116.41 kNm</td>
<td>211.65 kN</td>
<td>0.97</td>
<td>218.00 kN</td>
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<td><strong>SS3X2M</strong></td>
<td>109.37 kNm</td>
<td>198.85 kN</td>
<td>0.88</td>
<td>121.36 kNm</td>
<td>220.65 kN</td>
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<td>225.60 kN</td>
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<td><strong>SCM</strong></td>
<td>107.58 kNm</td>
<td>195.60 kN</td>
<td>0.87</td>
<td>119.97 kNm</td>
<td>218.13 kN</td>
<td>0.97</td>
<td>224.80 kN</td>
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Table 4. Ratios of measured strengths (ultimate loads) and deflections of strengthened beams to that of the reference specimen (SVM)

<table>
<thead>
<tr>
<th>SPECIMEN</th>
<th>$P_{\text{max}}$ (kN)</th>
<th>$P_{\text{max}} / P_{\text{SVM}}$ (%)</th>
<th>$\delta_{\text{mid}@P_{\text{max}}}$ (mm)</th>
<th>$\delta_{\text{mid}@P_{\text{max}}}/\delta_{\text{mid}@P_{\text{max},SCM}}$</th>
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</thead>
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<tr>
<td>SVM</td>
<td>117.6</td>
<td>100.0</td>
<td>--</td>
<td>--</td>
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<tr>
<td>SS3X2M</td>
<td>225.6</td>
<td>191.8</td>
<td>21.7</td>
<td>1.04</td>
</tr>
<tr>
<td>SS12XM</td>
<td>218.0</td>
<td>185.9</td>
<td>24.4</td>
<td>1.17</td>
</tr>
<tr>
<td>SCM</td>
<td>224.8</td>
<td>191.2</td>
<td>20.8</td>
<td>1.00</td>
</tr>
</tbody>
</table>
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