



# City Research Online

## City, University of London Institutional Repository

---

**Citation:** Kapetanios, G., Labhard, V. and Price, S. (2007). Forecasting using Bayesian and information theoretic model averaging: an application to UK inflation (07/15). London, UK: Department of Economics, City University London.

This is the unspecified version of the paper.

This version of the publication may differ from the final published version.

---

**Permanent repository link:** <https://openaccess.city.ac.uk/id/eprint/1476/>

**Link to published version:** 07/15

**Copyright:** City Research Online aims to make research outputs of City, University of London available to a wider audience. Copyright and Moral Rights remain with the author(s) and/or copyright holders. URLs from City Research Online may be freely distributed and linked to.

**Reuse:** Copies of full items can be used for personal research or study, educational, or not-for-profit purposes without prior permission or charge. Provided that the authors, title and full bibliographic details are credited, a hyperlink and/or URL is given for the original metadata page and the content is not changed in any way.

**Department of Economics  
School of Social Sciences**

**Forecasting using Bayesian and information theoretic model  
averaging: an application to UK inflation**

**George Kapetanios<sup>1</sup>  
Queen Mary University of London**

**Vincent Labhard<sup>2</sup>  
Bank of England**

**Simon Price<sup>3</sup>  
Bank of England and City University**

**Department of Economics  
Discussion Paper Series  
No. 07/15**

---

<sup>1</sup> Email: [g.kapetanios@qmul.ac.uk](mailto:g.kapetanios@qmul.ac.uk).

<sup>2</sup> Email: [vincent.labhard@bankofengland.co.uk](mailto:vincent.labhard@bankofengland.co.uk)

<sup>3</sup> Department of Economics, City University, Northampton Square, London, EC1V  
0HB, UK. Email: [simon.price@bankofengland.co.uk](mailto:simon.price@bankofengland.co.uk)

# Forecasting using Bayesian and information theoretic model averaging: an application to UK inflation\*

George Kapetanios<sup>†</sup>  
Queen Mary University of London

Vincent Labhard<sup>‡</sup>  
Bank of England

Simon Price<sup>§</sup>  
Bank of England and City University

June 2006

## Abstract

Model averaging often improves forecast accuracy over individual forecasts. It may also be seen as a means of forecasting in data-rich environments. Bayesian model averaging methods have been widely advocated, but a neglected frequentist approach is to use information theoretic based weights. We consider the use of information-theoretic model averaging in forecasting UK inflation, with a large data set, and find that it can be a powerful alternative to Bayesian averaging schemes.

Keywords: forecasting, inflation, Bayesian model averaging, Akaike criteria, forecast combining

JEL: C110, C150, C530

---

\*This paper represents the views and analysis of the authors and should not be thought to represent those of the Bank of England or Monetary Policy Committee members. We are grateful for comments from two anonymous referees, the Editor and an Associate Editor of the JBES.

<sup>†</sup>g.kapetanios@qmul.ac.uk

<sup>‡</sup>vincent.labhard@bankofengland.co.uk

<sup>§</sup>simon.price@bankofengland.co.uk

# 1 Introduction

A key metric of a satisfactory forecast is precision, often defined in a root mean square error sense, and techniques that can deliver this are highly desirable. Model averaging is one such that often improves forecast accuracy over individual forecasts.

Another aspect of forecasting is appropriate methodology in data-rich environments, and in recent years there has been increasing interest in forecasting methods that utilise large datasets. There is an awareness that there is a huge quantity of information available in the economic arena which might be valuable for forecasting, but standard econometric techniques are not well suited to extract this in a useful form. This is not an issue of mere academic interest. Lars Svensson described what central bankers do in practice in Svensson (2004). ‘Large amounts of data about the state of the economy and the rest of the world ... are collected, processed, and analyzed before each major decision.’ In an effort to assist in this task, econometricians began assembling large macroeconomic data sets and devising ways of forecasting with them: James Stock and Mark Watson (*e.g.*, Stock and Watson (1999)) were in the vanguard of this campaign.

One popular methodology is forecast combination, where information in many forecasting models, typically simple and incomplete, are combined in some manner. Stepping back, forecast combination originated not in the large data set programme, but from observations by forecast practitioners that for whatever reasons, combining forecasts (initially by simple averaging) produced a forecast superior to any element in the combined set. This may seem odd, as if it were possible to identify the correctly specified model (and the data generating process (DGP) is unchanging), then it might seem natural so to do, although this is less obvious than it may seem. The true DGP may include very many variables that make it infeasible to estimate, and there is a general benefit from parsimony in forecasting. But the weight of evidence dating back to Bates and Granger (1969) and Newbold and Granger (1974) reveals that combinations of forecasts often outperform individual forecasts. Recent surveys of forecast combination from a frequentist perspective are to be found in Newbold and Harvey (2002) and Clements and Hendry (1998); see also Clements and Hendry (2002). Models may be incomplete, in different ways; they employ different information sets. Forecasts might be biased, and biases can offset each other. Even if forecasts are unbiased, there will be covariances between forecasts which should

be taken into account. Thus, combining misspecified models may, and often will, improve the forecast.

An alternative way of looking at this problem is from a Bayesian perspective. Here it is assumed that there is a distribution of models, thus delineating the concept of model uncertainty quite precisely. The basic problem, that a chosen model is not necessarily the correct one, can then be addressed in a variety of ways, one of which is Bayesian model averaging. From this point of view, a chosen model is simply the one with the best posterior odds; but posterior odds can be formed for all models under consideration, thereby suggesting a straightforward way of constructing model weights for forecast combinations. This has been used in many recent applications; for example, forecasting US inflation in Wright (2003a).

There is an analagous frequentist information theoretic approach. In this context, information theory suggest ways of constructing model confidence sets. We use this term in a broader sense than in the related literature of Hansen, Lunde, and Nason (2005) and Kapetanios, Labhard, and Schleicher (2006). Given we have a set of models, we can define relative model likelihood. Model weights within this framework have been suggested by Akaike (initially, Akaike (1978)). Such weights are easy to construct using standard information criteria. Our purpose, then, is to consider this way of model averaging as an alternative to Bayesian model averaging.

In this paper we develop the information-theoretic alternative to Bayesian model averaging and assess the performance of these techniques by means of a Monte Carlo study. We then compare their performance in forecasting UK inflation. For this, we use a UK data set which emulates the data set in Stock and Watson (2002) (see Appendix.) Our findings support those of Wright (2003a), who concludes that Bayesian model averaging can provide superior forecasts for US inflation, but we find that the frequentist approach also works well and in some cases better in the cases we examine for UK data.

## 2 Forecasting using Model Averaging

### 2.1 Bayesian Model Averaging

The idea behind forecasting using model averaging reflects the need to account for model uncertainty in carrying out statistical analysis. From a Bayesian perspective, model uncertainty is straightforward to handle using posterior model probabilities. See for example Min and Zellner (1993), Koop and Potter (2003), Draper (1995a) and Wright (2003a,b). Briefly, under Bayesian model averaging a researcher starts with a set of models which have been singled out as useful representations of the data. We denote this set as  $\mathcal{M} = \{M_i\}_{i=1}^N$  where  $M_i$  is the  $i$ -th of the  $N$  models considered. The focus of interest is some quantity of interest for the analysis, denoted by  $\Delta$ . This could be a parameter, or a forecast, such as inflation  $h$  quarters ahead. The output of a Bayesian analysis is a probability distribution for  $\Delta$  given the set of models and the observed data at time  $t$ . Denote the relevant information set at time  $t$  by  $D_t$ , and the probability distribution as  $pr(\Delta|D, \mathcal{M})$ . This is given by

$$pr(\Delta|D_t, \mathcal{M}) = \sum_{i=1}^N pr(\Delta|M_i, D_t)pr(M_i|D_t) \quad (1)$$

where  $pr(\Delta|M_i, D_t)$  denotes the conditional probability distribution of  $\Delta$  given a model  $M_i$  and the data  $D_t$  and  $pr(M_i|D_t)$  denotes the conditional probability of the model  $M_i$  being the true model given the data. Implementation requires two quantities to be obtained at each point in time. First,  $pr(\Delta|M_i, D_t)$  which is easily obtained from standard model specific analysis. Second, the weights,  $pr(M_i|D_t)$ . The weights are formed as part of a stochastic process where  $pr(M_i|D_t)$  is obtained from  $pr(M_i|D_{t-1})$ , the conditional probability of the model  $M_i$  being true, given the previous period's data. This requires prior distributions for  $pr(M_i|D_0) = pr(M_i)$  and  $pr(\theta_i|M_i, D_{t-1})$  to be specified.

Thus we need to obtain a number of expressions for (1) to be operational. First, using Bayes' theorem

$$pr(M_i|D_t) = \frac{pr(D_t|M_i, D_{t-1})pr(M_i|D_{t-1})}{pr(D_t|D_{t-1})} = \frac{pr(D_t|M_i, D_{t-1})pr(M_i|D_{t-1})}{\sum_{i=1}^N pr(D_t|M_i, D_{t-1})pr(M_i|D_{t-1})} \quad (2)$$

where  $pr(D_t|M_i, D_{t-1})$  denotes the conditional probability distribution of the data given the model  $M_i$  and the previous period's data and

$$pr(D_t|M_i, D_{t-1}) = \int pr(D_t|\theta_i, M_i, D_{t-1})pr(\theta_i|M_i, D_{t-1})d\theta_i \quad (3)$$

is the likelihood of model  $M_i$ , where  $\theta_i$  are the parameters of model  $M_i$ . Given this, the quantity of interest is

$$E(\Delta|D_t) = \sum_{i=1}^N \hat{\Delta}_i pr(M_i|D_t) \quad (4)$$

In theory (see *e.g.* Madigan and Raftery (1994)) when  $\Delta$  is a forecast, this sort of averaging provides better average predictive ability than single model forecasts.

## 2.2 Information Theoretic Model Averaging

In the context of non-Bayesian methods of forecasting the idea of model averaging (*i.e.*, forecast combination) has a long tradition starting with Bates and Granger (1969). The aim is to use forecasts obtained during some forecast evaluation period to determine optimal weights from which a forecast can be constructed along the lines of (4). These weights are usually constructed using some regression method and the available forecasts. But a problem arises if  $N$  is large. For example,  $N=93$  as in Wright (2003a) requires an infeasibly large forecast evaluation period.

Although the literature on model averaging inference is dominated by work with Bayesian foundations, there has also been some research based on frequentist considerations. Hjort and Claeskens (2003) provide a brief overview in the context of analysing model averaging estimators from a likelihood perspective. Most frequentist work focuses on the construction of distributions and confidence intervals for estimators of parameters that take into account, in some way, model uncertainty. Examples include Hurvich and Tsai (1990), Draper (1995b), Kabaila (1995), Pötscher (1991), Leeband and Pötscher (2000) and Kapetanios (2001). The work of Burnham and Anderson (1998), on which we build, forms a substantial part of the frequentist model averaging work available in the literature. But the present paper is one of the first to focus on forecasting as opposed to the construction of confidence intervals in the context of frequentist model averaging.

Our alternative to Bayesian model averaging is based on the analogue of  $pr(M_i|D_t)$  for frequentist statistics. Such a weight scheme has been implied in a series of papers by Akaike and others (see, *e.g.*, Akaike (1978, 1981, 1983, 1979) and Bozdogan (1987)) and expounded further by Burnham and Anderson (1998). Akaike's suggestion derives from the Akaike information criterion (*AIC*). *AIC* is an asymptotically unbiased measure of minus twice the log likelihood of a given model. It contains a term in the number of

parameters in the model, which may be viewed as a penalty for over-parameterization. Akaike's original frequentist interpretation relates to the classic mean-variance trade-off, although Akaike (1979) offers a Bayesian interpretation. In finite samples, when we add parameters there is a benefit (lower bias), but also a cost (increased variance). More technically, from an information theoretic point of view,  $AIC$  is an unbiased estimator of the Kullback and Leibler (1951) (KL) distance of a given model where the KL distance is given by

$$I(f, g) = \int f(x) \log \left( \frac{f(x)}{g(x|\theta^*)} \right) dx.$$

Here  $f(x)$  is the unknown true model generating the data,  $g(x|.)$  is the entertained model and  $\theta^*$  is the probability limit of the parameter vector estimate for  $g(x|.)$ .  $I(f, g)$  is not known. It can be replaced by

$$\hat{I}(f, g) = \int f(x) \log \left( \frac{f(x)}{g(x|\hat{\theta})} \right) dx.$$

where  $\hat{\theta}$  is the estimator of the parameter vector  $\theta$ . However,  $\hat{I}(f, g)$  cannot be used either as  $f(x)$  is not known. Using an observed sample  $x_1, \dots, x_T$ ,  $\hat{I}(f, g)$  can be approximated by

$$\tilde{I}(f, g) \frac{1}{T} \sum_{t=1}^T \log f(x_t) - \frac{1}{T} \sum_{t=1}^T \log g(x_t|\hat{\theta})$$

The first term of  $\tilde{I}(f, g)$  is still unknown, but it remains constant when comparing different models  $g$  and so is an operational model selection criterion. However, although  $\tilde{I}(f, g)$  and  $\hat{I}(f, g)$  have the same probability limit, the mean of the asymptotic distribution of  $T(\tilde{I}(f, g) - \hat{I}(f, g))$  is not zero. Akaike's main contribution is to derive an expression for this bias under certain regularity conditions. In particular, Akaike showed that the asymptotic expectation of  $T(\tilde{I}(f, g) - \hat{I}(f, g))$  is  $p$  where  $p$  is the dimension of  $\theta$ . More details on the derivation of this asymptotic expectation may be found in, *e.g.*, Gouriéroux and Monfort (1995, pp. 308-309).

So the difference of the  $AIC$  for two different models can be given a precise meaning. It is an estimate of the difference between the KL distance for the two models. Further,  $\exp(-1/2\Psi_i)$  is the relative likelihood of model  $i$  where  $\Psi_i = AIC_i - \min_j AIC_j$  and  $AIC_i$  denotes the  $AIC$  of the  $i$ th model in  $\mathcal{M}$ . Thus  $\exp(-1/2\Psi_i)$  can be thought of as the odds for the  $i$ th model to be the best KL distance model in  $\mathcal{M}$ . So this quantity can be viewed as the weight of evidence for model  $i$  to be the KL best model given that there is some model in  $\mathcal{M}$  that is KL best as a representation of the available data. Note that we



do not require the assumption that the true model belongs to  $\mathcal{M}$ . We are only considering the ranking of models in terms of KL distance. It is natural to normalise  $\exp(-1/2\Psi_i)$  so that

$$w_i = \frac{\exp(-1/2\Psi_i)}{\sum_{i=1}^N \exp(-1/2\Psi_i)} \quad (5)$$

where  $\sum_i w_i = 1$ . We refer to these as AIC weights. As the Akaike criterion is only one of several criteria which can form the basis of such weights, we also consider weights based on the Schwartz information criterion (SIC), which has a similar rationale. We consider both versions of the information-theoretic model averaging (ITMA) approach in the exercises we report below: one based on AIC weights (AITMA), and another based on SIC weights (SITMA).

We note  $w_i$  are not the relative frequencies with which given models would be picked up according to *AIC* as the best model given  $\mathcal{M}$ . Since the likelihood provides a superior measure of data based weight of evidence about parameter values compared to such relative frequencies (see, *e.g.*, Royall (1997)), it is reasonable to suggest that this superiority extends to evidence about a best model given  $\mathcal{M}$ . In Bayesian language, the  $w_i$  might be thought of as model probabilities under noninformative priors. However, this analogy should not be taken literally as these model weights are firmly based on frequentist ideas and do not make explicit reference to prior probability distributions about either parameters or models.

### 3 Monte Carlo evidence

We now undertake a small Monte Carlo study to explore the properties of various model averaging techniques in the context of forecasting. As we discussed above, model averaging aims to address the problem of model uncertainty in small samples. There are two broad cases that may be considered. The first is when the model that generates the data belongs to the class under consideration. In this case it addresses the issue that the chosen model is not necessarily the true model, and by assigning probabilities to various models provides a forecast that is, to some extent, robust to model uncertainty. The second, perhaps more relevant case, is where the true model does not belong to the class of models being considered. Here there is no possibility that the chosen model will capture all the features of the true model. As a result, the motivation for model averaging becomes stronger,

since forecasts from different models can inform the overall forecast in different ways. We examine this latter case.

In the experimental design, we adapt the setup proposed in Fernandez, Ley, and Steel (2001) and subsequently used repeatedly, for example in Eklund and Karlsson (2005). It therefore offers a standard problem to examine. Let  $\mathbf{X} = (x_1, \dots, x_N)$  be a  $T \times N$  matrix of regressors, where  $x_i = (x_{i,1}, \dots, x_{i,T})'$ . The series in the first  $2N/3$  columns are given by

$$x_{i,t} = \alpha_i x_{i,t-1} + \epsilon_{i,t}, i = 1, \dots, N, \quad t = 1, \dots, T \quad (6)$$

where  $\epsilon_t$  is i.i.d.  $N(0, 1)$ . The last  $N/3$  series are constructed as

$$(x_{2N/3+1}, \dots, x_N) = (x_1, \dots, x_{N/3})(0.3, \dots, 0.3 + (N/3 - 1)0.2)'(1, \dots, 1) + E \quad (7)$$

where  $E$  is a  $T \times N/3$  matrix of standard normal variates. This setup allows for some cross sectional correlation in the predictor variables. The true model is given by

$$y_t = 2x_{1,t} - x_{5,t} + 1.5x_{7,t} + x_{11,t} + 0.5x_{13,t} + 2.5\epsilon_t \quad (8)$$

where  $\epsilon_t$  is i.i.d.  $N(0, 1)$ . The numbering of the variables is prompted partly by the size of the data set and features of the models investigated in the source references, but this is not a critical feature of the design. The important point is that none of the models considered are the true DGP.

The design in Eklund and Karlsson (2005) sets  $N = 15$  and  $\alpha_i = 0$ . We generalise it in two directions. First, we set  $N = 60$ , the nearest round number to our own dataset. Second, we let  $\alpha_i \sim U(0.5, 1)$ . The  $\alpha_i$  introduce persistence, which we allow to be random.

The benchmark is the forecast produced by a simple  $AR(1)$  model for  $y_t$ . For the remaining forecasts, we use the model

$$y_{t+h} = a'x_t + by_t + \epsilon_t \quad (9)$$

for the  $h$ -step ahead forecast, where  $x_t$  is a  $K$ -dimensional regressor set, and  $K$  takes the value of 1 or 2. As  $K$  is no greater than 2, the true model can never be selected.

The combinations we evaluate are based on the complete set of models of form (9). The first three combinations are produced by Bayesian Model Averaging (BMA), which in some sense are benchmarks given their wide adoption, differing by a shrinkage parameter described below. The Bayesian weights are set following Wright (2003a). In particular,

we set the model prior probabilities  $P(M_i)$  to the uninformative priors  $1/N$ . The prior for the regression coefficients is chosen to be given by  $N(0, \phi\sigma^2(X'X)^{-1})$ , conditional on  $\sigma^2$ , where  $X$  is the  $T \times p$  regressor matrix for a given model and  $p$  is the numbers of regressors. We assume strict exogeneity of the  $X$ . The improper prior for  $\sigma^2$  is proportional to  $1/\sigma^2$ . The specification for the prior of the regression coefficients implies a degree of shrinkage towards zero (which implies no predictability). The degree of shrinkage is controlled by  $\phi$ . The rationale is that some degree of shrinkage steers away from models that may fit well in sample (by chance, or because of overfitting) but have little forecasting power. There is empirical evidence that such shrinkage is beneficial for out-of-sample forecasting, but no *a priori* guidance for what values should be selected. Following Wright (2003a) we consider conventional choices of  $\phi = 20, 2, 0.5$ . Given the above, routine integration gives model weights which are proportional to

$$(1 + \phi)^{-p/2} S^{-(T+1)} \tag{10}$$

where

$$S^2 = Y'Y - Y'X(X'X)^{-1}X'Y \frac{\phi}{1 + \phi} \tag{11}$$

and  $Y$  is the  $T \times 1$  regressand vector.

We next consider the ITMA weights introduced above, namely AITM and SITMa. Finally, we examine equal-weight model averaging (AV) where the weights are given by  $1/N$ . This last scheme, employed for example in Stock and Watson (2004) (see also Stock and Watson (2003)), is commonly used and often thought to work well in practice.

We set  $T = 50, 100$ . The forecast evaluation period for each sample is the last 30 observations. We examine the forecast horizons  $h = 1, \dots, 8$ . For all model averaging techniques we consider two different classes of models over which the weighting scheme is applied. The first is all models with one predictor variables ( $K = 1$ ), and the second all models with two predictor variables ( $K = 2$ ), neither of which contains the true model. We do not allow for higher  $K$  for two reasons. First, most forecasting models used in practice, and found to have good performance, are parsimonious. Second, weights are assigned to all members of the model class. With our setup and  $K = 2$  we have 1770 models to consider. For (say)  $K = 3$  the number of models rises to 34220 and therefore becomes computationally intensive. Methods to search the model space efficiently do exist that bypass this problem. One is that discussed by Fernandez, Ley, and Steel (2001) and based on Markov Chain Monte Carlo algorithms. Another is by Kapetanios (2005) which

uses genetic and simulated annealing algorithms to search for good models in terms of information criteria. But we do not explore these methods in this paper.

Results for forecast performance in terms of RMSE relative to the benchmark are given in Table 1. The best forecast method in a particular row (that is, for given  $K$ ,  $T$  and  $h$ ) are indicated in bold. These are evaluated to three decimal places, so in some cases more than one model is ‘best’, although at higher levels of numerical precision there is always a single best performer. Variations in performance are reasonably large. It is immediately evident that for this design the simple  $AR(1)$  benchmark does not perform well, being dominated for most combinations of  $K$ ,  $T$  and  $h$  by the combined forecasts. Using simple averaging does better than the AR but is never best. In the Bayesian cases, the low shrinkage parameter tends to do worst. A high shrinkage parameter improves performance, but performance is best for the intermediate value. It is best in 16 out of 32 cases, especially for short horizons. The average value of the RRMSE is 0.942.

Our main interest is in the the information-criteria based methods. The two methods (AITMA and SITMA) are based on penalty factors that are numerically similar in this experiment, and the results are correspondingly close. As can be seen, they do well, especially at longer horizons, where they tend to dominate BMA. Both AITMA and SITMA and have the best forecast in 15 out of 32 cases, only one less than for the intermediate BMA; similarly, the average RRMSE is a mere 0.003 greater at 0.945. The equivalent performance is a robust result across samples and choice of  $K$ . Essentially, it is hard to choose between the intermediate BMA and the information theoretic based methods. In the remainder of the paper we see whether these conclusions carry over to the real data.

## 4 Evidence from inflation forecasts

Our primary focus in this paper is practical, and in particular on the practice of inflation forecasting using the model averaging schemes examined in the Monte Carlo study. The models we consider are a standard specification, as discussed in Stock and Watson (2004). We modify our Monte Carlo design by using a  $k_1$  lags autoregressive process augmented with a  $k_2$  distributed lag on a single predictor variable. The number of lags in the pair  $(k_1, k_2)$  (*i.e.*, on the lagged dependent variable and the predictor variable) are chosen as

$(k, 1)$  where  $k$  is chosen optimally for each model, each sample and each forecast horizon using the Akaike information criterion: we refer to these models as  $ARX(k)$ . Consequently, the lag structure for each predictor-variable model may vary with the horizon. Thus, model  $i$  for forecasting horizon  $h$  is given by

$$\pi_{t+h} = \alpha + \sum_{j=1}^{k_1} \beta_j \pi_{t-j+1} + \sum_{j=1}^{k_2} \gamma_j x_{it-j+1} + \epsilon_t \quad (12)$$

where  $\pi_t$  is UK year-on-year CPI inflation,  $x_{it}$  is the  $i$ -th predictor variable at time  $t$  and  $\epsilon_t$  is the error term, with variance  $\sigma^2$ . As for the Monte Carlo experiment, the errors will exhibit a  $MA(h-1)$  process. We consider 58 predictor variables, where the data span 1980Q2-2004Q1. We further include the  $AR$  forecast, making a total of 59 forecasts to combine. Alongside the information theoretic combinations (based alternatively on AIC and SIC as in the Monte Carlo exercise) we consider Bayesian and equal-weight model averaging. The information theoretic weights are given by (5). The Bayesian weights are given by the scheme discussed in the Monte Carlo section using (10) and (11).

We use data from the period 1980Q2 to 1990Q1. We evaluate the forecasts over two post-sample periods: 1990Q2-1997Q1 (pre-MPC) and 1997Q2-2004Q1 (MPC). These are natural dates to choose, as from May 1997 monetary policy was set by the Bank of England's Monetary Policy Committee under an inflation targeting regime. Here we focus on an evaluation in terms of a RMSE criterion; in the working paper version of this paper Kapetanios, Labhard, and Price (2005) we also evaluate the combinations in terms of forecast densities. We consider horizons up to three years (that is,  $h = 1, \dots, 12$ ).

The forecasts are generated using a recursive forecasting scheme. For example, for the first evaluation period models are estimated up to 1990Q1 and 12 forecasts constructed (that is, for each period between 1990Q2 and 1993Q1). Then the models are re-estimated over the period 1980Q2 to 1990Q2 and forecasts constructed for the next 12 periods as before. This is repeated for all the possible forecasts within the evaluation period. From each re-estimation, the estimated log-likelihood is used to construct the relevant information criterion which is in turn used to construct the information theoretic weights, and similarly for the Bayesian weights. We report performance in terms of relative RMSE, compared to the benchmark  $AR$  model, as well as two other indicators: the percentage of models of the form (12) which perform worse than a given model averaging scheme in terms of relative RMSE; and the proportion of periods in which the model averaging scheme has a smaller absolute forecast error than the  $AR$  model. The results from these

three indicators are ranked similarly so we discuss only those from the first. In the relative RMSE tables we report a Diebold-Mariano (DM) test (Diebold and Mariano (1995)) of whether the forecast is significantly different from the benchmark AR model at the 10% level, indicated with an asterisc.

It is well known that the asymptotic distribution of the DM test statistic under the null hypothesis of equal predictive ability for the two forecasts is not normal when the models used to produce the forecasts are nested. A number of solutions have been proposed for this problem: see Corradi and Swanson (2006) for a survey. We use the parametric bootstrap to obtain the necessary critical values. An earlier example of the use of the bootstrap for the Diebold Mariano test statistic is Killian (1999). Our bootstrap design is straightforward. Under the null hypothesis the model generating the data is an  $AR(p)$  model. We use the parametric bootstrap to construct bootstrap samples for inflation from the recursively estimated  $AR(p)$  model. These bootstrap series are then combined with the predictor variables, which are kept fixed in the bootstrap sample. Forecasts are recursively produced for all the models and model averaging methods considered in the forecasting exercise, in exactly the same way as the original forecasts. Then DM statistics are produced and stored for every bootstrap replication. These statistics form the empirical distribution from which the bootstrap critical values are obtained. 199 bootstrap replications are used.

We first consider the MPC forecast evaluation period (Tables 2-4). The Akaike information theory based AITMA beats the AR benchmark at all horizons. This is also true for the simple average AV, but AITMA provides the best forecast in 8 out of 12 cases while the AV provides none. In the table, ‘best’ is defined to three decimal places, so more than one model can be ‘best’. In several cases the AIC and SIC are numerically identical to three decimal places, but AITMA is absolutely best in all eight cases. The difference from the AR benchmark is significant in six of the eight cases. This is a strong result, as forecast predictive tests have notoriously low power: Ashley (1998) concludes that ‘a model which cannot provide at least a 30% MSE improvement over that of a competing model is not likely to appear significantly better than its competitor over post sample periods of reasonable size.’ Moreover, AITMA beats the benchmark by a large margin in many cases - with a RMSE advantage of over 5% in all cases, of 20% or more in eight cases, and more than 30% in three cases. It does particularly well at long horizons, although it is also strong at short horizons. This all makes AITMA a powerful method in

this sample and this data set. The Bayesian BMA scheme works best for intermediate  $\phi$  in terms of the individual best forecast, but high  $\phi$  (giving the data a high weight) is the best Bayesian scheme overall, although clearly inferior to AITMA; and even the low  $\phi$  scheme is close to dominating the simple averaging scheme AV (which amounts to setting  $\phi = 0$ ).

In the working paper version of this paper we report the top-ten ranked models for the Bayesian and information theoretic schemes over the same period. The higher is  $\phi$ , the more weight is put on the variables with the highest in-sample explanatory power. Comparing the high  $\phi$  and information theoretic schemes, the variables selected and weights are very similar. However, the latter two give a little more weight to the best performer, and the subsequent weights decline at a slower rate relative to the Bayesian scheme. The AITMA and SITMA rankings are not identical but are extremely similar. Although there is clearly a concentrated peak on the most important variable, in each combination all the models enter with a non-zero weight; in that sense, the information in the entire data set is being combined, although by the tenth variable the weight in both the SITMA and the BMA with the highest  $\phi$  are down to 0.5%.

The conclusions remain broadly the same in the pre-MPC forecast evaluation period (Tables 5-7), although the AITMA is no longer so clearly dominant. The best-performing Bayesian ( $\phi = 20$ ) combination provides best forecasts at five horizons, compared to a score of the four best for AITMA. Six of the AITMA forecasts are significantly better than the benchmark: four of the Bayesian. In this period, while the AITMA continues to place more weight on fewer variables, the weights are much less concentrated than in the previous case. The variables selected by the high  $\phi$  BMA and AITMA are now less similar, but there is a high degree of commonality (as there is between the two samples).

Conceptually and practically, the two forecast combination methods are similar; as mentioned above, the model weights are not identical but there is a high degree of commonality. In both cases information is being gleaned from the data in-sample and used to inform the forecast method. In the low-shrinkage case, the frequentist analogy is to the likelihood-weighted scheme. As usual, the information theoretic measures steer away from the raw likelihood with a parameter penalty, which can be seen as similar to the way information criteria avoid overfitting in standard model selection. It is well known that information criteria can be given a Bayesian interpretation: see the discussion in Kadane and Lazar (2004). There is in principle no *a priori* reason to expect a particular approx-

imation to the Bayes factor to perform systematically better or worse than any other; all we can conclude is that in these samples and data the AITMA performs comparably to the Bayesian method. And unlike the Bayesian averaging, there is no requirement to select a particular value for a key parameter ( $\phi$ ). Although we have not explored it in this paper, in related work (Kapetanios, Labhard, and Price (2006)) we have extended the approach to use information theoretic weights constructed with the predictive likelihood, which is also a good performer. Finally, we note that although we find these information-theoretic techniques work well, and consider them a useful alternative to other techniques, we naturally do not suggest that they would or should be used as the main or only forecasting tool by any central bank.

## 5 Conclusions

Model averaging provides a well-established means of improving forecast performance which works well in practice and has sound theoretical foundations. It may also be helpful for another reason. In particular, in recent years there has been a rapid growth of interest in forecasting methods that utilise large datasets, driven partly by the recognition that policymaking institutions process large quantities of information, which might be helpful in the construction of forecasts. Standard econometric methods are not well suited to this task, but model averaging can help here as well.

In this paper we consider two averaging schemes. The first is Bayesian model averaging. This has been used in a variety of forecasting applications with encouraging results. The second is an information theoretic scheme which we derive in this paper using the concept of relative model likelihood developed by Akaike. Although the information theoretic approach has received less attention than Bayesian model averaging, the evidence we produce from a Monte Carlo study and an application forecasting UK inflation indicate that it has at least some potential to produce more precise forecasts and therefore might be a useful complement to other forecasting techniques. There are some advantages in practice. In the frequentist approach the weights are straightforward to compute, and there is less need to make arbitrary assumptions, for example about the shrinkage parameter or the prior distribution.

As there is a clear correspondence with Bayesian averaging, inasmuch as both are based



on model performance, it would be odd if the alternative scheme were not also useful. But our work shows that it may outperform Bayesian weights in some cases. Moreover, it has a clear frequentist interpretation and is easy to implement with little judgement required about ancillary assumptions. While it is highly unlikely that a single technique would be more useful than all others in all settings, our work indicates that information theoretic model averaging may provide a useful addition to the forecasting toolbox.

## References

- AKAIKE, H. (1978): “A Bayesian Analysis of the Minimum AIC Procedure,” *Annals of the Institute of Statistical Mathematics*, 30, 9–14.
- (1979): “A Bayesian Extension of the Minimum AIC Procedure of Autoregressive Model Fitting,” *Biometrika*, 66, 237–242.
- (1981): “Modern Development of Statistical Methods,” in *Trends and progress in system identification*, ed. by P. Eykhoff, pp. 169–84. Pergamon Press Paris.
- (1983): “Information Measures and Model Selection,” *International Statistical Institute*, 44, 277–291.
- ASHLEY, R. (1998): “A New Technique for Postsample Model Selection and Validation,” *Journal of Economic Dynamics and Control*, 22, 647–65.
- BATES, J. M., AND C. W. J. GRANGER (1969): “The Combination of Forecasts,” *Operations Research Quarterly*, 20, 451–68.
- BOZDOGAN, H. (1987): “Model Selection and Akaike’s Information Criterion (AIC): the General Theory and its Analytical Extensions,” *Psychometrika*, 52(3), 345–70.
- BURNHAM, K. P., AND D. R. ANDERSON (1998): *Model Selection and Inference*. Berlin: Springer Verlag.
- CLEMENTS, M. P., AND D. F. HENDRY (1998): *Forecasting Economic Time Series*. Cambridge: CUP.
- (2002): “Pooling of Forecasts,” *Econometrics Journal*, 5, 1–26.

- CORRADI, V., AND N. R. SWANSON (2006): “Predictive Density Evaluation,” in *Handbook of Economic Forecasting*, ed. by C. W. J. G. G. Elliot, and A. Timmerman, pp. 197–284. (Amsterdam: Elsevier).
- DIEBOLD, F. X., AND R. S. MARIANO (1995): “Comparing Predictive Accuracy,” *Journal of Business and Economic Statistics*, 13, 253–63.
- DRAPER, D. (1995a): “Assessment and propagation of model uncertainty,” *Journal of the Royal Statistical Society Series B*, 57, 45–97.
- DRAPER, D. (1995b): “Assessment and propagation of model uncertainty,” *Journal of the Royal Statistical Society, Series B*, 57, 45–97.
- EKLUND, J., AND S. KARLSSON (2005): “Forecast Combination and Model Averaging Using Predictive Measures,” *CEPR Working Paper No. 5268*.
- FERNANDEZ, C., E. LEY, AND M. F. STEEL (2001): “Benchmark Priors for Bayesian Model Averaging,” *Journal of Econometrics*, 100, 381–427.
- GOURIEROUX, C., AND A. MONFORT (1995): *Statistics and Econometric Models: Volume 2*. Cambridge: Cambridge University Press.
- HANSEN, P. R., A. LUNDE, AND J. M. NASON (2005): “Model Confidence Sets for Forecasting Models,” Working Paper 2005-7, Federal Reserve Bank of Atlanta.
- HJORT, N. L., AND G. CLAESKENS (2003): “Frequentist model average estimators,” *Journal of the American Statistical Association*, 98, 879–99.
- HURVICH, C. M., AND C.-L. TSAI (1990): “The impact of model selection on inference in linear regression,” *The American Statistician*, 44, 214–17.
- KABAILA, P. (1995): *Econometric Theory* 11, 537.
- KADANE, J. B., AND N. LAZAR (2004): “Methods and Criteria for Model Selection,” *Journal of the American Statistical Association*, 99, 279–90.
- KAPETANIOS, G. (2001): “Incorporating lag order selection uncertainty in parameter inference for AR models,” *Economics Letters*, 72, 137–44.
- KAPETANIOS, G. (2005): “Variable Selection Using Non-Standard Optimisation of Information Criteria,” Queen Mary and Westfield College, University of London, Mimeo.

- KAPETANIOS, G., V. LABHARD, AND S. PRICE (2005): “Forecasting using Bayesian and information theoretic model averaging: an application to UK inflation,” *Bank of England Working Paper No. 268*.
- (2006): “Forecasting Using Predictive Likelihood Model Averaging,” *Economics Letters*, 91, 373–79.
- KAPETANIOS, G., V. LABHARD, AND C. SCHLEICHER (2006): “Conditional Model Confidence Sets with an Application to Forecasting Models,” Manuscript, Bank of England.
- KILLIAN, L. (1999): “Exchange Rates and Monetary Fundamentals: What Do We Learn from Long-Horizon Regressions?,” *Journal of Applied Econometrics*, 14, 491.
- KOOP, G., AND S. POTTER (2003): “Forecasting in Large Macroeconomic Panels Using Bayesian Model Averaging,” *Federal Reserve Bank of New York Report 163*.
- KULLBACK, S., AND R. A. LEIBLER (1951): “On Information and Sufficiency,” *Annals of Mathematical Statistics*, 22, 79–86.
- LEEBAND, H., AND B. M. PÖTSCHER (2000): “The Finite-Sample Distribution of Post-Model-Selection Estimators, and Uniform Versus Non-Uniform Approximations,” *Technical Report TR 2000-03, Institut für Statistik und Decision Support Systems, Universität Wien*.
- MADIGAN, D., AND A. E. RAFTERY (1994): “Model Selection and Accounting for Model Uncertainty in Graphical Models using Occam’s Window,” *Journal of the American Statistical Association*, 89, 1,535–46.
- MIN, C., AND A. ZELLNER (1993): “Bayesian and Non-Bayesian Methods for Combining Models and Forecasts with Applications to Forecasting International Growth Rates,” *Journal of Econometrics*, 56, 89–118.
- NEWBOLD, P., AND C. W. J. GRANGER (1974): “Experience with Forecasting Univariate Time Series and the Combination of Forecasts,” *Journal of the Royal Statistical Society, Series A*, 137, 131–65.
- NEWBOLD, P., AND D. I. HARVEY (2002): “Forecast Combination and Encompassing,” in *A Companion to Economic Forecasting*, ed. by M. Clements, and D. F. Hendry, chap. 12. Oxford: Basil Blackwell.

- PÖTSCHER, B. M. (1991): “Effects of Model Selection on Inference,” *Econometric Theory*, 7, 163–85.
- ROYALL, R. M. (1997): *Statistical Evidence: a Likelihood Paradigm*. New York: Chapman and Hall.
- STOCK, J. H., AND M. W. WATSON (1999): “Forecasting Inflation,” *Journal of Monetary Economics*, 44, 293–335.
- STOCK, J. H., AND M. W. WATSON (2002): “Macroeconomic Forecasting Using Diffusion Indices,” *Journal of Business and Economic Statistics*, 20, 147–62.
- (2003): “Forecasting Output and Inflation: the Role of Asset Prices,” *Journal of Economic Literature*, 41, 788–829.
- (2004): “Combination Forecasts of Output Growth in a Seven Country Dataset,” *Journal of Forecasting*, 23, 405–30.
- SVENSSON, L. E. O. (2004): “Monetary Policy with Judgment: forecast Targeting,” unpublished.
- WRIGHT, J. H. (2003a): “Bayesian Model Averaging and Exchange Rate Forecasts,” *Board of Governors of the Federal Reserve System, International Finance Discussion Papers No 779*.
- (2003b): “Forecasting US Inflation by Bayesian Model Averaging,” *Board of Governors of the Federal Reserve System, International Finance Discussion Papers No 780*.

Table 1: Monte Carlo Study: RMSE of various Model Averaging schemes

<b>K</b>	<b>T</b>	<b>Horizon</b> <b>h</b>	<b>BMA</b> ( $\phi = 20$ )	<b>BMA</b> ( $\phi = 2$ )	<b>BMA</b> ( $\phi = 0.5$ )	<b>AITMA</b>	<b>SITMA</b>	<b>AV</b>
1	50	1	0.993	<b>0.990</b>	0.994	0.996	0.996	0.995
		2	0.976	<b>0.970</b>	0.979	0.978	0.978	0.984
		3	0.959	<b>0.954</b>	0.966	0.961	0.961	0.975
		4	0.947	<b>0.936</b>	0.952	0.950	0.950	0.965
		5	0.935	0.923	0.941	<b>0.905</b>	<b>0.905</b>	0.959
		6	0.919	0.910	0.932	<b>0.907</b>	<b>0.907</b>	0.954
		7	0.922	0.908	0.929	<b>0.902</b>	<b>0.902</b>	0.952
		8	0.921	0.907	0.927	<b>0.903</b>	<b>0.903</b>	0.949
1	100	1	<b>0.984</b>	0.985	0.993	<b>0.984</b>	<b>0.984</b>	0.996
		2	0.979	<b>0.976</b>	0.986	0.980	0.980	0.993
		3	0.972	<b>0.968</b>	0.979	0.973	0.973	0.990
		4	0.973	<b>0.966</b>	0.974	0.974	0.974	0.988
		5	0.973	0.963	0.969	<b>0.946</b>	<b>0.946</b>	0.986
		6	0.964	0.958	0.967	<b>0.948</b>	<b>0.948</b>	0.985
		7	0.969	0.961	0.965	<b>0.953</b>	<b>0.953</b>	0.985
		8	0.964	<b>0.955</b>	0.959	0.959	0.959	0.983
2	50	1	1.005	<b>0.991</b>	0.994	1.015	1.015	0.996
		2	0.964	<b>0.952</b>	0.962	0.971	0.971	0.970
		3	0.943	<b>0.926</b>	0.940	0.949	0.949	0.954
		4	0.919	<b>0.908</b>	0.922	0.926	0.926	0.938
		5	0.899	0.889	0.910	<b>0.881</b>	<b>0.881</b>	0.934
		6	0.885	0.880	0.903	<b>0.879</b>	<b>0.879</b>	0.927
		7	0.885	0.877	0.899	<b>0.863</b>	<b>0.863</b>	0.925
		8	0.891	0.878	0.898	<b>0.873</b>	<b>0.873</b>	0.925
2	100	1	<b>0.980</b>	0.983	0.992	0.981	0.981	0.995
		2	0.977	<b>0.971</b>	0.981	0.980	0.980	0.988
		3	0.969	<b>0.959</b>	0.969	0.971	0.971	0.981
		4	0.967	<b>0.958</b>	0.964	0.970	0.970	0.978
		5	0.959	0.947	0.954	<b>0.944</b>	<b>0.944</b>	0.973
		6	0.945	<b>0.935</b>	0.944	0.944	0.944	0.969
		7	0.941	0.933	0.943	<b>0.930</b>	<b>0.930</b>	0.967
		8	0.932	0.924	0.937	<b>0.920</b>	<b>0.920</b>	0.965

*BMA* indicates Bayesian Model Averaging where  $\phi$  indicates shrinkage factor

*AITMA*, *SITMA* indicate Akaike, Schwartz Information Criteria weights

*AV* indicates simple average

**bold** indicates best forecast in row (to third decimal place)

Table 2: Relative RMSE of Out-of-Sample CPI Forecasts using ARX(k) Models (Period: 1997Q2-2004Q1)

Horizon	$BMA(\phi = 20)$	$BMA(\phi = 2)$	$BMA(\phi = 0.5)$	$AITMA$	$SITMA$	AV
1	1.130*	1.028*	1.002	<b>0.948</b>	1.072	0.993
2	0.904	0.955*	0.962*	<b>0.774*</b>	0.833*	0.964*
3	0.747*	0.920*	0.959*	<b>0.706*</b>	<b>0.706*</b>	0.967*
4	0.875	0.906*	0.957*	<b>0.849</b>	0.893	0.967*
5	0.908	<b>0.808*</b>	0.903*	0.924	0.932	0.934*
6	0.877	<b>0.819</b>	0.906	0.858	0.868	0.940
7	0.805	0.805*	0.890*	0.797	0.794	0.934*
8	0.729	0.788*	0.881*	<b>0.718*</b>	<b>0.718</b>	0.929
9	0.713*	0.801*	0.898	<b>0.706*</b>	<b>0.706*</b>	0.939
10	0.704*	0.817*	0.915*	<b>0.694*</b>	<b>0.694*</b>	0.949*
11	0.700*	0.828*	0.916*	<b>0.689*</b>	<b>0.689*</b>	0.946
12	0.702*	0.836*	0.917*	0.684*	<b>0.683*</b>	0.946*

\* 10% rejection of Diebold-Mariano test that the forecast differs from the benchmark

**bold** indicates best forecast in row (to third decimal place)

$BMA$  indicates Bayesian Model Averaging where  $\phi$  indicates shrinkage factor

$AITMA$ ,  $SITMA$  indicate Akaike, Schwartz Information Criteria weights

$AV$  indicates simple average

Table 3: Proportion of individual models with higher relative RMSE for Out-of-Sample CPI Forecasts using ARX(k) Models (Period: 1997Q2-2004Q1)

Horizon	$BMA(\phi = 20)$	$BMA(\phi = 2)$	$BMA(\phi = 0.5)$	$AITMA$	$SITMA$	AV
1	0.121	0.414	0.672	0.897	0.224	0.759
2	0.914	0.810	0.776	0.948	0.931	0.776
3	0.931	0.897	0.845	0.948	0.948	0.845
4	0.914	0.879	0.776	0.931	0.879	0.776
5	0.793	0.914	0.793	0.793	0.793	0.776
6	0.862	0.931	0.845	0.862	0.862	0.793
7	0.914	0.914	0.828	0.914	0.914	0.759
8	0.931	0.897	0.828	0.931	0.931	0.759
9	0.983	0.914	0.810	0.983	0.983	0.776
10	0.983	0.897	0.810	0.983	0.983	0.793
11	0.983	0.897	0.776	0.983	0.983	0.759
12	0.983	0.897	0.776	0.983	0.983	0.776

$BMA$  indicates Bayesian Model Averaging where  $\phi$  indicates shrinkage factor

$AITMA$ ,  $SITMA$  indicate Akaike, Schwartz Information Criteria weights

$AV$  indicates simple average

Table 4: Proportion of Periods in which model has smaller absolute forecast error than AR model for Out-of-Sample CPI Forecasts using ARX(k) Models (Period: 1997Q2-2004Q1)

Horizon	$BMA(\phi = 20)$	$BMA(\phi = 2)$	$BMA(\phi = 0.5)$	$AITMA$	$SITMA$	AV
1	0.375	0.406	0.438	0.500	0.313	0.500
2	0.625	0.719	0.750	0.656	0.656	0.719
3	0.688	0.750	0.750	0.688	0.688	0.750
4	0.625	0.656	0.594	0.750	0.688	0.594
5	0.719	0.750	0.813	0.719	0.719	0.813
6	0.719	0.688	0.750	0.719	0.719	0.688
7	0.719	0.750	0.719	0.719	0.719	0.781
8	0.781	0.813	0.781	0.781	0.781	0.781
9	0.844	0.813	0.844	0.844	0.844	0.813
10	0.875	0.875	0.906	0.875	0.875	0.844
11	0.906	0.906	0.938	0.906	0.906	0.875
12	0.938	0.938	0.938	0.938	0.938	0.906

$BMA$  indicates Bayesian Model Averaging where  $\phi$  indicates shrinkage factor  
 $AITMA$ ,  $SITMA$  indicate Akaike, Schwartz Information Criteria weights  
 $AV$  indicates simple average

Table 5: Relative RMSE of Out-of-Sample CPI Forecasts using ARX(k) Models (Period: 1990Q2-1997Q1)

Horizon	$BMA(\phi = 20)$	$BMA(\phi = 2)$	$BMA(\phi = 0.5)$	$AITMA$	$SITMA$	AV
1	0.999	0.987	0.983	<b>0.963</b>	0.967	0.982*
2	0.953	0.970*	0.970*	<b>0.885</b>	0.902	0.970*
3	0.828*	0.909*	0.932*	0.822	<b>0.821</b>	0.941*
4	0.752*	0.865*	0.909*	0.749*	<b>0.745*</b>	0.923*
5	0.732*	0.840*	0.895*	<b>0.698*</b>	0.702*	0.914*
6	<b>0.689</b>	0.812	0.885	0.696	0.697	0.911
7	<b>0.662</b>	0.781	0.873	0.796*	0.716*	0.905
8	<b>0.643</b>	0.785*	0.869	0.747*	0.708*	0.893
9	<b>0.749</b>	0.840*	0.894	0.780	0.760	0.906
10	<b>0.793</b>	0.876	0.909	0.844*	0.827	0.913
11	0.892*	0.899	0.919	<b>0.848*</b>	0.879*	0.920
12	0.971	<b>0.923</b>	0.933	0.936	0.941	0.932

\* 10% rejection of Diebold-Mariano test that the forecast differs from the benchmark

**bold** indicates best forecast in row (to third decimal place)

$BMA$  indicates Bayesian Model Averaging where  $\phi$  indicates shrinkage factor  
 $AITMA$ ,  $SITMA$  indicate Akaike, Schwartz Information Criteria weights  
 $AV$  indicates simple average

Table 6: Proportion of individual models with higher relative RMSE for Out-of-Sample CPI Forecasts using ARX(k) Models (Period: 1990Q2-1997Q1)

Horizon	$BMA(\phi = 20)$	$BMA(\phi = 2)$	$BMA(\phi = 0.5)$	$AITMA$	$SITMA$	AV
1	0.707	0.793	0.793	0.879	0.879	0.793
2	0.862	0.828	0.828	0.983	0.931	0.828
3	0.931	0.862	0.828	0.948	0.948	0.810
4	0.983	0.862	0.828	0.983	0.983	0.828
5	0.983	0.862	0.828	0.983	0.983	0.810
6	1.000	0.931	0.828	0.983	0.983	0.759
7	1.000	0.914	0.828	0.897	0.966	0.793
8	1.000	0.914	0.845	0.914	0.966	0.810
9	0.966	0.914	0.845	0.948	0.948	0.845
10	0.966	0.914	0.862	0.931	0.948	0.862
11	0.931	0.914	0.862	0.966	0.931	0.845
12	0.759	0.897	0.879	0.879	0.862	0.879

$BMA$  indicates Bayesian Model Averaging where  $\phi$  indicates shrinkage factor  
 $AITMA$ ,  $SITMA$  indicate Akaike, Schwartz Information Criteria weights  
 $AV$  indicates simple average

Table 7: Proportion of Periods in which model has smaller absolute forecast error than AR model for Out-of-Sample CPI Forecasts using ARX(k) Models (Period: 1990Q2-1997Q1)

Horizon	$BMA(\phi = 20)$	$BMA(\phi = 2)$	$BMA(\phi = 0.5)$	$AITMA$	$SITMA$	AV
1	0.656	0.719	0.688	0.688	0.563	0.688
2	0.750	0.688	0.688	0.656	0.719	0.688
3	0.781	0.750	0.781	0.781	0.781	0.781
4	0.750	0.875	0.844	0.688	0.719	0.906
5	0.719	0.719	0.813	0.688	0.656	0.844
6	0.656	0.813	0.813	0.594	0.625	0.813
7	0.781	0.844	0.906	0.656	0.688	0.906
8	0.781	0.813	0.844	0.688	0.688	0.844
9	0.688	0.688	0.719	0.625	0.625	0.750
10	0.750	0.781	0.781	0.719	0.656	0.781
11	0.719	0.781	0.813	0.781	0.781	0.781
12	0.719	0.750	0.719	0.625	0.625	0.719

$BMA$  indicates Bayesian Model Averaging where  $\phi$  indicates shrinkage factor  
 $AITMA$ ,  $SITMA$  indicate Akaike, Schwartz Information Criteria weights  
 $AV$  indicates simple average



# Data Appendix

In this appendix, we provide a list of the series used in Section 4 to forecast U.K. inflation. These series come from a data set which has been constructed to match the set used by Stock and Watson (2002). In total, this data set has 131 series, comprising 20 output series, 25 labour market series, 9 retail and trade series, 6 consumption series, 6 series on housing starts, 12 series on inventories and sales, 8 series on orders, 7 stock price series, 5 exchange rate series, 7 interest rate series and 6 monetary aggregates, 19 price indices and an economic sentiment index. We retained the 58 series with at least 90 observations. The series are grouped under 10 categories. For each series we give a brief description: more details, summary statistics and the transformations applied to ensure stationarity are available on request.

## **Series 1 to 8: Real output and income.**

- S1: Gross Domestic Product.
- S2: Manufacturing
- S3: Durable Manufacturing
- S4: Semi-durable Manufacturing
- S5: Non-durable Manufacturing
- S6: Mining & quarrying
- S7: Electricity, gas and water supply
- S8: Real households disposable income

## **Series 9 to 21: Employment and hours.**

- S9: UK Workforce jobs
- S10: Employed, Nonagricultural
- S11: Employment Rate

- S12: Employees total nonagricultural
- S13: Employees private nonagricultural
- S14: Employee jobs: Production
- S15: Employee jobs: Construction
- S16: Employee jobs: Manufacturing
- S17: Employee jobs: Wholesale & retail trade
- S18: Employee jobs: Banking, finance & insurance
- S19: Employee jobs: Total services
- S20: Employee jobs Public admin. & defence
- S21: Average weekly manufacturing hours

**Series 22 to 23: Trade.**

- S22: BOT Goods
- S23: BOT: Manufactures

**Series 24 to 29: Consumption.**

- S24: Household final consumption expenditure
- S25: Durable goods
- S26: Semi-durable goods
- S27: Non-durable goods
- S28: Services
- S29: Purchase of vehicles

**Series 30 to 35: Real inventories and inventories sales.**

- S30: Change in Inventories: Manufacturing
- S31: Change in Inventories Textiles & Leather
- S32: Manuf & Trade Invent: Nondurable Goods
- S33: Change in Inventories: Wholesale
- S34: Change in Inventories: Retail
- S35: Inventory/Output Mfg & Trade

**Series 36 to 38: Stock prices.**

- S36: FTSE All Share Price Index
- S37: FTSE100
- S38: FTSE All Share Dividend Yield

**Series 39 to 43: Exchange rates.**

- S39: Sterling effective rate
- S40: Euro/£
- S41: Swiss Franc/£
- S42: Yen/£
- S43: US\$/£

**Series 44 to 47: Interest rates.**

- S44: Spread 6 months to 1 month
- S45: Spread 1 year to 1 month
- S46: Spread 5 years to 1 month

- S47: Spread 10 years to 1 month

**Series 48 to 50: Monetary and quantity credit aggregates.**

- S48: M4
- S49: M0
- S50: Reserves & other accounts outstanding

**Series 51 to 57: Price indices.**

- S51: Output of manufactured products
- S52: CPI
- S53: Household final consumption
- S54: Durable goods
- S55: Semi-durable goods
- S56: Non-durable goods
- S57: Services

**Series 58: Surveys.**

- S58: MORI General Economic Optimism index