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# Theoretical study of multispectral structured illumination for depth resolved imaging of non-stationary objects: focus on retinal imaging

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**Abstract:** Current implementations of structured illumination microscopy for depth-resolved (three-dimensional) imaging have limitations that restrict its use; specifically, they are not applicable to non-stationary objects imaged with relatively poor condenser optics and in non-fluorescent mode. This includes *in-vivo* retinal imaging. A novel implementation of structured illumination microscopy is presented that overcomes these issues. A three-wavelength illumination technique is used to obtain the three sub-images required for structured illumination simultaneously rather than sequentially, enabling use on non-stationary objects. An illumination method is presented that produces an incoherent pattern through interference, bypassing the limitations imposed by the aberrations of the condenser lens and thus enabling axial sectioning in non-fluorescent imaging. The application to retinal imaging can lead to a device with similar sectioning capabilities to confocal microscopy without the optical complexity (and cost) required for scanning systems.

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## 1. Introduction

Structured illumination microscopy has been proposed and developed as a technique which enables optical sectioning of a three-dimensional (3D) object resulting in images similar to those obtained using a confocal scanning microscope [1, 2, 3]. It has also been used for enhanced lateral resolution, allowing superresolution beyond the diffraction limit [4, 5]. In the depth-resolving case, the basic principle between structured illumination microscopy and confocal microscopy is similar, namely that only planes that are in focus are imaged efficiently and out-of-focus planes contribute significantly less to the image. However they are fundamentally different optical systems. Structured illumination microscopy has the advantage of being an optically simple technique that does not require laser illumination nor scanning of the beam or sample. The non-scanning configuration of the structured illumination microscope enables a simple optical set up with minimal moving parts, and thus the potential for cost-effectiveness and robustness. Furthermore, in the confocal microscope the detector pinhole rejects light in order to achieve axial sectioning, and in practice, especially in the ophthalmic imaging case of the confocal Scanning Laser Ophthalmoscope (SLO), trade offs have to be made between pinhole size and confocality, thus limiting the axial sectioning capabilities of the device. Structured illumination microscopy does not reject any light prior to detection and can therefore image the sample more efficiently.

In structured illumination microscopy, the sample is illuminated with a sinusoidal pattern along one of its lateral dimensions. For weak objects, it has been shown that it is only the zero-order spatial frequency that does not attenuate with defocus [6]. The sinusoidal illumination enables us to recover an image in which the zero-order term is absent; all remaining spatial frequencies will therefore attenuate with defocus ensuring that the in-focus plane is the one that contributes most significantly to the image obtained [1]. However, it is necessary to acquire three successive images with the sinusoidal pattern displaced by phases of  $2\pi/3$  and  $-2\pi/3$  with respect to the first image. From these three images, an optically sectioned image of the sample can be obtained, as well as an image analogous to the conventional microscope for comparison [1, 2, 3].

## 2. Non-stationary objects and retinal imaging

When dealing with non-stationary objects, such as in retinal imaging where the involuntary and voluntary tremors and saccades of the eye result in a continuously moving sample, the sequential acquisition of the three images with shifted sinusoidal patterns cannot work as the desired phase shift cannot be obtained. A solution has been proposed by Shroff *et al.* for the application of structured illumination for superresolution in which a postprocessing algorithm has been developed to estimate the random phase shifts introduced by a non-stationary object [7, 8, 9].

In this Paper a novel implementation of structured illumination is proposed in which the three images with displaced sinusoidal illumination are acquired simultaneously instead of sequentially, thus avoiding the problems introduced by the non-stationarity of the object. This is achieved by illuminating the sample with three different wavelengths each projecting a sinusoidal pattern with the required phase. The use of different wavelengths for obtaining optical

sectioning was first proposed by Krzewina *et al.* [10]. In the method described in this Paper, the wavelengths are chosen to match the peak responsivity of the three detector types in a colour CCD camera so that, after appropriate filtering to minimise cross-talk, the three required images can be extracted from the three colour channels of a single image from the CCD camera from which the final optically sectioned image can be retrieved. The resulting multispectral image will of course be a result of three sub-images which are not exactly identical owing to the difference in reflectivity of the imaged layer for the three wavelengths. However, the spatial frequency of the grid will be high with respect to the structures being imaged (as discussed below) and therefore any artefacts will be negligible. Furthermore, in practical situations it is likely that a number of successive optically sectioned images will be aligned and averaged to maximise contrast and minimise noise, and hence the non-stationarity of the object is now advantageous as the averaging process will ensure that the inhomogeneities due to wavelength differences of a single image are also averaged. The final image will therefore be a composite of three wavelengths, yielding more information than a monochromatic image.

When imaging the human retina, standard structured illumination microscopy encounters a further problem that prevents its application to retinal imaging. The structured pattern illuminating the sample is achieved in one of two ways, namely grid projection or fringe projection [1, 2, 3]. In the former, a sinusoidal grid is illuminated incoherently and imaged onto the sample, in the latter a laser beam is used to generate a coherent fringe pattern on the sample. It has been shown by Karadaglić and Wilson that axial sectioning can only be obtained under incoherent imaging [2, 3] and therefore the fringe projection method can only be used for fluorescence microscopy as the incoherence is obtained through the mutual independence of the fluorophores; non-invasive retinal imaging is not a fluorescence technique and hence fringe projection cannot be used. Grid projection is limited by the Modulation Transfer Function (MTF) of the condenser lens as the spatial frequency of the grid affects the axial resolution. Because of the relatively poor optics of the human eye (which acts as both condenser and objective in retinal imaging) the highest spatial frequency that can be obtained by the grid projection technique (about 60 cycles per degree (cpd), this being the frequency cut-off of a typical eye [11]) is too low for achieving the desired axial resolution (which Neil *et al.* [1] showed to be a maximum when the spatial frequency  $\nu$  of the grid is given by  $\nu = NA/\lambda$ , where  $NA$  is the numerical aperture of the eye and  $\lambda$  the wavelength, giving approximately 500cpd for a 4mm pupil at 500nm).

The technique proposed in this Paper resolves this issue by introducing a third projection method which is a modified fringe projection method that we will refer to as Fizeau fringe projection technique. The technique, described in detail in the next section, can project fringes whose spatial frequency is not limited by the optics of the eye (or more generally by the collector lens) and illuminates the sample incoherently as required for non-fluorescent axial sectioning using structured illumination.

### 3. Fizeau Fringe Projection technique

The modified, or incoherent, fringe projection technique is based on a Michelson interferometer set up in which an incoherent extended light source is used to project straight Fizeau fringes directly onto the retina. (We will illustrate this technique with specific reference to the ophthalmic case though it is applicable to structured illumination microscopy in general.) We will summarise the theory to highlight the nature of the fringes, as this is critical in structured illumination microscopy, though further detail can be found in most optics texts [12, 13]. Figure 1 shows a representation of a Michelson interferometer in which all branches are superimposed onto the same optical axis. The plane  $\Sigma$  represents the extended incoherent light source,  $M_1$  and  $M_2$  represent the mirrors (one of which is actually the image of the mirror on the beamsplitter,

not shown). The axial optical path length of the mirrors from the source is equal, though one mirror is tilted with respect to the other by a small angle  $\alpha$ . If we consider a point source  $S$  on the extended source  $\Sigma$ , then each mirror creates an image of this source,  $S'_1$  and  $S'_2$  respectively. The fringes are localised at the plane of the air wedge produced by the two mirrors, and therefore the eye will focus at the plane containing  $M_1$  and  $M_2$ .

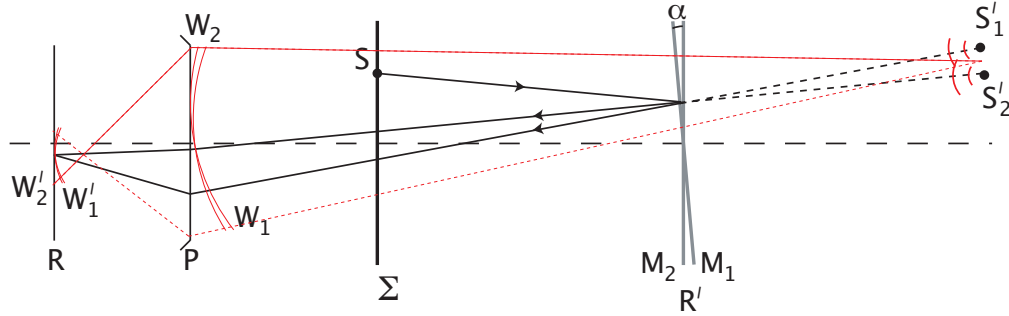


Fig. 1. Schematic representation of the Michelson interferometry set up used for the Fizeau fringe projection technique. The schematic superimposes all branches onto the same axis for clarity. The ray shown coming from  $S$  will reflect off both mirrors such that the optical path difference of the reflected rays is only dependant on the thickness of the optical air wedge formed by the mirror, for small tilt angles  $\alpha$ . In relation to Fig. 2,  $\Sigma$  represents the plane of the rotating diffuser,  $M_2$  is the common reference mirror and  $M_1$  the wavelength specific mirror.  $P$  and  $R$  are the pupil plane and retinal plane respectively, representing the eye. The plane containing the mirrors,  $R'$ , is conjugate to  $R$ .

We can therefore consider the light reaching the eye to be coming from the two point sources  $S'_1$  and  $S'_2$  both of which are emitting diverging spherical waves, so that at the pupil plane of the eye we can define wavefronts  $W_1$  and  $W_2$  coming from the respective sources. These wavefronts have the same curvature since the two sources  $S'_1$  and  $S'_2$  are equidistant from the eye for small angle  $\alpha$ , and their respective angular tilt is  $\alpha$ . As the eye is focused at the plane containing the mirrors  $M_1$  and  $M_2$ , these wavefronts will focus before the retina (as shown by the dotted red lines in Fig. 1) and we can therefore define two diverging wavefronts  $W'_1$  and  $W'_2$  at the retina that are again identical except for tilt. The interference produced by these wavefronts will therefore form an interference pattern on the retina consisting of parallel straight fringes. It should be noted that because  $\alpha$  is small, the angular subtense of the sources  $S'_1$  and  $S'_2$  at the eye can be assumed to be well within the isoplanatic patch of the eye, therefore any aberrations introduced at the pupil plane of the eye will be common to both  $W_1$  and  $W_2$ , and hence  $W'_1$  and  $W'_2$ . Thus the fringe pattern produced is not affected by the optics of the eye and the spatial frequency of the sinusoidal pattern is only a function of the angle  $\alpha$  and the wavelength  $\lambda$  [12]. This holds for all point sources  $S$  on the extended incoherent source plane  $\Sigma$ , thus giving an incoherently illuminated sinusoidal grid pattern whose spatial frequency can be tuned by rotating one of the mirrors to vary the angle  $\alpha$ . The phase of the illuminating sinusoidal pattern can be altered by moving one of the mirrors axially to alter the relative optical path difference between the two branches. By separating the three wavelengths it is possible to adjust the frequency and phase of each fringe pattern separately by using three different mirrors in one of the arms of the interferometer.

Since the Fizeau fringes produced are localised at the plane of the optical air wedge formed by the two mirrors, and hence at the retinal plane conjugate to this plane, we also need to consider the nature of the illumination for out-of-focus planes. At the localisation plane on the

retina, the interference pattern produced by the virtual point sources  $S'_1$  and  $S'_2$  due to the actual point source  $S$  of the extended source  $\Sigma$  is only a function of the tilt  $\alpha$ . Stated alternatively, the interference at any point on the localisation plane depends only on the thickness of the air wedge at that point, as expected for Fizeau fringes (fringes of equal thickness). For out-of-focus planes this is no longer the case; the interference pattern produced by each point source  $S$  on  $\Sigma$  is now also dependant on the location of the point source so that each point source will produce a pattern which has a slight phase shift with respect to its neighbour. As a result the pattern is now dependant on the effective size of the extended source and the distance of the source from the mirrors. The aperture of any detection system (such as the eye) will also impact on the effective size of the source. Therefore in general, the modulation of the fringes will decrease with increasing defocus but the rate of change of the modulation with defocus depends on the system set up. This is the topic of a future paper and will not be discussed further here.

In the case of non-stationary targets such as in retinal imaging, we propose the simultaneous projection of fringes at three different wavelengths, as shown in Fig. 2. As each wavelength has its own mirror, the spatial frequency and phase of each fringe pattern can be adjusted separately to give sinusoidal patterns with the same spatial frequency and relative phases of  $\phi_0$ ,  $\phi_0 + 2\pi/3$  and  $\phi_0 - 2\pi/3$ . It should be noted that the angle  $\alpha$  affects the spatial frequency of the fringes at the plane of the mirrors  $M_1$  and  $M_2$ . In practical cases, there will be a magnification which is less than unity between this plane and the retinal plane. This magnification is a parameter that can be used to optimise the rate of change of spatial frequency of the illumination pattern with changing angle  $\alpha$ .

#### 4. Structured Illumination Ophthalmoscope

We can now describe an implementation of this novel methodology for obtaining structured illumination imaging applied to the field of retinal imaging. Achieving high lateral and axial resolution when imaging the living human retina is essential for early detection and diagnosis of retinal disease, when treatment is more effective and cost-efficient. Imaging devices that can resolve small retinal structures both laterally and in depth also aid clinicians who study these diseases and their treatment and management. The SLO was the first device to offer optical sectioning of the retina, and Optical Coherence Tomography (OCT) has the capability of achieving very high axial resolution. The Structured Illumination Ophthalmoscope (SIO) proposed in this Paper has a number of potential advantages over the existing systems. Unlike the SLO and OCT techniques, there is no lateral scanning as the illumination is wide-field. This makes the SIO an optically simple device that does not rely on mechanical scanning devices and the optical design trade-offs required for scanning systems. In addition to the potential for reduced design, engineering and production costs of future commercial devices, there is no distortion due to intra-frame eye movements and other potential artefacts introduced by the scanning processes in the SLO and OCT.

The use of incoherent light sources eliminates speckle effects that can introduce artefacts particularly when imaging at high resolution, and as none of the illumination light is discarded at the sample as with the confocal pinhole in the SLO, or the interference conditions required in OCT, the SIO is light efficient. In the SLO in particular, the trade-off between having a small confocal pinhole size which would give higher axial resolution, and having sufficient signal-to-noise ratio at the detector is a major drawback which the SIO does not suffer from. This latter point is especially important in retinal imaging since the incident light on the sample is limited by ocular safety considerations. The multispectral imaging characteristics of the SIO will also enable efficient imaging of more retinal layers and structures within a single image.

The image formation theory of the structured illumination microscope is well documented for grid projection and fringe projection techniques [1, 2, 3]. A similar approach will be followed

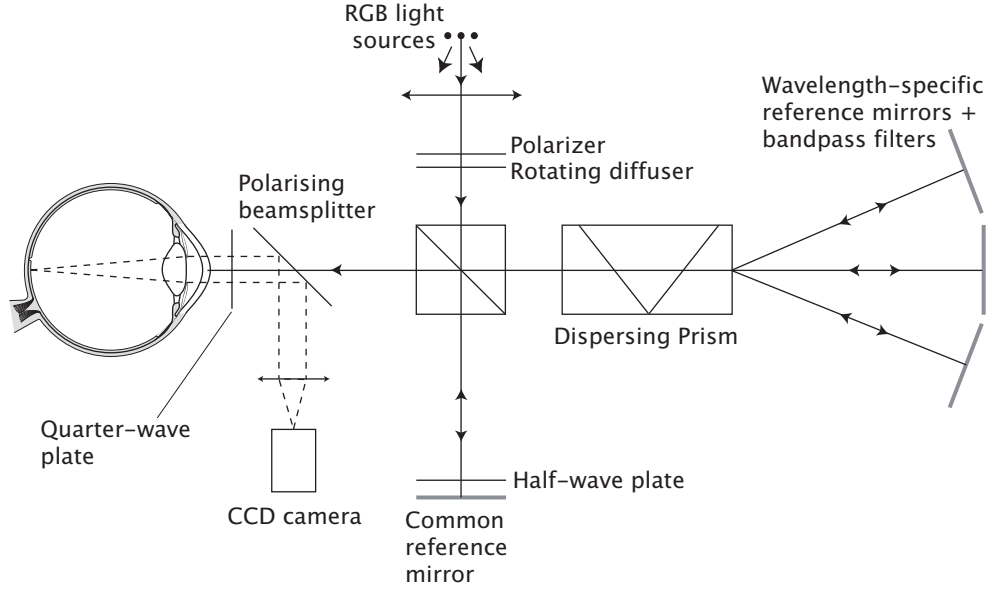


Fig. 2. Schematic representation of the proposed Structured Illumination Ophthalmoscope using the Fizeau fringe projection technique and three wavelengths for illumination. Red, green and blue incoherent light sources are used. These are matched to the detection peaks for the detectors in the colour CCD camera and, with appropriate filtering, cross-talk is minimised. A rotating diffuser is used to enhance spatial incoherence. A beamsplitter splits the light into the two branches of a Michelson interferometer, one containing a mirror common to all wavelengths, the other containing a dispersing prism and three mirrors, one for each of the illuminating wavelengths. The fringes produced are projected onto the retina by the optics of the eye. Incoming and outgoing light from the eye is split using a polarizing beamsplitter and a quarter-wave plate in front of the eye to maximise the returning light based on the eye's birefringence. A half-wave plate in the common branch of the interferometer controls fringe modulation.

to formalise the theory for the Fizeau fringe projection technique described.

If we let  $(x_o, y_o)$  represent the lateral coordinates at the object plane (i.e. retina), we can then define the normalised coordinates  $(t_o, w_o) = k(x_o, y_o)n \sin \alpha$ , where  $k = 2\pi/\lambda$  and  $n \sin \alpha$  is the numerical aperture  $NA$  [6]. (Figure 3 shows a simplified schematic showing the relevant planes.) If the amplitude reflectance of the retina is  $r(t_o, w_o)$  and it is illuminated by a structured incoherent intensity pattern given by

$$I_{illumination}(t_o, w_o) = 1 + \mu \cos(vt_o + \phi), \quad (1)$$

where  $\mu$  and  $v$  are the modulation and frequency respectively of the sinusoidal pattern, and  $\phi$  is the phase, then the object intensity becomes

$$I_{object}(t_o, w_o) = [1 + \mu \cos(vt_o + \phi)] \rho(t_o, w_o), \quad (2)$$

where  $\rho = |r|^2$  is the intensity reflectance of the retina. The intensity image of this object formed incoherently at the image plane  $(t_i, w_i)$  is therefore

$$I(t_i, w_i) = \iint [1 + \mu \cos(vt_o + \phi)] \rho(t_o, w_o) |h(t_i + t_o, w_i + w_o)|^2 dt_o dw_o, \quad (3)$$

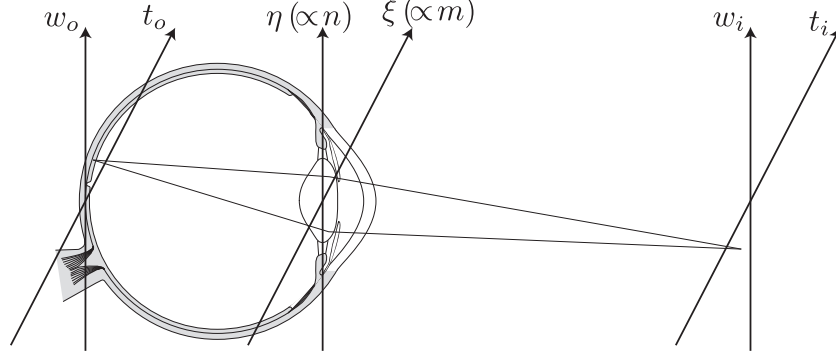


Fig. 3. Simplified geometry for the imaging system showing the object and image planes with their normalised coordinate pairs  $(t_o, w_o)$  and  $(t_i, w_i)$  respectively, and the pupil plane with coordinates  $(\xi, \eta)$  with are proportional to the spatial frequency coordinates  $(m, n)$  [6, 14]. Focussing optics is not shown.

where  $h$  is the amplitude point spread function of the objective (i.e. the optics of the eye). We assume unit magnification between object and image plane throughout these derivations, and integration is over all space. We can now expand Eq. 3 using the expansion of cosine in terms of Euler's formula, and for compactness we pre-define the following functions:

$$I_0(t_i, w_i) = \iint \rho(t_o, w_o) |h(t_i + t_o, w_i + w_o)|^2 dt_o dw_o, \quad (4)$$

$$I_V(t_i, w_i) = \iint e^{i\nu t_o} \rho(t_o, w_o) |h(t_i + t_o, w_i + w_o)|^2 dt_o dw_o, \quad (5)$$

$$I_{-V}(t_i, w_i) = \iint e^{-i\nu t_o} \rho(t_o, w_o) |h(t_i + t_o, w_i + w_o)|^2 dt_o dw_o, \quad (6)$$

which yields

$$I(t_i, w_i) = I_0(t_i, w_i) + \frac{\mu}{2} e^{i\phi} I_V(t_i, w_i) + \frac{\mu}{2} e^{-i\phi} I_{-V}(t_i, w_i). \quad (7)$$

$I_0(t_i, w_i)$  is simply the conventional incoherent image in a standard microscope with homogeneous illumination ( $\mu = 0$ ), and we also note that  $I_{-V} = I_V^*$ , where  $*$  denotes the complex conjugate. The intensity image obtained using the structured illumination therefore can be considered as having three components, one of which is equivalent to the standard microscope. The relative weighting of these three components depends on the modulation of the illuminating pattern,  $\mu$ . Before proceeding to show that  $I_V$  and  $I_{-V}$  possess axial sectioning properties, we note that in order to extract these components we require more than one intensity image so that  $I_0$  can be eliminated. Thus, three intensity images  $I_1$ ,  $I_2$  and  $I_3$  are obtained with phases  $\phi_1 = \phi_0$ ,  $\phi_2 = \phi_0 + 2\pi/3$  and  $\phi_3 = \phi_0 - 2\pi/3$  respectively. We can therefore show that the desired component can be obtained through either of the following two expressions [1, 3]:

$$|I_{\pm V}| = |I_1 + I_2 e^{\mp i2\pi/3} + I_3 e^{\pm i2\pi/3}|, \quad (8)$$

$$|I_{\pm V}| = \left( \frac{(I_1 - I_2)^2 + (I_1 - I_3)^2 + (I_2 - I_3)^2}{2} \right)^{\frac{1}{2}}. \quad (9)$$

The conventional incoherent image can also be easily recovered from the three acquired images through

$$I_0 = \frac{1}{3}(I_1 + I_2 + I_3). \quad (10)$$



We can now define the object intensity spectrum  $\mathcal{R}(m, n) = \mathcal{F}\{\rho(t_o, w_o)\}$  where  $\mathcal{F}$  represents the Fourier transform operator and  $(m, n)$  are spatial frequencies corresponding to  $(t_o, w_o)$ , we can therefore substitute for  $\rho$  in Eq. 5 to give

$$I_v(t_i, w_i) = \iiint e^{ivt_o} \mathcal{R}(m, n) e^{-i(mt_o+nw_o)} |h(t_i+t_o, w_i+w_o)|^2 dt_o dw_o dm dn. \quad (11)$$

Since  $P(m, n) = \mathcal{F}^{-1}\{h(t_o, w_o)\}$ , where  $P$  is the generalised pupil function [6, 14], then through use of the shift theorem and autocorrelation theorem for Fourier transforms [15] we have

$$e^{i(mt_i+nw_i)} P(m, n) \otimes P^*(m, n) = \mathcal{F}^{-1}\{|h(t_o+t_i, w_o+w_i)|^2\} \quad (12)$$

$$= \iint |h(t_o+t_i, w_o+w_i)|^2 e^{-i(mt_o+nw_o)} dt_o dw_o. \quad (13)$$

In anticipation of our final result we define the transfer function  $C(m, n) = P(m, n) \otimes P^*(m, n)$ , and following a further application of the shift theorem to take into account the exponential term in Eq. 11 we get

$$I_v(t_i, w_i) = e^{ivt_i} \iint \mathcal{R}(m, n) C(m+v, n) e^{i(mt_i+nw_i)} dm dn. \quad (14)$$

In order to investigate the effect of defocus on the structured illumination microscope, we need to consider the effect of defocus on the illumination pattern. This is fairly straightforward for the grid projection and fringe projection techniques. In the former, as the illumination pattern is an image of a sinusoidal grid formed on the sample, the axial behaviour of the structured pattern is determined by the three-dimensional point spread function of the collector lens which is responsible for the illumination. The modulation of the sinusoidal pattern therefore decreases with defocus. In fringe illumination the sinusoidal pattern is formed through the interference of two laser beams and is independent of axial position; the modulation therefore does not decrease with defocus. For the Fizeau fringe projection technique described in this Paper, the defocus considerations are more involved as described above. One practical scenario is the case when the extended source is small or distant so that we can assume all rays are nearly parallel to the optical axis. This is a valid assumption for an ophthalmic imaging system owing to the restrictions imposed by the pupil of the eye. In this case we can assume that the modulation  $\mu$  of the sinusoidal pattern is not a function of defocus. Equation 3 can therefore be rewritten as

$$I(t_i, w_i; u) = \iint [1 + \mu \cos(vt_o + \phi)] \rho(t_o, w_o; u) |h(t_i+t_o, w_i+w_o; u)|^2 dt_o dw_o, \quad (15)$$

where  $u$  is the normalised axial coordinate representing defocus, related to the actual axial coordinate  $z$  through  $u = 4knz \sin^2(\alpha/2)$ . Similarly, all subsequent equations derived from Eq. 3 become functions of  $u$ .

Therefore we note that the transfer function  $C(m+v, n; u)$  of the structured illumination brightfield microscope with the Fizeau (incoherent) fringe projection technique is identical to the transfer function of a structured illumination fluorescence microscope illuminated with the (coherent) fringe projection technique [3], and will therefore express the same axial sectioning characteristics which are comparable to those of the confocal microscope. Similarly, the imaging system will exhibit an increase in lateral resolution owing to the higher cut-off frequency of  $C(m+v, n; u)$  with respect to that of the standard incoherent microscope and the confocal microscope, for all non-zero values of  $v$  [3]. It should be noted that the assumption leading to constant modulation of the structured pattern with defocus represents a worst case scenario, since any attenuation would lead to better axial sectioning [3]. The choice of size and distance of the extended source in designing the system can therefore to some extent enhance

the optical sectioning properties of the imaging system. On the other hand, the use of different wavelengths to obtain the three required intensity images, while making the technique feasible for ophthalmic use, will affect the axial sectioning capabilities as the  $I_0$  term will not be fully eliminated in Eqs. 8 and 9. Future work to be published later includes detailed simulation of these processes to investigate and quantify their effects on resolution.

## 5. Conclusion

A novel implementation of structured illumination microscopy has been described and assessed theoretically in this Paper. The technique is suited for the imaging of non-stationary objects, including *in-vivo* retinal imaging. The novel aspects of the technique proposed include a new technique to deliver the sinusoidal illumination pattern required for structured illumination, namely a Fizeau (incoherent) fringe projection technique, and a multiple wavelength illumination system that enables the three images required with phase-shifted structured patterns to be acquired simultaneously, rather than sequentially, enabling imaging of moving objects. We show that for practical implementations in the ophthalmic case, the theoretical axial sectioning is identical to that obtained through fluorescence imaging through structured illumination with the coherent fringe projection system, and in the general case the geometry of the extended source in relation to the objective can be altered to improve the axial sectioning further.

In the application to retinal imaging, this technique has the potential to obtain axially sectioned images comparable to those of the SLO. It also offers a number of advantages over the SLO which include better light efficiency, improved lateral resolution, multi-spectral imaging and a marked reduction in optical and opto-mechanical complexity as no lateral scanning mechanisms are required. The latter point has implications in image quality but also in potential future development and manufacture costs, and maintenance and reliability of commercial devices. The potential for an inexpensive retinal imaging system with high quality 3D imaging capabilities is one of importance clinically in the drive to detect retinal disease early through screening.

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