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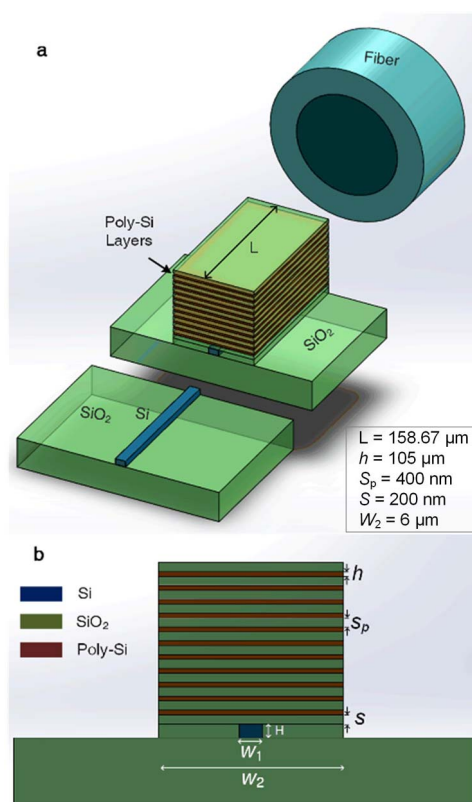
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# Multi-Poly-Silicon-Layer-Based Spot-Size Converter for Efficient Coupling Between Silicon Waveguide and Standard Single-Mode Fiber

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# Multi-Poly-Silicon-Layer-Based Spot-Size Converter for Efficient Coupling Between Silicon Waveguide and Standard Single-Mode Fiber

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**Abstract:** A novel spot-size converter (SSC) incorporating a phase-matched polycrystalline-silicon (Poly-Si) multilayer is proposed and optimized for efficient nanophotonic coupling, which can be fabricated by using the complementary metal–oxide–semiconductor (CMOS) compatible process and can be directly integrated. An efficient algorithm, combining the rigorous **H**-field-based full-vectorial finite-element method and the least square boundary residual method, is developed for the design optimization of the SSC. The use of simple single-layer and multilayer Poly-Si-based SSCs is investigated, in which the coupling process and phase matching for isolated and composite waveguides are also carried out. The coupling loss can be reduced to 2.72 dB by using an 11-Poly-Si-layer-based SSC. The on-chip integrated SSC opens up the feasibility of a low-cost passive-aligned fiber-pigtailed electronic–photonic integrated-circuit (PIC) platform.

**Index Terms:** Silicon photonics, spot-size converter, multilayer.

## 1. Introduction

Silicon photonics is showing great promise as the platform for developing large scale photonic integrated circuits (PICs) and the next-generation optical telecommunications [1], [2]. The silicon photonics, based on Silicon-On-Insulator (SOI) substrate enables high density PICs due to the high index contrast between the silicon core and the oxide cladding, which can be fabricated by using highly developed standard Complementary-Metal-Oxide-Semiconductor (CMOS) technology [3]. However, the major obstacles remaining in the wider adaptation of silicon photonics are lack of any practical silicon based lasers, highly efficient modulators, and coupling to outside systems [4]–[6]. In spite of progress in developing on-chip laser sources and modulators in silicon photonics, at present, practical approaches require coupling light into and out of silicon devices [7]–[10]. A particular challenge is the coupling of light from an SOI waveguide to a standard single mode fiber (SMF) due to the large mode-area mismatch [11]–[14].

Recently, various coupling schemes have been proposed to achieve a high coupling efficiency between the silicon waveguide and SMF. One approach could be the use of a one-dimensional or two-dimensional grating structure to couple light from an SOI waveguide into a fiber, which has the advantage of not requiring polished facets for coupling [15]–[17]. Nevertheless, a grating-based coupling is inherently limited in spectral bandwidth, which also needs a vertical/tilted fiber-alignment. Another approach could be the use of lenses, either bulk-optic lenses or a lensed fiber [18], [19], but lenses require multiple anti-reflection (AR) coatings and complicated rigid packaging. In addition, disadvantages of using lensed fiber are of critical fabrication process and small alignment tolerance. Another approach is to integrate a taper spot-size converter (SSC) into the PIC system [20]–[22]. A 3-D taper structure can adiabatically transform the mode of an SOI waveguide to the fiber mode. However, the fabrication of a vertical taper requires gray scale lithography, which is not compatible with the standard CMOS process. An inverted taper using CMOS technology can make an adiabatic taper structure, while requires a thick buried oxide layer. Furthermore, the taper based SSC often has inherent loss, which is also suffer from the tip end reflection [23], [24]. Therefore, the efficient coupling of the silicon nanophotonic waveguide into optical fiber is still a challenge.

Here, a novel concept of multi-layer based SSC is proposed, which does not incorporate a taper for the coupling between the silicon nanophotonic waveguide and optical fiber, and can be fabricated by using the standard CMOS process. In this case, the rigorous **H**-field based full-vectorial finite-element method (VFEM) is used to find the vector modes and supermodes of the coupled structure. Following that, the least squares boundary residual (LSBR) method is used to find the power transfer efficiency and coupling loss, which is a rigorous approach for nonidentical and strongly coupling waveguide structure. The single and multi-layer polycrystalline-silicon (Poly-Si) based SSCs are investigated, in which the coupling process, phase matching for the isolated, and coupled waveguides are also given. The propagation constants, height and inner separation of the Poly-Si layer, separation between upper and lower waveguides, coupling length, and power transfer efficiency of the SSCs are also investigated. Moreover, the mode field profiles of the isolated multi-Poly-Si layers and the output fields of the SSCs are given. Our numerical results show that with the eleven Poly-Si layers based SSC, the coupling loss between the silicon waveguide and SMF can be reduced to 2.7 dB, which can be easily incorporated in a photonic subsystem chip.

## 2. Theory

The **H**-field based VFEM has established as one of the most accurate and efficient techniques, since unlike the alternative **E**-field formulation, all three components of **H**-field are naturally continuous across the dielectric interfaces. This formulation has been widely used to find the mode field profiles of the waveguides and composite couplers. The full-vectorial formulation used here is based on the minimization of the following energy functional [25] in terms of the nodal values of the full **H**-field vector:

$$\omega^2 = \frac{\iint [(\nabla \times \mathbf{H})^* \cdot \epsilon^{-1}(\nabla \times \mathbf{H}) + p(\nabla \cdot \mathbf{H})^*(\nabla \cdot \mathbf{H})] dx dy}{\int \mathbf{H}^* \cdot \mu \cdot \mathbf{H} dx dy} \quad (1)$$

where **H** is the full-vectorial magnetic field; \* denotes a complex conjugate and transpose;  $\omega^2$  is the eigenvalue, where  $\omega$  is the optical angular frequency of the wave;  $p$  is a weighting factor for the penalty term and  $\epsilon$  and  $\mu$  are the permittivity and permeability, respectively; and these material parameters can be arbitrarily tensor.

The calculation of the field profiles of the isolated modes or supermodes for the couplers and their propagation constants can be carried out by various mode analysis methods. The constituent elements of the **H**-field based VFEM can be of various sizes and shapes, which can provide a powerful approach to accurately characterize waveguide of any cross-section with a complex boundary, particularly useful for the multi-layer based waveguides, as considered here. The vector mode field profiles and propagation constants for all modes in each individual waveguide

and all supermodes for a coupled structure consisting of two waveguides can be accurately obtained by using the **H**-field based VFEM, even when they are non-identical and strongly coupled.

To calculate the power transfer efficiency between two nonidentical waveguides, it is necessary to find the power transfer from the individual modes of the isolated waveguides and the supermodes of the complete coupling structures. If the two waveguides are nonidentical, most of the traditional coupled mode methods may be inadequate to calculate accurately the power transfer between two strongly coupled nonidentical waveguides due to the coefficients of two supermodes will be highly unequal when the guides are not phase matched. The LSBR method has been proven to be an accurate and efficient approach for such a structure [26], [27], which is used here to calculate the power transfer efficiency by imposing the continuity of the field at the junction interface in a least-squares sense and obtain the modal coefficients of the transmitted and reflected fully hybrid modes or supermodes at the discontinuity interface. The LSBR method looks for a stationary solution to satisfy the continuity conditions in a least squares sense both the by minimizing the error energy functional  $J$ , as given by [28]

$$J = \int |E_t^I - E_t^{II}|^2 + \alpha \cdot Z_0^2 |H_t^I - H_t^{II}|^2 d\Omega \quad (2)$$

where  $E_t^I$ ,  $H_t^I$ , and  $E_t^{II}$ ,  $H_t^{II}$  are the transverse electric and magnetic fields in Sections 1 and 2, respectively.  $Z_0$  is the free-space impedance, and  $\alpha$  is the dimensionless weighting factor to balance the electric and magnetic components of the error functional  $J$ . The integration is carried out at the junction interface,  $\Omega$ .

Since VFEM provides accurate solutions for the supermodes of the coupled structures, the power transfer efficiency can be calculated by using the LSBR method. This approach is better than the use of traditional overlap integral methods as many modes are needed to satisfy the field continuity at the discontinuity junction plane. Such an approach will be as accurate as a full-vectorial 3-D beam propagation method (BPM) approach, but computationally more efficient than the BPM. It has also been shown that the LSBR approach is more rigorous and can be used to find both the transmission and reflection coefficients at the butt-coupled junctions.

In this paper, both for the VFEM and LSBR approaches based in-house codes are used, in which the power transfer between two coupled waveguides can be accurately calculated by using the accurate eigenvalues and eigenvectors, calculated by the VFEM, along with the LSBR method. In the design process, the VFEM is used to find the vector modes and supermodes of the coupled structures and the LSBR is used to find the supermode coefficients. The combination of the LSBR and the FEM is used to find the transmission and reflection coefficients from a discontinuity junction between two nonidentical waveguides.

### 3. Results and Discussion

The schematic of the proposed SSC is shown in Fig. 1, in which the optical signal can be easily transferred from the silicon nanophotonic waveguide to the fiber with low coupling loss. The schematic diagram of the coupling process for the silicon nanowire (NW) and the single mode fiber with the multi-layer based SSC is shown in Fig. 1(a). The cross-section of the SSC section is shown in Fig. 1(b). It consists of two phase matched waveguides with different spot-sizes, in which the primary waveguide  $a$  is a typical silicon NW with a small spot-size, shown here as the lower waveguide. The second waveguide  $b$  consists of multi-Poly-Si layers to expand the spot-size, shown here as the upper waveguide. In the present design approach, the height and inner separation of the multi-Poly-Si layers are adjusted to achieve the phase matching with the lower waveguide. The fabrication process for the proposed SSC studied here can be as follows: i) The silicon NW can be obtained by using traditional plasma enhanced chemical vapor deposition (PECVD) and the reactive ion etching (RIE); ii) then, the multiple layers can be deposited by using the PECVD and be etched the whole stack together, which only needs one additional mask for the multi-layer.

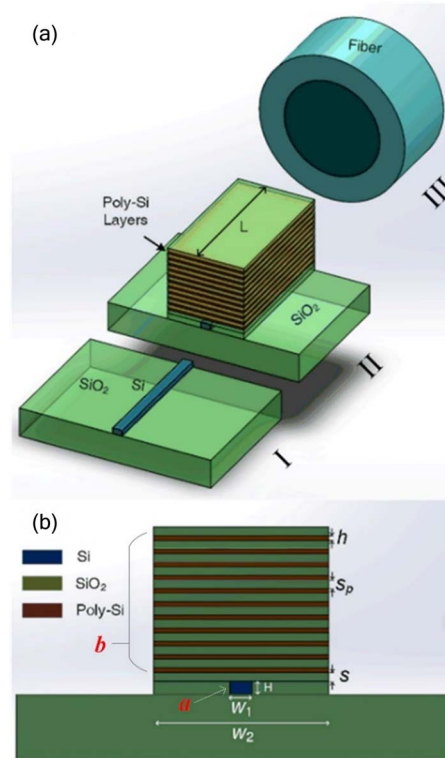


Fig. 1. Schematic of a multilayer-based SSC. (a) Schematic diagram for the coupling process. (b) Cross section of the SSC.

The width, height, and inner separation of the multi-Poly-Si layers are taken as  $W_2$ ,  $h$  and  $S_p$ , respectively, in which the coupling loss can be adjusted by using different layer numbers. The length of SSC section and separation between multi-layer and the silicon NW with the size of  $W_1 \times H$  are  $L$  and  $S$  shown in Fig. 1(a) and (b), respectively. The silicon NW with the size of  $W_1 \times H = 400 \text{ nm} \times 220 \text{ nm}$  is taken here as an example, which may be considered as a typical representative of the silicon NWs. The refractive indices of the Si, Poly-Si and  $\text{SiO}_2$  are taken as 3.47548, 3.48, and 1.46, respectively, at the operating wavelength of 1550 nm. In this study, the width ( $W_2$ ) of the Poly-layer is taken as  $6 \mu\text{m}$  for studying the coupling with a SMF with its radius, core and cladding refractive indices as  $4.225 \mu\text{m}$ , 1.4552 and 1.45, respectively. In order to explain the mechanism, the multi-layer based SSCs with one, two and eleven layers are sequentially simulated by using the rigorous **H**-field based VFEM and the LSBR method. In each case, the height ( $h$ ) and separation ( $S$ ) need to be adjusted to achieve the phase matching between the upper and lower waveguides.

At first, the analysis for a single Poly-Si layer based SSC is considered. Effective index ( $n_{\text{eff}}$ ) for the fundamental quasi-TE  $H_y^{11}$  mode of the NW is accurately calculated as being  $n_{\text{eff}} = 2.23248$  and shown by a horizontal dashed red line in Fig. 2. A single layer of wider Poly-Si can be phase matched to silicon NW by varying its height  $h$ . Here, its width is taken as  $6 \mu\text{m}$  to expand its spot-size horizontally. Variation of  $n_{\text{eff}}$  with the height of the Poly-Si layer  $h$  for the  $H_y^{11}$  mode is shown in Fig. 2 by a solid blue line. It can be noted that as the height  $h$  of the Poly-Si layer is increased, the  $n_{\text{eff}}$  of the  $H_y^{11}$  mode is increased and at the crossing point, when  $h = 107 \text{ nm}$ , has the same effective index as that of the silicon NW. Although the phase matching condition is shown, when these two guides are isolated, however, the phase matching condition for coupled guides also needs to be studied. To identify phase matching between two nonidentical waveguides, it is essential to solve for the supermodes as the phase matching



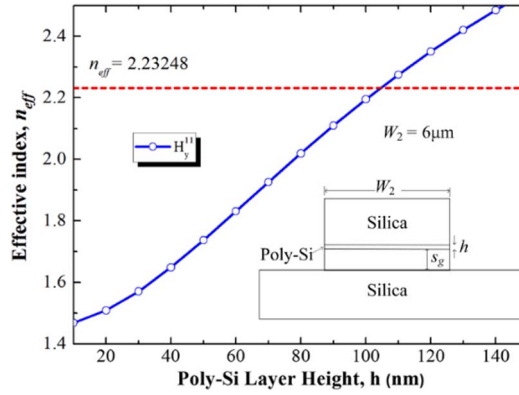


Fig. 2. Variations of  $n_{\text{eff}}$  with the height of the Poly-Si layer  $h$  for the  $H_y^{11}$  mode. The horizontal line represents the  $n_{\text{eff-TE}}$  of the silicon NW without the upper layer.

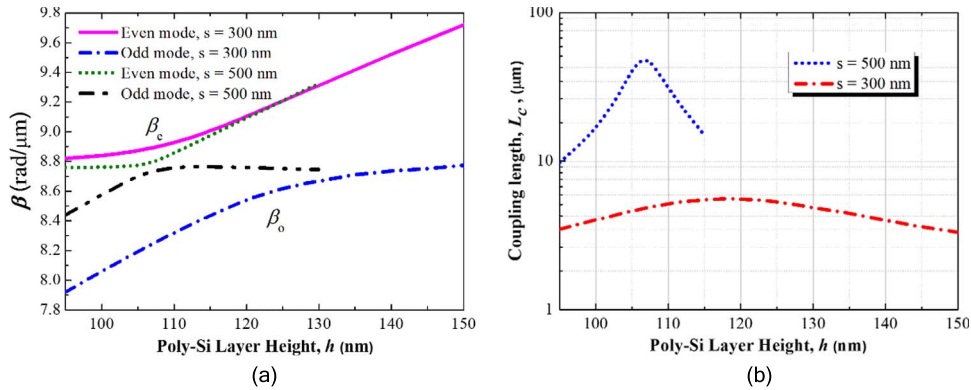


Fig. 3. Coupling characteristics of a one-layer-based SSC. (a) Even and odd supermode  $\beta$  variations with Poly-Si height  $h$  for  $S = 300$  and  $500$  nm, respectively. (b) Semi-log plot of the variation of coupling length  $L_c$  with  $h$  for  $S = 300$  and  $500$  nm, respectively.

conditions may differ considerably from the solutions of two isolated waveguides, due to the unequal loading of each waveguide by the other.

To achieve phase matching for the nonidentical structure, variations of the propagation constants ( $\beta$ ) should be calculated with the separation ( $S$ ) and height ( $h$ ) to identify the necessary height for a given separation. The VFEM is used to find the supermodes of the coupled structures consisting two nonidentical waveguides. Variations of the propagation constants for even and odd supermodes with the height of the Poly-Si layer for two different separations,  $S$  are shown in Fig. 3(a). When the separation is large, for  $S = 500$  nm, the first supermode, which is even or even-like, is shown by a green dotted line. Its second supermode, which is odd or odd-like is shown by a red dash-dotted line. When the Poly-Si layer height  $h \sim 107$  nm, these two propagation constants become closer. The horizontal line sections of these two curves represent the propagation constants of the  $H_y^{11}$  mode in the lower silicon NW (almost constant), while the slanted line sections of these two curves represent the propagation constants of the  $H_y^{11}$  mode in the upper Poly-Si layer which is increasing as the  $h$  is increased. However, these two curves do not cross each other and both supermodes go through a transformation around this anti-crossing region. Near the phase matching condition, two propagation constants are close to each other and the phase difference between these modes will be smallest. In this situation, two modes become degenerate, get mixed up and formed two supermodes. Especially, curves for  $S = 500$  nm are closer than those for  $S = 300$  nm, which could indicate the curves



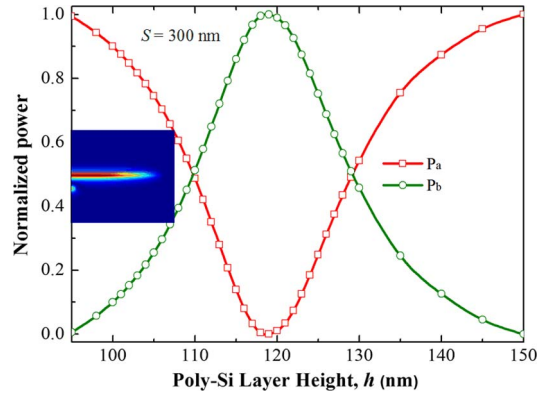


Fig. 4. Variation of the normalized power transfer efficiency with  $h$  for  $S = 300$  nm. (Inset) Output field at  $z = L_c$ .

of propagation constants become closer for larger separation between upper and lower waveguides due to weaker interactions. It can be noted, for  $S = 300$  nm, the difference between two curves of propagation constants become larger due to the strong coupling. In this case, the phase matching  $h$  moves from  $h = 107$  nm for isolated or weakly coupled guides to  $h = 120$  nm, which is due to the strong coupling.

The coupling length can be defined as  $L_c = \pi/(\beta_{\text{even}} - \beta_{\text{odd}})$  [29] where  $\beta_{\text{even}}$  and  $\beta_{\text{odd}}$  are the propagation constants of the even and odd supermodes, respectively. Variations of coupling length with the height ( $h$ ) of the Poly-Si layer are shown in Fig. 3(b) for  $S = 300$  and 500 nm, respectively. It can be observed that, when phase matching was achieved, the difference between the propagation constants of the two supermodes was smallest and the coupling length shows a peak value. As separation ( $S$ ) increases, the peak value of the  $L_c$  gets larger due to weaker coupling near the phase matching region. Especially, for a smaller separation, it not only yields a smaller coupling length, but also less sensitive to the variation of the height of the Poly-Si layer, which makes it less sensitive to the fabrication tolerances. For the separation  $S = 300$  nm at the phase matching condition, the coupling length and the SSC length should be  $5.5 \mu\text{m}$ .

As shown in Fig. 1, an input NW in the Section 1 is butt-coupled to the start of the Section 2 containing the SSC section, identified as  $z = 0$ . Transfer of butt-coupled power at this junction to the lower NW of a coupled SSC section is calculated by using the LSBR method from the excited supermodes' coefficients in the directional coupler section. After propagating along the Section 2, the optical power can be evanescently coupled from the lower silicon NW to the upper Poly-Si array at  $z = L_c$ . The transfer of optical power from the lower primary silicon NW,  $a$ , to the upper secondary Poly-Si layer,  $b$ , by evanescent coupling at exactly  $z = L_c$  may be calculated from the modal coefficients of two supermodes and their field profiles. For the nonidentical waveguides, most of the traditional coupled mode methods may be inadequate to calculate accurately the power transfer between two strongly coupled nonidentical waveguides due to the coefficients of two supermodes will be highly unequal when the guides are not phase matched. The LSBR method has been proved to be an accurate and efficient approach for these type of structures, which is used here to calculate the power transfer efficiency by imposing the continuity of the tangential  $\mathbf{E}$  and  $\mathbf{H}$  fields at the junction.

The variations of the normalized power transfer efficiency with  $h$  for  $S = 300$  nm are shown in Fig. 4, in which  $P_a$  and  $P_b$  are the power remaining in the silicon NW and the power coupled to the Poly-Si layer at  $z = L_c$ , respectively. It can be observed that the maximum power transfer could be achieved when the height ( $h$ ) of the Poly-Si layer is 118 nm, and the waveguides are phase matched and in this case the power transfer efficiency is 93.2%. It can also be noted that the output power remains within 1 dB of its maximum value when the height,  $h$  remains between 114 to 124 nm. The field profile at the end of the SSC section ( $z = L_c$ ) is shown as an inset in Fig. 4, which indicates that the field profile has been expanded horizontally by using the SSC. In

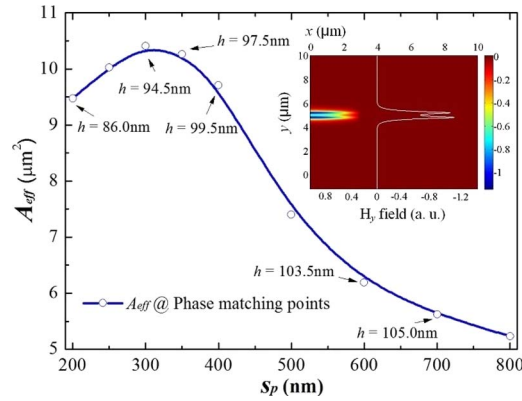


Fig. 5. Variations of effective area  $A_{\text{eff}}$  with the separation between the Poly-Si layers  $S_p$  at phase-matching points for two Poly-Si layers without the lower silicon NW. (Inset) Modal field profile of the isolated Poly-Si layers for maximum  $A_{\text{eff}}$ .

this case, the effective area ( $A_{\text{eff}}$ ) [30] of the upper waveguide core is  $5.168 \mu\text{m}^2$ , which is more than 12.8 times larger than that of the lower silicon NW. Subsequently, the LSBR method is used again to calculate the coupling efficiency between the SSC and a standard SMF. Since the spot-size has been expanded at the end of the SSC, the coupling efficiency at this junction increased to 21.6% when a single layer wider SSC is considered, compared to only 3.9% for the direct coupling. The total coupling loss is 6.961 dB considering the coupling efficiency of two separate values (93.2% and 21.6%). Meanwhile, power reflection for the single layer based SSC-SMF is reduced to 9.4% compared to the original 30% for the direct butt-coupling of NW to a standard SMF.

Following this, design of a two-layer based SSC is considered to reduce the coupling loss further. For two-layer based SSC, the effective area of the two isolated layers also needs to be studied to identify the optimum inner separation. The effective areas are calculated at the phase matching points for different inner separations. Variation of the effective area,  $A_{\text{eff}}$ , with the inner separation,  $S_p$ , of two Poly-Si layers is shown in Fig. 5. It can be noted that, for  $S_p = 300$  nm and  $h = 94.5$  nm, the maximum  $A_{\text{eff}}$  of  $10.4 \mu\text{m}^2$  for the isolated 2-layers can be achieved, and in this case the field profile of the isolated 2-layers Poly-Si is shown as the inset in Fig. 5, providing the maximum spot-size for coupling with the fiber.

Although the poly-Si layer thickness necessary for phase matching of isolated waveguides have been determined, but as the thickness necessary would change slightly when these isolated waveguides form a strongly coupled directional coupler with the NW. Next, for the combined coupled structure with fixed  $S_p = 300$  nm, the variations of the propagation constants for even and odd supermodes with the height of the Poly-Si layer are shown in Fig. 6(a). Variations of the propagation constants for even and odd supermodes are calculated with the separation ( $S$ ) of 500 and 800 nm, respectively. Variations of coupling length with the height ( $h$ ) of the Poly-Si layer are shown in Fig. 6(b) for  $S = 500$  and 800 nm, respectively. It can be observed that, when the separation  $S = 500$  and 800 nm, the necessary phase matching can be achieved with the height,  $h = 96.0$  and 95.4 nm, respectively, and these values are different from the height  $h = 94.5$  nm required for two isolated waveguides for phase matching. For the separation  $S = 500$  nm, at phase matching the coupling length and the SSC length needs to be  $61 \mu\text{m}$ .

Next, transfer of optical power from the input NW to the lower silicon NW in the SSC section at  $z = 0$  and from the lower silicon NW to the upper two Poly-Si layers at  $z = L_c$  are calculated by using the LSBR method. The modal coefficients can be calculated by using the LSBR method and from these modal coefficients and modal field profiles of the supermodes, obtained by the FEM, the power transfer efficiency could be calculated. The variations of the normalized power transfer efficiency with  $h$  for  $S = 500$  nm are shown in Fig. 7, in which  $P_a$  and  $P_b$  are the

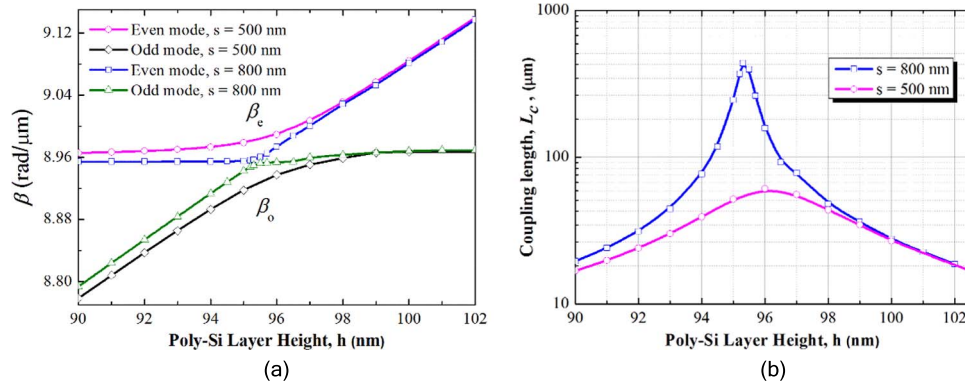


Fig. 6. Coupling characteristics of a two-layer-based SSC. (a) Even- and odd-like supermode  $\beta$  variations with Poly-Si height  $h$  for  $S = 500$  and  $800$  nm, respectively. (b) Semi-log plot of the variation of coupling length  $L_c$  with  $h$  for  $S = 500$  and  $800$  nm, respectively.

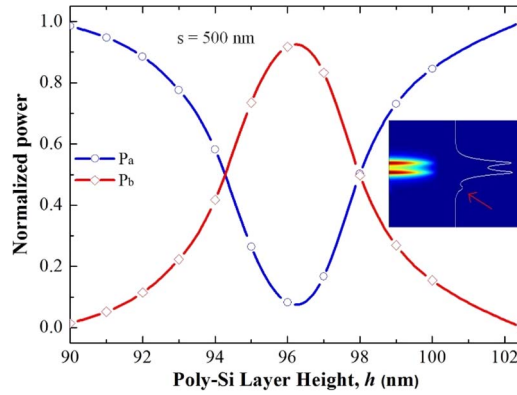


Fig. 7. Variation of the normalized power transfer efficiency with  $h$  for  $S = 500$  nm. (Inset) Output modal field at  $z = L_c$ .

power remaining in the silicon NW and the power coupled to the two Poly-Si layers at  $z = L_c$ , respectively. It can be observed that the maximum power transfer could be achieved when the height ( $h$ ) of the Poly-Si layer is 96 nm, in which the power transfer efficiency is 91.8%. It can be also noted that the output power remains within 1 dB of its maximum value when the height,  $h$  remains between 95.2 to 97.2 nm. The field profile at the end of the SSC section ( $z = L_c$ ) is shown as an inset in Fig. 7, which demonstrate that the field profile has been expanded by using the SSC. A small kink below the two-layer, shown by a red arrow, indicates a small amount of field remained in the lower NW. In this case, the  $A_{\text{eff}}$  of the upper waveguide core is  $10.41 \mu\text{m}^2$ , which is more than 26 times larger than that of the lower silicon NW. The LSBR method is used again to calculate the coupling efficiency between the SSC and a standard SMF. Since the spot-size has been expanded at the end of the SSC, the coupling efficiency at this junction increased from 3.9% for the direct coupling to 27.0% when a two-layer based SSC is considered. The total coupling loss is 6.06 dB considering the coupling efficiency at two separate junctions (91.8% and 27.0%) and reflected power at the end of the two-layer based SSC-SMF interface is 8.9%.

To increase the spot-size further in the vertical direction, design of an eleven-layer based SSC is considered. To achieve phase matching for 11 isolated waveguides, it is necessary to calculate the variations of the effective indices of the upper waveguide  $n_{\text{eff}}$  with the height

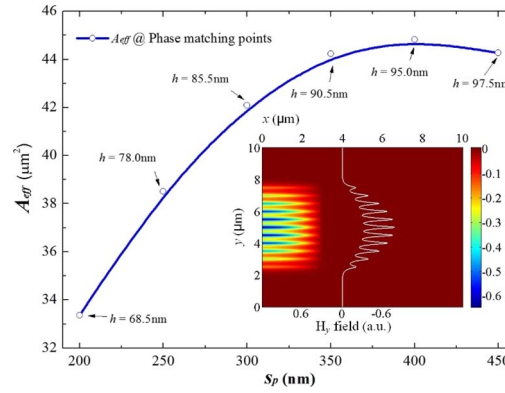


Fig. 8. Variations of effective area  $A_{\text{eff}}$  with the separation between the Poly-Si layers  $S_p$  for the even modes at phase-matching points for 11 Poly-Si layers. (Inset) Modal field profile of the isolated layers for maximum  $A_{\text{eff}}$ .

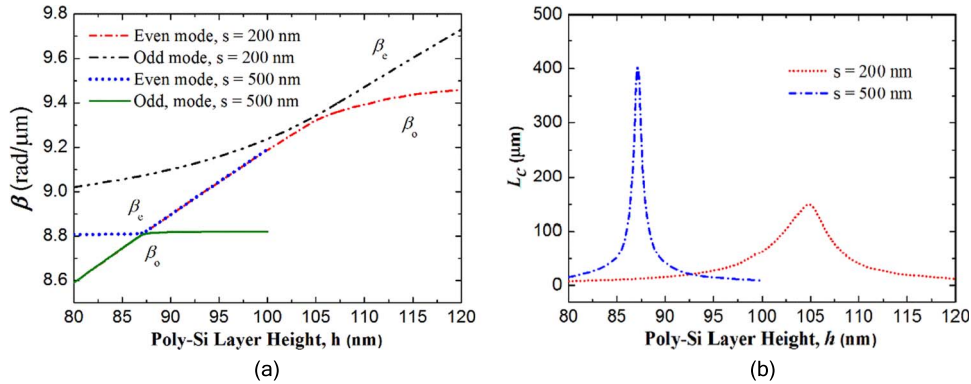


Fig. 9. Coupling characteristics of an 11-layer-based SSC. (a) Even- and odd-like supermode  $\beta$  variations with Poly-Si height  $h$  for  $S = 200$  and  $500$  nm, respectively. (b) Variation of coupling length  $L_c$  with  $h$  for  $S = 200$  and  $500$  nm, respectively.

( $h$ ) and inner separation ( $S_p$ ) to identify the necessary inner separation. Variations of the effective area  $A_{\text{eff}}$  with inner separation  $S_p$  of 11 Poly-Si layers are shown in Fig. 8. The effective areas are calculated at phase matching points for different inner separations. It can be noted that for  $S_p = 400$  nm and  $h = 95.0$  nm, the maximum  $A_{\text{eff}}$  of  $44.8 \mu\text{m}^2$  for the isolated 11 layers can be achieved, and in that case, the field profile of the isolated Poly-Si 11-layers is shown as the inset in Fig. 8, providing the maximum spot-size for coupling with the fiber.

Next, for the combined coupled structure fixed  $S_p = 400$  nm, the variations of the propagation constants for even and odd supermodes with the height of the Poly-Si layer are shown in Fig. 9(a). The propagation constants for even and odd supermodes are calculated with the separation ( $S$ ) of 200 and 500 nm, respectively. Then, the variations of coupling length with the height ( $h$ ) of the Poly-Si layer are shown in Fig. 9(b) for  $S = 200$  and 500 nm, respectively. It can be observed that, when the separation  $S = 200$  and 500 nm, the necessary phase matching can be achieved with the height  $h = 105$  and 87.2 nm, respectively. When a coupled structure is composed of eleven identical waveguides, they are always phase matched when the separation between them changes. However, for nonidentical waveguides, the phase matching also depends on mutual loading of the waveguides, in which their phase matching condition can be altered significantly due to unequal loading of each other. Therefore, the phase matching condition for height value changes with  $S$  shown here, which is also different from the height for phase matching of the 11 isolated

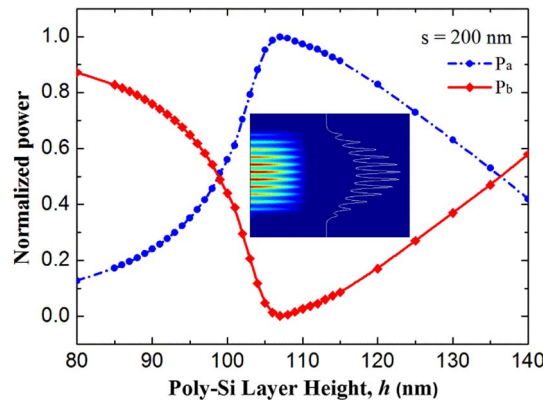


Fig. 10. Variations of the normalized power transfer efficiency with  $h$  for  $s = 200$  nm. (Inset) Output modal field at  $z = L_c$ .

waveguides. For the separation  $S = 200$  nm, at phase matching the coupling length and the SSC length needs to be  $158.67 \mu\text{m}$ .

Next, transfer of optical power from the input NW to the lower silicon NW of the SSC at  $z = 0$  and from the lower silicon NW to the upper 11 Poly-Si layers at exactly  $z = L_c$  are calculated by using the LSBR method. The modal coefficients can be obtained from these modal coefficients and modal field profiles of the supermodes by using the LSBR method. Following that, the power transfer efficiency can be calculated with these modal coefficients and modal field profiles of the supermodes. As shown in Fig. 10, the variations of the normalized power transfer efficiency are with  $h$  for  $S = 200$  nm, in which  $P_a$  and  $P_b$  are the powers remaining in the silicon NW and coupled to the 11 Poly-Si layers at  $z = L_c$ , respectively. The maximum 95.2% power transfer could be achieved when the height ( $h$ ) of the Poly-Si layer is 105 nm. It can be noted that the output power remains within 1 dB of its maximum value when the height,  $h$  remains between 103 to 121.5 nm. The field profile at the end of the SSC section ( $z = L_c$ ) is shown as an inset in Fig. 10, which can indicate that the field profile has been expanded significantly by using the SSC. In this case, the  $A_{\text{eff}}$  of the upper waveguide core is  $44.5 \mu\text{m}^2$ , which is more than two orders larger than that of the lower silicon NW. The LSBR method is used again to calculate the coupling efficiency between the SSC and the SMF. Since the spot-size has been expanded at the end of the SSC, the coupling efficiency at this junction will increase from 3.9% for the direct coupling to 56.1% when an eleven-layer wider SSC is considered. The total coupling loss is only 2.72 dB considered the coupling efficiency of two separate values (95.2% and 56.1%) at two junctions and the 11 layer based SSC-SMF power reflection is 6.8%. However, instead of a standard SMF, if a smaller lensed fiber can be introduced to couple with the multi-layer based SSC, a higher coupling efficiency can be achieved. For the same normalized frequency,  $V$ , as for a standard SMF, the radius of a lensed fiber is taken as  $2 \mu\text{m}$  as an example and the core and cladding refractive indices are taken as 1.4731 and 1.45, respectively. The coupling efficiency between the 11 layer based SSC and the lensed fiber can be dramatically improved to 97.1%, and the total coupling loss is reduced to only 0.34 dB. The reflected power at the end of the 11-layer based SSC-SMF interface is reduced to only 1.8%.

To give the coupling performance for different Poly-Si layers, the SSC with one, two, five and eleven Poly-Si layers are calculated, which are summarized in Table 1. It can be noted that the coupling efficiency of the Junction 1 is the power transfer from the silicon NW to the multi-Poly-Si layers, while the Junction 2 is the coupling between the SSC and the standard SMF. The total coupling loss is the sum of the coupling losses of the Junctions I and II. It can be observed from Table 1 that the effective area is increased with the increase of the layer number, and therefore, larger spot-size could be achieved with more layers. Therefore, the total coupling loss can be significantly reduced from 14.05 dB to 2.72 dB by using an 11 layer based SSC. It can also be



TABLE 1

Coupling performance for different Poly-Si layers

N	S (nm)	h (nm)	$A_{eff}(\mu\text{m}^2)$	Coupling Efficiency		Total Coupling Loss (dB)	Reflectance
				Junction 1	Junction 2		
0	---	---	0.4	---	3.9%	14.05	30.0%
1	300	107	5.2	93.2%	21.6%	6.96	9.4%
2	500	94.5	10.4	91.8%	27.0%	6.06	8.9%
5	300	95.5	21.0	97.5%	40.6%	4.03	8.0%
11	200	105	44.8	95.2%	56.1%	2.72	6.8%
11*	200	105	44.8	95.2%	97.1%	0.34	1.8%

\* Coupling between an eleven-layer based SSC and a lensed fiber of radius 2  $\mu\text{m}$ .

observed that the 11 layer based SSC-SMF power reflection is reduced to 6.8% compared to the original 30% for the direct silicon NW and SMF coupling. It should be noted that, when a silicon NW is directly butt-coupled to a standard SMF, the reflection is due to both mode-size mismatch and impedance mismatch. On the other hand, when this multi-layer based SSC is butt-coupled to the standard SMF, the mode size mismatch is reduced but remaining impedance mismatch is responsible for the reflection, although much smaller. The SSC facet could be anti-reflection coated for a further reduction in the overall power reflection.

Recently, the use of an inverted taper obtained by the reduction of the width of the silicon nanowire with a fiber-adapted polymer waveguide, yield a coupling loss of  $\sim 0.66$  dB and  $\sim 0.36$  dB between the inverted taper and the tapered fiber with  $2.9\text{-}\mu\text{m}$  mode-size diameter for the TE and TM polarizations, respectively [31]. However, such structure requires a taper tip width smaller than 15 nm for a smaller than 250-nm-thick silicon layer, which is not trivial to fabricate by using the standard CMOS process.

#### 4. Conclusion

In conclusion, we have proposed a novel concept and designed and optimized the nanophotonic coupling using a multi-layer based SSC, which is composed of non-tapered structure. This compact structure can be fabricated by using the CMOS process and be directly integrated. An efficient algorithm, combining the VFEM and the LSBR, has been developed to find the mode profiles and power transfer efficiency for the SSC. Here, the single and multi-Poly-Si layers based SSCs are investigated, in which the coupling process, phase matching for isolated and combined waveguides are given. With an 11 Poly-Si layers based SSC, the coupling loss between the silicon NW and the SMF can be reduced to 2.72 dB. On the other hand, instead of a standard SMF, a lensed fiber of radius 2  $\mu\text{m}$  is used, the coupling loss is considerably reduced to 0.34 dB. However, if desired, the coupling loss can be further reduced by using more layers and using the Poly-Si layer of larger width, which can be incorporated in the PIC system on chip.

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