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# Essays on Information and Corporate Finance



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## Abstract

This dissertation includes three essays on information and corporate finance.

In Chapter 1 (joint with Weihan Ding), we study the optimal disclosure policy in security issuance using a Bayesian persuasion approach. An issuer designs a signal to persuade an investment bank to underwrite. The bank forms a posterior on the basis of the signal and makes its underwriting and retention decisions. When there is no demand uncertainty, a partially informative disclosure is enough to curb primary market underpricing due to informed sales by the underwriter in the secondary market. When demand is uncertain, the underwriter may shy away because of more retention than his privately optimal level and larger losses due to increased total cost of capital. The optimal disclosure can solve such hold-up problem resulting from weak demand and induce the bank to underwrite. We derive predictions on the effects of the issuer's fundamentals, the underwriter's cost of capital, the demand uncertainty, and the market liquidity on the informativeness of the optimal disclosure. Our model not only captures the adverse selection problem in the originate-to-distribute lending model, but also rationalizes the phenomenon that arrangers may be willing to provide underwriting guarantee and retain large and costly stakes in leveraged loan syndication. Finally, if viewed as an extant blockholder, we show that the underwriter may exert governance by exit to promote more transparent disclosure by the issuing firm.

Chapter 2 (joint with Siyang Tian) analyzes the spillover effects of hostile takeovers on target firms' product-market peers. We use a target's hostile takeover announcement as a source of exogenous variation in its peers' control threats. We identify treatment sample as rivals to the target in the same product market but different sectors. Our control group consists of firms that are in the same sector as each peer yet do not have similar products to the target. We find that the treated firms, especially those that are peers of the targets which are not acquired, provide more transparent balance sheets, their idiosyncratic risk decreases, and analyst coverage grows after experiencing more takeover pressure. The reduction in idiosyncratic volatility implies a decline in sophisticated investors' private information gathering. Indeed, reduced information asymmetries in firms' balance sheets discourage these investors from further pursuing private information to discover under-valued firms by analyzing the balance sheets which reflect firms' long-term prospects. Moreover, the more refined balance sheet reporting does not lead to improvement in the frequency and accuracy of analyst forecasts as well as market liquidity which are sensitive to information from income statements, the part not affected by the externality of hostile takeovers. Nevertheless, the improved information environment is welcomed by a significant increase in merger proposals, which is attributable to peers in more competitive sectors. Our casual evidence suggests that the spillover effects of hostile takeover are most salient on firms' information environments: compared with changes of financial policies, the exposed firms use a less costly way, which is to expand information in their balance sheets, to signal their commitment to efficient management and reduce valuation uncertainty in future takeover activities.

In Chapter 3, we present evidence of tunneling by large shareholders via the abuse of private placement (PP) of public equity. Using data from China stock markets where PP is the most prevailing way of refinancing, we show that controlling shareholders strategically benchmark the issue prices against prices in periods of underperformance to expropriate minority shareholders through deep discounts. Pre-announcements of a PP, before the issue day when the impact of price discount materializes, are associated with positive cumulative abnormal returns. While the discount incentivizes participants and improves firm value by 3.38%, it leads to a direct tunneling of 5.6%of a firm's value, resulting in a 2.22% value destruction. A controlling shareholder is more likely to tunnel a well performing firm, but he refrains from tunneling if a firm's performance is rather poor. Using the interaction between past performance and a dummy for large shareholder's participation as a plausible instrumental variable for the discount, we find that each percent of price discount causes a 0.67%loss of an issuing firm's market value.

# Chapter 1

# Strategic Disclosure, Primary Market Uncertainty, and Informed Trading

"In today's aggressive marketplace, listed companies can no longer rely on their numbers to do the talking. If companies can't communicate their achievements and strategy, mounting research evidence suggests, they will be overlooked, their cost of capital will increase and stock price will suffer."

-Westbrook (2014)

## 1.1 Introduction

The design and transmission of information plays a vital role in security offering in that it shapes issuers', intermediaries' and investors' expectations of the future, and thus profoundly influences the resulting supply-demand equilibrium. One overarching friction which plagues the well-being of the market participants is information asymmetry: usually one party holds a payoff-relevant informational advantage over another. Issuers have considerable discretion in the disclosure of information to advance their own interests. Intermediaries, by underwriting and investing in the deals, acquire proprietary information which helps them predict future performance but cannot be credibly communicated to other investors. Moreover, they may gain from trading on their private information. Accordingly, understanding such friction and evaluating feasible options for alleviating it is of great importance.

The goal of this paper is to provide a comprehensive theoretical framework to address the following questions. First, how does information disclosure by the issuer potentially affect a financial intermediary's decision to retain and trade the issued securities? Second, can strategic information disclosure help the issuer maximize proceeds from security offering, mitigate adverse selection, and induce the investment bank to underwrite even if some unfavorable market friction (e.g. weak demand) may initially deter the bank from doing so? Third, what are the effects of the issuer's fundamentals, the underwriter's cost of capital, the primary market condition, and the secondary market liquidity on the informativeness of the optimal disclosure policy?

In this paper, we develop a tractable yet comprehensive model that links the issuer's information disclosure in the capital raising process to various primary and secondary market activities by the underwriter and other investors. We model the optimal design of disclosure policy by the issuer as a Bayesian persuasion game à la Kamenica and Gentzkow (2011). In their seminal paper, Kamenica and Gentzkow (2011) present a model where a sender chooses a signal to reveal to a receiver, who then takes an action that affects the welfare of both players. They solve for the sender-optimal signal by reframing the problem as maximizing the sender's payoff over distributions of posterior beliefs subject to the Bayesian plausibility condition that the average posteriors should be consistent with the prior. The effectiveness of Bayesian persuasion is that it improves the sender's expected payoff by inducing the receiver to choose a better action. The maximal

value is obtained by finding the concave closure of the sender's payoff function for any posterior held by the receiver.

In general, the Bayesian persuasion approach fits the process of security issuance very well. The issuing party (sender) has to first draft a proposal which will be sent to a potential underwriting bank (receiver). Routinely, the issuer possesses marked flexibility in selecting what to disclose and how precise the disclosure is. In effect, issuers usually exercise discretion in reporting forwardlooking information which contributes to the valuation of the proposed security. Such information includes but is not limited to forecasts of future sales, earnings, and growth opportunities, which can be either purely qualitative, or quantitative with varying precision -a range or a point estimate. Moreover, issuers often choose to release unique marketing information about business models, corporate strategy, and prospects of the industry to attract potential investors. In sum, the proposal-drafting stage resembles the sender's communication about the optimally designed signal system to the receiver. After seeing the proposal, the investment bank further investigates the realization of the signal through due diligence if it still cannot decide whether it should underwrite. If the bank agrees to underwrite, it engages in information production with the issuer to prepare the information memorandum (for debt) or prospectus (for equity), which is then circulated to potential investors (other receivers). In this sense, the information memorandum or prospectus reflects the informativeness of the issuer's disclosure. The underwriter then prices the security based on the collected information. This stage corresponds to the mapping from the signal realization to the pricing of the security.

Specifically, we consider an issuer who designs an information disclosure system and reveals it to an investment bank to invite it to underwrite the deal. The issuer may represent a borrower in a debt issue, an originator in securiti-

zation, or an entrepreneur in an equity issue. The investment bank may serve as a lead bank in loan syndication, an arranger in the sale of asset-backed security (ABS), or an underwriter in equity and bond offering.<sup>1</sup> If the investment bank decides to underwrite, it further helps communicate the signal to potential investors, chooses its stake, and allocates the remaining securities to the participant investors. We assume that the underwriter obtains proprietary information from its underwriting activity and retention. Similar assumptions regarding the generation of private information are commonly used in the literature on banking and blockholders (e.g. Edmans and Manso, 2011; Parlour and Plantin, 2008), and well documented empirically (e.g. Edmans, Fang, and Zur, 2013; Lummer and McConnell, 1989). Nevertheless, the acquisition of material information in our model is an inevitable but adverse consequence of the underwriter's involvement in the issuance. As a result, the underwriting bank can profit from insider trading when the secondary market opens. Following Maug (1998), Hennessy and Zechner (2011), and Chemla and Hennessy (2014), who model the secondary markets of equity, bond, and ABS respectively, the market structure is in the spirit of Kyle (1985) where investors submit their market orders to a continuum of deeppocketed risk-neutral market makers who price the security competitively after observing aggregate demand. If the participant investors anticipate that there is adverse selection in the secondary market, they will demand a discount in the issue price to offset their future losses, a fact widely used in the literature (e.g. Edmans and Manso, 2011; Holmström and Tirole, 1993; Maug, 1998).

In our baseline model, we consider a secondary market where the underwriter is banned from selling the security short (or alternatively, short sale is prohibitively costly for him). In reality, it is almost impossible to sell certain assets

<sup>&</sup>lt;sup>1</sup>The investment bank can also be viewed as an extant blockholder in the firm who makes decision on whether to support and participate in a seasoned security offering. See more discussion on the corporate governance implication of the blockholder on Page 14.

such as loans short. Furthermore, short sale of securities by underwriters has long been contended as highly controversial and is viewed unfavorably by regulators as well as market participants. Moreover, the SEC has made an effort to restrict short sale of the ABS by securitization participants. For instance, in a proposed rule of "Prohibition against Conflicts of Interests in Certain Securitizations" in September 2011, they prohibit a large group of interested parties including underwriters from engaging in certain transactions, among which a particular one is short sale. Moreover, investors are fiercely opposed to short-selling securities by underwriters, and petitions from institutional investors to urge constraint on short sale in the City of London in recent years are common occurrences. In other financial markets such as the ones in China, short sale of any securities is strictly forbidden. This is why we primarily focus on the case in which there is a short sale constraint for the underwriters.

Like in Aghion, Bolton, and Tirole (2004), we assume that the underwriter's capital is scarce and he incurs an opportunity cost (i.e. cost of capital) proportional to his investment in the security. Consequently, even though the underwriter can fully enjoy the adverse selection discount, in equilibrium the additional cost due to the retention depresses his stake to the level that is just enough for him to camouflage as liquidity traders and gain from informed trading. Interestingly, a unique equilibrium of informed-sales arises naturally in which the underwriter liquidates his holdings if his private information indicates that the security will subsequently underperform, and he refrains from trading otherwise. Our results speak to the issues associated with the rise of the originate-to-distribute (OTD) lending model in debt markets (Bord and Santos, 2012). Because of the development of active secondary markets, banks' incentives to screen and monitor loans have diminished (Keys, Mukherjee, Seru, and Vig, 2010). Moreover, they tend to sell loans that are of excessively poor quality (Purnanadam, 2010), and under-

perform their peers by about 9% per year subsequent to the initial sales (Berndt and Gupta, 2009). To this end, our model fully captures the resultant adverse selection problem from OTD.

Working backward, we consider the optimal design of disclosure by the issuer. If she does not disclose additional information, the underwriter will choose to retain a stake only when the *ex ante* uncertainty about the security's payoff is relatively high. Because otherwise his private information has low value and his trading profits are not enough to compensate for his opportunity cost of investment. As a result, underpricing occurs only if the security is more risky. This is consistent with the evidence in Cai, Helwege, and Warga (2007) that find significant underpricing on speculative-grade debt offerings but no significant underpricing on investment-grade bond IPOs. Since the underpricing undermines the issuer's proceeds, she can do better by inducing posteriors beliefs which reduce the uncertainty to the degree that the investment bank is just indifferent between no retention and a positive stake. In this case, the optimal disclosure is partially informative. A sender-preferred equilibrium prescribes that the underwriter should not retain any share, thus no discount will occur in equilibrium.

Next we extend our model by introducing *demand uncertainty* (i.e. demand may fall short of supply) in the primary market. With a positive probability the shares net of the underwriter's planned retention cannot be fully subscribed by the participant investors. In order to complete the deal, the underwriter has to acquire all the remaining shares. Unlike before where the investment bank's decision to underwrite is trivial, the bank will shy away from the deal if his expected payoff is negative. This creates a hold-up problem arising from the possibility of demand shock. Intuitively, the bank will choose to underwrite and hold a stake only if uncertainty about the cash flows from the security is sufficiently high. Then, the underwriter is able to exploit his private information, and his

expected trading gain is enough to offset his expected loss from excessive retention. Therefore, the issuer's optimal information design will be as follows. If the ex ante uncertainty about the security is so high that the investment bank is always willing underwrite, the issuer will design a signal system inducing posteriors beliefs which reduce the uncertainty to the level that makes the investment bank just indifferent between whether or not to underwrite. This in turn reduces adverse selection and increases the issuer's expected revenue. However, if the ex ante uncertainty about the security is relatively low, the investment bank will not underwrite unless the signal changes his prior. The issuer's overriding interest in this scenario is to be able to sell the security and maximize her expected payoff with strategic disclosure. Thanks to the Bayesian plausibility constraint which requires that the average posteriors to be equal to the prior, Bayesian persuasion by the issuer can induce the investment bank to underwrite with positive probability and balances this with a worse belief that leaves the bank's underwriting decision unchanged, which improves the issuer's expected payoff. The optimal disclosure is such that on the one hand it may induce the worst belief which leads to the investment bank's withdrawal from underwriting, but on the other hand it may generate signal that makes the investment bank just willing to underwrite at the relevant beliefs. At the latter belief, the security's uncertainty is in fact increased, and the underwriter's private information thus becomes sufficiently valuable again, although on average the disclosure system still reduces the uncertainty relative to that at the prior belief. Our model features an interesting mechanism where increased payoff uncertainty can mitigate the hold-up problem brought about by demand uncertainty. We contribute to the literature by demonstrating a possible way to avoid security issuance failure due to weak demand, and by offering alternative insight into the "pipeline risk" in Bruche, Malherbe, and Meisenzahl (2018), where they document the successful issuance of leveraged

syndicated loans along with the costly excessive retention by the underwriting banks. We argue that it may stem from the fact that the banks are successfully persuaded by the borrowers albeit the presence of high demand uncertainty.

Our model yields novel empirical predictions that relate the informativeness of the optimal disclosure to various aspects of the primary and secondary markets. We show that the effects are not simply monotonic and depend on the exante uncertainty of the security's payoff. Specifically, when the ex ante payoff uncertainty is relatively high, both better growth option of the firm/borrower and more secondary market liquidity lead to more transparent disclosure. Conversely, greater issue size, larger cost of underwriting bank's capital, higher probability of demand shock, and weaker demand are associated with less informative disclosure. Better growth option and more liquidity allow the underwriter to enjoy more profits by trading on his private information. Hence the optimal system only needs to induce less uncertainty at posteriors that make the underwriter just break-even. In contrast, larger issue size and cost of underwriting bank's capital make it more costly for the underwriter to hold a stake in order to gain from informed trading. Thus more uncertainty should be introduced to make the underwriter's private information more valuable. Likewise, higher probability of demand shock and weaker demand make it more costly for the bank to underwrite, thus the optimal system should induce beliefs with higher uncertainty so that his stake carries more trading value in the secondary market. Our result is similar to the model of Pagano and Volpin (2012) which shows that coarse information enhances primary market liquidity at the cost of reducing secondary market liquidity. In contrast, the motivation for the revelation of coarse information in our model is to solve the hold-up problem and promote an active primary market with the underwriter's participation. Moreover, the issuer cannot control over the realizations of the signal, thus the coarse information does not come with

certainty.

The results for the security with *ex ante* relatively low payoff uncertainty in the presence of demand uncertainty is just the opposite: better growth option and more liquidity dampen the informativeness of the disclosure, while greater issue size, larger cost of capital, higher probability of demand shock, and weaker improve the informativeness. Especially noteworthy is that in the latter cases although the overall uncertainty is reduced by the optimal disclosure, to attract the bank to underwrite, the inherent uncertainty at the posterior beliefs that make the bank just indifferent actually becomes larger than that at the prior. The uncertainty at these posteriors should vary according to the intuition discussed in the previous paragraph. But the informativeness hinges on how *dispersed* the distribution of the posteriors is.

Finally, we extend our model by relaxing the assumption on the short sale constraint in the secondary market. Without short-sale constraint, it is optimal for the underwriter not to acquire any security in the primary market, but to exploit his private information by selling the asset short in the secondary market. If there is no demand uncertainty, only a fully informative disclosure can deter the underwriter from engaging in informed trading. Nevertheless, when demand is uncertain, all of the results on optimal disclosure we have obtained with short-selling constraint extends to the case without it. Compared with the case where short sale is prohibited, the issuer only needs less transparent disclosure to persuade the investment bank to underwrite when the uncertainty about the security's payoff is relatively low. But she has to design more transparent disclosure to alleviate adverse selection when the payoff uncertainty is relatively high.

Our paper is related to several strands of the literature. First, our work contributes to the theoretical literature that attempts to address the question of how the rapidly evolving debt markets can go awry (e.g. Chemla and Hennessy, 2014; Pagano and Volpin, 2012; Parlour and Plantin, 2008). We model the adverse selection problem in the OTD lending model, and show that strategic disclosure not only benefits the issuer, but also reduces this informational friction.

Second, our theoretical framework enriches the large literature on blockholders' governance by exit (e.g. Aghion, Bolton, and Tirole, 2004; Edmans and Manso, 2011; Faure-Grimaud and Gromb, 2004). Importantly, the applicability of our model naturally goes beyond debt markets and extends to equity markets if we view the underwriter as an extant blockholder in a firm. Under this interpretation, we model the blockholder's decision to support and participate in a security offering (e.g. seasoned equity offering). As long as he participates, the blockholder has an informational advantage over other dispersed investors from holding and learning. As we have explained, he can exert governance by exit to push the firm to *ex ante* disclose more transparent information when the payoff uncertainty of the security is relatively high.

Third, our paper adds to a growing body of literature on information design theory (e.g. Alonso and Câmara, 2016; Bergemann and Morris, 2018; Kamenica and Gentzkow, 2011; Rayo and Segal, 2010) as well as its application in corporate finance (e.g. Azarmsa, 2017; Azarmsa and Cong, 2018; Boleslavsky, Carlin, and Cotton, 2017; Goldstein and Leitner, 2018; Huang, 2016; Szydlowski, 2016). We extend the basic Bayesian persuasion framework by including a second receiver (the participant investors) who indirectly affects the welfare of both the sender and the first receiver.

Fourth, our theoretical analysis offers new insight to the empirical literature on the effect of disclosure on liquidity (e.g. Balakrishnan, Billings, Kelly, and Ljungqvist, 2014). In contrast with the extant literature, we focus on how firms will design their disclosure in security issuance when faced with varying market liquidity. Our model provides a rationale for whether a liquid secondary market contributes to a better information environment of the issuing firm. To our best knowledge, we are the first to consider the security issuer's optimal design of information disclosure in the presence of both the financing and the trading frictions. We thus call for empirical investigations of the relationship between the informativeness of disclosure (through the lens of the information memoranda and the prospectuses) and the subsequent market activities as predicted in our model.

This paper is organized as follows. Section 1.2 introduces the setup of the model. Section 1.3 solves for the secondary market trading equilibrium and the primary market issue price given an active secondary market. Section 1.4 presents the core results of the model with a secondary market that has short sale constraint. The equilibrium disclosure policies are analyzed both with and without demand uncertainty in the primary market. Section 1.5 changes the secondary market structure by removing the short sale ban and solve for the optimal disclosure policies. Section 1.6 conducts welfare analysis for the investment bank and the issuer under different primary market conditions and secondary market structures. Section 1.7 concludes. All proofs not in the main body of the paper are deferred to the Appendix in Section 1.8.

# 1.2 The Model

The model has four dates and no discounting. There are three types of players: an issuer, an investment bank, and a group of investors, all of whom are risk-neutral.

### 1.2.1 The Issuer

The issuer (also called "she" or "firm") wants to sell claims to cash flows from a productive asset. Examples of such claims include bonds, (syndicated/securitized)

loans, or equity stocks. For brevity, we shall simply call them securities. We normalize the number of securities to be issued to 1. The state of the economy  $\omega$ is binary: it can be Good (G) or Bad (B) with prior probability distribution  $\mathbb{P}[\omega = G] = \mu_0$  and  $\mathbb{P}[\omega = B] = 1 - \mu_0$  respectively. Cash flows  $\tilde{v}$  from state B and state G are  $V_H \equiv V_L + \Delta V$  and  $V_L$  respectively.



Figure 1.1: Cash flows distribution under the prior

The issuer designs an experiment which we refer to as a disclosure system  $\pi$  with binary signal  $s \in \{h, \ell\}$ . The signal realization follows the conditional distribution:  $\pi_G \equiv \mathbb{P}[s = h | \omega = G] \geq \pi_B \equiv \mathbb{P}[s = h | \omega = B]$ , which also represents the precision of the system. Figure 1.2 illustrates how the disclosure system maps each state to a signal. Using Bayes' rule, the posteriors  $\mu_s$  upon observing  $s \in \{h, \ell\}$  are

$$\mu_h \equiv \mathbb{P}[\omega = G|s = h] = \frac{\pi_G \mu_0}{\pi_G \mu_0 + \pi_B (1 - \mu_0)},$$
$$\mu_\ell \equiv \mathbb{P}[\omega = G|s = \ell] = \frac{(1 - \pi_G)\mu_0}{(1 - \pi_G)\mu_0 + (1 - \pi_B)(1 - \mu_0)}.$$

Moreover, Bayesian updating requires that the average posterior is consistent with the prior, which gives the Bayesian plausibility condition:

$$\mathbb{P}[s=h] \cdot \mu_h + \mathbb{P}[s=\ell] \cdot \mu_\ell = \mu_0.$$

Therefore, the information design problem for the issuer is equivalent to choosing



Figure 1.2: The disclosure system  $\pi$ 

a pair of posteriors  $\{\mu_h, \mu_\ell\}$  whose distribution must satisfy the above constraint.

### 1.2.2 Informativeness of the Disclosure System

Following Gentzkow and Kamenica (2014), we use the entropy measure to gauge the uncertainty associated with a given belief. In our binary-state economy, if the belief that the state is G conditional on observing s is  $\mu_s$ , its entropy is  $H(\mu_s) =$  $-\mu_s \ln \mu_s - (1 - \mu_s) \ln (1 - \mu_s)$ . Hence the belief achieves the highest uncertainty when  $\mu_s = 1/2$ , and the closer it is to the endpoints of its support (i.e. 0 or 1), the less uncertain the belief is. Moreover, the informativeness of a disclosure system  $\pi$  is measured as the reduction in entropy  $L(\pi) = H(\mu_r) - \mathbb{E}_{\langle \pi | \mu_r \rangle}[H(\mu_s)]$ , where  $\mu_r$  is a fixed reference belief independent of the system  $\pi$ , and the subscript  $\langle \pi | \mu_r \rangle$  indicates that the expectation is taken under the distribution of posteriors (i.e. the probabilities of s = h and  $s = \ell$ ) given the reference prior  $\mu_r$ .<sup>1</sup>

The fact that the above  $L(\pi)$  function is convex in  $\mu_s$  implies a simpler yet more intuitive interpretation of the informativeness: the more dispersed the distribution of posteriors, the more informative the disclosure system. Formally,

<sup>&</sup>lt;sup>1</sup>The introduction of this reference belief  $\mu_r$  ensures that the disclosure informativeness does not vary with the prior  $\mu_0$ .

consider two systems  $\pi$  and  $\pi'$  with possible signal realizations  $\{h, \ell\}$  and  $\{h', \ell'\}$ , and induced posteriors  $\{\mu_h, \mu_\ell\}$  and  $\{\mu_{h'}, \mu_{\ell'}\}$ . Suppose that

$$0 \le \mu_{\ell} \le \mu_{\ell'} \le \mu_{h'} \le \mu_h \le 1$$

with either the second or fourth inequality (or both) holding strictly, then we claim that system  $\pi$  is more informative than system  $\pi'$  in the spirit of Blackwell (1951). Furthermore, from the Bayesian updating formulas of the two posteriors, both a higher  $\pi_G$  and a lower  $\pi_B$  imply a more informative signal system. It is because such changes in the precision parameters lead to a higher  $\mu_h$  and a lower  $\mu_{\ell}$ , which are consistent with our definition of the informativeness above. In this paper we use "informativeness" and "transparency" interchangeably to describe the quality of a disclosure system.

#### **1.2.3** The Investment Bank and the Participant Investors

In addition to the issuer, there are two other types of players: an investment bank and a group of participant investors. To issue the securities, the issuer has to find an investment bank (also called "underwriter" or "he") to help her underwrite the deal in the primary market. The investment bank can be an underwriting bank in a public offering of bond or equity, a lead bank in loan syndication, or an arranger in securitization. The issuer reveals the disclosure system  $\pi$  to the investment bank. The investment bank then engages in due diligence to find out the realization of the signal s. After observing s the investment bank makes decision on whether to underwrite. If he agrees to underwrite, he further chooses the fraction of securities  $\beta$  to retain. Instead, he can also withdraw from underwriting if he finds it unfavorable, and thus the issue fails.<sup>1</sup> We denote the

<sup>&</sup>lt;sup>1</sup>In practice when primary market demand for the security is weak and the underwriter is not willing to retain additional shares, he may choose to delay (suspend) the issuance indefinitely,

action set of the investment bank as follow

 $a_{IB} \in \{(\text{Underwrite \& Retain } \beta), (\text{Not Underwrite})\}.$ 

Following Aghion, Bolton, and Tirole (2004), we assume that capital is scarce for the investment bank and he incurs an opportunity cost (i.e. cost of capital) r > 0per unit of investment.<sup>1</sup> Moreover, there are a unit mass of participant investors who can also invest in a risk-free asset with zero return. They will invest in the remaining  $(1 - \beta)$  shares as long as they are break-even.

#### 1.2.4 Time Line

At T = 0, nature determines the prior distribution of the states. The issuer designs a signal system  $\pi$  which will generate a signal s at T = 1. She finds an investment bank and reveals this experiment  $\pi$  to him.

At T = 1, signal s realizes. The investment bank first engages in due diligence to discover s and then decides if he will underwrite the issuance. If the investment bank chooses to underwrite, he materializes and communicates the signal s to participant investors. He sells  $(1 - \beta)$  to the participant investors and acquires the remaining  $\beta$ , both at price  $P_0$ .

At T = 2, a secondary market opens. The market structure is like Kyle (1985). The investment bank and the participant investors submit their market orders to a continuum of deep-pocketed risk-neutral market makers (MM) who

and only to close the deal when the securities can be fully subscribed. For simplicity, we also regard this scenario as failure

<sup>&</sup>lt;sup>1</sup>We assume throughout the paper that the investment bank will always incur this opportunity cost of his capital expenditure in both the primary and the secondary markets. This helps to eliminate multiple equilibria in the secondary market. Removal of such assumption in the secondary market does not affect the equilibrium we will characterize. Moreover, r cannot be too large as otherwise the investment bank will always find it unfavorable to underwrite. We characterize the exact requirements that r should satisfy in order to ensure the existence of interior solutions of the model in the appendix.

price the security competitively after observing the total net order flow y. The market maker sets price  $P_1 = \mathbb{E}_s[\tilde{v}|y]$ . The trading episode proceeds with three sub-stages:

- 1. The investment bank observes the true state  $\omega$  and determines his trading strategy, i.e. the amount of securities  $\{x_{IB}\}$  to trade.
- 2. Liquidity shocks happen with probability  $\gamma \in (0, 1)$ . The participant investors submit their aggregate market order  $\{x_{PI}\}$ , whereby
  - a. with probability  $\gamma$  a fraction  $\phi \in (0, \frac{1}{2})$  of the participant investors experience liquidity shocks and have to liquidate their holdings;
  - b. with probability  $(1 \gamma)$ , there is no liquidity shock and these participant investors don't sell.
- 3. The MM receive the net order flow from the investment bank and the participant investors  $y \equiv x_{IB} + x_{PI}$ , and set  $P_1$ .

At T = 3, payoffs of the underlying securities are realized, and all parties get paid.

The time line is summarized in Figure 1.3.

### 1.2.5 Payoff Functions

We next define the expected payoff functions of the issuer, the investment bank, and the participant investors at T = 1 in the primary market. Consider the situation after the signal s has realized. The issuer's expected payoff is

$$U_E(\beta, \mu_s) = \mathbf{1}_{a_{IB} = \{\text{Underwrite}, \beta\}} P_0.$$

#### 1.2 The Model

T = 0	T = 1	T = 2	T = 3
<ul> <li>Nature determines the prior μ<sub>0</sub>.</li> <li>The issuer designs a disclosure system π which will generate a signal s at T = 1.</li> </ul>	<ul> <li>Signal s realizes, and is revealed by the issuer to an investment bank.</li> <li>The investment bank decides whether or not to underwrite after observing the signal s. If not, the game ends.</li> <li>If the investment bank decides to underwrite, he communicates this s to participant investors. He sells fraction (1 - β) to participant investors and retains β, both at a price P<sub>0</sub>.</li> </ul>	<ul> <li>Secondary market opens.</li> <li>The investment bank observes the state and decides about his trading strategy.</li> <li>The participant investors experience liquidity shocks with probability γ.</li> <li>The MM receive orders from the investment bank and the participant investors, and set price P<sub>1</sub>.</li> </ul>	Payoff realizes and all parties are paid.

Figure 1.3: Time line of the game

 $\mathbf{1}_{a_{IB}=\{\text{Underwrite, }\beta\}}$  is an indicator function which takes value 1 if  $a_{IB} = \{\text{Underwrite, }\beta\}$ (i.e. the investment bank underwrites and acquires  $\beta$ ), and 0 otherwise. Since the investment bank will make his underwriting and retention decisions after observing *s*, it follows that  $a_{IB}$  will be a function of posterior belief  $\mu_s$ .  $P_0$  is the price of the securities and the money she will obtain in the primary market conditional on the investment bank choosing to underwrite. We follow the Bayesian persuasion literature (e.g. Huang, 2016; Kamenica and Gentzkow, 2011; Szydlowski, 2016) by assuming that information design incurs no cost, and when the issuer is indifferent between two disclosure systems, she always selects the one that is less informative.<sup>1</sup>

Back to T = 0 when the issuer designs the disclosure system  $\pi$ , she rationally anticipates the best response by the investment bank conditional on induced

 $U_E(\beta, \mu_s) = \mathbf{1}_{a_{IB} = \{\text{Underwrite, }\beta\}} P_0 - C,$ 

 $<sup>^{1}</sup>$ This assumption ensures the tractability of our model as well as the uniqueness of the equilibrium. Alternatively, we can define the issuer's expected payoff as

posterior belief. Her expected payoff is therefore

$$\mathbb{E}_{\pi}[U_E(a_{IB},\mu_s)].$$

Here the subscript  $\pi$  implies that the expectation is taken under the distribution of signal realizations (posteriors).

The investment bank's expected payoff after observing s depends on whether he becomes an underwriter as well as his retention  $\beta$  if he chooses to underwrite:

$$U_{IB}(a_{IB}) = \mathbf{1}_{a_{IB} = \{\text{Underwrite, }\beta\}} \times \{\beta[(\mu_s \Delta V + V_L) - (1+r)P_0] + \mathbb{E}_s[\Pi]\},\$$

where  $\beta[(\mu_s \Delta V + V_L) - (1 + r)P_0]$  is his net payoff from retaining  $\beta$  shares in the primary market, and  $\mathbb{E}_s[\Pi]$  is his expected trading profits in the secondary if there is any at T = 2. Here the subscript *s* implies that we take the expectation under the distribution of underlying states induced by signal *s*.

Finally, for the participant investors to acquire the remaining  $(1 - \beta)$  shares, they will demand a price  $P_0$  which makes them at least break even. Therefore the issuer will offer a price such that their expected payoff is  $U_{PI}(\beta, \mu_s) = 0$ .

$$C(\pi) \equiv kL(\pi) = k\{H(\mu_r) - \mathbb{E}_{\langle \pi | \mu_r \rangle}[H(\mu_s)]\}.$$

where C represents a sunk cost of disclosure which varies with the informativeness of the disclosure system  $\pi$  as in Gentzkow and Kamenica (2014):

Note that k > 0 is the cost of a one-unit reduction in entropy. Therefore, at T = 0 when two disclosure systems deliver the issuer the same expected proceeds, she prefers the one that is less informative and thus less costly. When the unit cost  $k \to 0^+$ , the optimal disclosure policies converge to the ones in our paper. Also, for small k our main intuitions still go through and thus our results are robust to costly information disclosure.

# 1.3 Secondary Market Trading and Primary Market Discount

In this section, we solve for the subgame perfect equilibrium of the game by backward induction. Suppose that the investment bank chooses to underwrite at T = 1. Then at T = 2, the disclosure system  $\pi$ , the signal realization s, the share price  $P_0$  in the primary market, and the investment bank's retention  $\beta$  are all taken as given.

Now that the investment bank has observed the true underlying state at T = 2, he decides about the optimal market order  $x_{IB}$  he should submit. We characterize the unique informed-sale equilibrium where the investment bank do not trade in state G and sell  $(1 - \beta)\phi$  in state B as follows.

In state G, the true value of the security is  $V_H$ . The investment bank has no incentive to sell simply because the secondary market price cannot exceed the security's intrinsic value, i.e.  $P_1 \leq V_H$ . Moreover, the investment bank has no incentive to purchase additional shares in this state too. This is because if he buys, the aggregate order flow y > -u if liquidity shocks happen, and y > 0 if there is no liquidity shock. In order to pool in state B, he may need to buy shares too. Yet he could lose money because the cash flow in state B is only  $V_L$  but the price  $P_1 \geq V_L$ , and buying in bad state is thus sequentially irrational. Therefore, although he could gain in state G he would suffer a loss in state B. Such crosssubsidization renders him at most the same expected net trading profits as in the informed-sale equilibrium while his purchases incur additional opportunity cost,<sup>1</sup> and such trading strategy is obviously sub-optimal. Accordingly, in state G when there are liquidity shocks the net order flow will be y = -u, yet it will be y = 0

<sup>&</sup>lt;sup>1</sup>Recall that the investment bank will also incur opportunity cost as long as he acquires shares in the secondary market, although the informed-sale equilibrium is robust to the removal of the assumption about the investment bank's opportunity cost in the secondary market.

State	Liq. Sh.	$\tilde{v}$	Prob.	$x_{PI}$	$x_{IB}$	y	$P_1$
G	Yes	$V_H$	$\mu_s\gamma$	-u	0	-u	$\frac{\mu_s \gamma \Delta V}{\mu_s \gamma + (1 - \mu_s)(1 - \gamma)} + V_L$
G	No	$V_H$	$\mu_s(1-\gamma)$	0	0	0	$V_H$
В	Yes	$V_L$	$(1-\mu_s)\gamma$	-u	-u	-2u	$V_L$
В	No	$V_L$	$(1-\mu_s)(1-\gamma)$	0	-u	-u	$\frac{\mu_s \gamma \Delta V}{\mu_s \gamma + (1 - \mu_s)(1 - \gamma)} + V_L$
Note: $u \equiv (1 - \beta)\phi$ .							

Table 1.1: Secondary Market Trading and Pricing

if there is no liquidity shock.

In state B, since the price is always at least as much as the security's intrinsic value (i.e.  $P_1 \ge V_L$ ), the investment bank can potentially benefit from sale. The maximal amount that can be sold in order to at least partially conceal his private information is u. In this case the aggregate order flow will be y = -2u if participant investors are hit by liquidity shocks, and y = -u otherwise. Therefore, the MM cannot tell which state the economy is in when the net order flow is -u, and the investment bank enjoys informed trading profits if the true state happens to be bad.

In sum, to best exploit his private information, the investment bank refrains from trading in good state and liquidates  $(1 - \beta)\phi$  in bad state to maximize his expected informed trading profits while not fully reveal his identity.

We tabulate the equilibrium in the secondary market in Table 2.6, and summarize in the following proposition.

#### **Proposition 1** (Secondary market equilibrium):

1. The investment bank's optimal trading strategy is to submit an order  $x_{IB} = 0$ in state G, and an order  $x_{IB} = -(1 - \beta)\phi$  in state B. 2. The MM's posterior belief about the probability of state G is

$$\mu_{MM} = \begin{cases} 1 & \text{if } y = 0, \\ \frac{\mu_s \gamma}{\mu_s \gamma + (1 - \mu_s)(1 - \gamma)} & \text{if } y = -(1 - \beta)\phi, \\ 0 & \text{if } y = -2(1 - \beta)\phi. \end{cases}$$

3. The MM set price

$$P_{1} = \begin{cases} V_{H} & \text{if } y = 0, \\ \frac{\mu_{s} \gamma \Delta V}{\mu_{s} \gamma + (1 - \mu_{s})(1 - \gamma)} + V_{L} & \text{if } y = -(1 - \beta)\phi, \\ V_{L} & \text{if } y = -2(1 - \beta)\phi. \end{cases}$$

Having obtained the trading equilibrium, we now derive the primary market issue price taking into account the adverse selection in the secondary market. Recall from Table 2.6 that the investment bank's trading strategy mixes case {State G, Liquidity Shocks} with case {State B, No Liquidity Shocks}, and he only makes profits in the second case where he manages to camouflage as liquidity traders. His informed-sale profits per share are

$$G \equiv P_1 - V_L = \frac{\mu_s \gamma \Delta V}{\mu_s \gamma + (1 - \mu_s)(1 - \gamma)}$$

The next proposition derives the investment bank's total expected trading profits and the primary market issue price when he observes signal s at T = 1.

**Proposition 2** (Expected trading profits, and Primary market underpricing):

1. The investment bank's total expected trading profits are

$$\mathbb{E}_s[\Pi] = (1-\beta)\phi \ \mathbb{E}_s[G] = \frac{(1-\beta)\phi(1-\mu_s)(1-\gamma)\mu_s\gamma\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}.$$

2. Since the investment bank's gain per share is just the participant investors' loss per share, in order for these investors to purchase at T = 1,

$$P_{0} \equiv \mathbb{E}_{s}[\tilde{v}] - \Delta P$$
  
=  $(\mu_{s}\Delta V + V_{L}) - \frac{\mathbb{E}_{s}[\Pi]}{1 - \beta}$   
=  $(\mu_{s}\Delta V + V_{L}) - \frac{(1 - \mu_{s})\mu_{s}(1 - \gamma)\gamma\phi\Delta V}{\mu_{s}\gamma + (1 - \mu_{s})(1 - \gamma)}$ 

The fact that securities are issued with a discount due to adverse selection in the secondary market has been commonly in the literature (e.g. Edmans and Manso, 2011; Holmström and Tirole, 1993; Maug, 1998).

# 1.4 Short Sale Constraint (SS)

As we will see, whether short sale by the underwriter is allowed in the secondary market has somewhat different implications for the equilibrium in the primary market at T = 1 as well as the issuer's choice of optimal disclosure policy at T = 0. Note that whether there is short sale constraint in the secondary market does not affect the equilibrium strategies we have characterized in the previous section. We first consider the baseline model where the investment bank cannot sell the security short. Then we proceed with the model in which there is no short sale constraint.

The next lemma establishes the condition under which strategic trading by the investment bank is feasible when there is short sale constraint in the secondary market.

**Lemma 1** (Minimal stake): When selling the security short is not allowed in the secondary market, the investment bank can engage in strategic informed trading
Suppose that part of the participant investors are hit by liquidity shocks. They will liquidate a fraction of  $u \equiv (1 - \beta)\phi$  shares in total. To gain informed trading profits, the investment bank has to camouflage as liquidity traders. Because he cannot short sell, to achieve this goal his holdings  $\beta$  should not be too samll, i.e. no less than  $(1 - \beta)\phi$ . Also note that  $\beta$  should be strictly less than 1 because otherwise the market is completely illiquid and there will be no liquidity traders.

### 1.4.1 No Demand Uncertainty (NDU)

In this section we first consider the benchmark model where there is no demand uncertainty in the primary market, i.e. all the shares can be fully subscribed by the participant investors even if the investment bank does not acquire any.

At T = 1, from Lemma 1 we have already established that when  $\beta \in [0, \frac{\phi}{1+\phi})$  or  $\beta = 1$ , the investment bank cannot gain from trading on his private information, because either his stake is not enough or the secondary market is completely illiquid. Thus the issue price will not include the adverse selection discount. The following proposition characterizes the price in the primary market for different levels of retention by the investment bank.

**Proposition 3** (Primary market issue price): The issue price in the primary market is

$$P_0(\beta,\mu_s) = \begin{cases} \mu_s \Delta V + V_L - \frac{(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma+(1-\mu_s)(1-\gamma)} & \text{if } \beta \in \left[\frac{\phi}{1+\phi},1\right), \\ \mu_s\Delta + V_L & \text{if } \beta \in \left[0,\frac{\phi}{1+\phi}\right) \text{ or } \beta = 1. \end{cases}$$

### 1.4.1.1 Investment Bank's Optimal Decision I

Absent any demand uncertainty, the investment bank can always stay break-even by choosing to underwrite yet retaining no shares. Therefore, the investment bank's decision to underwrite is trivial in our benchmark model here.

At T = 1 after signal s has realized and posterior belief  $\mu_s$  has been formed, the investment bank decides on his stake  $\beta$  to maximize his expected payoff, denoted  $U_{IB}^1(\beta, \mu_s)$ :

$$\max_{\beta \in [0,1]} \left\{ \begin{array}{c} \beta \cdot \left[ (\mu_s \Delta V + V_L) - (1+r) P_0(\beta, \mu_s) \right] \\ + \mathbf{1}_{\{\beta \ge (1-\beta)\phi\}} \cdot (1-\beta)\phi \cdot \frac{(1-\mu_s)\mu_s(1-\gamma)\gamma\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)} \end{array} \right\}.$$

The first term above represents the investment bank's expected payoff in the primary market which is the intrinsic value of the  $\beta$  shares net of his capital expenditure and opportunity cost. The second term is his expected trading profits as we have shown in Proposition 2 if he has acquired adequate stake in the primary market. Observe that the above expected utility function  $U_{IB}^1(\beta, \mu_s)$  is in fact piece-wise linear in  $\beta$ . Hence its maximum must be attained at  $\beta^* = 0$ , or 1, or  $\frac{\phi}{1+\phi}$ , or  $\beta^* \uparrow 1$  (i.e.  $\beta^* = 1^-$ ). The investment bank's optimal retention problem thus becomes

$$\beta^* = \arg\max_{\beta \in \{0,1,\frac{\phi}{1+\phi},1^-\}} \left\{ U_{IB}^1(0,\mu_s), U_{IB}^1(1,\mu_s), U_{IB}^1(\frac{\phi}{1+\phi},\mu_s), U_{IB}^1(1^-,\mu_s) \right\}.$$

The investment bank's expected payoff  $U_{IB}^1(\beta, \mu_s)$  is calculated as follows:

- (i). If  $\beta^* = 0$ , there will be no informed trading in the secondary market and no price discount in the primary market,  $U_{IB}^1(0, \mu_s) = 0$ .
- (ii). If  $\beta^* = 1$ , the secondary market is completely illiquid and the issue price

has no discount,

$$U_{IB}^{1}(1,\mu_{s}) = (\mu_{s}\Delta V + V_{L}) - (1+r)P_{0}(1,\mu_{s}) = -r(\mu_{s}\Delta V + V_{L}).$$

(iii). If  $\beta^* = \frac{\phi}{1+\phi}$ , informed trading is feasible and thus issue price must be discounted,

$$U_{IB}^{1}(\frac{\phi}{1+\phi},\mu_{s}) = \frac{\phi}{1+\phi} \left[ (\mu_{s}\Delta V + V_{L}) - (1+r)P_{0}(\frac{\phi}{1+\phi},\mu_{s}) \right]$$
$$+ \frac{1}{1+\phi} \cdot \frac{(1-\mu_{s})\mu_{s}(1-\gamma)\gamma\phi\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)}.$$

(iv). Finally, if  $\beta^* = 1^-$ , there is (infinitesimal) informed trading profit yet still a relatively sizable adverse selection discount,

$$\begin{aligned} U_{IB}^{1}(1^{-},\mu_{s}) \\ &= 1^{-} \cdot \left[ (\mu_{s}\Delta V + V_{L}) - (1+r)P_{0}(1^{-},\mu_{s}) \right] + 0^{+} \cdot \frac{(1-\mu_{s})\mu_{s}(1-\gamma)\gamma\phi\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} \\ &\doteq (\mu_{s}\Delta V + V_{L}) - (1+r)P_{0}(1^{-},\mu_{s}) \\ &= (\mu_{s}\Delta V + V_{L}) - (1+r) \left[ (\mu_{s}\Delta V + V_{L}) - \frac{(1-\mu_{s})\mu_{s}(1-\gamma)\gamma\phi\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} \right]. \end{aligned}$$

To pin down the optimal retention by the investment bank in response to the observed signal s, it suffices to show for different  $\mu_s$  which of the above  $U_{IB}^1$ 's achieve the largest value. The lemma below provides some important properties of the investment bank's expected payoff function if he chooses to retain  $\beta = \frac{\phi}{1+\phi}$ .

**Lemma 2** (Indifference cut-off posteriors I):

- 1. There exists a pair  $\{\underline{\mu}, \overline{\mu}\}$  with  $0 < \underline{\mu} < \frac{1}{2} < \overline{\mu} < 1$  such that  $U_{IB}^1(\frac{\phi}{1+\phi}, \underline{\mu}) = U_{IB}^1(\frac{\phi}{1+\phi}, \overline{\mu}) = 0.$
- 2.  $U_{IB}^1(\frac{\phi}{1+\phi},\mu_s) > 0$  if  $\mu_s \in (\underline{\mu},\overline{\mu})$ , and  $U_{IB}^1(\frac{\phi}{1+\phi},\mu_s) < 0$  if  $\mu_s \in [0,\underline{\mu})$  or

 $\mu_s \in (\overline{\mu}, 1].$ 

Therefore, at posteriors  $\mu_s = \underline{\mu}$  and  $\overline{\mu}$ , the investment bank is indifferent between holding  $\beta = \frac{\phi}{1+\phi}$  and  $\beta = 0$ . Furthermore, the investment bank will only consider purchasing a fraction of the shares when uncertainty about the security is large (i.e. the posterior belief  $\mu_s$  lies in an intermediate range).

The following proposition characterizes the investment bank's optimal strategy and the relevant equilibrium payoffs under different posterior beliefs.

**Proposition 4** (Investment bank's optimal strategy and relevant payoffs I): The investment bank's optimal stake is

$$\beta^* = \begin{cases} \frac{\phi}{1+\phi} & \text{if } \mu_s \in (\underline{\mu}, \overline{\mu}), \\ 0 & \text{if } \mu_s \in [0, \underline{\mu}] \cup [\overline{\mu}, 1] \end{cases}$$

His equilibrium payoff is

$$\hat{U}_{IB}^{1}(\mu_{s}) = \begin{cases} U_{IB}^{1}(\frac{\phi}{1+\phi},\mu_{s}) & \text{if } \mu_{s} \in (\underline{\mu},\overline{\mu}), \\ 0 & \text{if } \mu_{s} \in [0,\underline{\mu}] \cup [\overline{\mu},1]. \end{cases}$$

In Figure 1.4 the blue line shows the payoff of the investment bank if he chooses to retain  $\beta = \frac{\phi}{1+\phi}$ , i.e.  $U_{IB}^1(\frac{\phi}{1+\phi},\mu_s)$ . The red dashed line depicts his equilibrium payoff under his optimal retention strategy, denoted by  $\hat{U}_{IB}^1(\mu_s)$ . In equilibrium when  $\mu_s \in [0, \underline{\mu}] \cup [\overline{\mu}, 1]$ , the investment bank does not retain any share, and his payoff is zero. Yet when  $\mu_s \in (\underline{\mu}, \overline{\mu})$ , he chooses his retention  $\beta = \frac{\phi}{1+\phi}$  and his payoff is  $U_{IB}^1(\frac{\phi}{1+\phi}, \mu_s)$ , which corresponds to the hump-shaped part of the red dashed line. So in equilibrium both the investment bank's optimal stake and his expected payoff depend only on his belief  $\mu_s$ .



Figure 1.4: The investment bank's payoff (i)

The intuition of Proposition 4 is straightforward: when uncertainty about the security's payoff is relatively small, the investment bank's informed trading profits in the secondary market is not enough to cover his cost of capital in the primary market, even though he free rides on the discounted issue price. This results in zero retention by the bank. When the uncertainty about the security is relatively large, it is profitable for the investment bank to acquire some shares in order to later trade on his private information strategically. Yet such gain in the secondary market trades off against the opportunity cost incurred from his primary market capital expenditure. In equilibrium the investment bank optimally chooses his retention such that it is just enough for him to camouflage as liquidity traders in the secondary market. This minimizes his total cost of capital while maximizes his expected trading profits. Our result contrasts with the retention equilibrium in Leland and Pyle (1977) where a firm holds a large fraction of its shares to have some skin in the game and signal to the market its quality when information asymmetry problem is severe. In our model, the investment bank acquires a stake to later gain from informed sales in the secondary market when the security's cash flows are relatively more uncertain. In this regard, such retention exacerbates the adverse selection problem.

### 1.4.1.2 Optimal Disclosure System I

Given the optimal retention scheme by the investment bank described in Proposition 4, it follows naturally that the issuer's expected revenue conditional on signal s at T = 1 will be either the intrinsic value of the security if the bank does not acquire any share, or the expected cash flows from the security net of an adverse selection discount if the bank holds a positive stake  $\frac{\phi}{1+\phi}$ . This gives the following proposition.

**Proposition 5** (Issuer's payoff after information design I): At T = 1 the issuer's expected payoff conditional on signal s is:

$$U_E^1(\mu_s) = \begin{cases} \mu_s \Delta V + V_L - \frac{(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma+(1-\mu_s)(1-\gamma)} & \text{if } \mu_s \in (\underline{\mu}, \overline{\mu}), \\ \\ \mu_s \Delta V + V_L & \text{if } \mu_s \in [0, \underline{\mu}] \cup [\overline{\mu}, 1]. \end{cases}$$

Note that at the two posteriors  $\underline{\mu}$  and  $\overline{\mu}$ , the investment bank is actually indifferent between retaining 0 and a positive stake  $\frac{\phi}{1+\phi}$ . Following the convention of information disclosure literature, we select the sender-preferred equilibrium in which the investment bank does not acquire any share in the primary market when he is indifferent, and thus there will be no discount. In reality, given the high cost of bank capital, we have reason to believe that if the issuer is not opposed to it, investment banks are more prone to no retention although a positive stake gives him the same expected payoff.

At T = 0 the issuer designs the optimal disclosure policy to maximize her expected proceeds from issuing the security. She has to choose the precision of her signal  $\pi_G$  and  $\pi_B$  for the disclosure system  $\pi$ . By Bayes' rule, essentially her problem is equivalent to the optimal choice of two posteriors  $\mu_h$  and  $\mu_\ell$ .

Because we have assumed that demand never falls short of the supply in the primary market, the investment bank does not have to worry about the risk of retaining more shares than his privately optimal level. Thus he will always underwrite, and his decision problem is reduced to the choice of stake  $\beta$ . We can write the issuer's payoff at T = 1 as

$$U_E^1(\beta, \mu_s) = \mathbf{1}_{a_{IB} = \{\text{Underwrite, }\beta\}} P_0(\beta, \mu_s)$$

Since we already know from Proposition 4 that the investment bank's optimal retention  $\beta^*$  depends on  $\mu_s$ , the issuer's expected proceeds will only depend on  $\mu_s$  in equilibrium, which we denote by  $U_E^1(\mu_s) \equiv U_E^1(\beta^*, \mu_s) = P_0(\beta^*, \mu_s)$ . So the issuer solves the following maximization problem:

$$\hat{U}_{E}^{1}(\mu_{0}) \equiv \max_{\{\mu_{\ell},\mu_{h}\}} \mathbb{E}_{\pi}[U_{E}^{1}(\mu_{s})]$$
s.t. 
$$\beta^{*}(\mu_{s}) = \arg_{\beta \in [0,1]} \max U_{IB}^{1}(\beta,\mu_{s}),$$

$$\mathbb{P}[s=h] \cdot \mu_{h} + \mathbb{P}[s=\ell] \cdot \mu_{\ell} = \mu_{0},$$

$$\mathbb{P}[s=h] + \mathbb{P}[s=\ell] = 1.$$

The first constraint states that the investment bank will choose the stake that maximizes his expected payoff based on his posterior belief. The second constraint is the Bayesian plausibility condition in which the expectation of posteriors must equal the prior. The last constraint requires that the probabilities of signal realizations should sum to one.

To solve this problem, we use the concavification technique in Kamenica and Gentzkow (2011). In particular, the issuer's *ex ante* optimal design of disclosure

system can be derived by finding the concave closure of  $U_E^1(\mu_s)$ , which we define as  $\hat{U}_E^1(\mu_s)$ . A graphic representation is given in Figure 1.5. The black line depicts the issuer's expected payoff conditional on different posteriors. When the uncertainty is relatively large, the investment bank retains a stake and there is underpricing. Thus we observe a dent from the graph when  $\mu_s \in (\underline{\mu}, \overline{\mu})$ . The blue dashed line illustrates  $\hat{U}_E^1(\mu_s)$  – the issuer's maximized expected payoff from the optimal disclosure system.

Intuitively, for any given prior  $\mu_0$ , it must be equal to some convex combination of two posteriors  $\mu_\ell$  and  $\mu_h$  induced by the optimal system due to the Bayesian plausibility condition (i.e.  $\mu_0 = \lambda \mu_\ell + (1-\lambda)\mu_h$  for some  $\lambda \in [0, 1]$ ). So the issuer's *ex ante* expected payoff under the distribution of posteriors must be a convex combination of two expected payoffs conditional on relevant signal realizations too (i.e.  $\mathbb{E}_{\pi}[U_E^1(\mu_s)] = \lambda U_E^1(\mu_\ell) + (1-\lambda)U_E^1(\mu_h)$ ). Obviously, the optimal  $\mathbb{E}_{\pi}[U_E^1(\mu_s)]$ is attained on the concave closure of  $U_E^1(\mu_s)$ . The optimal  $\mu_\ell$  and  $\mu_h$  are obtained at the intersections of  $U_E^1(\mu_s)$  and its concave closure, which are to the left and right of  $\mu_0$  respectively.<sup>1</sup>  $\lambda$  and  $(1-\lambda)$  are the probabilities of posteriors  $\mu_\ell$  and  $\mu_h$ . The proposition below characterizes the optimal disclosure policy employed by the issuer at T = 0.

**Proposition 6** (Optimal information design I): At T = 0 the issuer's optimal disclosure policy is:

- 1. If  $\mu_0 \in [0, \underline{\mu}] \cup [\overline{\mu}, 1]$ , the optimal disclosure system has  $\pi_G = \pi_B \in (0, 1)$ , and is therefore completely uninformative, yielding posteriors  $\mu_\ell = \mu_h = \mu_0$ .
- 2. If  $\mu_0 \in (\underline{\mu}, \overline{\mu})$ , the optimal disclosure system has  $\pi_G = \frac{\overline{\mu}(\mu_0 \underline{\mu})}{\mu_0(\overline{\mu} \underline{\mu})}$  and  $\pi_B = \frac{(1 \overline{\mu})(\mu_0 \underline{\mu})}{(1 \mu_0)(\overline{\mu} \mu)}$ , yielding posteriors  $\mu_\ell = \underline{\mu}$  and  $\mu_h = \overline{\mu}$ .

One caveat is worth some discussion here. When  $\mu_0 \in (\mu, \overline{\mu})$ , there are mul-

<sup>&</sup>lt;sup>1</sup>In a completely uninformative system,  $\mu_{\ell} = \mu_h = \mu_0$ .



Figure 1.5: The issuer's payoff (i)

tiple disclosure systems which gives the issuer the same expected payoff. In fact she can set any arbitrary  $\pi_G$  and  $\pi_B$ , as long as they induce posteriors  $\mu_{\ell} \in [0, \underline{\mu}]$ and  $\mu_h \in [\overline{\mu}, 1]$  subject to  $\mathbb{P}[s = h] \cdot \mu_h + \mathbb{P}[s = \ell] \cdot \mu_{\ell} = \mu_0$ . But since we have assumed before that if multiple disclosure policies give the issuer the same expected payoff, she selects the one that is the least informative (and thus the least costly if we assume an infinitesimal cost of reduction in entropy due to the disclosure that varies with the informativeness of the system). Accordingly, Proposition 6 characterizes the least informative optimal disclosure system at T = 0.

From Figure 1.5 it is clear that if the issuer does not release information, underpricing happens when uncertainty about the firm is relatively large. This is consistent with Cai, Helwege, and Warga (2007) that find significant underpricing on speculative-grade debt IPOs but no significant underpricing on investmentgrade bond IPOs. We take a further step by showing that in fact issuer can strategically design her disclosure policy to curb underpricing even if *ex ante* the uncertainty about the security is relatively large. This is achieved by designing a system which decreases the uncertainty associated with the security to the degree that the investment bank is just indifferent between holding either zero or a positive stake. Also, a security with its payoff uncertainty below some thresholds will in turn have no discount. In practice, because of other possible frictions such as issuer's limited capability in reducing uncertainty, we will still observe some underpricing. Later we will show that when there is demand uncertainty in the primary market, underpricing always arises in equilibrium, but strategic disclosure can reduce it on average.

Since we have derived the optimal disclosure policy, it is natural to ask what factors may potentially affect the informativeness of the optimal system. Moreover, how do firms with different levels of uncertainty alter their optimal strategies in response to changes in those factors? We address these important questions in Proposition 7.

**Proposition 7** (Comparative statics I):

 $\begin{array}{ll} (1) & \frac{\partial \mu}{\partial V_L} > 0 \ and \ \frac{\partial \overline{\mu}}{\partial V_L} < 0. \\ (2) & Define \ \eta \equiv \frac{\Delta V}{V_L}, \ then \ \frac{\partial \mu}{\partial \eta} < 0 \ and \ \frac{\partial \overline{\mu}}{\partial \eta} > 0. \\ (3) & \frac{\partial \mu}{\partial r} > 0 \ and \ \frac{\partial \overline{\mu}}{\partial r} < 0. \\ (4) & \frac{\partial \mu}{\partial \phi} < 0 \ and \ \frac{\partial \overline{\mu}}{\partial \phi} > 0. \end{array}$ 

Result (1) states that as  $V_L$  increases, the lower-bound cut-off posterior  $\underline{\mu}$ , at which the investment bank is indifferent between holding 0 and  $\frac{\phi}{1+\phi}$ , becomes larger and the similar upper-bound cut-off posterior  $\overline{\mu}$  becomes smaller. This implies that the range  $(\underline{\mu}, \overline{\mu})$  shrinks inward.  $V_L$  is the reservation value of the security, and can be viewed as a proxy for the issue size. We first discuss the implications of the comparative statics if the system is completely uninformative. In this case the posterior belief is simply the prior. A larger  $V_L$  makes it more costly for the underwriter to retain a stake. So at the cut-off posterior beliefs, only marginally higher uncertainty will induce the underwriter to have a positive retention and stay break-even. The enhanced uncertainty makes the bank's private information more valuable in the secondary market trading, hence offsetting the additional cost brought about by the larger  $V_L$ .

Turning to the optimal disclosure, a larger  $V_L$  means that only firms that are relatively more uncertain (i.e.  $\mu_0 \in (\underline{\mu}, \overline{\mu})$ ) will employ a system which induces a pair of posteriors  $\{\underline{\mu}, \overline{\mu}\}$ . Yet as  $V_L$  becomes larger, the resulting optimal system will be less transparent because of the inward-shrunken  $(\underline{\mu}, \overline{\mu})$ , (i.e. less dispersed distribution of posteriors).<sup>1</sup> Therefore, for firms whose security payoffs are *ex ante* highly uncertain, larger issue size allows them to use less transparent disclosure to curb underpricing in the primary market.

Result (2) concerns the effect of the firm's growth option  $\eta$  on the optimal disclosure policy used by the issuer. Better growth option is potentially beneficial to the underwriting bank because it makes his informed trading more profitable. Consequently, at the cut-off beliefs, even marginally lower uncertainty still ensures a non-negative payoff from his retention and subsequent informed trading. As a result, the range ( $\underline{\mu}, \overline{\mu}$ ) expands, and the issuer will use more transparent system as the growth option improves if the security's *ex ante* payoff uncertainty is high.

Result (3) shows that the greater cost of capital of the investment bank will push the two cut-off posteriors inward. Similar to Result (1), at the cut-off beliefs, only marginally higher uncertainty will compensate the underwriter's increased cost of capital by making his private information more valuable in the secondary market trading. Therefore, greater cost of capital of the investment bank results in less transparent disclosure by the issuer with high *ex ante* payoff uncertainty.

Finally, result (4) relates disclosure to market liquidity. A more liquid sec-

<sup>&</sup>lt;sup>1</sup>Recall from our definition of informativeness in Section 2.2, an inward (outward) shrunken range of posteriors  $(\mu, \overline{\mu})$  indicates less (more) informativeness of the system.

ondary market pushes the two threshold posteriors outward. In effect, higher liquidity is beneficial to the underwriter as it improves his trading profits. Hence at the margins, cut-off beliefs with relatively lower uncertainty are sufficient to make the underwriter just break-even by holding a stake. Also, the optimal disclosure reduces more uncertainty, rendering it more transparent if the prior is associated with high uncertainty. Result (4) implies a benefit of the market liquidity in that potentially a more liquid secondary market can push the issuer to design a more transparent disclosure system when issuing securities although this is not the complete story as we will see in the next section.

## 1.4.2 Demand Uncertainty (DU)

In this section, we extend the model by introducing the possibility of negative demand shock in the primary market. When demand shock happens, the securities are under-subscribed and the underwriting bank has to acquire additional shares to close the deal if he chooses to underwrite the issue. Note that the demand shock does not affect our secondary market equilibrium as well as the discounted issue price due to informed trading discussed in Section 3. We thus proceed with our analysis from T = 1 and then work backward to determine the optimal disclosure policy at T = 0.

Formally, we assume that if demand shock happens in the primary market, the demand for the issuer's security is only  $\psi$  which satisfies the following inequality:

$$0 < \psi < 1 - \frac{\phi}{1 + \phi}$$

Therefore, if the investment bank plans to retain a fraction  $\beta \leq \frac{\phi}{1+\phi}$ , the aggregate demand for the security will fall short of the supply (i.e.  $\beta+\psi<1$ ). We further assume that if initially the investment bank has entered into an agreement

to underwrite the issue, he has to acquire all of the remaining  $(1 - \psi)$  shares. Also, recall from Lemma 1 that with short sale constraint informed trading is feasible for the investment bank if and only if the fraction of his retention is at least  $\frac{\phi}{1+\phi}$  yet strictly less than 1, and the pricing of shares in the primary still follows Proposition 3.

More specifically, suppose that at T = 1 after the investment bank has agreed to underwrite and makes his initial retention plan  $\hat{\beta}$ ,

- a. with probability  $\epsilon \in (0, 1)$ , the total demand of shares by the participant investors is only  $\psi$ . So the investment bank has to acquire  $\beta = 1 - \psi$ . The issue price is  $P_0(1 - \psi, \mu_s)$ ;
- b. with probability  $(1 \epsilon)$ , there is no demand shock. The investment bank's ultimate retention is  $\beta = \hat{\beta}$  and the issue price is  $P_0(\hat{\beta}, \mu_s)$ .<sup>1</sup>

#### 1.4.2.1 Investment Bank's Optimal Decision II

In this scenarior, even if the investment bank initially decides to retain only  $\hat{\beta} = 0$ , the possible demand shock may force him to acquire more than he plans and depress his expected payoff below zero. Nevertheless, the investment bank has an exit option "Not Underwrite" to stay break-even. So the decision to underwrite is no longer trivial, and it depends crucially on the posteriors induced by the issuer's disclosure. We denote the investment bank's payoff by  $U_{IB}^2(\hat{\beta}, \mu_s)$ if he enters into the underwriting contract and makes his initial retention plan  $\hat{\beta}$ .

Consider the situation in which the investment bank chooses to underwrite. He needs to determine his initial retention plan  $\hat{\beta}$  to maximize his expected payoff before the demand uncertainty is resolved. With probability  $\epsilon$ , the demand shock

<sup>&</sup>lt;sup>1</sup>To avoid confusion, we use  $\beta$  and  $\hat{\beta}$  respectively to distinguish between the issuer's planned and ultimate retention.

happens and the investment bank has to buy  $(1 - \psi)$ . His expected payoff is:

$$A(1-\psi,\mu_s) \equiv (1-\psi)[(\mu_s\Delta V + V_L) - (1+r)P_0(1-\psi,\mu_s)] + \frac{\psi(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}.$$

With probability  $(1-\epsilon)$ , the demand shock does not occur, and the underwriter's payoff is the same as in the no demand uncertainty case:

$$\begin{split} B(\hat{\beta},\mu_s) &\equiv \hat{\beta} \cdot \left[ (\mu_s \Delta V + V_L) - (1+r) P_0(\hat{\beta},\mu_s) \right] \\ &+ \mathbf{1}_{\{\hat{\beta} \ge (1-\hat{\beta})\phi\}} \cdot \frac{(1-\hat{\beta})(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)} \end{split}$$

Therefore, after observing signal s, the investment bank has to first decide whether he will underwrite. If he underwrites, he further chooses a planned retention  $\hat{\beta}$ to maximize his expected payoff. Formally, he chooses his optimal action  $a_{IB}^*$  to solve the following maximization problem

$$\max_{a_{IB} \in \{\{\mathrm{NU}\}, \{\mathrm{U},\hat{\beta}\}\}} \mathbf{1}_{a_{IB} = \{\mathrm{U},\hat{\beta}\}} \cdot [\epsilon A(1-\psi,\mu_s) + (1-\epsilon)B(\hat{\beta},\mu_s)].$$

To derive the investment bank's optimal action, we first characterize the investment bank's optimal planned retention  $\hat{\beta}$  if he chooses to underwrite based on the observed signal in the proposition below.

**Proposition 8** (Investment bank's optimal planned retention): If the investment bank decides to underwrite, it is a dominant strategy for him to choose an initial retention  $\hat{\beta} = \frac{\phi}{1+\phi}$  before demand uncertainty is unraveled.

Proposition 8 implies that the investment bank's planned retention is independent of the issuer's disclosure. Such planned purchase serves as an insurance scheme against the demand uncertainty. The result can be understood in the following way. If demand shock happens, the investment bank is forced to complete

the deal by acquiring all the remaining  $(1 - \psi)$  shares. In this case any *ex ante* planned retention  $\hat{\beta} \leq 1 - \psi$  will not affect his expected payoff. Meanwhile, any initial stake that is larger than  $(1-\psi)$  is never optimal. As we have seen in Proposition 4, any stake  $\beta$  that is larger than  $\frac{\phi}{1+\phi}$  for the range of more uncertain beliefs  $(\mu,\overline{\mu})$  is sub-optimal in that it incurs more cost of capital while the informed trading profits become less owing to lower liquidity  $\phi(1-\beta)$ . Therefore, acquiring a stake that is larger than  $(1 - \psi)$  is even less desirable. When there is no demand shock, a retention which is just enough for the investment bank to camouflage as liquidity traders, i.e.  $\frac{\phi}{1+\phi}$ , is optimal as we have shown before. Consequently, it is optimal for the investment bank to choose an initial retention  $\hat{\beta} = \frac{\phi}{1+\phi}$ . In order for the investment bank to underwrite, his expected payoff should be at least zero. Compared with the cut-off posteriors  $\mu$  and  $\overline{\mu}$  before, it is obvious that the new thresholds satisfy  $\underline{\mu}^* > \underline{\mu}$  and  $\overline{\mu}^* < \overline{\mu}$ . It is because at the old posteriors the investment bank's expected payoff when demand shock happens, i.e.  $A(\mu_s)$ , will be strictly negative as a result of the higher-than-optimum retention  $(1 - \psi)$ . Thus only a larger lower bound  $\mu^*$  and a smaller upper bound  $\overline{\mu}^*$  will suffice to make the investment bank just break-even by accepting to underwrite.

Recall that  $U_{IB}^2(\hat{\beta}, \mu_s) \equiv \epsilon A(\mu_s) + (1 - \epsilon)B(\hat{\beta}, \mu_s)$  is the investment bank's expected payoff conditional on posterior  $\mu_s$  if he accepts to underwrite. Also,  $\hat{\beta}$  represents his planned retention before demand uncertainty is resolved. We summarize our discussion above in Lemma 3.

**Lemma 3** (Indifference cut-off posteriors II):

- 1. There exists a pair  $\{\underline{\mu}^*, \overline{\mu}^*\}$  with  $0 < \underline{\mu} < \underline{\mu}^* < \frac{1}{2} < \overline{\mu}^* < \overline{\mu} < 1$  such that  $U_{IB}^2(\frac{\phi}{1+\phi}, \underline{\mu}^*) = U_{IB}^2(\frac{\phi}{1+\phi}, \overline{\mu}^*) = 0.$
- 2.  $U_{IB}^2(\frac{\phi}{1+\phi},\mu_s) > 0$  if  $\mu_s \in (\underline{\mu}^*,\overline{\mu}^*)$ , and  $U_{IB}^2(\frac{\phi}{1+\phi},\mu_s) < 0$  if  $\mu_s \in [0,\underline{\mu}^*)$  or  $\mu_s \in (\overline{\mu}^*,1]$ .

Unlike before, if the investment bank's expected payoff is negative conditional on the observed signal s, he will choose not to underwrite. This happens when the induced posterior  $\mu_s$  lies in either  $[0, \underline{\mu}^*)$  or  $(\overline{\mu}^*, 1]$ . In general, the bank will not always underwrite, and he withdraws from underwriting when  $\mu_s \in$  $[0, \underline{\mu}^*) \cup (\overline{\mu}^*, 1]$ . Proposition 9 summarizes the investment bank's best response to different posteriors induced by the issuer's disclosure system and his equilibrium payoff given his optimal action.

**Proposition 9** (Investment bank's optimal strategy and relevant payoffs II): The investment bank's optimal action is

$$a_{IB}^*(\mu_s) = \begin{cases} Underwrite \ and \ \hat{\beta}^* = \frac{\phi}{1+\phi} & if \ \mu_s \in [\underline{\mu}^*, \overline{\mu}^*], \\ Not \ Underwrite & if \ \mu_s \in [0, \underline{\mu}^*) \cup (\overline{\mu}^*, 1]. \end{cases}$$

His equilibrium payoff is

$$\hat{U}_{IB}^2(\mu_s) = \begin{cases} U_{IB}^2(\frac{\phi}{1+\phi},\mu_s) & \text{if } \mu_s \in [\underline{\mu}^*,\overline{\mu}^*], \\ 0 & \text{if } \mu_s \in [0,\underline{\mu}^*) \cup (\overline{\mu}^*,1] \end{cases}$$

Since  $\hat{\beta}^*$  in equilibrium depends on the posterior  $\mu_s$  only, we can simply write the investment bank's expected payoff as  $\hat{U}_{IB}^2(\mu_s)$ , a function of  $\mu_s$  too. In Figure 1.6, the red dashed line depicts the investment bank's expected payoff given his optimal action  $a_{IB}^*$ , while the yellow solid line is his expected payoff if he sticks to a planned retention  $\hat{\beta} = \frac{\phi}{1+\phi}$  regardless of his posterior. For comparison, we also draw the investment bank's expected payoff if he always retains  $\frac{\phi}{1+\phi}$ shares when there is no demand uncertainty (i.e. the blue dashed line, which corresponds to the blue solid line in Figure 1.4). The yellow line is beneath the blue dashed one in that the presence of possible demand shock extracts a rent



Figure 1.6: The investment bank's payoff (ii)

from the investment bank thus decreases its expected payoff in general. In this case the two cut-off posteriors are less dispersed. Indeed, to induce the investment bank to underwrite, higher uncertainty in the primary market is needed. Then the losses due to unfortunate retention can be offset by larger trading profits from the underwriter's private information in the secondary market.

Accordingly, when the uncertainty in the primary market is relatively small (i.e.  $\mu_s \in [0, \underline{\mu}^*) \cup (\overline{\mu}^*, 1]$ ), the investment bank's private information is less valuable and on average he expects to suffer a loss from accepting to underwrite. His optimal strategy is to withdraw from underwriting the issue. Only when the uncertainty is relatively large (i.e.  $\mu_s \in [\underline{\mu}^*, \overline{\mu}^*]$ ) can the investment bank's expected loss from unfortunate retention be compensated by his informed trading profits owing to more valuable private information. In this case, he will agree to underwrite even though he may end up with more retention than he originally plans.

### 1.4.2.2 Optimal Disclosure System II

Since we have solved for the optimal strategy of the investment bank, it is easy to derive the issuer's expected proceeds from security issuance conditional on different signal realizations at T = 1.

**Proposition 10** (Issuer's payoff after information design II):

1. When  $\mu_s \in [0, \underline{\mu}^*) \cup (\overline{\mu}^*, 1]$ , the investment bank does not underwrite, and  $U_E^2(\mu_s) = 0.$ 

2. When 
$$\mu_s \in [\underline{\mu}^*, \overline{\mu}^*], U_E^2(\mu_s) \equiv U_E^2(\frac{\phi}{1+\phi}, \mu_s) = \epsilon P_0(1-\psi, \mu_s) + (1-\epsilon)P_0(\frac{\phi}{1+\phi}, \mu_s)$$
$$= \mu_s \Delta V + V_L - \frac{(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}.$$

The second part of Proposition 10 implies that the issue prices are the same under two different levels of retention by the investment bank,  $(1 - \psi)$  and  $\frac{\phi}{1+\phi}$ . This is because as long as the bank acquires a stake of at least  $\frac{\phi}{1+\phi}$ , the issue price will always have an adverse selection discount. Yet such discount does not vary with the investment bank's retention in that each participant investor's expected loss per share from trading in the secondary market is independent of the investment bank's ultimate stake  $\beta$ , a result that has already been shown in Proposition 2. From Proposition 10 it is easy to see that conditional on signal s, the issuer's expected revenue  $U_E^2(\hat{\beta}^*, \mu_s)$  depends on posterior  $\mu_s$  only, thus we denote it by  $U_E^2(\mu_s)$ .

At T = 0, taking into account the optimal action that will be taken by the investment bank at different posteriors, the issuer designs the disclosure system to maximize her expected payoff. In particular, she chooses a distribution of



Figure 1.7: The issuer's payoff (ii)

posteriors to solve

$$\begin{split} \hat{U}_{E}^{2}(\mu_{0}) &\equiv \max_{\{\mu_{\ell},\mu_{h}\}} \mathbb{E}_{\pi}[U_{E}^{2}(\mu_{s})] \\ \text{s.t.} \ a_{IB}^{*}(\mu_{s}) &= \max_{a_{IB} \in \{\{\mathbf{U},\hat{\beta}\}, \{\mathbf{NU}\}\}} \mathbf{1}_{\{a_{IB} = \{\mathbf{U},\hat{\beta}\}\}} \cdot U_{IB}^{2}(\hat{\beta},\mu_{s}), \\ \mathbb{P}[s = h] \cdot \mu_{h} + \mathbb{P}[s = \ell] \cdot \mu_{\ell} = \mu_{0}, \\ \mathbb{P}[s = h] + \mathbb{P}[s = \ell] = 1. \end{split}$$

The first constraint concerns the investment bank's optimal underwriting decision, and his planned retention if he chooses to underwrite. The second constraint is the Bayesian plausibility condition. The third constraint ensures that the sum of probabilities of high signal h and low signal  $\ell$  equals 1. We solve this constrained maximization problem by finding the concave closure of  $U_E^2(\mu_s)$ . In Figure 1.7 the black solid line depicts the issuer's expected payoff  $U_E^2(\mu_s)$  as characterized in Proposition 10. The blue dashed line is the concave closure of  $U_E^2(\mu_s)$ , which is denoted by  $\hat{U}_E^2(\mu_s)$ . Hence we can read off the optimal disclosure system directly from the graph. **Proposition 11** (Optimal information design II): At T = 0, the issuer's optimal disclosure policy is:

- 1. If  $\mu_s \in [0, \underline{\mu}^*)$ , the optimal disclosure system has  $\pi_B = \frac{\mu_0(1-\underline{\mu}^*)}{\underline{\mu}^*(1-\mu_0)}$  and  $\pi_G = 1$ , yielding posteriors  $\mu_\ell = 0$  and  $\mu_h = \mu^*$ .
- 2. If  $\mu_s \in (\underline{\mu}^*, \overline{\mu}^*)$ , the optimal disclosure system has  $\pi_G = \frac{\overline{\mu}^*(\mu_0 \underline{\mu}^*)}{\mu_0(\overline{\mu}^* \underline{\mu}^*)}$  and  $\pi_B = \frac{(1 \overline{\mu}^*)(\mu_0 \underline{\mu}^*)}{(1 \mu_0)(\overline{\mu}^* \underline{\mu}^*)}$ , yielding posteriors  $\mu_\ell = \underline{\mu}^*$  and  $\mu_h = \overline{\mu}^*$ .
- 3. If  $\mu_s \in (\overline{\mu}^*, 1]$ , the optimal disclosure system has  $\pi_B = \frac{\mu_0 \overline{\mu}^*}{\mu_0(1 \overline{\mu}^*)}$  and  $\pi_G = 0$ , yielding posteriors  $\mu_\ell = \overline{\mu}^*$  and  $\mu_h = 1$ .
- 4. If  $\mu_0 = \underline{\mu}^*$  or  $\overline{\mu}^*$ , the optimal disclosure system has  $\pi_G = \pi_B \in (0, 1)$ , and is therefore completely uninformative, yielding posteriors  $\mu_\ell = \mu_h = \mu_0$ .

Again, we have characterized the sender-preferred equilibrium. At the two cut-off posteriors  $\underline{\mu}^*$  and  $\overline{\mu}^*$ , the investment bank is indifferent between declining and underwriting with a planned retention  $\frac{\phi}{1+\phi}$ . Yet the latter is strictly preferred by the issuer in that she would otherwise fail to issue the security. So we assume that for the sake of the issuer's interest, the investment bank will underwrite when he is indifferent. Here the merit of strategic disclosure lies in that even though an *ex ante* prior  $\mu_0 \in (0, \underline{\mu}^*) \cup (\overline{\mu}^*, 1)$  implies failure of issuance owing to the investment bank's unwillingness to underwrite, the optimal disclosure policy is still able to induce the investment bank to underwrite with strictly positive probability. In this sense, strategic disclosure may solve the hold-up problem introduced by the demand shock in the primary market. The other advantage of this disclosure policy manifests in that when uncertainty is higher  $\mu_0 \in (\underline{\mu}^*, \overline{\mu}^*)$ , the expected issue-price discount is reduced compared with that under no informative disclosure, as is clear from the wedge between the blue dashed line and the black line in Figure 1.7.

Moreover, although the optimal disclosure reduces payoff uncertainty on average, with some particular signal realization, the uncertainty is actually enhanced. For instance, if the prior  $\mu_0 \in (0, \mu^*)$ , an h signal leads to a posterior belief of  $\underline{\mu}^*$ . Also,  $\underline{\mu}^*$  is more uncertain than  $\mu_0$  as it has higher entropy. When the signal realization is  $\ell$ , the disclosure is fully revealing and the underlying state is B. The same logic applies to posterior  $\overline{\mu}^*$  induced by signal  $\ell$  as it has higher entropy than  $\mu_0$  when  $\mu_0 \in (\overline{\mu}^*, 1)$ . Also, an h signal indicates that the state is G. Thanks to the Bayesian plausibility constraint, the strategic disclosure by the issuer can induce the investment bank to underwrite with positive probability and balances this with a worse belief that leaves the bank's underwriting decision unchanged, which generally improves the issuer's expected payoff. The optimal disclosure is such that on the one hand it induces the worst beliefs which lead to the investment bank's withdrawal from underwriting, and on the other hand it generates signals that make the investment bank just willing to underwrite at the other beliefs. At these beliefs that the underwrite chooses to underwrite, the security's uncertainty is in fact enhanced, and the underwriter's private information becomes sufficiently valuable, although on average the disclosure system reduces the uncertainty compared with the situation at the prior belief. In the meantime the issuer's expected proceeds from the issue is maximized. In this regard, the optimal disclosure features a mechanism in which the increased payoff uncertainty can offset the loss brought about by the demand uncertainty so that the investment bank will change to the better action that is favored by the issuer.

Nevertheless, a posterior of either  $\underline{\mu}^*$  or  $\overline{\mu}^*$  does not necessarily mean that the demand risk is alleviated. In fact it is entirely possible that the investment bank will acquire more than his planned retention eventually. Our result sheds some light on the empirically documented "Pipeline Risk" (or "Unfortunate Retention") in leveraged loan syndication by Bruche, Malherbe, and Meisenzahl (2018). We have shown that because of the issuer's disclosure policy, even in the presence of demand uncertainty a fully rational investment bank will still agree to underwrite. But when demand shock happens, the investment bank will suffer large losses as a result of excessive retention.

The next proposition provides some empirical predictions that relate the optimal disclosure to various aspects of the primary and secondary markets.

**Proposition 12** (Comparative statics II):

 $(1) \quad \frac{\partial \mu^{*}}{\partial \epsilon} > 0 \text{ and } \frac{\partial \overline{\mu}^{*}}{\partial \epsilon} < 0.$   $(2) \quad \frac{\partial \mu^{*}}{\partial \psi} < 0 \text{ and } \frac{\partial \overline{\mu}^{*}}{\partial \psi} > 0.$   $(3) \quad \frac{\partial \mu^{*}}{\partial V_{L}} > 0 \text{ and } \frac{\partial \overline{\mu}^{*}}{\partial V_{L}} < 0.$   $(4) \quad \text{Recall that } \eta = \frac{\Delta V}{V_{L}}, \text{ then } \frac{\partial \mu^{*}}{\partial \eta} < 0 \text{ and } \frac{\partial \overline{\mu}^{*}}{\partial \eta} > 0.$   $(5) \quad \frac{\partial \mu^{*}}{\partial r} > 0 \text{ and } \frac{\partial \overline{\mu}^{*}}{\partial r} < 0.$   $(6) \quad \frac{\partial \mu^{*}}{\partial \phi} < 0 \text{ and } \frac{\partial \overline{\mu}^{*}}{\partial \phi} > 0.$ 

From result (1), it is easy to see that as the probability of demand shock in the primary market becomes higher, the two cut-off posteriors shrink inward. So when the prior belief about the security's cash flow is relatively more uncertain (i.e.  $\mu_0 \in (\underline{\mu}^*, \overline{\mu}^*)$ ), higher likelihood of under-subscription results in less transparent disclosure designed by the issuer. Indeed, since the demand shock is more likely to occur in the primary market, in order for the investment bank to at least stay break-even from underwriting the issue, the disclosure should bring in more uncertainty so that his stake carries more trading value with his private information in the secondary market. Also, the additional informed trading profits can offset his expected loss from "unfortunate retention" due to demand shock. Anticipating this, the issuer will employ a relatively more opaque disclosure ex ante.

However, when the uncertainty about the security's payoff is relatively low (i.e.  $\mu_0 \in (0, \underline{\mu}^*)$  or  $\mu_0 \in (\overline{\mu}^*, 1)$ ), larger  $\epsilon$  leads to more transparent disclosure. In this case,  $\pi_B$  is smaller, suggesting that the *h* signal is more indicative of the good state and the  $\ell$  signal is more indicative of the bad state. As in this case, only a marginally higher payoff uncertainty will be enough to compensate for the additional expected loss due to higher probability of demand shock and make the unwilling bank to accept the deal again at the high-uncertainty posterior belief.

Result (2) contrasts with result (1) above: if demand shock happens, a stronger demand (larger  $\psi$ ), or equivalently, a smaller unfortunate retention (smaller  $(1 - \psi)$ ) by the underwriter, expands the two cut-off posteriors outward. Therefore, if demand shock happens, this in turn reduces the additional cost of capital incurred from the investment bank's unfortunate retention and increases his future trading profits thanks to more liquidity traders. As a result, when the *ex ante* payoff uncertainty is relatively large, a more transparent disclosure will be employed in equilibrium as in this case marginally less uncertain cut-off posteriors are enough to make the investment bank indifferent between whether or not to underwrite. Nevertheless, when *ex ante* uncertainty is relatively small, a higher  $\psi$  result in less transparent disclosure. Both lower  $\underline{\mu}$  and higher  $\overline{\mu}$  bring about less transparent disclosure systems for  $\mu_0 \in (0, \underline{\mu}^*)$  and  $\mu_0 \in (\overline{\mu}, 1)$  respectively. In both cases, due to Bayesian plausibility condition, the probabilities of full revelation will be smaller, and the probabilities of the more uncertain posteriors will be higher, making the systems less informative.

The dichotomy remains valid regarding result (3). Higher  $V_L$  (issue size or reservation value of the firm) expands the range of posterior beliefs  $(\underline{\mu}, \overline{\mu})$ . As  $V_L$  grows, it is more costly for the investment bank to underwrite and retain a positive stake. So when prior belief about the uncertainty of the security's payoff is relatively large, marginally more uncertain cut-off posteriors (i.e. higher  $\underline{\mu}$  and lower  $\overline{\mu}$ ) should be generated for the system so that the investment bank will be just willing to underwrite. Yet when the *ex ante* payoff uncertainty is relatively small, both higher  $\underline{\mu}$  and lower  $\overline{\mu}$  result in more transparent disclosure systems for  $\mu_0 \in (0, \underline{\mu}^*)$  and  $\mu_0 \in (\overline{\mu}, 1)$  respectively. So the probabilities of fully revealing states will be higher, and the probabilities of the more uncertain posteriors will be lower, rendering the systems more informative.

Result (4) asserts that higher growth option  $(\eta)$  gives rises to the expansion of  $(\underline{\mu}, \overline{\mu})$ . When prior belief about uncertainty is relatively large, as growth option improves, the investment bank will benefit more from his informed sales in the secondary market. Hence the optimal disclosure will be more informative as now marginally less uncertain cut-off posteriors are still able to induce the investment bank to underwrite. When the *ex ante* payoff uncertainty is relatively small, better growth option leads to less informative disclosure. The reasoning is similar to what we have discussed in result (3): less uncertain cut-off posteriors give rise to higher probabilities of high-uncertainty posteriors and lower probability of fully revealing signals. In addition, a less informative information disclosure arises naturally in equilibrium.

With the same token, result (5) states that higher r makes the disclosure system less informative when *ex ante* uncertainty is relatively high, but it leads to less informative disclosure when the uncertainty is relatively low. Higher opportunity cost per unit of investment by the bank makes him less willing to retain a positive stake at the old cut-off posteriors. To induce him to underwrite and compensate his additional cost of capital, posteriors with higher uncertainty must be generated from the optimal system.

Likewise, the implications of result (6) depend on the prior  $\mu_0$ . When the

ex ante payoff uncertainty is relatively high, a more liquid secondary market leads to more transparent disclosure. This is because better liquidity in the secondary market allows the underwriter to gain more from trading on his private information. Therefore, a more transparent system, although decreases the value of the investment bank's private information, is still able to make the investment bank just break-even by underwriting the deal. Yet when uncertainty about the firm is relatively low, the disclosure becomes less transparent as the secondary market liquidity increases. Recall that in order to change the investment bank's decision of not underwriting, the system should produce one particular signal which increases the payoff uncertainty to the extent that the investment bank is just willing to serve as an underwriter. As liquidity pumps up, the optimal disclosure only needs to generate a marginally less uncertain high-uncertainty posterior (higher  $\underline{\mu}^*$  or lower  $\overline{\mu}^*$ ) such that the bank still wants to underwrite. As a result the disclosure becomes less informative than before.

# 1.5 No Short Sale Constraint (NSS)

In this section, we briefly layout the equilibria by relaxing the previous assumption that the underwriter is not allowed to sell the security short in the secondary market. We also assume that short sale does not incur any other cost to the underwriter. As before, we divide into two scenarios: 1. the security can always be fully subscribed by the participant investors even in the absence of underwriter retention; and 2. there is demand uncertainty in the primary market. In face, in case 2, the results on the optimal disclosure we have obtained with short-selling constraint extend to the scenario without the ban on short sale.

### 1.5.1 No Demand Uncertainty (NDU)

We first consider the case in which there is neither demand uncertainty in the primary market nor ban on short sale in the secondary market. Since the demand for the security will never fall short of the supply, the investment bank is always willing to underwrite.

**Proposition 13** (Investment bank's optimal retention): It is optimal for the investment bank to retain zero stake in the primary market regardless of the signal realization (i.e.  $\beta^*(\mu_s) = 0$ ).

The intuition is fairly straightforward: recall from Part 1 of Proposition 2, the underwriting bank's informed trading profits are proportional to the fraction of liquidity traders  $(1 - \beta)\phi$ . Hence such profits are maximized at  $\beta = 0$  when the liquidity in the secondary market is maximized. Since now the underwriter can sell the security short, he no longer has to hold a stake, but is still able to camouflage as liquidity traders. Meanwhile, zero retention is optimal in the primary market in that any positive retention in the primary market would incur an opportunity cost for the investment bank while his gain per share from primary market underpricing is the same as his informed trading profit per share in the secondary market. Hence the investment bank's expected payoff is just his expected trading profits from the secondary market:

$$\hat{U}_{IB}^3(\mu_s) = U_{IB}^3(0,\mu_s) \equiv \frac{(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}.$$

Figure 1.8 depicts the investment bank's expected payoff as a function of the posterior belief  $\mu_s$ . Also, given the investment bank's zero retention and short-sale trading strategy, from Part 2 of Proposition 2 the issuer's expected proceeds



Figure 1.8: The investment bank's payoff (iii)

conditional on signal s at T = 1 is

$$U_E^3(\mu_s) \equiv (\mu_s \Delta V + V_L) - \frac{(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}.$$

To solve the optimal information design problem faced by the issuer at T = 0, it suffices to find the concave closure of  $U_E^3(\mu_s)$ , which we denote by  $\hat{U}_E^3(\mu_s)$ . In Figure 1.9, the black line represents  $U_E^3(\mu_s)$  and the blue dashed line is its concave closure  $\hat{U}_E^3(\mu_s)$ . Since  $U_E^3(\mu_s)$  is concave on the support of  $\mu_s$ , the optimal disclosure system is fully revealing.

**Proposition 14** (Optimal information design III): At T = 0, the issuer's optimal disclosure policy is completely informative, i.e.  $\pi_G = 1$  and  $\pi_B = 0$ , yielding posteriors  $\mu_{\ell} = 0$  and  $\mu_h = 1$ .

## 1.5.2 Demand Uncertainty (DU)

We next explore the scenario where there is demand uncertainty in the primary market.



Figure 1.9: The issuer's payoff (iii)

First suppose that the investment bank chooses to underwrite. Then if demand shock does not happen, the investment bank's optimal underwriting, retention and short selling strategy coincides with what we have obtained in the previous subsection. Yet if demand shock happens, the investment bank is forced to acquire a stake of  $(1 - \psi)$ . As he is able to short sell in the secondary market, his planned retention should still be zero before the demand uncertainty is unraveled. His expected payoff from underwriting with zero planned retention is

$$\begin{split} U_{IB}^4(0,\mu_s) \equiv \\ \epsilon \cdot \bigg\{ (1-\psi) \cdot \left[ (\mu_s \Delta V + V_L) - (1+r) P_0(1-\psi,\mu_s) \right] + \psi \cdot \frac{(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)} \bigg\} \\ + (1-\epsilon) \cdot \frac{(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}, \end{split}$$

where  $P_0(1 - \psi, \mu_s)$  is the issue price defined in Part 2 of Proposition 2. The first term above represents the investment bank's expected payoff if demand shock happens while the second is his expected payoff if the demand shock does not occur, both at posterior belief  $\mu_s$ . The second term is always strictly positive while the first one can be negative for some set of beliefs which are associated with low uncertainty.

Consequently, choosing to underwrite regardless of his posterior belief is not a best response for the investment bank. This is because when the *ex ante* uncertainty about the security's payoff is relatively small, the expected profits from trading on his private information are far from enough to cover the investment bank's opportunity cost of unfortunate retention. Although the bank can always enjoy a strictly positive payoff from short selling when the demand shock does not occur, the investment bank's expected payoff before the resolution of the demand uncertainty under these low-uncertainty beliefs will still be negative. As a result, the investment bank will shy away from underwriting the deal.

### **Lemma 4** (Indifference cut-off posteriors III):

- 1. There exists a pair  $\{\underline{\mu}^{**}, \overline{\mu}^{**}\}$  with  $0 < \underline{\mu}^{**} < \underline{\mu}^{*} < \frac{1}{2} < \overline{\mu}^{*} < \overline{\mu}^{**} < 1$  such that  $U_{IB}^{4}(0, \mu^{*}) = U_{IB}^{4}(0, \overline{\mu}^{**}) = 0$ .
- 2.  $U_{IB}^4(0,\mu_s) > 0$  if  $\mu_s \in (\underline{\mu}^{**}, \overline{\mu}^{**})$ , and  $\tilde{U}_{IB}(0,\mu_s) < 0$  if  $\mu_s \in [0,\underline{\mu}^{**})$  or  $\mu_s \in (\overline{\mu}^{**}, 1]$ .

**Proposition 15** (Investment bank's optimal strategy and relevant payoffs III): The investment bank's optimal action is

$$a_{IB}^*(\mu_s) = \begin{cases} \text{Underwrite and } \hat{\beta}^* = 0 & \text{if } \mu_s \in [\underline{\mu}^{**}, \overline{\mu}^{**}], \\ \text{Not Underwrite} & \text{if } \mu_s \in [0, \underline{\mu}^{**}) \cup (\overline{\mu}^{**}, 1] \end{cases}$$



Figure 1.10: The investment bank's payoff (iv)

His equilibrium payoff is

$$\hat{U}_{IB}^{4}(\mu_{s}) = \begin{cases} U_{IB}^{4}(0,\mu_{s}) & \text{if } \mu_{s} \in [\underline{\mu}^{**}, \overline{\mu}^{**}], \\ 0 & \text{if } \mu_{s} \in [0,\underline{\mu}^{**}) \cup (\overline{\mu}^{**}, 1]. \end{cases}$$

In Figure 1.10, the green line depicts  $U_{IB}^4(0, \mu_s)$  (i.e. the investment bank's expected payoff from underwriting with zero planned retention) while the red dashed line depicts the investment bank's expected payoff under his optimal underwriting and retention strategy. For comparison, the yellow dashed line is the investment bank's expected payoff by underwriting and retaining  $\frac{\phi}{1+\phi}$  when there is demand uncertainty yet short sale is not allowed, the scenario that we have discussed in Section 4.2. An interesting observation is that compared with before, even if the issuer does not disclosure additional information, there is a wider

range of beliefs under which the investment bank is willing to underwrite. This is because the feasibility of short sale by underwriter enables the investment bank to enjoy positive expected payoffs under two sets of relatively less uncertainty beliefs  $(\underline{\mu}^{**}, \underline{\mu}^{*})$  and  $(\overline{\mu}^{*}, \overline{\mu}^{**})$ . The removal of short sale constraint reduces the total cost of capital due to primary market retention to zero, yet allows the underwriter to trade more intensively on his private information. In turn the indifference cut-off posteriors only need to involve less uncertainty.

Given the optimal strategy of the investment bank, the next proposition follows naturally.

**Proposition 16** (Issuer's payoff after information design III):

- 1. When  $\mu_s \in [0, \underline{\mu}^{**}) \cup (\overline{\mu}^{**}, 1]$ , the investment bank does not underwrite, and  $U_E^4(\mu_s) = 0.$
- 2. When  $\mu_s \in [\underline{\mu}^{**}, \overline{\mu}^{**}], \ U_E^4(\mu_s) \equiv U_E^4(\hat{\beta}^* = 0, \mu_s) = (\mu_s \Delta V + V_L) \frac{(1-\mu_s)\mu_s(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma+(1-\mu_s)(1-\gamma)}.$

Concavification of  $U_E^4(\mu_s)$  gives us the optimal disclosure system designed by the issuer at T = 0, as illustrated in Figure 1.11.

**Proposition 17** (Optimal information design III): At T = 0, the issuer's optimal disclosure policy is:

- 1. If  $\mu_s \in [0, \underline{\mu}^{**})$ , the optimal disclosure system has  $\pi_B = \frac{\mu_0(1-\underline{\mu}^{**})}{\underline{\mu}^{**}(1-\mu_0)}$  and  $\pi_G = 1$ , yielding posteriors  $\mu_\ell = 0$  and  $\mu_h = \mu^{**}$ .
- 2. If  $\mu_s \in (\underline{\mu}^{**}, \overline{\mu}^{**})$ , the optimal disclosure system has  $\pi_G = \frac{\overline{\mu}^{**}(\mu_0 \underline{\mu}^{**})}{\mu_0(\overline{\mu}^{**} \underline{\mu}^{**})}$  and  $\pi_B = \frac{(1 \overline{\mu}^{**})(\mu_0 \underline{\mu}^{**})}{(1 \mu_0)(\overline{\mu}^{**} \underline{\mu}^{**})}$ , yielding posteriors  $\mu_\ell = \underline{\mu}^{**}$  and  $\mu_h = \overline{\mu}^{**}$ .
- 3. If  $\mu_s \in (\overline{\mu}^{**}, 1]$ , the optimal disclosure system has  $\pi_B = \frac{\mu_0 \overline{\mu}^{**}}{\mu_0(1 \overline{\mu}^{**})}$  and  $\pi_G = 0$ , yielding posteriors  $\mu_\ell = \overline{\mu}^{**}$  and  $\mu_h = 1$ .



Figure 1.11: The issuer's payoff (iv)

4. If  $\mu_0 = \underline{\mu}^{**}$  or  $\overline{\mu}^{**}$ , the optimal disclosure system has  $\pi_G = \pi_B \in (0, 1)$ , and is therefore completely uninformative, yielding posteriors  $\mu_\ell = \mu_h = \mu_0$ .

**Proposition 18** (Comparative statics III):

 $\begin{aligned} (1) \quad &\frac{\partial \underline{\mu}^{**}}{\partial \epsilon} > 0 \ and \ &\frac{\partial \overline{\mu}^{**}}{\partial \epsilon} < 0. \\ (2) \quad &\frac{\partial \underline{\mu}^{**}}{\partial \psi} < 0 \ and \ &\frac{\partial \overline{\mu}^{**}}{\partial \psi} > 0. \\ (3) \quad &\frac{\partial \underline{\mu}^{**}}{\partial V_L} > 0 \ and \ &\frac{\partial \overline{\mu}^{**}}{\partial V_L} < 0. \\ (4) \ Recall \ that \ \eta &= \frac{\Delta V}{V_L}, \ then \ &\frac{\partial \underline{\mu}^{**}}{\partial \eta} < 0 \ and \ &\frac{\partial \overline{\mu}^{**}}{\partial \eta} > 0. \\ (5) \quad &\frac{\partial \underline{\mu}^{**}}{\partial r} > 0 \ and \ &\frac{\partial \overline{\mu}^{**}}{\partial r} < 0. \\ (6) \quad &\frac{\partial \underline{\mu}^{**}}{\partial \phi} < 0 \ and \ &\frac{\partial \overline{\mu}^{**}}{\partial \phi} > 0. \end{aligned}$ 

Note that Proposition 17 and 18 are identical to what we have obtained in Proposition 11 and 12. Therefore, all the intuitions go through.

# **1.6 Welfare Analysis**

We have explored the four possible scenarios: 1. (No Short Sale, No Demand Uncertainty), 2. (No Short Sale, Demand Uncertainty), 3. (Short Sale, No Demand Uncertainty), and 4. (Short Sale, Demand Uncertainty). Now suppose that the economy is populated with a continuum of mass 1 issuers with their types  $\mu_0$  drawn from a uniform distribution U[0, 1], and each issuer invites an investment bank to underwrite.<sup>1</sup>

Let  $i \in \{1, 2, 3, 4\}$  denote one of the above four scenarios. Recall that  $U_E^i(\mu_0)$ is a type- $\mu_0$  issuer's expected payoff and  $\hat{U}_{IB}^i(\mu_0)$  is the relevant investment bank's expected payoff conditional on his prior (or equivalently if the issuer does not disclose additional information). Moreover,  $\hat{U}_E^i(\mu_0)$  is the type- $\mu_0$  issuer's maximized expected payoff under optimal disclosure system in scenario i.<sup>2</sup> Since the optimal disclosure always makes the investment bank just break-even at any of the posteriors induced by the signal generated from the optimal system, the investment bank's expected utility will be zero given the issuer's optimal disclosure strategy.

Therefore, if the issuers do not disclose additional information at T = 0, their welfare in scenario i is

$$W_E(i) \equiv \int_0^1 U_E^i(\mu_0) \, d\mu_0,$$

and the investment banks' welfare in scenario i is

$$W_{IB}(i) \equiv \int_0^1 \hat{U}_{IB}^i(\mu_0) \, d\mu_0.$$

<sup>&</sup>lt;sup>1</sup>Alternatively, assume that a generic issuer has type  $\mu_0 \sim U[0, 1]$ . Hence the welfare is just the issuer's expected payoff.

<sup>&</sup>lt;sup>2</sup>Note that we have already characterized  $U_E^i(\mu_0)$ ,  $U_{IB}^i(\mu_0)$ , and  $\hat{U}_E^i(\mu_0)$ , each corresponds to the issuer's expected payoff at T = 1 given the investment bank's best response (the black solid line in Figure 1.5, 1.7, 1.9, and 1.11), the investment bank's expected payoff at T = 1 with his optimal underwriting and retention decision (the red dashed line in Figure 1.4, 1.6, 1.8, and 1.10), and the issuer's expected payoff at T = 0 under the optimal disclosure system (the blue dashed line in Figure 1.5, 1.7, 1.9, and 1.11).

The issuers' welfare with their optimal disclosure policies in scenario i is

$$\hat{W}_E(i) \equiv \int_0^1 \hat{U}_E^i(\mu_0) \, d\mu_0$$

We first look at the investment banks' welfare if the issuers do not disclose any informative signal. The ranking of their welfare in the four scenarios depends on the probability of demand shocks  $\epsilon$ .

**Proposition 19** (Investment banks' welfare):

(1) When  $0 < \epsilon < \frac{\phi}{(1-\psi)(1+\phi)}$ ,

(	) <u>µ</u> *	** /	<u>ι</u> μ	<u>ı</u> *		$\overline{\mu}^*$	$\overline{\mu}$	$\overline{\mu}^{**}1$	• μ <sub>s</sub>

 $W_{IB}(SS, NDU) > W_{IB}(SS, DU) > W_{IB}(NSS, NDU) > W_{IB}(NSS, DU).$ 

(2) When 
$$\frac{\phi}{(1-\psi)(1+\phi)} < \epsilon < 1$$
,  

$$0 \quad \underline{\mu} \quad \underline{\mu}^{**} \quad \underline{\mu}^{*} \qquad \overline{\mu} \quad \overline{\mu}^{*} \quad \overline{\mu}^{**} \quad 1 \quad \mu_{s}$$

$$W \quad (\Omega \subseteq NDU) > W \quad (N \subseteq \Omega \setminus DU) > W$$

 $W_{IB}(SS, NDU) > W_{IB}(NSS, NDU) > W_{IB}(SS, DU) > W_{IB}(NSS, DU).$ 

(3) When 
$$\epsilon = \frac{\phi}{(1-\psi)(1+\phi)}$$
,

 $0 \quad \underline{\mu} = \underline{\mu}^{**} \quad \underline{\mu}^{*} \qquad \overline{\mu}^{*} \quad \overline{\mu} = \overline{\mu}^{**} \quad 1 \quad \mu_{s}$ 

$$W_{IB}(SS, NDU) > W_{IB}(NSS, NDU) = W_{IB}(SS, DU) > W_{IB}(NSS, DU).$$

The red, blue, and black cut-offs posteriors represent the threshold beliefs that make the investment bank just break-even as an underwriter in scenarios (SS, DU), (NSS,NDU), and (NSS, DU) respectively. Also, {0,1} are relevant

beliefs in scenario (SS,NDU). In general, the more dispersed the cut-off posteriors, the better off the investment banks as a whole. (NSS,DU) is the least desirable. This is because demand uncertainty gives rise to possible unfortunate retention by the investment banks. Furthermore, the ban on short sale forces the investment bank to retain a stake so that he can trade strategically. Yet his stake incurs additional cost of bank capital. In contrast, (SS,NDU) renders the investment banks the highest welfare in that they can always sell the security short to gain informed trading profits in the secondary market while they do not have to acquire any stake in the primary market. The comparison between the welfare of the remaining two scenarios is more involved. When  $\epsilon$  is small (Case (1)), the investment banks' welfare is still higher if short sale is allowed compared to the scenario where there is no demand uncertainty but short selling is banned. Yet when  $\epsilon$  is large (Case (2)), the investment banks are strictly better off without demand uncertainty even if short sale is prohibited. The trade-off hinges on whether the gain brought about by short sale is able to compensate for the loss due to the demand shock.

Finally, we summarize the rankings of the issuers' welfare in the next proposition.

**Proposition 20** (Issuers' Welfare): If the issuers do not disclosure additional information, their welfare have the following ranking:

 $W_E(NSS, NDU) > W_E(SS, NDU) > W_E(SS, DU) > W_E(NSS, DU).$ 

Yet if they use Bayesian persuasion to maximize their expected proceeds,

$$\hat{W}_E(NSS, NDU) = \hat{W}_E(SS, NDU) > \hat{W}_E(SS, DU) > \hat{W}_E(NSS, DU).$$



Figure 1.12: The entrepreneur's expected payoff

A graphical illustration of Proposition 20 is given in Figure 1.12. The proposition asserts that if issuers do not reveal informative signals, they achieve the highest welfare when there is no demand uncertainty in the primary market and short sale is not allowed in the secondary market. A primary market without demand uncertainty along with a short selling ban in the secondary market delivers the issuers the second highest welfare. They are worse off if demand shocks may happen in the primary market and underwriters are allowed to sell the security short. Their welfare is the lowest if it is probable that the security will be under-subscribed by participant investors in the primary market and there is short sale constraint in the secondary market. From the perspective of the issuers, they strictly prefer a primary market that has no demand uncertainty. Then the investment banks are always willing to underwrite, and the issuers can sell off their securities with certainty. Absent any possibility of demand shocks, they prefer a secondary market where underwriters are prohibited from short selling the securities. However, if demand is uncertain, the option of short sale allows the
investment banks to reduce the opportunity cost associated with primary market retention and gain more from informed trading when demand shocks do not happen. This induces more banks to underwrite and thus enables more issuers to successfully issue their securities.

Under the issuers' optimal persuasion mechanisms, most parts of the ranking remain the same. They still dislike demand uncertainty in the primary market. However, with strategic disclosure the issuers will be indifferent between whether or not there is short sale constraint if there is no demand uncertainty. In both scenarios, the aim of the optimal disclosure is to discourage the investment bank from trading on his private information in the secondary market. To achieve this goal the optimal disclosure needs to be fully informative if short sale is allowed in the secondary market while a partially informative disclosure suffices to do the job if there is the short-sale ban.

## 1.7 Conclusion

This paper presents a novel Bayesian persuasion model of security offering and trading with issuer's strategic disclosure. We show that disclosure can be used to boost the issue's expected revenue, mitigate underpricing resulting from underwriter's informed trading, and increase the likelihood of security issue even when demand is weak and underwriters may shy away. On average, the optimal disclosure reduces the uncertainty of the security's payoff. Nevertheless, full transparency is not always optimal. Signal realizations that introduce more uncertainty can potentially solve the hold-up problem brought about by demand uncertainty. In general, the optimal information design depends crucially on the *ex ante* level of payoff uncertainty. We provide new empirical predictions which relate the informativeness of the optimal disclosure to the issue size and the is-

suer's growth option, the underwriter's cost of capital, the uncertainty about demand, and the secondary market liquidity. Moreover, the underwriter in our model can be viewed as an existing blockholder in the firm who makes decision on whether to support and participate in a security issue (e.g. seasoned debt/equity offering). We show that the blockholder, by participating, may exert governance by exit to push the firm to disclose more transparent information. In sum, corporate finance application of information design theory appears to be a promising topic to work on. Future work can be done by extending our model with issuer's moral hazard and signal manipulation as well as investors' information acquisition. Empirical side, textually analysis of the information memoranda and the prospectuses in both debt and equity issuance can be performed to test the new empirical predictions generated from our model.

## 1.8 Appendix

**Proof of Proposition 1.** Suppose that the investment bank trades x when the state is G, and z when the state is B. He incurs additional cost of capital if he further acquires shares in the secondary market (i.e. either x > 0 or z > 0). Also, recall that  $u \equiv (1 - \beta)\phi$ .

	State	Liq. Sh.	$\tilde{v}$	Prob.	$x_{PI}$	$x_{IB}$	y
(I).	G	Yes	$V_H$	$\mu_s\gamma$	-u	x	$y_I \equiv -u + x$
(II).	G	No	$V_H$	$\mu_s(1-\gamma)$	0	x	$y_{II} \equiv x$
(III).	B	Yes	$V_L$	$(1-\mu_s)\gamma$	-u	z	$y_{III} \equiv -u + z$
(IV).	B	No	$V_L$	$(1-\mu_s)(1-\gamma)$	0	z	$y_{IV} \equiv z$

To camouflage as liquidity traders, the investment bank has to design his trading strategy such that two of the above four scenarios have the same aggregate order flows. This gives four possibilities:  $y_I = y_{III}$  (i.e. -u+x = -u+z),  $y_I = y_{IV}$ (i.e. -u+x = z),  $y_{II} = y_{III}$  (i.e. x = -u+z) or  $y_{II} = y_{IV}$  (i.e. x = z). Note that the first and the last coincide. Hence we investigate the following three cases: 1. x = z, 2. z = -u + x, and 3. z = u + x.

Case 1. x = z:

	State	Liq. Sh.	Prob.	$x_{PI}$	$x_{IB}$	y	$P_1$
(I).	G	Yes	$\mu_s\gamma$	-u	x	-u+x	$\frac{\mu_s \gamma \Delta V}{\mu_s \gamma + (1 - \mu_s) \gamma} + V_L$
(II).	G	No	$\mu_s(1-\gamma)$	0	x	x	$\frac{\frac{\mu_s(1-\gamma)\Delta V}{\mu_s(1-\gamma)+(1-\mu_s)(1-\gamma)}}{+V_L}$
(III).	B	Yes	$(1-\mu_s)\gamma$	-u	x	-u+x	$\frac{\mu_s \gamma \Delta V}{\mu_s \gamma + (1 - \mu_s) \gamma} + V_L$
(IV).	В	No	$(1-\mu_s)(1-\gamma)$	0	x	x	$\frac{\mu_s(1-\gamma)\Delta V}{\mu_s(1-\gamma)+(1-\mu_s)(1-\gamma)} + V_L$

It is easy to see that  $P_1 = \mu_s \Delta V + V_L$  since the net order flows are only indicative of whether or not there is liquidity shock, but reveals no information concerning the underlying state due to the investment bank's consistent trading strategy regardless of his private information. So the market maker will set a price to the intrinsic value of the security conditional on the posterior belief  $\mu_s$ . The investment bank's expected payoff from this trading strategy is

$$\begin{split} \mathbb{E}_{s}[\Pi_{1}] &= [V_{H} - (\mu_{s}\Delta V + V_{L})][\mu_{s}\gamma + \mu_{s}(1-\gamma)]x \\ &+ [V_{L} - (\mu_{s}\Delta V + V_{L})][(1-\mu_{s})\gamma + (1-\mu_{s})(1-\gamma)]x - \mathbf{1}_{\{x>0\}} r(\mu_{s}\Delta V + V_{L})x \\ &= -\mathbf{1}_{\{x>0\}} r(\mu_{s}\Delta V + V_{L})x \\ &\leq 0. \end{split}$$

Case 2. z = -u + x:

	State	Liq. Sh.	Prob.	$x_{PI}$	$x_{IB}$	y	$P_1$
(I).	G	Yes	$\mu_s\gamma$	-u	x	-u+x	$\frac{\mu_s \gamma \Delta V}{\mu_s \gamma + (1 - \mu_s)(1 - \gamma)} + V_L$
(II).	G	No	$\mu_s(1-\gamma)$	0	x	x	$V_H$
(III).	B	Yes	$(1-\mu_s)\gamma$	-u	-u+x	-2u + x	$V_L$
(IV).	В	No	$(1-\mu_s)(1-\gamma)$	0	-u+x	-u+x	$\frac{\mu_s \gamma \Delta V}{\mu_s \gamma + (1 - \mu_s)(1 - \gamma)} + V_L$

The investment bank's expected trading profits from this trading strategy are

 $\mathbb{E}_{s}[\Pi_{2}]$ 

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$$= \left( V_{H} - \frac{\mu_{s}\gamma\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} - V_{L} \right) \mu_{s}\gamma x \\ + \left( V_{L} - \frac{\mu_{s}\gamma\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} - V_{L} \right) (1-\mu_{s})(1-\gamma)(-u+x) \\ - \mathbf{1}_{\{x>0\}} rx \left[ \mu_{s}\gamma \frac{\mu_{s}\gamma\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} + V_{L} + \mu_{s}(1-\gamma)V_{H} \right] \\ - \mathbf{1}_{\{-u+x>0\}} r(-u+x) \left[ (1-\mu_{s})\gamma V_{L} + (1-\mu_{s})(1-\gamma) \left( \frac{\mu_{s}\gamma\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} + V_{L} \right) \right] \\ = \frac{\mu_{s}\gamma(1-\mu_{s})(1-\gamma)\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} \cdot u - \mathbf{1}_{\{x>0\}} rx \left[ \mu_{s}\gamma \frac{\mu_{s}\gamma\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} + V_{L} + \mu_{s}(1-\gamma)V_{H} \right] \\ - \mathbf{1}_{\{-u+x>0\}} r(-u+x) \left[ (1-\mu_{s})\gamma V_{L} + (1-\mu_{s})(1-\gamma) \left( \frac{\mu_{s}\gamma\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} + V_{L} \right) \right] \\ \leq \frac{\mu_{s}\gamma(1-\mu_{s})(1-\gamma)\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} \cdot u.$$

In this case, it is optimal to set x = 0 and z = -u such that the investment bank can achieve the maximal expected trading profits  $\frac{\mu_s \gamma (1-\mu_s)(1-\gamma)\Delta V}{\mu_s \gamma + (1-\mu_s)(1-\gamma)} \cdot u$  while do not incur additional cost of capital from acquiring shares in the secondary market. It is an informed sales equilibrium where the investment bank only sell his stake when his private information is unfavorable. Moreover, such trading strategy is sequentially rational as well.

Finally, we consider Case 3. (z = u + x):

	State	Liq. Sh.	Prob.	$x_{PI}$	$x_{IB}$	y	$P_1$
(I).	G	Yes	$\mu_s\gamma$	-u	x	-u+x	$V_H$
(II).	G	No	$\mu_s(1-\gamma)$	0	x	x	$\frac{\mu_s(1-\gamma)\Delta V}{\mu_s(1-\gamma)+(1-\mu_s)\gamma} + V_L$
(III).	B	Yes	$(1-\mu_s)\gamma$	-u	u + x	x	$\frac{\mu_s(1-\gamma)\Delta V}{\mu_s(1-\gamma)+(1-\mu_s)\gamma} + V_L$
(IV).	B	No	$(1-\mu_s)(1-\gamma)$	0	u + x	u + x	$V_L$

His relevant expected trading profits are

 $\mathbb{E}_{s}[\Pi_{3}]$ 

$$= \left[ V_{H} - \frac{\mu_{s}(1-\gamma)\Delta V}{\mu_{s}(1-\gamma) + (1-\mu_{s})\gamma} - V_{L} \right] \mu_{s}(1-\gamma)x \\ + \left[ V_{L} - \frac{\mu_{s}(1-\gamma)\Delta V}{\mu_{s}(1-\gamma) + (1-\mu_{s})\gamma} - V_{L} \right] (1-\mu_{s})\gamma x \\ - \mathbf{1}_{\{x>0\}} rx \left[ \mu_{s}\gamma V_{H} + \mu_{s}(1-\gamma) \left( \frac{\mu_{s}(1-\gamma)\Delta V}{\mu_{s}(1-\gamma) + (1-\mu_{s})\gamma} + V_{L} \right) \right] \\ - \mathbf{1}_{\{x+u>0\}} r(x+u) \left[ (1-\mu_{s})\gamma \left( \frac{\mu_{s}(1-\gamma)\Delta V}{\mu_{s}(1-\gamma) + (1-\mu_{s})(1-\gamma)} + V_{L} \right) + (1-\mu_{s})\gamma V_{L} \right] \\ \leq - \mathbf{1}_{\{x>0\}} rx \left[ \mu_{s}\gamma V_{H} + \mu_{s}(1-\gamma) \left( \frac{\mu_{s}(1-\gamma)\Delta V}{\mu_{s}(1-\gamma) + (1-\mu_{s})\gamma} + V_{L} \right) \right] \\ - \mathbf{1}_{\{x+u>0\}} r(x+u) \left[ (1-\mu_{s})\gamma \left( \frac{\mu_{s}(1-\gamma)\Delta V}{\mu_{s}(1-\gamma) + (1-\mu_{s})(1-\gamma)} + V_{L} \right) + (1-\mu_{s})\gamma V_{L} \right] \\ \leq 0.$$

This strategy is obviously suboptimal.

In sum, the investment bank's optimal trading strategy is  $x_{IB} = 0$  in state G and  $x_{IB} = -u$  in state B. This gives the equilibrium characterized in Proposition 1.

### Proof of Lemma 2.

$$\begin{split} U_{IB}^{1}(\frac{\phi}{1+\phi},\mu_{s}) \\ &= \frac{\phi}{1+\phi} \left[ (\mu_{s}\Delta V + V_{L}) - (1+r)P_{0}(\frac{\phi}{1+\phi},\mu_{s}) \right] + \frac{1}{1+\phi} \cdot \frac{(1-\mu_{s})\mu_{s}(1-\gamma)\gamma\phi\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} \\ &= \frac{\phi}{1+\phi} \cdot \left[ -r(\mu_{s}\Delta V + V_{L}) + (1+r) \cdot \frac{\mu_{s}(1-\mu_{s})\gamma(1-\gamma)\phi\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} \right] \\ &+ \frac{1}{1+\phi} \cdot \frac{\mu_{s}(1-\mu_{s})\gamma(1-\gamma)\phi\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} \\ &= \frac{\phi}{1+\phi} \cdot \{ -r \mathbb{E}_{s}[\tilde{v}] + (1+r)\Delta P \} + \frac{1}{1+\phi} \cdot \Delta P \\ &= -\frac{r\phi}{1+\phi} \cdot \mathbb{E}_{s}[\tilde{v}] + \left(1 + \frac{r\phi}{1+\phi}\right) \cdot \Delta P. \end{split}$$

Note that

$$\frac{\partial \mathbb{E}_s[\tilde{v}]}{\partial \mu_s} = \frac{\partial (\mu_s \Delta V + V_L)}{\partial \mu_s} = \Delta V, \qquad \frac{\partial^2 \mathbb{E}_s[\tilde{v}]}{\partial \mu_s^2} = 0,$$

and

$$\begin{aligned} \frac{\partial \Delta P}{\partial \mu_s} &= \frac{\partial}{\partial \mu_s} \left( \frac{\mu_s (1-\mu_s)\gamma(1-\gamma)\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)} \right) \\ &= \gamma(1-\gamma)\phi\Delta V \cdot \frac{(1-2\gamma)\mu_s^2 - 2(1-\gamma)\mu_s + (1-\gamma)}{[\mu_s\gamma + (1-\mu_s)(1-\gamma)]^2}. \end{aligned}$$

Moreover,

$$\frac{\partial^2 \Delta P}{\partial \mu_s^2} = \gamma (1-\gamma) \phi \Delta V \cdot \frac{-2\gamma (1-\gamma)}{[\mu_s \gamma + (1-\mu_s)(1-\gamma)]^3} < 0.$$

Therefore

$$\frac{\partial U_{IB}^1}{\partial \mu_s} = -\frac{r\phi\Delta V}{1+\phi} + \left(1 + \frac{r\phi}{1+\phi}\right) \cdot \frac{\gamma(1-\gamma)\phi\Delta V[(1-2\gamma)\mu_s^2 - 2(1-\gamma)\mu_s + (1-\gamma)]}{[\mu_s\gamma + (1-\mu_s)(1-\gamma)]^2},$$

and

$$\frac{\partial^2 U_{IB}^1}{\partial \mu_s^2} = \left(1 + \frac{r\phi}{1+\phi}\right) \cdot \left(\frac{\partial^2 \Delta P}{\partial \mu_s^2}\right) < 0,$$

i.e.  $U_{IB}^1$  is concave and  $\partial U_{IB}^1 / \partial \mu_s$  is decreasing in  $\mu_s \in (0, 1)$ .

To ensure that the interior optimum is attained at some  $\mu^* \in (0, 1)$ , the following must be satisfied:

$$\frac{\partial U_{IB}^1}{\partial \mu_s}\Big|_{\mu_s=0} = -\frac{r\phi\Delta V}{1+\phi} + \left(1+\frac{r\phi}{1+\phi}\right)\gamma\phi\Delta V > 0;$$
$$\frac{\partial U_{IB}^1}{\partial \mu_s}\Big|_{\mu_s=1} = -\frac{r\phi\Delta V}{1+\phi} - \left(1+\frac{r\phi}{1+\phi}\right)(1-\gamma)\phi\Delta V < 0.$$

The first implies that  $r < \frac{\gamma(1+\phi)}{1-\gamma\phi}$  while the second is always satisfied. Then  $\partial U_{IB}^1/\partial \mu_s = 0$  when  $\mu_s = \mu^*$ . Also, for  $\mu_s \in [0, \mu^*)$ ,  $\partial U_{IB}^1/\partial \mu_s > 0$  yet  $\partial U_{IB}^1/\partial \mu_s < 0$  for  $\mu_s \in (\mu^*, 1]$ . Therefore,  $U_{IB}^1$  is single-peaked and has a hump shape on [0, 1].

Since from above we know that

$$U_{IB}^{1}\left(\frac{\phi}{1+\phi},\mu_{s}\right) = -\frac{r\phi}{1+\phi}\cdot\left(\mu_{s}\Delta V + V_{L}\right) + \left(1+\frac{r\phi}{1+\phi}\right)\cdot\frac{(1-\mu_{s})\mu_{s}(1-\gamma)\gamma\phi\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)},$$

it is obvious that there always exists a set of  $\mu_s \in (0, 1)$  such that  $U_{IB}^1(\frac{\phi}{1+\phi}, \mu_s) > 0$  as long as r is not too large. In particular, we impose that for  $\mu_s = \frac{1}{2}$ ,  $U_{IB}^1(\frac{\phi}{1+\phi}, \frac{1}{2}) > 0$ . This implies  $r < \frac{\gamma(1-\gamma)(1+\phi)\Delta V}{\Delta V-\gamma(1-\gamma)\phi\Delta V+2V_L}$ . Therefore,  $0 < r < \min\{\frac{\gamma(1+\phi)}{1-\gamma\phi}, \frac{\gamma(1-\gamma)(1+\phi)\Delta V}{\Delta V-\gamma(1-\gamma)\phi\Delta V+2V_L}\}$ , i.e.  $r \in (0, \frac{\gamma(1-\gamma)(1+\phi)\Delta V}{\Delta V-\gamma(1-\gamma)\phi\Delta V+2V_L})$ .

In the meantime,  $U_{IB}^{1}(\frac{\phi}{1+\phi}, 0) = -\frac{\phi r V_{L}}{1+\phi} < 0$  and  $U_{IB}^{1}(\frac{\phi}{1+\phi}, 1) = -\frac{\phi r (\Delta V + V_{L})}{1+\phi} < 0$ 

0. Hence there must be a pair of  $\{\underline{\mu}, \overline{\mu}\}$  with  $0 < \underline{\mu} < \frac{1}{2} < \overline{\mu} < 1$  such that  $U_{IB}^1(\frac{\phi}{1+\phi}, \underline{\mu}) = U_{IB}^1(\frac{\phi}{1+\phi}, \overline{\mu}) = 0$ . In addition,  $U_{IB}^1(\frac{\phi}{1+\phi}, \mu_s) > 0$  if  $\mu_s \in (\underline{\mu}, \overline{\mu})$ , and  $U_{IB}^1(\frac{\phi}{1+\phi}, \mu_s) < 0$  if  $\mu_s \in [0, \underline{\mu}) \cup (\overline{\mu}, 1]$ .

Last but not least, it follows naturally that  $\partial U_{IB}^1/\partial \mu_s > 0$  at  $\mu_s = \underline{\mu}$  but  $\partial U_{IB}^1/\partial \mu_s < 0$  at  $\mu_s = \overline{\mu}$ , an important observation that will be useful to calculate the comparative statics of the optimal disclosure later.

**Proof of Proposition 4.** When  $\beta \in [\frac{\phi}{1+\phi}, 1)$ , there will be discount in the issue price. Also,

$$U_{IB}^1(\beta,\mu_s) = \beta\{-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P\} + (1-\beta)\Delta P.$$

Note that  $\{-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P\} - \Delta P$ 

$$= -r(\mathbb{E}_{s}[\tilde{v}] - \Delta P)$$
  
=  $-r\left[V_{L} + \mu_{s}\Delta V \cdot \frac{\mu_{s}\gamma + (1 - \mu_{s})(1 - \gamma)(1 - \gamma\phi)}{\mu_{s}\gamma + (1 - \mu_{s})(1 - \gamma)}\right]$   
< 0.

Hence to maximize  $U_{IB}^1(\beta, \mu_s)$ , we want  $(1 - \beta)$  to be as large as possible. This is achieved by choosing the smallest  $\beta = \frac{\phi}{1+\phi}$  such that informed trading is still feasible. Also, it is easy to see that  $U_{IB}^1(\frac{\phi}{1+\phi}, \mu_s) > U_{IB}^1(1^-, \mu_s)$  for all  $\mu_s \in (0, 1)$ . So in equilibrium, stake  $\frac{\phi}{1+\phi}$  strictly dominates stake 1<sup>-</sup>. Moreover, we know that for  $\beta = 0$ ,  $U_{IB}^1(0, \mu_s) = 0$ , and for  $\beta = 1$ ,  $U_{IB}^1(1, \mu_s) < 0$ . So  $\beta = 0$  strictly dominates  $\beta = 1$ . To characterize the investment bank's optimal retention at posterior belief  $\mu_s$ , it suffices to compare  $U_{IB}^1(0, \mu_s)$  with  $U_{IB}^1(\frac{\phi}{1+\phi}, \mu_s)$ . From

Lemma 2, it follows that the investment bank's optimal stake is

$$\beta^* = \begin{cases} \frac{\phi}{1+\phi} & \text{if } \mu_s \in (\underline{\mu}, \overline{\mu}), \\ 0 & \text{if } \mu_s \in [0, \underline{\mu}] \cup [\overline{\mu}, 1] \end{cases}$$

His equilibrium payoff is

$$\hat{U}_{IB}^{1}(\mu_{s}) = \begin{cases} U_{IB}^{1}(\frac{\phi}{1+\phi},\mu_{s}) & \text{if } \mu_{s} \in (\underline{\mu},\overline{\mu}), \\ 0 & \text{if } \mu_{s} \in [0,\underline{\mu}] \cup [\overline{\mu},1] \end{cases}$$

Q.E.D.

**Proof of Proposition 5.** From Proposition 4 we know that the investment bank will hold a positive stake  $\frac{\phi}{1+\phi}$  only when  $\mu_s \in (\underline{\mu}, \overline{\mu})$ . So for this set of posterior beliefs, there will be informed trading by the bank and thus an adverse selection discount in the issue price. The issuer's expected proceeds are

$$U_E^1(\mu_s) = \mu_s \Delta V + V_L - \frac{\mu_s(1-\mu_s)\gamma(1-\gamma)\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}.$$

At any other posterior belief, the investment bank retains zero stake and cannot engage in informed trading. The issue price will just be the intrinsic value of the security, i.e.

$$U_E^1(\mu_s) = \mu_s \Delta V + V_L$$

Q.E.D.

**Proof of Proposition 6.** At any prior belief  $\mu_0 \in [0, \underline{\mu}] \cup [\overline{\mu}, 1]$ , a sender-preferred equilibrium prescribes that the investment bank should not retain any shares. In this case, the issue price will be the expected value of the cash flows from the security with no discount. Thus the issuer does not benefit from persuasion and

the optimal disclosure system should be completely uninformative, i.e  $\pi_G = \pi_B \in (0, 1)$ , yielding posteriors  $\mu_\ell = \mu_h = \mu_0$ .

At prior belief  $\mu_0 \in (\underline{\mu}, \overline{\mu})$ , the investment bank holds a strictly positive stake, and there will be a discounted associated with the issue price. The issuer's expected payoff under any Bayesian plausible posteriors  $\mu_h$  and  $\mu_\ell$  is

$$\mathbb{E}_{\pi}[U_E^1(\mu_s)]$$

$$= \mathbb{E}_{\pi} [\mathbf{1}_{\{\mu_{0} \in [0,\underline{\mu}] \cup [\overline{\mu},1]\}} \cdot (\mu_{s} \Delta V + V_{L}) + \mathbf{1}_{\{\mu_{0} \in (\underline{\mu},\overline{\mu})\}} (\mu_{s} \Delta V + V_{L} - \Delta P)]$$

$$= \mathbb{P}[\mu_{h}] \cdot [\mathbf{1}_{\{\mu_{h} \in [0,\underline{\mu}] \cup [\overline{\mu},1]\}} \cdot (\mu_{h} \Delta V + V_{L}) + \mathbf{1}_{\{\mu_{h} \in (\underline{\mu},\overline{\mu})\}} (\mu_{h} \Delta V + V_{L} - \Delta P)]$$

$$+ \mathbb{P}[\mu_{\ell}] \cdot [\mathbf{1}_{\{\mu_{\ell} \in [0,\underline{\mu}] \cup [\overline{\mu},1]\}} \cdot (\mu_{\ell} \Delta V + V_{L}) + \mathbf{1}_{\{\mu_{\ell} \in (\underline{\mu},\overline{\mu})\}} (\mu_{\ell} \Delta V + V_{L} - \Delta P)]$$

$$\leq \mathbb{P}(\mu_{h}) (\mu_{h} \Delta V + V_{L}) + \mathbb{P}(\mu_{\ell}) (\mu_{\ell} \Delta V + V_{L}),$$

where the last inequality is satisfied with if  $\mu_{\ell} \in [0, \underline{\mu}], \ \mu_h \in [\overline{\mu}, 1]$  and  $\mathbb{P}(\mu_h)\mu_h + \mathbb{P}(\mu_{\ell}) = \mu_0$ . Hence the least informative optimal disclosure yields posteriors  $\mu_{\ell} = \underline{\mu}$  and  $\mu_h = \overline{\mu}$ . In this case  $\hat{U}_E^1(\mu_0) = \max \mathbb{E}_{\pi}[U_E^1(\mu_s)] = \mu_0 \Delta V + V_L$ . Using Bayes' theorem, simple algebra gives  $\pi_B = \frac{(1-\overline{\mu})(\mu_0-\underline{\mu})}{(1-\mu_0)(\overline{\mu}-\underline{\mu})}$  and  $\pi_G = \frac{\overline{\mu}(\mu_0-\underline{\mu})}{\mu_0(\overline{\mu}-\underline{\mu})}$ .

**Proof of Proposition 7.** Recall that  $\overline{\mu}$  and  $\underline{\mu}$  are two roots to the equation  $U_{IB}^1(\frac{\phi}{1+\phi},\mu_s)=0$ . Write explicitly,

$$U_{IB}^{1}(\frac{\phi}{1+\phi},\mu_{s}) = \frac{\phi}{1+\phi} \cdot \left[ -r(\mu_{s}\Delta V + V_{L}) + (1+r) \cdot \frac{\mu_{s}(1-\mu_{s})\gamma(1-\gamma)\phi\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} \right] \\ + \frac{1}{1+\phi} \cdot \frac{\mu_{s}(1-\mu_{s})\gamma(1-\gamma)\phi\Delta V}{\mu_{s}\gamma + (1-\mu_{s})(1-\gamma)} \\ = 0.$$

Multiply both sides by  $\frac{1+\phi}{\phi}$ , and define

$$F(\mu_s, \theta) \equiv \frac{1+\phi}{\phi} \cdot U_{IB}^1(\frac{\phi}{1+\phi}, \mu_s)$$
  
=  $-r(\mu_s \Delta V + V_L) + [1+(1+r)\phi] \cdot \frac{\mu_s(1-\mu_s)\gamma(1-\gamma)\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)},$ 

where  $\theta \in \{V_L, \frac{\Delta}{V_L}, r, \phi\}$ . By the implicit function theorem, at  $\mu_s = \underline{\mu}$  or  $\overline{\mu}$ ,

$$\frac{\partial F}{\partial \mu_s} \cdot \frac{\partial \mu_s}{\partial \theta} + \frac{\partial F}{\partial \theta} = 0.$$

This gives

$$\operatorname{sign}\left(\frac{\partial\mu_s}{\partial\theta}\right) = -\operatorname{sign}\left(\frac{\partial F}{\partial\mu_s} \cdot \frac{\partial F}{\partial\theta}\right)$$

•

Next we calculate  $F(\mu_s, \theta)$ 's partial derivatives with respect to different  $\theta \in \{V_L, \eta, r, \phi\}$ :

$$\begin{array}{lll} \displaystyle \frac{\partial F}{\partial V_L} &=& -r < 0; \\ \displaystyle \frac{\partial F}{\partial r} &=& -V_L - \mu_s \Delta V \left[ 1 - \frac{(1-\mu_s)(1-\gamma)\gamma\phi}{\mu_s\gamma + (1-\mu_s)(1-\gamma)} \right] < 0; \\ \displaystyle \frac{\partial F}{\partial \phi} &=& (1+r) \cdot \frac{\mu_s(1-\mu_s)\gamma(1-\gamma)\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)} > 0. \end{array}$$

Define  $\eta \equiv \frac{\Delta V}{V_L}$ , and

$$f \equiv \frac{F}{\Delta V} = -r(\mu_s \Delta V + \frac{1}{\eta}) + [1 + (1+r)\phi] \cdot \frac{\mu_s(1-\mu_s)\gamma(1-\gamma)}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}.$$

So

$$\frac{\partial f}{\partial \eta} = \frac{r}{\eta^2} > 0 \implies \frac{\partial F}{\partial \eta} = \frac{r\Delta V}{\eta^2} > 0.$$

Moreover, in the proof of Lemma 2 we have shown that  $\frac{\partial F}{\partial \mu_s} > 0$  at  $\mu_s = \underline{\mu}$  but  $\frac{\partial F}{\partial \mu_s} < 0$  at  $\mu_s = \overline{\mu}$ . Consequently, we have (1)  $\frac{\partial \mu}{\partial V_L} > 0$  and  $\frac{\partial \overline{\mu}}{\partial V_L} < 0$ ; (2)  $\frac{\partial \mu}{\partial \eta} < 0$ 

and 
$$\frac{\partial \overline{\mu}}{\partial \eta} > 0$$
; (3)  $\frac{\partial \mu}{\partial r} > 0$  and  $\frac{\partial \overline{\mu}}{\partial r} < 0$ ; (4)  $\frac{\partial \mu}{\partial \phi} < 0$  and  $\frac{\partial \overline{\mu}}{\partial \phi} > 0$ .

**Proof of Proposition 8.** If the investment bank chooses to underwrite and his planned retention is  $\hat{\beta}$ , we can write his expected payoff as

$$U_{IB}^{2}(\hat{\beta},\mu_{s}) = \epsilon A(1-\psi,\mu_{s}) + (1-\epsilon)B(\hat{\beta},\mu_{s})$$
$$= [\epsilon(1-\psi) + (1-\epsilon)\hat{\beta}] \cdot [-r \mathbb{E}_{s}[\tilde{v}] + (1+r)\Delta P] + [\epsilon\psi + (1-\epsilon)(1-\hat{\beta})] \cdot \Delta P$$

Recall from the proof of Proposition 4 that  $-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P < \Delta P$ , thus we want  $\hat{\beta}$  to be as small as possible yet such stake still allows the underwriter to engage in informed trading if demand shock does not happen. The optimal planned retention is  $\hat{\beta} = \frac{\phi}{1+\phi}$ , the stake that is just enough for the bank to camouflage as liquidity traders.

**Proof of Lemma 3.** The proof resembles that of Lemma 2. Specifically, the equation now becomes

$$U_{IB}^{2}(\frac{\phi}{1+\phi},\mu_{s})$$

$$= [\epsilon(1-\psi) + (1-\epsilon)\hat{\beta}][-r\mathbb{E}_{s}[\tilde{v}] + (1+r)\Delta P] + [\epsilon\psi + (1-\epsilon)(1-\hat{\beta})]\Delta P$$

$$= 0.$$

 $\frac{\partial^2 U_{IB}^2}{\partial \mu_s^2} < 0$  because  $\frac{\partial^2 \Delta P}{\partial \mu_s^2} < 0$ . So  $U_{IB}^2$  is concave in  $\mu_s$ . To ensure that the interior optimum is attained at some  $\mu^* \in (0, 1)$ , the following must be satisfied:

$$\frac{\partial U_{IB}^2}{\partial \mu_s}\Big|_{\mu_s=0} = -Kr\Delta V + [(1+r)K + (1-K)]\gamma\phi\Delta V > 0;$$

$$\frac{\partial U_{IB}^2}{\partial \mu_s}\Big|_{\mu_s=1} = -Kr\Delta V - [(1+r)K + (1-K)](1-\gamma)\phi\Delta V < 0,$$

where  $K \equiv \epsilon(1-\psi) + (1-\epsilon)(\frac{\phi}{1+\phi})$  and  $1-K = \epsilon\psi + (1-\epsilon)(\frac{1}{1+\phi})$ . The first inequality implies

$$r < \frac{\gamma\phi(1+\phi)}{[(1+\phi)(1-\psi)\epsilon + \phi(1-\epsilon)](1-\gamma\phi)}$$

while the second is always satisfied.

Some simple algebra reveals that  $U_{IB}^2(\frac{\phi}{1+\phi}, 0) < 0$  and  $U_{IB}^2(\frac{\phi}{1+\phi}, 1) < 0$ . Moreover, we need  $U_{IB}^2(\frac{\phi}{1+\phi}, \frac{1}{2}) > 0$ . This implies

$$r < \frac{\gamma \phi(1+\phi)(1-\gamma)\Delta V}{[(1+\phi)(1-\psi)\epsilon + \phi(1-\epsilon)][\Delta V - \gamma \phi(1-\gamma)\Delta V + 2V_L]}.$$

Therefore,  $r < \min\left\{\frac{\gamma\phi(1+\phi)}{[(1+\phi)(1-\psi)\epsilon+\phi(1-\epsilon)](1-\gamma\phi)}, \frac{\gamma\phi(1+\phi)(1-\gamma)\Delta V}{[(1+\phi)(1-\psi)\epsilon+\phi(1-\epsilon)][\Delta V-\gamma\phi(1-\gamma)\Delta V+2V_L]}\right\}$ , i.e.  $r < \frac{\gamma\phi(1+\phi)(1-\gamma)\Delta V}{[(1+\phi)(1-\psi)\epsilon+\phi(1-\epsilon)][\Delta V-\gamma\phi(1-\gamma)\Delta V+2V_L]}$ . Note that both  $U_{IB}^1$  and  $U_{IB}^2$  are convex combinations of two ingredients  $-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P$  and  $\Delta P$  with the latter strictly larger than the former. It is easy to see that  $U_{IB}^1$  puts more weight on  $\Delta P$  and thus less weight on  $-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P$  than  $U_{IB}^2$ . Hence  $U_{IB}^1 > U_{IB}^2$ ,  $\forall \mu_s \in [0, 1]$ .

With the same logic used in the proof of Lemma 2, it follows naturally:

- 1. There exists a pair  $\{\underline{\mu}^*, \overline{\mu}^*\}$  with  $0 < \underline{\mu} < \underline{\mu}^* < \frac{1}{2} < \overline{\mu}^* < \overline{\mu} < 1$  such that  $U_{IB}^2(\frac{\phi}{1+\phi}, \underline{\mu}^*) = U_{IB}^2(\frac{\phi}{1+\phi}, \overline{\mu}^*) = 0.$
- 2.  $U_{IB}^2(\frac{\phi}{1+\phi},\mu_s) > 0$  if  $\mu_s \in (\underline{\mu}^*,\overline{\mu}^*)$ , and  $\tilde{U}_{IB}(\frac{\phi}{1+\phi},\mu_s) < 0$  if  $\mu_s \in [0,\underline{\mu}^*)$  or  $\mu_s \in (\overline{\mu}^*,1]$ .

Q.E.D.

**Proof of Proposition 9 and Proposition 10.** It follows naturally from Proposition 8 and Lemma 3 that at T = 1, the investment bank will agree to underwrite

if his planned retention  $\frac{\phi}{1+\phi}$  gives him a non-negative expected payoff. So he chooses to underwrite if  $\mu_s \in [\underline{\mu}^*, \overline{\mu}^*]$ , and not underwrite otherwise. The issuer is only able to issue the security when  $\mu_s \in [\underline{\mu}^*, \overline{\mu}^*]$ , and get an expected payoff of  $\mathbb{E}_s[\tilde{v}] - \Delta P$ .

**Proof of Proposition 11.** The optimal information design depends on the prior  $\mu_0$ .

1. First we investigate the optimal system when prior  $\mu_0 \in [0, \underline{\mu}^*)$ . In this case the investment bank does not underwrite if no additional information is disclosed. Consider any two arbitrary posteriors  $\mu_\ell$  and  $\mu_h$  with  $0 \leq \mu_\ell \leq \mu_0 \leq \mu_h \leq 1$  and  $\mathbb{P}[s = \ell]\mu_\ell + \mathbb{P}[s = h]\mu_h = \mu_0$ . To maximize her expected proceeds, the issuer will set  $\mu_\ell = 0$  to have the maximal  $\mathbb{P}[s = h]\mu_h$  which is  $\mu_0$ . Also, the issuer will set a  $\mu_h \in [\underline{\mu}^*, \overline{\mu}^*]$  so that the investment bank is willing to underwrite. Her expected payoff is therefore  $\mathbb{P}[s = h]P_0(\mu_h) = \frac{\mu_0 P_0(\mu_h)}{\mu_h}$ . Recall that

$$U_{IB}^{2}(\frac{\phi}{1+\phi},\mu_{s}) = K[-r\mathbb{E}_{s}[\tilde{v}] + (1+r)\Delta P] + (1-K)\Delta P = -rKP_{0}(\mu_{s}) + \Delta P(\mu_{s}),$$

where  $K = \epsilon (1 - \psi) + (1 - \epsilon) (\frac{\phi}{1 + \phi})$ , and  $\Delta P(\mu_s)$  means  $\Delta P$  is a function of  $\mu_s$ .

At  $\mu_s = \underline{\mu}^*$  or  $\overline{\mu}^*$ ,  $U_{IB}^2(\frac{\phi}{1+\phi}, \mu_s) = 0$ . This implies

$$= -rKP_0(\mu_s) + \Delta P(\mu_s) = 0$$

$$\Rightarrow \quad \frac{P_0(\mu_s)}{\mu_s} = \frac{\Delta P(\mu_s)}{rK\mu_s} = \frac{(1-\mu_s)\gamma(1-\gamma)\phi\Delta V}{rK[\mu_s\gamma + (1-\mu_s)(1-\gamma)]}$$

The last term is decreasing in  $\mu_s \in [\underline{\mu}^*, \overline{\mu}^*]$ . Since  $\underline{\mu}^* < \overline{\mu}^*$ , we have  $\frac{P_0(\underline{\mu}^*)}{\underline{\mu}^*} > \frac{P_0(\overline{\mu}^*)}{\overline{\mu}^*}$ .

Moreover, at  $\mu_s \in [\underline{\mu}^*, \overline{\mu}^*], U_{IB}^2(\frac{\phi}{1+\phi}, \mu_s) \geq 0$ . This implies

$$\Rightarrow \quad \frac{-rKP_0(\mu_s) + \Delta P(\mu_s) \ge 0}{\mu_s} \le \frac{\Delta P(\mu_s)}{rK\mu_s} \le \frac{\Delta P(\underline{\mu}^*)}{rK\underline{\mu}^*} = \frac{P_0(\underline{\mu}^*)}{\underline{\mu}^*}.$$

Therefore, the optimal system will induce two posteriors  $\mu_{\ell} = 0$  and  $\mu_{h} = \underline{\mu}^{*}$ . The relevant precision parameters are  $\pi_{B} = \frac{\mu_{0}(1-\underline{\mu}^{*})}{\underline{\mu}^{*}(1-\mu_{0})}$  and  $\pi_{G} = 1$ .

- 2. Second, we derive the optimal system when  $\mu_0 \in (\overline{\mu}^*, 1]$ . Consider any two arbitrary posteriors  $\mu_\ell$  and  $\mu_h$  with  $0 \leq \mu_\ell \leq \mu_0 \leq \mu_h \leq 1$  and  $\mathbb{P}[s = \ell]\mu_\ell + \mathbb{P}[s = h]\mu_h = \mu_0$ . To maximize her expected proceeds, the issuer will set  $\mu_h = 1$ . This ensures that for any fixed  $\mu_\ell$ , the probability of achieving this posterior  $\mathbb{P}[s = \ell] = \frac{\mu_h - \mu_0}{\mu_h - \mu_l}$  will be maximized, i.e. the probability of underwriting will be the highest. Her expected payoff is therefore  $\mathbb{P}[s = \ell]P_0(\mu_\ell) = \frac{1-\mu_0}{1-\mu_\ell} \cdot P_0(\mu_\ell)$ . Since both  $\frac{1-\mu_0}{1-\mu_\ell}$  and  $P_0(\mu_\ell)$  are increasing in  $\mu_\ell$ , it is optimal to set  $\mu_\ell = \overline{\mu}^*$ . Hence the optimal system yields two posteriors  $\mu_\ell = \underline{\mu}^*$  and  $\mu_h = 1$ . This gives  $\pi_B = \frac{\mu_0 - \overline{\mu}^*}{\mu_0(1-\overline{\mu}^*)}$  and  $\pi_G = 0$ .
- 3. Third, when  $\mu_0 = \underline{\mu}^*$  or  $\overline{\mu}^*$ , the investment bank is break-even by underwriting the deal. In this case, a completely uninformative disclosure system is optimal. It has  $\pi_G = \pi_B \in (0, 1)$ , yielding posteriors  $\mu_\ell = \mu_h = \mu_0$ .
- 4. Finally, we find the optimal system when  $\mu_0 \in (\underline{\mu}^*, \overline{\mu}^*)$ . Since  $\Delta P(\mu_s)$  is concave in  $\mu_s$ ,  $P_0(\mu_s) = \mathbb{E}_s[\tilde{v}] - \Delta P$  is convex and increases in  $\mu_s$ . First consider any arbitrary posteriors  $\mu_\ell$  and  $\mu_h$  such that  $\underline{\mu}^* \leq \mu_\ell \leq \mu_0 \leq \mu_h \leq \overline{\mu}^*$ .

In order for the two pairs of posteriors  $\{\underline{\mu}^*, \overline{\mu}^*\}$  and  $\{\mu_\ell, \mu_h\}$  to be Bayesian

plausible, they should satisfy

$$\mu_0 = \lambda \underline{\mu}^* + (1 - \lambda) \overline{\mu}^*,$$
  
$$\mu_0 = \overline{\lambda} \mu_\ell + (1 - \overline{\lambda}) \mu_h.$$

Moreover, we can write

$$\mu_{\ell} = \lambda_{\ell} \underline{\mu}^* + (1 - \lambda_{\ell}) \overline{\mu}^*,$$
  
$$\mu_h = \lambda_h \mu^* + (1 - \lambda_h) \overline{\mu}^*.$$

Here  $\lambda$ ,  $\lambda_{\ell}$ ,  $\lambda_h$ , and  $\bar{\lambda}$  all lie in [0, 1].

So we have

$$\mu_{0} = \overline{\lambda} [\lambda_{\ell} \underline{\mu}^{*} + (1 - \lambda_{\ell}) \overline{\mu}^{*}] + (1 - \overline{\lambda}) [\lambda_{h} \underline{\mu}^{*} + (1 - \lambda_{h}) \overline{\mu}^{*}]$$
  
$$= [\overline{\lambda} \lambda_{\ell} + (1 - \overline{\lambda}) \lambda_{h}] \underline{\mu}^{*} + [\overline{\lambda} (1 - \lambda_{\ell}) + (1 - \overline{\lambda}) (1 - \lambda_{h})] \overline{\mu}^{*}$$
  
$$= \lambda \mu^{*} + (1 - \lambda) \overline{\mu}^{*}.$$

By Jensen's inequality,

$$\begin{split} U_{E}^{2}(\frac{\phi}{1+\phi},\mu_{0}) \\ &= P_{0}(\mu_{0}) \\ &\leq \bar{\lambda}P_{0}(\mu_{\ell}) + (1-\bar{\lambda})P_{0}(\mu_{h}) \\ &\leq \bar{\lambda}[\lambda_{\ell}P_{0}(\underline{\mu}^{*}) + (1-\lambda_{\ell})P_{0}(\overline{\mu}^{*})] + (1-\bar{\lambda})[\lambda_{h}P_{0}(\underline{\mu}^{*}) + (1-\lambda_{h})P_{0}(\overline{\mu}^{*})] \\ &= [\bar{\lambda}\lambda_{\ell} + (1-\bar{\lambda})\lambda_{h}]P_{0}(\underline{\mu}^{*}) + [\bar{\lambda}(1-\lambda_{\ell}) + (1-\bar{\lambda})(1-\lambda_{h})]P_{0}(\overline{\mu}^{*}) \\ &= \lambda P_{0}(\underline{\mu}^{*}) + (1-\lambda)P_{0}(\overline{\mu}^{*}) \\ &= \hat{U}_{E}^{2}(\mu_{0}), \end{split}$$

where  $\lambda = \frac{\overline{\mu}^* - \mu_0}{\overline{\mu}^* - \underline{\mu}^*} = \mathbb{P}[s = \ell]$ . The issuer achieves expected payoff  $\hat{U}_E^2(\mu_0)$  by setting  $\mu_\ell = \mu^*$  and  $\mu_h = \overline{\mu}^*$ .

We further consider two other possibilities. If we set  $\mu_{\ell} = 0$ , then the issuer's expected payoff upon observing  $s = \ell$  is zero. Her expected payoff is thus  $\frac{\mu_0}{\mu_h} \cdot P_0(\mu_h) < P_0(\mu_h)$ . Since  $P_0(\mu_s)$  is convex in  $\mu_s$ , we have  $P_0(\mu_h) \leq \lambda P_0(\underline{\mu}^*) + (1 - \lambda)P_0(\overline{\mu}^*) = \hat{U}_E^2(\mu_0)$ . Hence  $\frac{\mu_0}{\mu_h} \cdot P_0(\mu_h) < P_0(\mu_h) \leq \hat{U}_E^2(\mu_0)$ , rendering this strategy suboptimal. If we set  $\mu_h = 1$ , under this system, the issuer's expected payoff is  $\frac{1-\mu_0}{1-\mu_\ell} \cdot P_0(\mu_\ell) < P_0(\mu_0) < \hat{U}_E^2(\mu_0)$  because  $P_0(\mu_s)$  is convex and increasing in  $\mu_s$ . Again, such system is not optimal too.

In sum, the optimal system will induce two posteriors  $\mu_{\ell} = \underline{\mu}^*$  and  $\mu_h = \overline{\mu}^*$ . By Bayes' theorem,  $\pi_G = \frac{\overline{\mu}^*(\mu_0 - \underline{\mu}^*)}{\mu_0(\overline{\mu}^* - \underline{\mu}^*)}$  and  $\pi_B = \frac{(1 - \overline{\mu}^*)(\mu_0 - \underline{\mu}^*)}{(1 - \mu_0)(\overline{\mu}^* - \underline{\mu}^*)}$ .

**Proof of Proposition 12.** Recall that if the investment bank chooses to underwrite and his planned retention is  $\frac{\phi}{1+\phi}$ , then

$$U_{IB}^{2}\left(\frac{\phi}{1+\phi},\mu_{s}\right) = -r\left[\epsilon(1-\psi)+(1-\epsilon)\frac{\phi}{1+\phi}\right]\left(\mu_{s}\Delta V+V_{L}\right) \\ +\left\{1+r\left[\epsilon(1-\psi)+(1-\epsilon)\frac{\phi}{1+\phi}\right]\right\}\cdot\frac{(1-\mu_{s})\mu_{s}(1-\gamma)\gamma\phi\Delta V}{\mu_{s}\gamma+(1-\mu_{s})(1-\gamma)}$$

Define  $G(\mu_s, \theta_1) \equiv U_{IB}^2(\frac{\phi}{1+\phi}, \mu_s) = 0$  where  $\theta_1 \in \{\epsilon, \psi, V_L, \frac{\Delta V}{V_L}, r, \phi\}$ . By the implicit function theorem, at  $\mu_s = \underline{\mu}^*$  or  $\overline{\mu}^*$ ,

$$\frac{\partial G}{\partial \mu_s} \cdot \frac{\partial \mu_s}{\partial \theta_1} + \frac{\partial G}{\partial \theta_1} = 0.$$

Like before,

$$\operatorname{sign}\left(\frac{\partial\mu_s}{\partial\theta_1}\right) = -\operatorname{sign}\left(\frac{\partial G}{\partial\mu_s} \cdot \frac{\partial G}{\partial\theta_1}\right).$$

Moreover,

$$\begin{split} \frac{\partial G}{\partial \epsilon} &= -r \left[ (1-\psi) - \frac{\phi}{1+\phi} \right] (\mathbb{E}_s[\tilde{v}] - \Delta P) < 0; \\ \frac{\partial G}{\partial \psi} &= r\epsilon (\mathbb{E}_s[\tilde{v}] - \Delta P) > 0; \\ \frac{\partial G}{\partial V_L} &= -r \left[ \epsilon (1-\psi) + (1-\epsilon) \frac{\phi}{1+\phi} \right] < 0; \\ \frac{\partial G}{\partial r} &= - \left[ \epsilon (1-\psi) + (1-\epsilon) \frac{\phi}{1+\phi} \right] (\mathbb{E}_s[\tilde{v}] - \Delta P) < 0. \end{split}$$

Multiply  $G(\mu_s, \phi)$  by  $(1 + \phi)$  we obtain

$$g_1(\mu_s, \phi) \equiv (1+\phi)G(\mu_s, \phi) = -rK_1 \mathbb{E}_s[\tilde{v}] + \{1+rK_1\}\Delta P = 0,$$

where  $K_1 \equiv \epsilon (1 - \psi)(1 + \phi) + (1 - \epsilon)\phi$ . This implies

$$\mathbb{E}_s[\tilde{v}] = \frac{(1 + rK_1)\Delta P}{rK_1}.$$

Note that

$$\frac{\partial K_1}{\partial \phi} = 1 - \psi \epsilon = \frac{K_1 - \epsilon(1 - \psi)}{\phi}.$$

Therefore,

$$\begin{aligned} \frac{\partial g_1}{\partial \phi} &= -r \cdot \frac{K_1 - \epsilon(1 - \psi)}{\phi} \cdot \frac{(1 + rK_1)\Delta P}{rK_1} \\ &+ r \cdot \frac{K_1 - \epsilon(1 - \psi)}{\phi} \cdot \Delta P + (1 + rK_1) \cdot \frac{\Delta P}{\phi} \\ &= \frac{\Delta P}{\phi} \cdot \left\{ -r[K_1 - \epsilon(1 - \psi)] \cdot \frac{1}{rK_1} + (1 + rK_1) \right\} \\ &= \frac{\Delta P}{\phi} \cdot \left[ \frac{\epsilon(1 - \psi)}{K_1} + rK_1 \right] \\ &> 0. \end{aligned}$$

We then divide  $g_1(\mu_s, \phi)$  by  $\Delta V$ , and obtain

$$g_2 \equiv -rK_1(\mu_s + \frac{1}{\eta}) + (1 + rK_1) \cdot \frac{\mu_s(1 - \mu_s)\gamma(1 - \gamma)}{\mu_s\gamma + (1 - \mu_s)(1 - \gamma)},$$

where  $\eta = \frac{\Delta V}{V_L}$ . So

$$\frac{\partial g_2}{\partial \eta} = \frac{rK_1}{\eta^2} > 0$$

Recall from the proof of Lemma 3, we know that  $\partial U_{IB}^2/\partial \mu_s > 0$  at  $\mu_s = \underline{\mu}^*$ yet  $\partial U_{IB}^2/\partial \mu_s < 0$  at  $\mu_s = \overline{\mu}^*$ . Hence at  $\mu_s = \underline{\mu}^*$ ,  $\partial G/\partial \mu_s > 0$ ,  $\partial g_1/\partial \mu_s > 0$ , and  $\partial g_2/\partial \mu_s > 0$ . Meanwhile at  $\mu_s = \overline{\mu}^*$ ,  $\partial G/\partial \mu_s < 0$ ,  $\partial g_1/\partial \mu_s < 0$ , and  $\partial g_2/\partial \mu_s < 0$ .

Accordingly, by the implicit function theorem, (1)  $\frac{\partial \underline{\mu}^*}{\partial \epsilon} > 0$  and  $\frac{\partial \overline{\mu}^*}{\partial \epsilon} < 0$ ; (2)  $\frac{\partial \underline{\mu}^*}{\partial \psi} < 0$  and  $\frac{\partial \overline{\mu}^*}{\partial \psi} > 0$ ; (3)  $\frac{\partial \underline{\mu}^*}{\partial V_L} > 0$  and  $\frac{\partial \overline{\mu}^*}{\partial V_L} < 0$ ; (4) Recall that  $\eta = \frac{\Delta V}{V_L}$ , then  $\frac{\partial \underline{\mu}^*}{\partial \eta} < 0$  and  $\frac{\partial \overline{\mu}^*}{\partial \eta} > 0$ ; (5)  $\frac{\partial \underline{\mu}^*}{\partial r} > 0$  and  $\frac{\partial \overline{\mu}^*}{\partial r} < 0$ ; (6)  $\frac{\partial \underline{\mu}^*}{\partial \phi} < 0$  and  $\frac{\partial \overline{\mu}^*}{\partial \phi} > 0$ .

**Proof of Proposition 13.** If there is no demand uncertainty, the investment bank chooses his optimal retention  $\beta$  to maximize his expected payoff:

$$U_{IB}^3(\beta,\mu_s) = \beta\{-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P\} + (1-\beta)\Delta P.$$

Because we know that  $\{-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P\} < \Delta P$ , it is optimal to choose the largest possible  $(1 - \beta)$ . Since the underwrite can sell the security short in the secondary market, he no longer has to retain any share in the primary market. Thus he chooses the optimal  $\beta^*(\mu_s) = 0$ , and his maximal expected payoff is just

$$\hat{U}_{IB}^3(\mu_s) = U_{IB}^3(0,\mu_s) = \frac{\mu_s(1-\mu_s)\gamma(1-\gamma)\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}.$$

Q.E.D.

Proof of Proposition 14. Given the investment bank's best response in the

primary market, the issuer's expected payoff conditional on posterior belief is

$$U_E^3(\mu_s) = (\mu_s \Delta V) - \frac{\mu_s (1 - \mu_s) \gamma (1 - \gamma) \phi \Delta V}{\mu_s \gamma + (1 - \mu_s) (1 - \gamma)} = P_0(\mu_s).$$

As we have shown before, this function is convex in  $\mu_s \in [0, 1]$ . For any posteriors  $\mu_\ell$  and  $\mu_h$  that are Bayesian plausible,

$$U_E^3(\mu_0) \leq \mathbb{P}[s=\ell]P_0(\mu_\ell) + \mathbb{P}[s=h]P_0(\mu_h)$$
$$\leq \mathbb{P}[s=\ell]P_0(0) + \mathbb{P}[s=h]P_0(1).$$

The last inequality follows form the convexity of the function, and it holds with strict inequality if  $\mu_0 \in (0, 1)$ . Therefore, the optimal system generates a low posterior  $\mu_{\ell} = 0$  and a high posterior  $\mu_h = 1$ . The system is fully informative in that  $\pi_G = 1$  and  $\pi_B = 0$ .

**Proof of Lemma 4.** If the investment bank agrees to underwrite and chooses a planed retention  $\hat{\beta} = 0$ , his expected payoff is

$$\begin{split} U_{IB}^{4}(\hat{\beta} = 0, \mu_{s}) &= \epsilon \{ (1 - \psi) [\mathbb{E}_{s}[\tilde{v}] - (1 + r)(\mathbb{E}_{s}[\tilde{v}] - \Delta P)] + \psi \Delta P \} + (1 - \epsilon) \Delta P \\ &= \epsilon (1 - \psi) \{ -r \, \mathbb{E}_{s}[\tilde{v}] + (1 + r) \Delta P \} + [\epsilon \psi + (1 - \epsilon)] \Delta P \\ &= -\epsilon (1 - \psi) r \, \mathbb{E}_{s}[\tilde{v}] + [(1 + r)\epsilon (1 - \psi) + \epsilon \psi + (1 - \epsilon)] \Delta P \\ &> U_{IB}^{2}(\hat{\beta} = \frac{\phi}{1 + \phi}, \mu_{s}). \end{split}$$

The last inequality holds because when demand shock does not happen and there is short sale constraint, the underwriter has to retain a positive stake to engage in informed trading, which incurs cost of capital and undermines the informed trading profits.

It is easy to see that  $U_{IB}^4(\hat{\beta}=0,\mu_s)$  is concave in  $\mu_s$  because of the concavity

of  $\Delta P$ . Like in the proofs of Lemma 2 and Lemma 3, to ensure its optimum appears at some  $\mu^{**} \in (0, 1)$ , we require

$$\frac{\partial U_{IB}^4}{\partial \mu_s}\Big|_{\mu_s=0} = -\epsilon(1-\psi)r\Delta V + [(1+r)\epsilon(1-\psi) + \epsilon\psi + (1-\epsilon)]\gamma\phi\Delta V > 0;$$

$$\frac{\partial U_{IB}^4}{\partial \mu_s}\Big|_{\mu_s=1} = -\epsilon(1-\psi)r\Delta V - [(1+r)\epsilon(1-\psi) + \epsilon\psi + (1-\epsilon)](1-\gamma)\phi\Delta V < 0.$$

The first requires that  $r < \frac{\gamma \phi}{\epsilon(1-\psi)(1-\gamma \phi)}$ , while the second always holds.

It's easy to see that  $U_{IB}^4(\hat{\beta}=0,0) < 0$  and  $U_{IB}^4(\hat{\beta}=0,1) < 0$ . We further require that  $U_{IB}^4(\hat{\beta}=0,\frac{1}{2}) > 0$ . This implies that  $r < \frac{\gamma(1-\gamma)\phi\Delta V}{\epsilon(1-\psi)[\Delta V-\gamma(1-\gamma)\phi\Delta V+2V_L]}$ . So  $r < \min\{\frac{\gamma\phi}{\epsilon(1-\psi)(1-\gamma\phi)}, \frac{\gamma(1-\gamma)\phi\Delta V}{\epsilon(1-\psi)[\Delta V-\gamma(1-\gamma)\phi\Delta V+2V_L]}\}$ , i.e.  $r < \frac{\gamma(1-\gamma)\phi\Delta V}{\epsilon(1-\psi)[\Delta V-\gamma(1-\gamma)\phi\Delta V+2V_L]}$ .

As long as all of the above are satisfied, it follows naturally that:

- 1. There exists a pair  $\{\underline{\mu}^{**}, \overline{\mu}^{**}\}$  with  $0 < \underline{\mu}^{**} < \underline{\mu}^{*} < \frac{1}{2} < \overline{\mu}^{*} < \overline{\mu}^{**} < 1$  such that  $U_{IB}^{4}(0, \underline{\mu}^{*}) = U_{IB}^{4}(0, \overline{\mu}^{**}) = 0.$
- 2.  $U_{IB}^4(0,\mu_s) > 0$  if  $\mu_s \in (\underline{\mu}^{**}, \overline{\mu}^{**})$ , and  $\tilde{U}_{IB}(0,\mu_s) < 0$  if  $\mu_s \in [0, \underline{\mu}^{**})$  or  $\mu_s \in (\overline{\mu}^{**}, 1]$ .

Q.E.D.

**Proof of Proposition 15.** From Proposition 13 we know that if demand shock does not happen, it is optimal for the investment bank not to retain any share in the primary market. If demand shock happens, he is forced to retain  $(1 - \psi)$ . Therefore, his optimal planned retention should always be zero if the bank decides to underwrite. From Lemma 4 we know that the investment bank will choose to underwrite only at posteriors  $\mu_s \in [\underline{\mu}^{**}, \overline{\mu}^{**}]$ , otherwise he will withdraw from underwriting. This gives his expected payoff

$$\hat{U}_{IB}^{4}(\mu_{s}) = \begin{cases} U_{IB}^{4}(\hat{\beta} = 0, \mu_{s}) & \text{if } \mu_{s} \in [\underline{\mu}^{**}, \overline{\mu}^{**}], \\ 0 & \text{if } \mu_{s} \in [0, \underline{\mu}^{**}) \cup (\overline{\mu}^{**}, 1]. \end{cases}$$

Q.E.D.

**Proof of Proposition 16.** Proposition 16 follows naturally from Proposition 15. ■

**Proof of Proposition 17.** Much of the proof resembles that of Proposition 11. Likewise, we consider four cases respectively.

1. If  $\mu_0 \in [0, \underline{\mu}^{**})$ , like part 1 of Proposition 11's proof, it is optimal to set  $\mu_{\ell} = 0$  and the issuer's expected payoff is  $\frac{\mu_0 P_0(\mu_h)}{\mu_h}$ . Define  $K_2 = \epsilon(1 - \psi)$ , so

$$U_{IB}^{4}(0,\mu_{s}) = -rK_{2}\mathbb{E}_{s}[\tilde{v}] + (1+rK_{2})\Delta P \ge 0$$

$$\Rightarrow rK_2(\mathbb{E}_s[\tilde{v}] - \Delta P) \le \Delta P$$
$$\Rightarrow \frac{\mu_0 P_0(\mu_s)}{\mu_s} \le \frac{\mu_0 \Delta P}{rK_2 \mu_s}.$$

The last holds with equality when  $\mu_s = \underline{\mu}^{**}$  or  $\overline{\mu}^{**}$ . Since

$$\frac{\Delta P}{\mu_s} = \frac{(1-\mu_s)(1-\gamma)\gamma\phi\Delta V}{\mu_s\gamma + (1-\mu_s)(1-\gamma)}$$

which is decreasing in  $\mu_s$  and achieves the maximum at  $\mu_s = \underline{\mu}^{**}$ . Therefore it is optimal for the issuer to set  $\mu_h = \underline{\mu}^{**}$  so that she gets the highest expected payoff  $\frac{\mu_0 P_0(\underline{\mu}^{**})}{\underline{\mu}^{**}}$ . In sum, the optimal system will induce two posteriors  $\mu_\ell = 0$  and  $\mu_h = \underline{\mu}^{**}$ . The relevant precision parameters are  $\pi_B = \frac{\mu_0(1-\underline{\mu}^{**})}{\underline{\mu}^{**}(1-\mu_0)}$ and  $\pi_G = 1$ .

- 2. If  $\mu_0 \in (\overline{\mu}^{**}, 1]$ , with the same reasoning as part 2 of Proposition 11's proof, it is optimal to set  $\mu_h = 1$ . Her expected payoff is therefore  $\mathbb{P}[s = \ell]P_0(\mu_\ell) = \frac{1-\mu_0}{1-\mu_\ell} \cdot P_0(\mu_\ell)$ . Since both  $\frac{1-\mu_0}{1-\mu_\ell}$  and  $P_0(\mu_\ell)$  are increasing in  $\mu_\ell$ , it is optimal to set  $\mu_\ell = \overline{\mu}^{**}$ . Hence the optimal system yields two posteriors  $\mu_\ell = \underline{\mu}^{**}$ and  $\mu_h = 1$ . This gives  $\pi_B = \frac{\mu_0 - \overline{\mu}^{**}}{\mu_0(1-\overline{\mu}^{**})}$  and  $\pi_G = 0$ .
- 3. Third, when  $\mu_0 = \underline{\mu}^{**}$  or  $\overline{\mu}^{**}$ , the investment bank is break-even by underwriting the deal. In this case, a completely uninformative disclosure system is optimal. It has  $\pi_G = \pi_B \in (0, 1)$ , yielding posteriors  $\mu_\ell = \mu_h = \mu_0$ .
- 4. Finally, we explore the cae when  $\mu_0 \in (\underline{\mu}^{**}, \overline{\mu}^{**})$ . Using a similar argument as in part 3 of Proposition 11's proof, we have  $\mu_\ell = \underline{\mu}^{**}$  and  $\mu_h = \overline{\mu}^{**}$  due to the convexity of  $U_{IB}^4(0, \mu_s)$  in  $\mu_s$  on  $[\underline{\mu}^{**}, \overline{\mu}^{**}]$ . Again, setting either  $\mu_\ell = 0$ or  $\mu_h = 1$  is suboptimal. Hence the optimal system has  $\pi_G = \frac{\overline{\mu}^{**}(\mu_0 - \underline{\mu}^{**})}{\mu_0(\overline{\mu}^{**} - \underline{\mu}^{**})}$ and  $\pi_B = \frac{(1 - \overline{\mu}^{**})(\mu_0 - \underline{\mu}^{**})}{(1 - \mu_0)(\overline{\mu}^{**} - \underline{\mu}^{**})}$ .

**Proof of Proposition 18.** Note that  $\overline{\mu}^{**}$  and  $\underline{\mu}^{**}$  are two roots of the following equation:

$$U_{IB}^4(0,\mu_s) = -rK_2 \mathbb{E}_s[\tilde{v}] + (1+rK_2)\Delta P = 0.$$

Define

$$J(\mu_s, \theta_1) = -rK_2 \mathbb{E}_s[\tilde{v}] + (1 + rK_2)\Delta P,$$

where  $K_2 = \epsilon(1 - \psi)$  and  $\theta_1 \in \{\epsilon, \psi, V_L, \frac{\Delta V}{V_L}, r, \phi\}$ . Some simple algebra gives

$$\begin{aligned} \frac{\partial J}{\partial \epsilon} &= -r(1-\psi)(\mathbb{E}_s[\tilde{v}] - \Delta P) < 0;\\ \frac{\partial J}{\partial \psi} &= r\epsilon(\mathbb{E}_s[\tilde{v}] - \Delta P) > 0; \end{aligned}$$

$$\begin{aligned} \frac{\partial J}{\partial V_L} &= -r\epsilon(1-\psi) < 0;\\ \frac{\partial J}{\partial r} &= -\epsilon(1-\psi)(\mathbb{E}_s[\tilde{v}] - \Delta P) < 0;\\ \frac{\partial J}{\partial \phi} &= [1 + r\epsilon(1-\psi)] \cdot \frac{\Delta P}{\phi} > 0 \end{aligned}$$

Let  $j = J/\Delta V$ , we obtain

$$\frac{\partial j}{\partial \eta} = \frac{r\epsilon(1-\psi)}{\eta^2} > 0.$$

Moreover, from the proof of Lemma 4, at  $\mu_s = \underline{\mu}^{**}$ ,  $\frac{\partial J}{\partial \mu_s} > 0$ , while at  $\mu_s = \overline{\mu}^{**}$ ,  $\frac{\partial J}{\partial \mu_s} < 0$ .

So by the implicit function theorem, we have (1)  $\frac{\partial \mu^{**}}{\partial \epsilon} > 0$  and  $\frac{\partial \overline{\mu}^{**}}{\partial \epsilon} < 0$ ; (2)  $\frac{\partial \mu^{**}}{\partial \psi} < 0$  and  $\frac{\partial \overline{\mu}^{**}}{\partial \psi} > 0$ ; (3)  $\frac{\partial \mu^{**}}{\partial V_L} > 0$  and  $\frac{\partial \overline{\mu}^{**}}{\partial V_L} < 0$ ; (4) Recall that  $\eta = \frac{\Delta V}{V_L}$ , then  $\frac{\partial \mu^{**}}{\partial \eta} < 0$  and  $\frac{\partial \overline{\mu}^{**}}{\partial \eta} > 0$ ; (5)  $\frac{\partial \mu^{**}}{\partial r} > 0$  and  $\frac{\partial \overline{\mu}^{**}}{\partial r} < 0$ ; (6)  $\frac{\partial \mu^{**}}{\partial \phi} < 0$  and  $\frac{\partial \overline{\mu}^{**}}{\partial \phi} > 0$ .

**Proof of Proposition 19.** Recall that  $i \in \{1, 2, 3, 4\}$  represents one of the following four scenarios: 1. (No Short Sale, No Demand Uncertainty), 2. (No Short Sale, Demand Uncertainty), 3. (Short Sale, No Demand Uncertainty), and 4. (Short Sale, Demand Uncertainty).

We have already shown that  $U_{IB}^1(\beta = \frac{\phi}{1+\phi}, \mu_s) > U_{IB}^2(\hat{\beta} = \frac{\phi}{1+\phi}, \mu_s)$  and  $0 < \underline{\mu} < \underline{\mu}^* < \frac{1}{2} < \overline{\mu}^* < \overline{\mu} < 1$ , as well as  $U_{IB}^4(\hat{\beta} = 0, \mu_s) > U_{IB}^2(\hat{\beta} = \frac{\phi}{1+\phi}, \mu_s)$  and  $0 < \underline{\mu}^{**} < \underline{\mu}^* < \frac{1}{2} < \overline{\mu}^* < \overline{\mu}^{**} < 1$ . Thus it remains to compare  $U_{IB}^1(\beta = \frac{\phi}{1+\phi}, \mu_s)$  and  $U_{IB}^4(\hat{\beta} = 0, \mu_s)$  to rank the welfare of the investment banks. Recall that

$$U_{IB}^4(\hat{\beta}=0,\mu_s) = \epsilon \{(1-\psi)\{\mathbb{E}_s[\tilde{v}] - (1+r)(\mathbb{E}_s[\tilde{v}] - \Delta P)\} + \psi \Delta P\} + (1-\epsilon)\Delta P,$$
  
=  $(\epsilon - \epsilon \psi)\{-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P\} + (\psi \epsilon + 1 - \epsilon)\Delta P,$ 

and

$$U_{IB}^1(\beta = \frac{\phi}{1+\phi}, \mu_s) = \frac{\phi}{1+\phi} \cdot \{-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P\} + \frac{1}{1+\phi} \cdot \Delta P.$$

Since we have shown that  $\{-r \mathbb{E}_s[\tilde{v}] + (1+r)\Delta P\} < \Delta P$ , it is easy to see:

(1) If  $\epsilon - \epsilon \psi < \frac{\phi}{1+\phi}$ , i.e.  $\epsilon < \frac{\phi}{(1-\psi)(1+\phi)}$ , then  $U_{IB}^1(\beta = \frac{\phi}{1+\phi}, \mu_s) < U_{IB}^4(\hat{\beta} = 0, \mu_s)$ , and  $0 < \underline{\mu}^{**} < \underline{\mu} < \underline{\mu}^* < \frac{1}{2} < \overline{\mu}^* < \overline{\mu} < \overline{\mu}^{**} < 1$ . Note that the investment banks' welfare is

$$W_{IB}(i) = \int_0^1 \hat{U}_{IB}^i(\mu_0) \, d\mu_0 = \int_{\underline{\mu}_{(i)}}^{\overline{\mu}_{(i)}} U_{IB}^i(\,\cdot\,,\mu_0) \, d\mu_0.$$

where  $\underline{\mu}_{(i)}$  and  $\overline{\mu}_{(i)}$  denote the relevant cut-offs in scenario *i*, and " $\cdot$ " denotes the investment banks' relevant retention in  $U_{IB}^{i}(\cdot, \mu_{s})$ . Hence we obtain the following ranking:

$$W_{IB}(SS, NDU) > W_{IB}(SS, DU) > W_{IB}(NSS, NDU) > W_{IB}(NSS, DU).$$

(2) Similarly, if  $\epsilon > \frac{\phi}{(1-\psi)(1+\phi)}$ , then  $0 < \underline{\mu} < \underline{\mu}^{**} < \underline{\mu}^* < \frac{1}{2} < \overline{\mu}^* < \overline{\mu}^{**} < \overline{\mu} < 1$ and

$$W_{IB}(SS, NDU) > W_{IB}(NSS, NDU) > W_{IB}(SS, DU) > W_{IB}(NSS, DU).$$

(3) Finally, if  $\epsilon = \frac{\phi}{(1-\psi)(1+\phi)}$ , then  $0 < \underline{\mu} = \underline{\mu}^{**} < \underline{\mu}^* < \frac{1}{2} < \overline{\mu}^* < \overline{\mu}^{**} = \overline{\mu} < 1$ and

$$W_{IB}(SS, NDU) > W_{IB}(NSS, NDU) = W_{IB}(SS, DU) > W_{IB}(NSS, DU).$$

Q.E.D.

**Proof of Proposition 20.** If the issuers do not disclose additional information, the investment banks' decisions to underwrite and the issuers' expected payoffs will depend directly on  $\mu_0$ . Also,

$$\begin{split} W_E(1) &= \int_0^{\underline{\mu}} (\mu_0 \Delta V + V_L) \, d\mu_0 + \int_{\underline{\mu}}^{\overline{\mu}} \left[ (\mu_0 \Delta V + V_L) - \frac{(1 - \mu_0)\mu_0(1 - \gamma)\gamma\phi\Delta V}{\mu_0\gamma + (1 - \mu_0)(1 - \gamma)} \right] \, d\mu_0 \\ &+ \int_{\overline{\mu}}^1 (\mu_0 \Delta V + V_L) \, d\mu_0, \end{split} \\ W_E(2) &= \int_0^{\underline{\mu}^*} 0 \, d\mu_0 + \int_{\underline{\mu}^*}^{\overline{\mu}^*} \left[ (\mu_0 \Delta V + V_L) - \frac{(1 - \mu_0)\mu_0(1 - \gamma)\gamma\phi\Delta V}{\mu_0\gamma + (1 - \mu_0)(1 - \gamma)} \right] \, d\mu_0 + \int_{\overline{\mu}^*}^1 0 \, d\mu_0, \end{split}$$

$$W_E(3) = \int_0^1 \left[ (\mu_0 \Delta V + V_L) - \frac{(1 - \mu_0)\mu_0(1 - \gamma)\gamma\phi\Delta V}{\mu_0\gamma + (1 - \mu_0)(1 - \gamma)} \right] d\mu_0,$$
  

$$W_E(4) = \int_0^{\underline{\mu}^{**}} 0 \, d\mu_0 + \int_{\underline{\mu}^{**}}^{\overline{\mu}^{**}} \left[ (\mu_0 \Delta V + V_L) - \frac{(1 - \mu_0)\mu_0(1 - \gamma)\gamma\phi\Delta V}{\mu_0\gamma + (1 - \mu_0)(1 - \gamma)} \right] d\mu_0 + \int_{\overline{\mu}^{**}}^1 0 \, d\mu_0$$

Therefore, the ranking is as follow,

$$W_E(NSS, NDU) > W_E(SS, NDU) > W_E(SS, DU) > W_E(NSS, DU).$$

We can write

$$P_0(\mu) = (\mu \Delta V + V_L) - \frac{(1-\mu)\mu(1-\gamma)\gamma\phi\Delta V}{\mu\gamma + (1-\mu)(1-\gamma)},$$

which is increasing in  $\mu$  and does not exceed  $(\mu \Delta V + V_L)$ . Then if all of the issuers design their disclosure policies optimally, their welfare under four different



Figure 1.13: Welfare comparison

scenarios are

$$\begin{split} \hat{W}_{E}(1) &= \int_{0}^{1} (\mu_{0} \Delta V + V_{L}) \, d\mu_{0}, \\ \hat{W}_{E}(2) &= \int_{0}^{\underline{\mu}^{*}} P_{0}(\underline{\mu}^{*}) \cdot \frac{\mu_{0}}{\underline{\mu}^{*}} \, d\mu_{0} + \int_{\underline{\mu}^{*}}^{\overline{\mu}^{*}} \left[ P_{0}(\underline{\mu}^{*}) + \frac{P_{0}(\overline{\mu}^{*}) - P_{0}(\underline{\mu}^{*})}{\overline{\mu}^{*} - \underline{\mu}^{*}} \cdot (\mu_{0} - \underline{\mu}^{*}) \right] \, d\mu_{0} \\ &+ \int_{\overline{\mu}^{*}}^{1} \left[ P_{0}(\overline{\mu}^{*}) - \frac{P_{0}(\overline{\mu}^{*})}{1 - \overline{\mu}^{*}} \cdot (\mu_{0} - \overline{\mu}^{*}) \right] \, d\mu_{0}, \\ \hat{W}_{E}(3) &= \int_{0}^{1} (\mu_{0} \Delta V + V_{L}) \, d\mu_{0}, \\ \hat{W}_{E}(4) &= \int_{0}^{\underline{\mu}^{**}} P_{0}(\underline{\mu}^{**}) \cdot \frac{\mu_{0}}{\underline{\mu}^{**}} \, d\mu_{0} + \int_{\underline{\mu}^{**}}^{\overline{\mu}^{**}} \left[ P_{0}(\underline{\mu}^{**}) + \frac{P_{0}(\overline{\mu}^{**}) - P_{0}(\underline{\mu}^{**})}{\overline{\mu}^{**} - \underline{\mu}^{**}} \cdot (\mu_{0} - \underline{\mu}^{**}) \right] \, d\mu_{0} \\ &+ \int_{\overline{\mu}^{**}}^{1} \left[ P_{0}(\overline{\mu}^{**}) - \frac{P_{0}(\overline{\mu}^{**})}{1 - \overline{\mu}^{**}} \cdot (\mu_{0} - \overline{\mu}^{**}) \right] \, d\mu_{0}. \end{split}$$

It is easy to see that  $\hat{W}_E(1) = \hat{W}_E(3)$ , and both achieve the highest possible welfare. It suffices to show that  $\hat{W}_E(4) > \hat{W}_E(2)$ . Intuitively, this is because the

graph of  $\hat{U}_E^2(\mu)$  is beneath that of  $\hat{U}_E^4(\mu)$  for  $\forall \mu \in (0,1)$  due to the convexity of  $P_0(\mu)$ .

Next we formally show that indeed  $\hat{U}_E^4(\mu_0)$  is piece-wise larger than  $\hat{U}_E^2(\mu_0)$ for any prior belief  $\mu_0 \in (0, 1)$ . A graphical illustration is given in Figure 1.13.

- 1. When  $\mu_0 \in (0, \underline{\mu}^{**}]$ , we have shown in the proofs of Proposition 11 and 17 that because  $\underline{\mu}^{**} < \underline{\mu}^*$ , we have  $\frac{P_0(\underline{\mu}^{**})}{\underline{\mu}^{**}} > \frac{P_0(\underline{\mu}^*)}{\underline{\mu}^*}$ . Hence  $\frac{P_0(\underline{\mu}^{**})\mu_0}{\underline{\mu}^{**}} > \frac{P_0(\underline{\mu}^*)\mu_0}{\underline{\mu}^*}$ , i.e.  $\hat{U}_E^4(\mu_0) > \hat{U}_E^2(\mu_0)$ .
- 2. When  $\mu_0 \in (\underline{\mu}^{**}, \underline{\mu}^*)$ ,  $\hat{U}_E^4(\mu_0)$  is a convex combination of  $P_0(\underline{\mu}^{**})$  and  $P_0(\overline{\mu}^{**})$ , which is strictly larger than  $P_0(\underline{\mu}^*)$  due to convexity of  $P_0(\mu)$ . Since  $\hat{U}_E^2(\mu_0) = \frac{P_0(\underline{\mu}^*)\mu_0}{\mu^*} < P_0(\underline{\mu}^*)$ , we have  $\hat{U}_E^4(\mu_0) > \hat{U}_E^2(\mu_0)$ .
- 3. When  $\mu_0 \in [\underline{\mu}^*, \overline{\mu}^*]$ , the convexity of  $P_0(\mu)$  implies that the convex combination of  $P_0(\underline{\mu}^{**})$  and  $P_0(\overline{\mu}^{**})$  strictly dominates the convex combination of  $P_0(\underline{\mu}^*)$  and  $P_0(\overline{\mu}^*)$ . This implies  $\hat{U}_E^4(\mu_0) > \hat{U}_E^2(\mu_0)$ .
- 4. When  $\mu_0 \in (\overline{\mu}^*, \overline{\mu}^{**}), \ \hat{U}_E^2(\mu_0) = P_0(\overline{\mu}^*) \frac{P_0(\overline{\mu}^*)}{1-\overline{\mu}^*} \cdot (\mu_0 \overline{\mu}^*) < P_0(\overline{\mu}^*).$ Also,  $P_0(\overline{\mu}^*)$  is strictly smaller than the convex combination of  $P_0(\underline{\mu}^{**})$  and  $P_0(\overline{\mu}^{**}).$  Hence  $\hat{U}_E^4(\mu_0) > \hat{U}_E^2(\mu_0).$
- 5. When  $\mu_0 \in [\overline{\mu}^{**}, 1)$ , we define

$$\Delta U(\mu_0) \equiv \hat{U}_E^2(\mu_0) - \hat{U}_E^4$$

$$= [(\mu_0) = P_0(\overline{\mu}^*) - \frac{P_0(\overline{\mu}^*)}{1 - \overline{\mu}^*} \cdot (\mu_0 - \overline{\mu}^*)] - [P_0(\overline{\mu}^{**}) - \frac{P_0(\overline{\mu}^{**})}{1 - \overline{\mu}^{**}} \cdot (\mu_0 - \overline{\mu}^{**})].$$

It is easy to see that  $\frac{\partial \Delta U}{\partial \mu_0} = \frac{P_0(\overline{\mu}^{**})}{1-\overline{\mu}^{**}} - \frac{P_0(\overline{\mu}^{*})}{1-\overline{\mu}^{*}} > 0$  and  $\Delta U(\mu_0) = 0$  if  $\mu_0 = 1$ . Hence at  $\mu_0 \in [\overline{\mu}^{**}, 1), \ \Delta U(\mu_0) < 0$ , i.e.  $\hat{U}_E^4(\mu_0) > \hat{U}_E^2(\mu_0)$ . Therefore, it follows naturally that

 $\hat{W}_E(NSS, NDU) = \hat{W}_E(SS, NDU) > \hat{W}_E(SS, DU) > \hat{W}_E(NSS, DU).$ 

Q.E.D.

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## Chapter 3

# Strategic Pricing and Large Shareholder Expropriation in Private Placement of Public Equity

## 3.1 Introduction

This paper presents new evidence on the cost of ownership concentration arising from expropriation behaviors by large (controlling) shareholders through strategic pricing and acquisition of large blocks of new issues in private placement of public equity. Indeed, concentrated ownership allows controlling shareholders to easily exercise full control over the firms and siphon resources out of the firm for their own interests, a practice termed tunneling and commonly observed in emerging markets where both investor protection and enforceability of law are weak (Johnson, La Porta, Lopez-de Silanes, and Shleifer, 2000). By demanding excessive price discounts which yet seems reasonable and justifiable ex ante and purchasing large stakes in private placements, these blockholders further consolidate their power in the firms at fairly low costs and expose the minority shareholders to direct dilution, which results in value destruction of the issuing firms.

Extant work explaining the role of private placement and the associated price discount mainly includes the monitoring hypothesis (Wruck, 1989) where active blockholders enhance their monitoring after subscribing the new issues; the certification hypothesis (Hertzel and Smith, 1993) where informed investors purchase new shares in private placement as certification of a firms market value to reduce information asymmetries between insiders and outside investors; and the reduction of coordination frictions hypothesis (Chakraborty and Gantchev, 2013) where private placement serves as a mechanism to reduce coordination frictions among existing equity holders because of the increase in ownership concentration. These studies start from different angles but come to the same conclusion that private placement is conducive to corporate governance and thus increases firm value. On the other hand, Barclay, Holderness, and Sheehan (2007) point to the negative consequence of private placement by providing extensive evidence to corroborate their managerial entrenchment hypothesis that the management place new shares to passive investors to solidify their control over the firm and subsequently become entrenched. Nevertheless, these explanations are established in capital markets of developed economies such as the US's, where the ownership structure is relatively dispersed and the main agency problem stems from the conflict of interests between managers and outside investors. Moreover, only limited attention has been paid to the functions and economic consequences of private placements in emerging markets, especially those where ownership structure is highly concentrated and a most severe agency conflict lies between large shareholders (very often a controlling shareholder) and other minority shareholders.

In this paper, by focusing on issuing firms with highly concentrated ownership structure, we propose an alternative hypothesis of controlling shareholder expropriation for private placement. In fact, previous literature has noted some drawback of private placement associated with ownership concentration. For instance, Wruck (1989) provides evidence that market reacts negatively to a private placement if it results in a controlling ownership position. We extend Wruck's finding and show that concentrated ownership, and more specifically, participation of a large shareholder in private placement, is at the root of expropriation. We analyze the determinants of pricing in private placement deals, and more importantly, quantify the economic impacts of the abuse of private placement by large shareholders in China listed firms from 2006 to 2013.

The listed firms in China provide us with an ideal laboratory to examine whether, when, and how expropriation by large shareholders through private placement takes place. We lay out the reasons as follows. First, private placement has in fact been the most popular way of refinancing for listed firms in China since 2006. During 2006-2013, for firms conducting seasoned equity offering (SEO), 91.43% of them use private placement. Furthermore, the total proceeds from private placement amount to approximately \$169.4 billion, representing 83.06% of the capital raised in SEO. Second, ownership concentration prevails in China financial markets – all the listed firms have at least one large shareholder if we use 5% as a threshold. In fact, as documented in Jiang and Kim (2015), since 2006, the average stake held by the largest shareholder of a listed (non-financial) firm exceeds 36% (median above 34%) while the 25th percentile of the largest blockholders holdings amounts to around 24%. Using the 20% threshold defined in La Porta, Lopez-de Silanes, and Shleifer (1999), this indicates that the vast majority of listed firms in China have controlling shareholders.<sup>1</sup> Not

<sup>&</sup>lt;sup>1</sup>Furthermore, as noted in Jiang and Kim (2015), there is a strand of literature which document the tunneling behavior by controlling shareholders in China (e.g., Cheung, Jing, Lu,

surprisingly, these shareholders with substantial control over the firm are able to raise fund excessively through private placement at their will and buy dilutive shares at favourable terms to expropriate minority shareholders. Third, China is a country that features weak investor protection which makes large shareholders less likely to hold accountable for their tunneling behaviors. Therefore, the private placement of Chinese listed firms provide a unique institutional and legal environments for the investigation of the markets ex ante valuation of financing decisions motivated by large shareholder expropriation.

Interestingly, private placement of public equity is in fact heavily regulated in China financial markets and there has been a debate among regulators on what legal limits should be placed on the ability of companies to issue securities privately to pre-determined groups of investors. On the one hand, approaches adopted to prevent the abuse of and misconduct in private placement by listed firms management as well as large shareholders are surely beneficial to minority shareholders. On the other hand, it may also hinder the growth of companies and the development of active capital markets. To this end, the revisions in relevant rules and security laws in recent years which attempt to protect minority shareholders still remain controversial. Based on "Rules for the Non-public Issuance of Stocks by Listed Companies" issued by the China Securities Regulatory Commission (CSRC) in 2007, the life-cycle of a private placement mainly consists of the following stages. For any listed company that wants to issue securities privately, it first has to hold a board meeting to pin down a preliminary plan, detailing the purpose of financing, the amount, the issue price, and the potential participants of the private placement, and make relevant disclosure to the public. Routinely, the preliminary plan is subject to the approval by shareholders during the gen-

Rau, and Stouraitis, 2009; Jiang, Lee, and Yue, 2010; Liu and Lu, 2007; Peng, Wei, and Yang, 2011, etc.). These papers find that tunneling occurs in quite different forms (e.g., controlling shareholders siphon, self-deal, and/or enjoy private benefits through corporate loans, earnings management, dividends, and related party transactions).

eral meeting of shareholders. If the plan is voted down during the shareholders meeting or the management wants to revise the plan (especially the pricing of the shares), then another board meeting will be held to amend the private placement prospectus. Again, each time a revised plan put forward by the board has to be approved in another shareholders meeting. The procedure can be repeated until agreement among the management team and the shareholders is achieved or until the board no longer needs any further revision of the plan. Note that timely disclosure of each (board or shareholders) meeting is always required. After reaching the consensus, the firm then files a statement to the CSRC to obtain official approval of issue. It is required that the issuing firm has to announce the (final) confirmation of private placement issuance within 6 months after obtaining approval from the CSRC, otherwise the firm has to apply for issuance again. There is also a lock-in period for shares newly issued. Shares that are placed to firm's related parties (larger shareholders in particular) cannot be traded publicly until 36 months after the final announcement of private issuance while shares placed to other investors usually have a lock-in period of 12 months. Usually, the whole process from the first board meeting to the final announcement will last for about a year.

One thing that is worth particular attention is that the CSRC has stringent rules about the pricing of new private placement issues. It is required that the issuing firm has to choose a *Base Day for Pricing (BDFP)* to fix a benchmark price. The BDFP can be one of the following three days: (i) the announcement day of a board meeting where a private placement plan is approved; (ii) the announcement day of a shareholder meeting where the private placement plan proposed in the previous board meeting is approved by shareholders; (iii) the day of final announcement of private placement issuance. Most of the time the issuing firm would choose (i) as the BDFP. The BDFP is used to calculate a benchmark price which is the trading-volume weighted average price of the last 20 trading days prior to this base day. The securities law prescribes that the minimal issue price should be no less than 90% of the benchmark price.

In this study, we find that the average issue price is 106.64% of the benchmark price. Even for shares placed exclusively to existing large shareholders, the discount is only 3.45% relative to the benchmark. Therefore, with such small discount (and even a premium) expropriation by large shareholders through private placement seems less likely. However, as the large shareholder has strong power in the issuing firm (an average holdings of 36.92% before the private placement in this study), they can strategically choose the BDFP when the firm is underperforming in the stock market. As a result, they are able to acquire a large stake at low price and dilute minority shareholders. Indeed, once we compare the issue price with the price 20 trading days prior to the last announcement of private issue, the average discount turns out to be 18.79%, and 20.38% if the new shares are sold to an extant large shareholder only, both of which are much higher than the ex ante seemingly fair premium (6.64%) and discount (3.45%). Moreover, as a result of the private sale, the holdings of a large shareholder increases from an average of 36.92% to an average of 41.76%, and from 35.09% to 54.79%. We next show that such deep private placement discounts and stock price reactions do reflect tunneling by the larger shareholders.

With the multiple-announcement structure of private placement in China, we are able to document market reaction to each announcement of the issuing firm at different stages of the private placement, and examine its economic implications. We find that the market reacts positively to the announcement of a board meeting that initiates a private placement plan. A further examination reveals that such announcement is associated with a 11.25% increase in equity value if a existing large shareholder is the only participant in the private placement, while the value

increase is only about 2.41% if controlling shareholder does not participate in the private placement. We posit that the stock price reaction consists of two components. First, the stock price movement may reflect market's evaluation of the financing and investment plan. Second, if a large shareholder has private information that the current stock price is undervalued so that he wants to initiate a private placement, the announcement of a private placement plan may serve as a signal to partially reveal this private information. Market adjusts accordingly. Nevertheless, we are unable to disentangle the magnitudes of these two forces econometrically. Also, at this stage investors are not able to form expectation of the exact sizes of the discounts because the private placement is not completed yet, and even might not be conducted eventually. In fact, the investors' evaluation of the price discount and the potential impact of large shareholder expropriation will be deferred until the final announcement of the private issuance when they can calculate the discount based on the price before the announcement.

We then investigate the market reaction to the final announcement and find a negative and significant cumulative abnormal return (CAR) of -2.22%. Using a simple decomposition of the CAR, we demonstrate that although the discounts provide monitoring incentive for private placement participants (Wruck, 1989) and enhance firm value by 3.38%, they result in a direct tunneling of 5.60%.

After confirming our claim that large shareholders can indeed expropriate the minority shareholders through deep discounts in the private sale of public equity, we develop and test the hypothesis that a controlling shareholder is more likely to tunnel a well performing firm (measured by lagged Return on Assets (ROA)), but he refrains from tunneling if a firm's performance is rather poor. We find a strong and negative association between private placement discount and the product of ROA, a dummy which equals 1 if ROA is *non-negative*, and a dummy which equals 1 if a large shareholder participates in the private placement. This means

that a large shareholder's incentive to tunnel is positively correlated with a firm's performance. Nonetheless we also find a weak positive association between price discount and the product of ROA, a dummy which equals 1 if ROA is *negative*, and a dummy which equals 1 if a large shareholder participates in the private placement. This seems to imply that the controlling shareholder is willing to prop up the firm by injecting liquidity to the firm while asking for smaller discount for his acquisition of a large stake during its difficult time. Finally, using the interaction between past performance and a dummy for a large shareholder's participation as a plausible instrumental variable (IV) for the discount, we find that each percent of price discount causes a 0.67% loss of an issuing firm's market value. The exclusion condition of the IV is satisfied because the market reaction to the final announcement only indicates market's evaluation of the magnitude of the realized price discount, yet the IV itself reflects the characteristics that has been incorporated in the stock price due to multiple announcements and thus does not affect the final announcement CAR directly.<sup>1</sup>

There are several contributions of this study. First, we provide a new explanation about the determinants of price discount of private placement – the expropriation hypothesis. Second, the findings of this study provide an improved understanding of private placement pricing and should be of interest to investors, to managers making capital-raising decisions, to exchanges competing for listing firms, and to policy makers in determining the effects of current and prospective regulations. Third, this study contributes to the existing literature by documenting a new form of looting of firms by their controlling shareholders. Moreover, it cautions the negative consequences of ownership concentration.

The rest of our paper is structured as follows. Section 3.2 describes our

<sup>&</sup>lt;sup>1</sup>The participants of the private placement are always disclosed well before the final announcement. We use lagged ROA from an issuing firm's annual financial reporting. Such information is incorporated into stock price when it is disclosed, also well before the final announcement.

sample construction. Section 3.3 presents and discusses the empirical regularities associated with private placements. Section 3.4 concludes.

# 3.2 Institutional Background and Sample Construction

China, now the second largest economy of the world, has gradually transited from a purely planned economy to a market-oriented one. The opening of Shanghai and Shenzhen Stock Exchanges in December 1990 and July 1991 respectively marks the most crucial step of privatization in China. As of now, the combined market capitalization of the two main stock exchanges is ranked second to only the New York Stock Exchange worldwide. The Shanghai Stock Exchange has a main board. The Shenzhen Stock Exchange has three boards: a main board, a board for small and medium sized firms, and a board for young firms. In a sense, the Shanghai Stock Exchange resembles the New York Stock Exchange, which on average has larger firms, while the Shenzhen Stock Exchange is similar to the NASDAQ. The two stock exchanges and the listed firms are regulated by the China Securities Regulatory Commission (CSRC), which can be viewed as the counterpart of the Securities and Exchange Commission (SEC) in the US. There are mainly three types of shares targeted at investors of different categories. The A-shares are regular shares for domestic investors. A small fraction of listed firms have B-shares at the same time. These shares are denominated in foreign currency (US or Hong Kong dollars) and were restricted to foreign investors only until 2001 when the B-Share market started to open to local Chinese. The last type of shares are those cross-listed shares known as H-Shares (if listed in Hong Kong), N-Shares (New York), S-Shares (Singapore), and L-Shares (London). Before 2005, a vast majority of the shares of the listed firms were owned by the state

(or the so-called Stated Owned Enterprises (SOE)) while public ownership was relatively small. Moreover, the state owned shares could not be publicly traded. In 2005, the CSRC launched the *Split Share Reform*, which lifts the restriction of public trading of those non-tradable shares, to further promote the privatization of China's financial markets. For more details, Jiang and Kim (2015) provide a comprehensive overview of the history and structure of China's financial markets.

In fact, the *Split Share Reform* has facilitated the bloom of seasoned equity offering, and especially private offering, by the listed firms since 2006. Private placement of public equity was rare before 2006, yet after the reform, private placement has gradually become the most popular vehicle of re-financing by listed firms in China. <sup>1</sup> As in the introduction we have already discussed the relevant rules and procedure of private placement in China, for brevity, we only summarize the timeline and the key steps in Figure 3.1. Note that the issuing firm can use the announcement day of a board meeting, a general meeting of shareholders, or final issuance as the base day for pricing, and benchmark the issue price against the trading-volume weighted average price of the last 20 trading days prior to the base day. To avoid dilution and expropriation against minority shareholders, the issue price should be no less than 90% of the benchmark. Yet as we will see in the next section, private placement acquirers can get around with this rule easily by strategically selecting periods of stock market underperformance as pricing benchmark to effectively enjoy high price discounts and achieve tunneling.

The primary source of data used in this study comes from the China Stock Market & Accounting Research (CSMAR) Database. We use data on firms listed

<sup>&</sup>lt;sup>1</sup>There is another reason for the popularity of private placement in China after 2005. Before 2006, the main form of seasoned equity financing for listed companies in China was public offering. Yet the listed companies must meet certain criteria regarding its performance to be qualified for new issues. On 9 May 2006, CSRC launched a rule which removes the requirements on prior performance for firms wanting to conduct private placement. Such deregulation makes it easier for listed companies to issue new shares and thus boosts the number of private placements since 2006.

#### 3.2 Institutional Background and Sample Construction



Figure 3.1: Timeline of a Private Placement

on the Main Boards in Shanghai Stock Exchange and Shenzhen Stock Exchange. We focus on deals that issue shares for domestic investors (A-Shares) only. The sample period starts from January 2006 until December 2013. We identify firms conducting private offering of public equity from CSMAR. We download all relevant issuance documents from http://www.cninfo.com.cn, which is the official public disclosure website for China listed companies, and hand collect information regarding the placements and the issuing firms. We exclude financial firms, firms with multiple issues within 100 trading days, issues completed in two steps and announce twice, issues with long periods of trading suspensions or large price jumps prior to deal completions,<sup>1</sup> and issues with missing information. Our final sample includes 707 offerings by 571 firms.

 $<sup>^1\</sup>mathrm{These}$  deals are treated as outliers because they substantially bias our event-study estimation.

# 3.3 Empirical Regularities associated with Private Placements

## 3.3.1 Descriptive Analysis

We first tabulate the frequency of private placements across our sample period in Table 3.1. There are only 44 placements in 2006. From 2007 to 2012, the number of placements has increased to around 90 except for 2008, the year of global financial crisis, which nonetheless still has 67 offerings completed. In 2013, we observe a surge in private placements, with a total number of 123 deals. We then examine the sample characteristics of the private placement deals. In Table 3.2, we summarize the key information regarding these private sales and compare among different types of investors. The average revenue from a private placement amounts to RMB 1,805.02 million, which is roughly \$257.86 million (1 USD  $\approx$  7 RMB). It ranges from RMB 48.67 million to RMB 29,118.76 million, with the median (RMB 19.14 million) quite close to the mean above. The average size of the block sold in the offering represents about 23.80% of the total shares outstanding after the issue, ranging from 1.11% to 86.2%. Dividing the whole sample into three subgroups, we find that shares placed exclusively to existing large shareholders (205 placements) enjoy the highest proceeds of RMB 2412.13 million on average, ranging from RMB 48.67 million to RMB 29,118.76 million, while shares sold to only institutional investors (251 placements) generate the lowest average revenue of RMB 1,150.62 million, ranging from RMB 104.50 million to RMB 12,000.00 million. The number of shares issued in the private placement also differs between these two types of offering. The fraction of shares issued in the former case is about 30.02% of the total outstanding shares after the placement, ranging from 1.47% to 84.71%, while in the latter case the fraction is only 16.28%, ranging from 1.11% to 60.37%. For deals that involve both the existing large shareholders and the institutional investors (245 placements), the average amount of financing is RMB 1,970.94 million, which is about 26.40% of the total shares after the placement. The total proceeds ranges from RMB 136.50 million to RMB 17,438 million and the ratio of the new shares to the total shares after the issuance ranges from 2.51% to 86.20%. In these deals, the controlling shareholder acquires on average 38.27% of the new shares, which represents 10.10% of the ex post outstanding equity of the issuing firm. Moreover, the fraction of new shares purchased by the large shareholder ranges from 5.00% to 98.81%. In all cases, the median new issue sizes (in percentage) are slightly smaller than yet very close to the means, while the median revenues from the offering are right-skewed, all being only approximately half of the means.

#### [Insert Table 3.2 here.]

Because in our sample each issuing firm has at least one large shareholder, we report the average change of ownership by the largest shareholder (controlling shareholder) in Table 3.3. We calculate the fraction of (voting) shares by the largest shareholder to gauge his effective ownership and control over the issuing firm if it has pyramid or more complex ownership structure by following the algorithm in Volpin (2002).<sup>1</sup> We find that the average holdings by the largest shareholder before private placement is 36.92%. For deals targeted at the largest shareholder, the institutional investors, and both, the largest shareholder's ex ante ownership is 35.09%, 41.43%, and 33.91% respectively. After the private offering, the largest shareholder's stake experiences a 4.85% increase and rises to 41.76%. For deals that are restricted to the largest shareholders, they enjoy a substantial top-up of 19.70% in shareholdings and on average become a dominant shareholder (54.79%) after the placement. For deals that the institutional

<sup>&</sup>lt;sup>1</sup>See a detailed description of the algorithm in Table 3.3.

investors are the only participants, the largest shareholder undergoes a decline in ownership from 41.43% to 34.68%. For placements that both the largest shareholder and the institutional investors participate, the increase in holdings by the largest shareholder appears to be at a mild level of 4.24%, going up from 33.91% to 38.14%.

#### [Insert Table 3.3 here.]

Table 3.4 summarizes how long it may take from the first board meeting in which a private placement plan is proposed until the final completion and announcement of the equity offering. The average duration of a private placement issuance  $(\Delta BM1st)$  is roughly a year (363.29 days), with the fastest below 2 months (56 days) and the slowest over 4 years (1504 days). Recall that the issuing firm also has to specify the base day for pricing in order to calculate the benchmark price which is the trading-volume weighted average price of the last 20 trading days prior to the base day. Moreover, the based day can be either the first board meeting or its subsequent shareholders meeting, or alternatively, the final announcement day of deal completion. The gap between the base day and the final announcement ( $\Delta BaseDay$ ) ranges from 0 (which means the base day coincides with the final announcement) to 1504 days, with an average of slightly less than a year (327.86 days). Both  $\Delta BM1st$  and  $\Delta BaseDay$  have medians that are slightly smaller than yet very close to the means. The fact that both gaps are as much as almost a year on average and at the medians implies that most issuing firms choose the first board meeting (or its subsequent shareholders meeting) as the base day for pricing. It is highly likely that the issuing firms are strategically choosing these important dates to sell new issues at favorable price to benefit the placement participants while get around with the rule that issue price should be no less than 90% of the benchmark, as we will show in the subsequent event studies of the next subsection.

[Insert Table 3.4 here.]

We present in Table 3.5 the ratio of the issue price to the benchmark price. The new shares are issued with a 6.64% premium on average. The median issue price is just the benchmark. The issue to benchmark ratio in the whole sample ranges from 38.31% to 549.30%, with its first quartile being 90% and third quartile being 104.48%. Note that although the securities law by the CSRC require that the issue price should not be below 90% of the benchmark, in case the issuing firm has just paid dividends, conducted rights offering, or experienced other important corporate event which may change the value of the shares, this 90% rule is not binding. In fact, in our sample there are 93 firms which price the new shares at lower than 90% of the benchmark. For this group of firms the average issue to benchmark ratio is 80.10% and the median is 87.80%. It ranges from 38.31% to 89.91% with a first quartile of 74.97% and a third quartile of 89.07%. We notice that the new shares sold exclusively to the extant large shareholder are issued at a discounted price of 96.55% of the benchmark, while the issue price of shares placed to only institutional investors is set at 111.01% of the benchmark. Also, the difference between the issue to benchmark ratios in the large-shareholder-only deals and the institutional-investors-only deals is statistically significant at 1% level. This implies a probable ex ante price discrimination against institutional investors and it seems that extant large shareholders exploit their power in the firm to bargain for a favorable purchase price. However, if both the existing large shareholder and the institutional investors participate, the average issue price is 110.68% of the benchmark, which is very close to the ratio in the institutionalinvestors-only deals. Recall that in this type of deals incumbent large shareholders only purchase 38.27%, it seems that large shareholders are not willing to demand a too low price which would also benefit other private placement participants. Nevertheless, by looking at the medians, the issue price is always roughly the benchmark price across different types of deals. In sum, we do not find strong evidence of deep price discounts ex ante at the pricing stage. As a preview, this pattern stands in sharp contrast to the actual price discount when we look at the discrepancies between the issue price and the price just before the final issuance announcement.

[Insert Table 3.5 here.]

## 3.3.2 Stock-Price Reaction Analysis

In this subsection, we present evidence of market reactions to several important announcements regarding the private placement, namely the announcement of the first board meeting that the private placement plan is proposed, the announcement which involves the determination of the base day for pricing used to set the ultimate issue price, and the final issuance announcement.

Following Barclay et al. (2007), we use market-model event-study methodology to document the shareholder wealth changes associated with the above three types of announcements. The model is estimated with a simple OLS regression of the issuing firm's daily stock returns on the Shanghai and Shenzhen Stock Exchanges Composite Indexes. Our estimation window starts from day -219 until day -40 (approximately one calendar year) with day 0 being the relevant announcement of interest. Prediction errors are calculated for each event day from day -20 to day 20; cumulative abnormal returns are obtained by summing and averaging the daily prediction errors over the event window.

We start by examining the stock-price reaction to the announcement of the first board meeting in which a private placement plan is put forward. The first graph in Figure 3.2 plot the price movement from day -20 to day 20 with the gray representing the 95% confidence interval associated with the CAR from day -20 to different days within the event window. We find that the equity value experiences a large and significant increase of up to 6.37% after the announcement. Again, we use the threefold classification of the private placement to identify the market reactions of large-shareholder-only, institutional-investors-only and bothparticipating deals and show the CAR movement in the second graph in Figure 3.2. We observe that the stock returns of the large-shareholder-only deals (red line) are invariably higher than deals of the other two types, with a CAR[-20,20] up to 11.25%. The both-participating deals (yellow line) rank the second in terms of stock returns, with a CAR[-20,20] up to 6.40%. The institutional-investors-only deals (green line) have the lowest CAR[-20,20], which is up to 2.41%.

## [Insert Figure 3.2 here.]

Upon the announcement of the first board meeting, the purpose for financing via private placement is often determined. Yet uncertainty is not always fully resolved, and the financing arrangement may be subject to revision in future meetings. Nevertheless, if the large shareholder is the only participant, it is always disclosed at this stage. Therefore, even though investors do not form expectation of the exact (actual) sizes of price discount, if they are fully rational, they realize that the stock price must be at relatively low level so that potential acquirers will be interested in participating in the private placement. They expect that if the only participant is the existing large shareholder, with his private information he is willing to initiate and take part in the placement when his private information indicates the price to be very low, while deals targeted at only institutional investors should allow some mild yet less degree of stock market underperformance compared to large-shareholder-only deals and bothparticipating deals, to attract participation which gives rise to the ranking of the CAR's among three types of deals as shown in the second graph of Figure 3.2. Effectively, the market reactions reflect investors' re-evaluations of the currently under-valued stock price. Of course, the market reactions also reveal investors' expectation how much value the private placement itself (the use of the proceeds) can bring to the issuing firm, yet econometrically we are not able to disentangle the under-performance component and the value-creation component from the CAR. It is likely that in large-shareholder-only deals, the more concentrated ownership would give the large shareholder more incentive to monitor the firm so that the value increase is the largest among the three types of deals. The reason that the institutional-investor-only deals are associated with the lowest positive CAR's may be that institutional investors in China are very different from those in developed economies. The average holding period of stock shares by an institutional investor in China financial market is only about half a year, and the motivation for equity investment by institutional investors appears to be merely speculative (Jiang and Kim, 2015).

A further analysis of the announcement that concerns the determination of the ultimate base day for pricing confirms our previous argument that the launch of a private placement signals to the market that the current stock price is undervalued. The first graph in Figure 3.3 documents a larger positive CAR[-20,20] (10.03%, p < 0.01) than that in the announcement of the first board meeting. The ranking of the CAR's among the three types of deals extend to what are depicted in the second graph of Figure 3.3. The relevant CAR[-20,20] are 16.02%, 10.57% and 5.25% for large-shareholder-only, both-participating and institutional-investors-only deals respectively, all being larger than their previous counterparts. Not surprisingly, the announcement which contains information about the base day for pricing conveys a stronger signal of stock market underperformance thus market reacts more aggressively to such news.

[Insert Figure 3.3 here.]

We then move to the event-study analysis of the final announcement of the issuance (see Figure 3.4 and Table 3.6). We find that it is associated with a negative CAR[-20,20] of -2.22% which is significant at 1% level. Splitting the sample into the three subgroups, we find that the large-shareholder-only deal on average experiences a significant reduction in equity value by 2.46% while the institutional-investors-only deal's average decline of stock price is -3..80% which is significant at 1% level. For the both-participating deal, the change in firm value is however negligible and not statistically significant.

[Insert Figure 3.4 here.]

[Insert Table 3.6 here.]

We tentatively interpret the results as the following. Note that all the information regarding the private placement are required to be disclosed in previous announcements of board meetings and shareholder meetings before they file a statement to the CSRC for official approval of issuance. <sup>1</sup> As a result, the market reaction to the final announcement of issuance only serves as investors' assessment of joint effect of the value tunneled by placement participants through the actual price discount and the value that will bring to the firm due to the incentive effect of the discount. In this sense, our negative and significant CAR[-20,20]

<sup>&</sup>lt;sup>1</sup>Recall from the timeline in Figure 3.1 that a firm can hold additional board meetings to finalize the private placement prospectus, obtain approval from shareholders, and make multiple announcements for each of the board and shareholders meetings. They are always required to disclose a complete private placement prospectus before they obtain official approval from the CSRC.

suggests that the actual price discount leads to a 2.22% net destruction of the issuing firm's market value.

## 3.3.3 The Actual Price Discount

We define the actual issue price discount around the final announcement of issuance as

$$\text{Discount}_t = \frac{P_t - P}{P_t},$$

where  $t \in [-20, 20]$  which lies within the event window,  $P_t$  is the stock price on day t, and P is the issue price. We calculate the actual price discounts  $P_t$  using stock prices on different event days, and report them in Table 3.7.

#### [Insert Figure 3.7 here.]

We observe that from day -20 to day 20, the actual price discount  $P_t$  first increases from day -20 to day -1 then decreases from day 0 until day 20, which appears to move in the same direction as CAR[-20,t] (Recall from Figure 3.4 that CAR[-20,t] is inverse-V shaped). So there seems to be a simultaneity problem associated with the actual discount and the CAR. In unreported plots, we observe a first negative then positive correlation between  $P_t$  and CAR[-20,20]. Therefore, to identify the true impact of price discount on firm value, we need an IV for the actual price discount. We defer our IV estimate and discussion later. For the moment, to alleviate the interaction between CAR[-20,20] and event day stock price  $P_t$ , I choose Discount<sub>t=-20</sub> as my measure of the actual discount. Table 3.8 presents the summary statistics for the actual price discount of our choice.

[Insert Table 3.8 here.]

Compared with the average issue to benchmark ratio in Table 3.5 which reflects a 6.64% premium, here we find that the issue price is actually discounted by 18.79%! While shares are discounted the most substantially in large-shareholderonly deals, which is 20.38%, the actual discounts in institutional-investors-only and both-participating deals do not appear too differently, which are 18.13% and 18.51% respectively. Accordingly, our results demonstrate that the issuing firms indeed engage in strategic pricing of the new shares in private placement. Figure 3.5 presents the scatter plot of CAR[-20,20] and  $P_{t=-20}$  and its OLS fitted line. We find that for a one-percent increase in the actual discount, it is associated with a decline of 0.168% in issuing firm's equity value which is significant at 1% level. However, as we have pointed out, because of the endogeneity problem, such result can be only interpreted cautiously as descriptive.

[Insert Figure 3.5 here.]

#### 3.3.4 Cumulative Abnormal Return Decomposition

We then use a simple framework to decompose CAR[-20,20] into two parts, the tunneling effect component and the value effect component. We denote the market capitalization of the issuing firm before and after the final announcement as  $P_0(N+M)$  and  $P_0(N+M) + P \Delta N + \Delta V$  respectively. N is the ex ante number of shares held by the large shareholder, M is the ex ante number of shares by dispersed investors, P is the issue price,  $\Delta N$  is the number of new shares issued in private placement, and  $\Delta V$  is the change of firm's market value. Then

$$CAR = \left[\frac{P_0(N+M) + P\,\Delta N + \Delta V}{N+M+\Delta N} - P_0\right]/P_0$$
Tun	neling Effect	Value Effect
$\overline{P-P_0}$	$\Delta N$	$\Delta V$
$=$ $\overline{P_0}$ .	$\boxed{N+M+\Delta N}$	$+ \overline{(M+N+\Delta N)P_0}$
-d	$\Delta \alpha$	

Here we use  $P_0 \equiv P_{t=-20}$  the day -20 stock price. The estimates of the tunneling and the value effects are reported in Table 3.9.

#### [Insert Table 3.9 here.]

We find that on average 5.60% of the equity value is directly tunneled away by large shareholders due to the average actual discount of 18.79%. Yet the value created due to the incentive effect of the actual discount amounts to 3.38%. Putting together, the actual price discount is believed to destroy firm's stock value by 2.22%.

### 3.3.5 Large Shareholder's Incentive of Expropriation

We next test the hypothesis that a large shareholder's incentive to expropriate minority shareholder through deep discount in private placement has to do with the issuing firm's performance. We use return on assets (ROA) as our main measure of firm performance. We calculate it as total net profit over its total asset in the year end prior to the base day for pricing. An existing large shareholder has more incentive to initiate a private placement and set a favorable issue price when the firm is performing well yet its stock is under-valued. Yet an large shareholder refrains from tunneling via excessive discount in private placement if the firm's performance is rather poor. Table 3.11 reports the OLS regression of the actual price discount  $P_{t=-20}$  on the interaction between *ROA* and *Participation1st* and a bunch of control variables. *Participation1st* is a dummy which takes one if an existing large shareholder participates in the private placement. From Model (1) we find that if the large shareholder takes part in the placement, a onepercent increase in ROA is associated with 0.683% more discount demanded by this large shareholder, which is significant at 5% level. By further decomposing  $ROA \times Participation1st$  into  $ROA \times 1\{ROA \ge 0\} \times Participation1st$  and  $ROA \times$  $1\{ROA < 0\} \times Participation1st$ , and after controlling for factors that may affect the actual discount, we find that when the issuing firm is not performing too badly, if a large shareholder participate in the private placement, for each percentage increase in ROA, it is accompanied by 1.479% more actual price discount enjoyed by the large shareholder as reporteded in Model (6). The insignificant coefficient of  $ROA \times 1\{ROA < 0\} \times Participation1st$  suggests that the large shareholder loses incentive to tunnel if the firm has really bad performance.

[Insert Table 3.11 here.]

## 3.3.6 IV Estimation of the Effect of Discount on Firm Value

In this subsection we identify the impact of actual price discount on firm value using an instrumental variable approach. Now that we have shown firm performance matters in determining large shareholder's incentive to demand price discount in private placement, it is natural to instrument  $ROA \times Participation1st$ . The exclusion restriction is satisfied because we use the lagged ROA which is prior to the base day for pricing. Moreover, because of the multiple disclosure associated with announcements at different stages of the private placement before the firm files a statement to the CSRC, whether the large shareholder participates is always observed by investors before the final announcement when the actual discount is realized. Therefore, the product of ROA and Participation1st affects CAR[-20,20] of the final announcement only through its impact on the price discount.

[Insert Table 3.12 here.]

We also include ROA, Participation1st, PreOwn1st which is the ownership of the largest shareholder in the firm before the issuance, and Firm Size in the first stage. The IV, namely  $ROA \times Participation1st$  is significant at 1% level. The F-statistic is 11.71 which is larger than 10. Our second stage estimation suggests that for each percent of actual price discount enjoyed by the placement participant, it causes a destruction of 0.67% of firm's stock value, which is significant at 5% level. A simple OLS regression of CAR[-20,20] on the actual discount and control variable, as presented in Table 3.13, reveals that the simultaneity problem between CAR and discount gives rise to under-estimation of the effect.

[Insert Table 3.13 here.]

### 3.4 Conclusion

This paper present direct evidence that large shareholders can expropriate minority shareholder in the form of paying low price for large blocks of new shares while get around with the seemingly stringent rules of private placement pricing when firm is under-valued in the stock market. The large shareholder's incentive to tunnel via substantial discount in private placement hinges on the discrepancy between firm's stock market and financial performance, and a better performing firm is more prone to looting of resources and has higher risk of dilution from the perspective of minority shareholders. We point out that it is because of the flexibility in choosing the base day for pricing and the benchmark price. It seems that by forcing issuing firms to employ the stock price on the issuance day as

the benchmark may mitigate the conflict of interest between controlling and dispersed shareholders. In fact, the CSRC has been aware of the severity of large shareholder expropriation in private placement. To combat the abuse of private placement and protect investors from tunneling, the CSRC revised the rule in December 2017 which requires that the issue price should be no less than 90% of the trading-volume weighted average price 20 days prior to the announcement of the final issuance. However, the adoption of the rule is accompanied by a drastic reduction in number of private placements conducted by listed firms, which hinders the development of China's capital markets as well as the growth of the listed firms. The main reason might be that these large investors are no longer willing to buy shares with a discount of at most 10%. The firm and its insiders are no longer able to strategically choose the issuance day on which the stock is underperforming because usually it takes a year for a private placement plan to be eventually carried out which involves much too uncertainty. It is subject to the revision by the board, and the approval from shareholders and the CSRC. Moreover, although the actual discount in private placement appears substantial and is heavily criticized by regulators and investors, a recent study by Dong, Gu, and He (2018) show that firms that conduce private placements which involve the participation of large shareholders perform better than those that do not manage to issue equity through private placement. In sum, how private placement in China should be regulated and what the fair price of new issues should be remain an open question for future investigation.

## 3.5 Appendix

Year	Frequency	Percent
2006	44	6.22%
2007	97	13.72%
2008	67	9.48%
2009	86	12.16%
2010	97	13.72%
2011	107	15.13%
2012	86	12.16%
2013	123	17.40%
Total	707	100%

Table 3.1: Distribution of Private Placements by Year

This table presents the frequencies of private placements by year from 2006 to 2013.

Sale Charactersitic	Mean	Median	Std. Dev.	Min	Max
Total (N=707) Block Size (%)	23.80	10.14	16.06	1 11	86.2
RMB Proceeds (millions)	1,805.02	917.40	2,632.62	48.67	29,118.76
Blockholder Only (N=208) Block Size (%) RMB Proceeds (millions)	30.02 2,412.13	27.08 1,124.27	18.87 3,726.68	$1.47 \\48.67$	84.71 29,118.76
Institutional Only (N=251) Block Size (%) RMB Proceeds (million)	16.28 1,150.62	$14.66 \\ 600.10$	9.03 1,435.90	1.11 104.50	60.37 12,000.00
Both (N=245) Block Size (%) Blockholder Fraction (%) RMB Proceeds (million)	26.40 38.27 1,970.94	21.28 33.84 1,100.00	18.59 23.29 2,315.20	$2.51 \\ 5.00 \\ 136.50$	86.20 98.81 17,438.07

Table 3.2: Sample Charactersitics of the Private Placements

This table presents the sample characteristics of the private placements. Blockholder Only indicates the subsample in which the shares are placed to existing large shareholders only in the private offerings. Institutional Only indicates the subsample in which the shares are placed to institutional shareholders only in the private offerings. Both indicates the subsample in which the shares are placed to both existing large shareholders and institutional shareholders in the private offerings. Block Size is measured in relation to total shares outstanding after private placement. RMB Proceeds (millions) measures the total revenue in a private placement in RMB. The exchange rate is roughly 1 USD = 7 RMB. Blockholder Fraction is the ratio of shares purchased by the largest shareholder to total shares placed.

Holdings of	Percent holdings	Percent holdings	Change in
largest shareholders	before (%)	after (%)	holdings $(\%)$
Total (N=707)			
Mean	36.92	41.76	$4.85^{***}$ (7.98)
Median	37.45	41.09	-0.30
Std. Dev.	17.47	17.11	16.15
Blockholder Only (N=208)			
Mean	35.09	54.79	$19.70^{***}$ (18.17)
Median	34.48	55.83	16.36
Std. Dev.	18.01	15.75	15.63
Institutional Only (N=251)			
Mean	41.43	34.68	$-6.75^{***}$ (-21.97)
Median	41.92	34.34	-5.41
Std. Dev.	16.53	14.35	4.87
Both $(N=245)$			
Mean	33.91	38.14	$\begin{array}{c} 4.24^{***} \\ (4.75) \end{array}$
Median	36.02	38.12	0
Std. Dev.	17.07	14.57	13.95

Table 3.3: Large Shareholder Ownership before and after Placement

This table presents the large shareholder's ownership before and after private placement. *Blockholder Only* indicates the subsample in which the shares are placed to existing large shareholders only in the private offerings. *Institutional Only* indicates the subsample in which the shares are placed to institutional shareholders only in the private offerings. *Both* indicates the subsample in which the shares are placed to both existing large shareholders and institutional shareholders in the private offerings. We calculate the fraction of (voting) shares by its ultimate controller following Volpin (2002): If a firm A is controlled indirectly via another traded firm B, the fraction of voting rights of A in the hands of the controlling shareholder is equal to the minimum between the voting rights owned by the controlling shareholder in B and the voting rights owned by firm B in firm A. This algorithm can be generalized to more layers of controls and to more complex control structures.

Table 3.4: Days from 1st Board Meeting/Base Day to Final Announcement

variable	0.05	mean	S.D.	Min	25%	Median	75%	Max
$\Delta BM1st$ 7	707	363.29	181.61	56	236	327	428	1504
$\Delta BaseDay$ 7	707	327.86	173.58	0	219	298	391	1504

This table presents the number of days from the 1st board meeting/base day for pricing to final announcement of private placement.  $\Delta BM1st$ : number of days between first board meeting and final announcement.  $\Delta BaseDay$ : number of days between base day for pricing and final announcement.

Table 3.5: Issue Price to Benchmark Price Ratio (in Percentage)

Issue Price to Benchmark	Mean	Median	Std. Dev.	Min	25%	75%	Max	
Total (N=704)	106.64	100.00	38.13	38.31	90.00	104.48	549.30	
Blockholder Only (N=205)	96.55	100.00	10.92	44.65	90.30	100.00	167.11	
Institutional Only $(N=251)$	111.01	98.06	39.19	38.37	90.00	116.09	355.32	
Both $(N=245)$	110.68	100.00	48.93	38.31	90.00	100.00	549.30	

This table presents the price discount/premium offered to private placement participants. It is calculated as the ratio between the issue price and the benchmark. The benchmark is defined as the weighted average price of the 20 trading days prior to the *Base Day for Pricing. Blockholder Only* indicates the subsample in which the shares are placed to existing large shareholders only in the private offerings. *Institutional Only* indicates the subsample in which the shares are placed to institutional shareholders only in the private offerings. *Both* indicates the subsample in which the shares are placed to both existing large shareholders and institutional shareholders in the private offerings.

	All	Blockholder Only	Institutional Only	Both
	(n=707)	(n=208)	(n=251)	(n=245)
CAR[-20,0]	$1.53\%^{***}$	$2.09\%^{**}$	0.09%	$2.49\%^{***}$
	(< 0.01)	(0.02)	(0.90)	(<0.01)
CAR[-20, 15]	$-1.94\%^{***}$	$2.68\%^{**}$	-3.12%***	0.20%
	(< 0.01)	(0.02)	(<0.01)	(0.86)
CAR[-20, 20]	-2.22%***	-2.46%**	-3.80%***	-0.45%
	(< 0.01)	(0.02)	(< 0.01)	(0.36)

Table 3.6: Mean Cumulative Abnormal Returns of the Final Announcement

This table presents the mean cumulative abnormal returns (CAR) using a market model with an estimation window from day -219 to day 40 and day 0 being the final announcement of the private placement. CAR[-20, t] stands for the CAR from day -20 to day t (t = 0, 15, 20). Blockholder Only indicates the subsample in which the shares are placed to existing large shareholders only in the private offerings. Institutional Only indicates the subsample in which the shares are placed to institutional shareholders only in the private offerings. Both indicates the subsample in which the shares are placed to both existing large shareholders and institutional shareholders in the private offerings. The p-value that the CAR is different from zero is reported in the parenthesis.

Discount	Obs	Mean	Median	S.D.	Min	Max
t = -20	707	18.79	18.66	29.16	-221.74	85.19
t = -10	707	19.68	19.79	29.11	-156.74	86.15
t = 0	707	21.06	21.30	28.99	-141.04	85.63
t = 10	707	19.50	20.86	30.46	-139.74	86.32
t = 20	707	19.27	21.22	31.39	-198.70	84.09

Table 3.7: Different Definitions of Actual Issue Price Discounts (in Percentage)

This table presents the actual issue price discount of private placement using different definitions. For each  $t \in \{-20, -10, 0, 10, 20\}$ , we calculate the relevant discount as  $\frac{P_t - P}{P_t}$  where  $P_t$  is the stock price at day t and P is the issue price in the private placement.

Table 3.8: Using Day -20 Stock Price to Define  $Discount \equiv \frac{P_{i,-20} - P_i}{P_{i,-20}}$ 

	Obs	Mean	Median	S.D.	Min	Max		
Total (%)	707	18.79	18.66	29.16	-221.74	85.19		
Block Only (%)	208	20.38	25.91	43.55	-221.74	85.19		
Institutional Only (%)	251	18.13	18.11	14.94	-55.66	70.18		
Both $(\%)$	245	18.51	15.81	24.65	-117.12	80.74		
This table presents subs	ample	distribu	utions of t	he actu	al issue pr	rice dis-		
count of private placem	ent. V	Ve calcu	late the d	iscount	as $\frac{P_{i,20} - P_{i,20}}{P_{i,20}}$	where		
$P_{i,-20}$ is firm <i>i</i> 's stock p	orice a	t day —	20 and $P_i$	is the i	issue price	e in the		
private placement. Note	that	day 0 is	the day of	f the fin	al announ	cement		
of the private placemen	t. Bla	ockholder	r Only ind	dicates 1	the subsat	mple in		
which the shares are pl	laced 1	to existi	ng large s	shareho	lders only	in the		
private offerings. Instit	tution	al Only	indicates	the sub	sample ir	n which		
the shares are placed to institutional shareholders only in the private								
offerings. <i>Both</i> indicates the subsample in which the shares are placed								
to both existing large shareholders and institutional shareholders in the								
private offerings.								

Table 3.9: Estimates of Tunneling and Value Effects (in Percentage)

	Obs	Mean	Median	S.E.
Tunneling Effect $(\%)$	707	-5.60	-2.89	0.45
Value Effect $(\%)$	707	3.38	2.64	0.77
CAR[-20,20] (%)	707	-2.22	-2.56	0.71

This table presents estimates of the tunneling and value effects from a simple decomposition of the CAR as the following. Market capitalization before and after final announcement are denoted as  $P_0(N+M)$ and  $P_0(N+M)+P\Delta N+\Delta V$  respectively. N: shares held by the large shareholder, M: shares by dispersed investors, P: issue price,  $\Delta N$ : new shares issued,  $\Delta V$ : change of firm's market value. Then

$$CAR = \left[\frac{P_0(N+M) + P \Delta N + \Delta V}{N+M + \Delta N} - P_0\right] / P_0$$
$$= \underbrace{\underbrace{\frac{P - P_0}{P_0}}_{-d} \cdot \underbrace{\frac{\Delta N}{N+M + \Delta N}}_{\Delta \alpha}}_{\text{A}} + \underbrace{\underbrace{\frac{\nabla A \text{Uue Effect}}{\Delta V}}_{(M+N+\Delta N)P_0}}_{\text{A}}.$$

Here we use  $P_0 \equiv P_{i,-20}$  the day -20 stock price of firm *i*.

Table 3.10: Variable Definitions

Variables	Definition
Discount	Actual price discount in private placement, defined as $\frac{P_{i,20}-P_i}{P_{i,20}}$ where $P_{i,-20}$ is firm <i>i</i> 's stock
	price at day $-20$ and $P_i$ is the issue price in the private placement. Note that day 0 is the
	day of the final announcement of the private placement.
Firm Size	Firm size, defined as the natural log of one plus a firm's total assets.
Paticipation1st	A dummy variable which takes 1 if the largest blockholder participates in private placement.
Paticipation Ins	A dummy variable which take 1 if institutional investors participate in private placement.
Payment	A dummy variable which take 1 if new shares are paid with assets.
PreOwn1st	The percentage ownership of the largest blockholder before private placement.
ROA	Return on assets, defined as a firm's total net profit over its total asset the year prior to the
	base day for pricing.
$1\{\text{ROA} \ge 0\}$	A dummy variable which takes 1 if $ROA \ge 0$ .
$1\{\text{ROA} < 0\}$	A dummy variable which takes 1 if $ROA < 0$ .

			Disc	count		
-	(1)	(2)	(3)	(4)	(5)	(6)
ROA	$-0.607^{***}$	$-0.607^{***}$	$-0.606^{***}$	$-0.806^{***}$	$-0.731^{***}$	$-0.769^{***}$
Paticipation1st	(0.222) -0.008 (0.023)	(0.222) -0.043 (0.027)	(0.225) $-0.053^{*}$ (0.027)	(0.225) $-0.051^{*}$ (0.027)	(0.224) -0.060** (0.027)	(0.220) (0.009) (0.046)
$ROA \times 1{ROA \ge 0} \times Paticipation1st$	()	$1.305^{***}$ (0.397)	$1.312^{***}$ (0.399)	$1.410^{***}$ (0.405)	$1.383^{***}$ (0.398)	$1.479^{***}$ (0.411)
$ROA \times 1{ROA < 0} \times Paticipation1st$		-0.202 (0.424)	-0.186 (0.429)	0.531 (0.428)	0.504 (0.419)	0.536 (0.433)
Paticipation Ins		~ /	-0.021 (0.030)	-0.017 (0.030)	-0.020 (0.029)	-0.037 (0.037)
Firm Size			. ,	-0.046*** (0.008)	-0.039 <sup>***</sup> (0.008)	-0.039*** (0.008)
PreOwn1st				. ,	$-0.151^{**}$ (0.059)	-0.034 (0.066)
$PreOwn1st \times Paticipation1st$						$-0.176^{*}$ (0.101)
Payment						-0.031 (0.040)
$ROA \times Paticipation1st$	$0.683^{**}$ (0.316)					
Constant	$0.207^{***}$ (0.016)	$0.207^{***}$ (0.016)	$0.228^{***}$ (0.034)	$\begin{array}{c} 1.242^{***} \\ (0.171) \end{array}$	$\begin{array}{c} 1.147^{***} \\ (0.174) \end{array}$	$1.127^{***}$ (0.188)
Observations	707	707	707	707	707	707
R-squared	0.005	0.016	0.017	0.066	0.074	0.078
This table reports the regression resu	ilts of the de	eterminants	of the actual	discount.	The depende	nt variable is

Table 3.11	: Determ	ninants d	of the	Actual	Discount
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This table reports the regression results of the determinants of the actual discount. The dependent variable is *Discount*, the actual discount. The definitions of both the dependent and the independent variables are presented in Table 3.10. White-corrected robust standard errors are provided in parentheses. \* significant at 10% level, \*\* significant at 5% level, \*\*\* significant at 1% level.

	First-Stage	Second-Stage		
	Discount	CAR[-20,20]		
Discount		-0.670**		
		(0.322)		
$ROA \times Paticipation1st$	$1.032^{***}$			
	(0.309)			
ROA	-0.745***	0.112		
	(0.224)	(0.129)		
Paticipation1st	-0.031	$0.032^{*}$		
	(0.023)	(0.017)		
PreOwn1st	-0.149**	-0.149**		
	(0.059)	(0.075)		
Firm Size	-0.042***	-0.022		
	(0.008)	(0.013)		
Constant	$1.190^{***}$	$0.623^{*}$		
	(0.169)	(0.366)		
F-statistic	11.71			
Observations	707	707		

Table 3.12: 2 SLS Estimation

This table reports the 2SLS regression results of the effect of price discount on CAR. The dependent variable of the first stage regression is *Discount*, the actual discount. The dependent variable of the second stage regression is CAR[-20, 20], the cumulative abnormal return from day -20 to day 20 centered around the final announcement of the issuance. The definitions of both *Discount* and the independent variables are presented in Table 3.10. Robust standard errors are provided in parentheses. \* significant at 10% level, \*\* significant at 5% level, \*\*\* significant at 1% level.

	CAR[-20,20]						
	(1)	(2)	(3)	(4)	(5)	(6)	
Discount	-0.168***	-0.170***	-0.177***	-0.181***	-0.182***	-0.179***	
	(0.025)	(0.025)	(0.026)	(0.026)	(0.026)	(0.026)	
Paticipation1st		$0.031^{*}$	$0.033^{**}$	0.027	$0.061^{*}$	$0.081^{**}$	
		(0.016)	(0.016)	(0.017)	(0.036)	(0.036)	
Paticipation Ins		0.013	0.011	0.010	0.010	0.011	
		(0.019)	(0.019)	(0.019)	(0.019)	(0.019)	
Payment		0.006	0.001	0.003	0.004	0.005	
		(0.019)	(0.019)	(0.019)	(0.019)	(0.020)	
Firm Size			-0.006	-0.003	-0.002	-0.001	
			(0.005)	(0.005)	(0.005)	(0.005)	
PreOwn1st				-0.071*	-0.014	-0.022	
				(0.042)	(0.067)	(0.067)	
$PreOwn1st \times Paticipation1st$					-0.089	-0.081	
					(0.081)	(0.081)	
ROA						$0.465^{*}$	
						(0.275)	
$ROA \times 1 \{ROA \ge 0\} \times Paticipation1st$						-0.499	
						(0.352)	
$ROA \times 1 \{ROA < 0\} \times Paticipation1st$						-0.474	
						(0.333)	
Constant	0.011	-0.020	0.115	0.072	0.033	-0.010	
	(0.008)	(0.022)	(0.108)	(0.113)	(0.118)	(0.123)	
Observations	707	707	707	707	707	707	
R-squared	0.061	0.067	0.069	0.073	0.074	0.078	

Table 3.13: OLS Comparison

This table reports the OLS regression results of the effect of price discount on CAR for comparison with the result obtained in the 2SLS estimation. The dependent variable is CAR[-20, 20], the cumulative abnormal return from day -20 to day 20 centered around the final announcement of the issuance. The definitions of the independent variables are presented in Table 3.10. White-corrected robust standard errors are provided in parentheses. \* significant at 10% level, \*\* significant at 5% level, \*\*\* significant at 1% level.



Figure 3.2: Market Reaction to the Announcement of the 1st Board Meeting



Figure 3.3: Market Reaction to the Announcement that Concerns the Base Day for Pricing



Figure 3.4: Market Reaction to the Final Announcement of the Private Placement



Figure 3.5: CAR-Discount Scatter Plot and Linear Fit

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