Experimental and Numerical Investigation on Progressive Collapse Resistance of Post-tensioned Precast Concrete Beam-Column Sub-assemblages

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ABSTRACT

In this paper, four 1/2 scaled precast concrete (PC) beam-column sub-assemblages with high performance connection were tested under push-down loading procedure to study the load resisting mechanism of PC frames subjected to different column removal scenarios. The parameters investigated include the location of column removal and effective prestress in tendons. The test results indicated that the failure modes of unbonded post-tensioned precast concrete (PTPC) frames were different from that of reinforced concrete (RC) frames: no cracks formed in the beams and wide opening formed near the beam to column interfaces. For specimens without overhanging beams, the failure of side column was eccentric compression failure. Moreover, the load resisting mechanisms in PC frames were significantly different from that of RC frames: the compressive arch action (CAA) developed in concrete during column removal was mainly due to actively applied pre-compressive stress in the concrete; CAA will not vanish when severe crush in concrete occurred. Thus, it may provide negative contribution for load resistance when the displacement exceeds one-beam depth; the tensile force developed in the tendons could provide catenary action from the beginning of the test. Moreover, to deeper understand the behavior of tested specimens, numerical analyses were carried out. The effects of concrete strength, axial compression ratio at side columns, and loading approaches on the behavior of the sub-assemblages were also investigated based on validated numerical analysis.

Author Keywords: Progressive Collapse; Precast Concrete; Load Resisting Mechanism; Beam-Column Sub-assembleage

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INTRODUCTION

Due to the increasing terrorist activities recently, the likelihood of structures subjected to extreme loads increased dramatically. After extreme loading, the structures may loss columns or partial of walls, which may cause the shear force and bending moment of the adjacent structural components increase significantly. For a structural frame designed primarily to resist gravity load, the beams adjoining to the damage zone are hardly able to resist the extra bending moment purely relied on their designed flexural strength, and prone to propagate the damage. This type of collapse is called disproportionate collapse or progressive collapse. Progressive collapse first caught the public attentions after the collapse of Ronan Point apartment in 1968. The collapse of Murrah Federal building in 1995 and Twin Tower in World Trade Center in 2001 re-ignited the upsurge for investigating the behavior of buildings to mitigate progressive collapse. Several design guidelines (GSA 2003 and DoD 2009) are successively promulgated. Two main design methods (indirect and direct design) are commonly accepted for evaluation of the progressive collapse risks. For indirect design method, the minimum redundancy, integrity, ductility, and tie-force is required. For direct design method, alternative load path method is commonly used as it is threat independent. As mentioned above, fully relying on flexural strength may be not enough to resist the propagation of damage. Therefore, it is necessary to pursue other possible load resisting mechanisms, which are not evoked in normal building design. Studies (Sasani and Kropelnicki 2008, Yi et al. 2008, Su et al. 2009, Orton et al. 2009, Sadek et al. 2011, Qian and Li
2013, Qian et al. 2015, Yu et al. 2017, Yu et al. 2019) were carried out to evaluate the reliability of compressive arch action (CAA) and tensile catenary action (TCA) to enhance the load resisting capacity of reinforced concrete (RC) frames. Qian and Li (2012), Qian and Li (2015), Lu et al. (2017), and Ren et al. (2016) quantified the slab effects on load resisting capacity of RC frames to mitigate progressive collapse. Orton and Kirby (2014), Qian and Li (2015), Peng et al. (2017), Qian and Li (2017), and Qian et al. (2018) investigated the dynamic response of RC beam-column substructures or flat slab substructures subjected to sudden column removal scenarios. The dynamic increase factors caused by sudden column removal and residual strength of the substructures after dynamic vibration are also evaluated and discussed. However, these experimental works mainly focused on conventional RC frames while studies on precast concrete (PC) frames were rare. Kang and Tan (2015, 2017) conducted two series of PC beam-column substructures with cast-in-place monolithic joints subjected to the loss of a middle column scenario. Moreover, Feng et al. (2019) simulated the behavior of PC frames to resist progressive collapse. These studies found that PC frames with cast-in-place monolithic joints performed similar behavior as conventional RC frames in terms of load resisting mechanism and failure modes. Qian and Li (2019) tested three-dimensional PC beam-column-slab specimens with monolithic joints to evaluate the behavior of PC frames subjected to a penultimate column removal scenario. It was found that PC slabs achieved similar integrity as cast-in-situ slabs. However, milder tensile membrane action could be mobilized due to discontinuous reinforcements in slab. Lew et al. (2017) tested two full-scale PC beam-column sub-assemblages with welded connection (dry connection) subjected to the loss of a middle column scenario. In contrast with conventional RC beam-column sub-assemblages, no TCA was observed in these PC specimens due to fracture of the anchorage bars at the welded connection. Qian and Li (2018)
tested a series of two PC and one RC beam-column-slab substructures subjected to a penultimate column loss scenario. Two PC substructures had welded or bolted beam-to-column connections, respectively. Similar to Lew et al. (2017), fracture of the anchorage studs at welded connection (dry connection) prevented the beams to develop TCA. For the bolted connection (another type of dry connection), the gap between the beam and column interfaces prevents the beams to develop CAA while beam discontinuous longitudinal reinforcements prevents the development of TCA in large deformation stage. The poor behavior of PC substructures with welded and bolted connection requires looking for more robustness type of dry connection to resist progressive collapse. Based on seismic evaluation, PC frames with post-tensioned connections or called post-tensioned precast concrete (PTPC) system may be an alternate choice (Lu et al. 2019).

PTPC system was first proposed by Cheok and Lew (1991) as a portion of PREcast Seismic Structural System (PRESSS) program. Fig. 1 exhibits typical types of PTPC connections: a) unbonded connection; b) partially bonded connection; and c) fully bonded connection. In these connections, two strands pass through the beams and columns parallely to assemble them. Spiral hoops are embedded at the beam ends to enhance the concrete strength. Before assembling, interfaces between the precast beams and columns are grouted. Seismic tests (Cui et al 2017, Guo et al 2019) indicated that PTPC connection has favorable self-centering ability. Fully bonded PTPC beam-column sub-assemblages performed comparable ductility as monolithic RC sub-assemblages. However, as fully bonded PTPC sub-assemblages were prone to develop inelastic strain in the post-tensioning tendons due to uneven distribution of stress. The effective prestressing force in the tendons would reduce in large deformation stage and resulted in the degradation of the ability of shear force transferred from beam to column. To overcome
these drawbacks, extensive studies were carried out on partially bonded or unbonded PTPC beam-column sub-assemblages subjected to seismic loads experimentally. Priestley and Tao (1993) discussed the lateral force-displacement characteristic of partially bonded PTPC beam-column sub-assemblages subjected to seismic loads. Stanton et al. (1997) tested a series of partially bonded PTPC beam-column sub-assemblages with bonded reinforcements at the top and bottom of the beam ends. They found that the hybrid system (post-tensioned tendons and mild reinforcements) could achieve similar flexural strength as conventional RC system even with similar member size. The shear resistance of the hybrid system was superior to that of conventional RC system as no degradation of the shear strength was observed during test. Similar conclusions were found in Stone et al. (1995) based on additional specimens with advanced hybrid system.

Based on above investigations, the advantages of PTPC beam-column sub-assemblages, especially unbonded ones, were summarized as below. If it is designed properly, the post-tensioned tendons will remain elastic at required ultimate displacement. Thus, no prestress force loss would be resulted after unloading from the design level of ductility. Consequently, no degradation of shear friction at beam-column interface occurred. The beam and column elements would only have elastic response and little damage. The PTPC connection has self-centering ability, which means the connections could return to its original equilibrium position without any residual deflection. Although PTPC has so many advantages, few studies were carried out on their progressive collapse resistance. Due to its special configuration of connections, the load resisting mechanisms of PTPC frames are expected to be quite different to that of conventional RC frames and normal PC frames with welded or bolted connection. To fill this gap, in this paper, a series of four unbonded PTPC beam-column sub-assemblages were designed and tested.
The load resisting mechanisms of this type of structure were investigated in detail. Relevant design recommendations were also made.

**Experimental Program**

Figs. 2(a) and (b) illustrate the bending moment diagram of a frame subjected to the loss of an interior and penultimate column, respectively. As shown in the figure, bending moment reverse was observed at the middle joint. Moreover, the negative bending moment at the side joints were increased significantly after removal of the column. Therefore, the sub-assemblages just above the removed column are the key components in the entire frame, as highlighted in Figs. 2(a) and (b). To well reflect the structural mechanisms of the frame, a sub-assemblage consisted of a double-span beam, two overhanging beams, two side columns, and one interior column stub was extracted from a multi-story frame at the inflection points of the bending moment diagram, as illustrated in Fig. 2(a). As shown in Fig. 2(b), for the frame subjected to the loss of a penultimate column scenario, no overhanging beams were designed as the horizontal constraints were mainly controlled by the side column without overhanging beam.

**Specimen Design**

Four 1/2 scaled specimens (UPI-0.4, UPI-0.65, UPE-0.4, and UPE-0.65) were tested in this study, as tabulated in Table 1. The prototype building is an eight-storey frame, which was designed in accordance with ACI 318-14 (2014). The prototype frame was located on a D class site. The design spectral acceleration parameters of $S_{DS}$ and $S_{D1}$ are 0.46 and 0.29, respectively. The design live load of the prototype frame is 2.0 kPa. The dead load including the ceiling weight is 5.1 kPa.

The specimens are named as follows: for an example, UPI-0.4 denotes a PTPC specimen, which has effective prestress of $0.4f_{pu}$ in tendons, subjected to the loss of an interior column.
scenario. Note that $f_{pu}$ represents the ultimate strength of prestressing tendons. Fig. 3 illustrates the dimensions and reinforcement details of tested specimens. All specimens have identical dimensions and reinforcement details. The difference between UPE and UPI series specimens was whether having overhanging beams. As shown in the figure, the cross section of the beam and column is 150 mm×250 mm and 250 mm×250 mm, respectively. For the purpose to install tendons in assembly stage, two PVC ducts with diameter of 20 mm were pre-embedded in PC members before casting. The PC beam was reinforced by 2T12 at both top and bottom layer with reinforcement ratio of 0.66 %. As the longitudinal reinforcements did not pass through the joints, they were bent up to 90 degrees hook with tail of 170 mm (larger than 12$d_b$). Note that, $d_b$ represents diameter of reinforcement. The design span of the beam was 3000 mm and thus, the span/depth ratio was 12. Two prestressing tendons with diameter of 12.7 mm and nominal area of 98.7 mm$^2$ were positioned in ducts in the two-span beams, side columns, and overhanging beams (if any), and were anchored for resisting the gravity and seismic load induced shear force. A steel plate with thickness of 20 mm was placed at jacking end of each tendon. Moreover, spiral hoops with diameter of 60 mm and pitch of 8 mm were installed at the beam ends to further enhance the compressive strength of concrete. For UPE-0.4 and UPI-0.4, effective prestress of 0.4$f_{pu}$ was designed as larger deformation ability was preferred and the fracture of tendons should be prevented in required deformation stage (Chock and Lew 1991). The only difference between UPE-0.65 and UPE-0.4 was higher effective prestress of 0.65$f_{pu}$ designed. As shown in Fig. 3, before post-tensioning, 15 mm wide construction gap between beam and column interfaces was filled by high strength grout (measured compressive strength about 50 MPa). To reduce the loss of prestressing force, the specimens were tested 24 hours after jacking.
**Material Properties**

Based on compressive and split cylinder concrete tests, the compressive strength and splitting tensile strength at the day of test was 40.0 MPa and 3.7 MPa, respectively. The properties of reinforcing bar and prestressing tendons were tabulated in Table 2.

**Test Setup and Instrumentation**

Fig. 4 illustrates the test setup and instrumentations layout of UPI-series specimens, which are similar to Yu and Tan (2017). Relied on the position of inflection points, the column height and length of overhanging beam were determined. Thus, pin support was applied at the bottom of each side column. To exam the effects of axial compressive force at the side column, the column top was supported by a roller, rather than a pin. As shown in Fig. 4(a), another horizontal roller was connected to the overhanging beam to replicate the horizontal constraints from surrounding bays. The axial compressive force \( 0.2f'_cA_x \), where \( f'_c \) is the compressive cylinder strength and \( A_x \) is the sectional area) was applied on the side column by a hydraulic jack (Item 4 in Fig. 4(a)) with a load capacity of 2000 kN and a commonly used self-equilibrium system (based on two 50 mm thick steel plates and four 50 mm diameter bolts). The interior or penultimate column was removed before applying the vertical load, which was applied by a hydraulic jack (Item 1 in Fig. 4(a)). To prevent undesired out-of-plane failure, a specially designed steel assembly (Item 3 in Fig. 4(a)) was installed underneath the jack. For UPE series, no overhanging beams were designed at both sides as the loss of a penultimate column was assumed. In reality, as shown in Fig. 2(b), overhanging beam should be included at one of the side columns to reflect the reality more accurate. However, as pointed by Yu and Tan (2017), for the scenario of loss of a penultimate column, the extent of horizontal constraints was controlled by the side column without overhanging beam. As shown in Fig. 3(c), for UPE series, the
horizontal constraints were only provided by the top roller and bottom pin support. To monitor the behavior of specimens, a series of load cells, linear variable displacement transducers (LVDTs), and strain gauges were installed externally or internally. The applied vertical load was measured by a load cell (Item 2 in Fig. 4(a)) just beneath the jack. The axial force of the roller installed horizontally was measured by the tension/compression load cell (Item 5 in Fig. 4(a)). The horizontal and vertical reaction force at the bottom pin connection was measured by the specially ordered load pin (Item 8 in Fig. 4(a)), which could measure the horizontal and vertical reaction force explicitly. The variation of prestress force in the tendon was monitored by two load cells (Item 7 in Fig. 4(a)). The axial force applied at the side column was monitored by the reading of oil pump for the jack (Item 4 in Fig. 4(a)). A series of LVDTs were installed along the beams and side columns to monitor the deformation of the beams and columns at different loading stages. A series of strain gauges were mounted at beam reinforcements to measure the varying of local strain in reinforcing bars during tests.

Test Results

Four PTPC beam-column sub-assemblages were tested by push-down loading procedure to investigate the behavior of unbonded PTPC frames to resist progressive collapse caused by different column removal scenarios. Main results were tabulated in Table 3 and discussed as below.

Global Behavior and Failure Modes

UPE Series

UPE-0.4 and UPE-0.65, which are subjected to the loss of a penultimate column scenario, have effective prestress \( f_{pe} \) of \( 0.4f_{pu} \) and \( 0.65f_{pu} \), respectively. Fig. 5 shows the applied load-vertical displacement relationship of the specimens. When the vertical displacement of
middle joint (MJD) reached 45 mm and 39 mm, respectively, first peak load of 30 kN and 39 kN were measured for UPE-0.4 and UPE-0.65, respectively, which indicates the specimen with higher effective prestress achieved higher compressive arch action (CAA) capacity due to higher pre-compressive stress in concrete. Further increasing the MJD to 246 mm, the load resistance of UPE-0.4 exceeds that of UPE-0.65 until the end of test. This is because that the specimen with higher effective prestress (UPE-0.65) suffered greater shear and bending moment demands for side columns as well as greater P-Δ effects, which leads to earlier strength and stiffness degradation. Further increasing MJD, wider cracks or opening occurred at beam-column interfaces and accompanied by concrete crushing at the compression toes. At MJD of 315 mm and 270 mm, flexural cracks were also observed at the side columns of UPE-0.4 and UPE-0.65, respectively. The ultimate load capacity of 66 kN was obtained at an MJD of 440 mm for UPE-0.65. At this loading stage, obvious inward lateral movements were observed at right column. Concrete crushing occurred at the outer side of the right column. Further increasing MJD, the failure of the side column became more severe and the load resistant capacity kept decreasing. The test of UPE-0.65 was stopped at an MJD of 599 mm due to severe damage occurred in the side columns. For UPE-0.4, the ultimate load capacity of 73 kN was obtained at an MJD of 540 mm. After that, the load resistance kept decreasing with further increasing the displacement. The failure modes of UPE-0.4 and UPE-0.65 were illustrated in Figs. 6 and 7, respectively.

As shown in the figures, the failure modes of UPE-0.4 and UPE-0.65 were quite similar. No cracks were observed along the whole beam span. This is quite different to conventional RC sub-assemblages (Yu and Tan 2017). In their tests, plastic hinges were formed at the beam ends. In TCA stage, full-depth penetrated flexural cracks formed along the beam as the tensile force in
RC sub-assemblages was provided by continual longitudinal reinforcements, rather than the unbonded prestressing tendons. For UPE series specimen, concrete crushing occurred in the beam’s compression toes with wide openings observed at beam-column interfaces regions. For UPE-0.65, the maximum opening width of 48 mm and 41 mm were measured at the middle column and side column interfaces, respectively. For right column, wide flexural cracks were observed at the inner face and severe concrete crushing occurred at the outer face, which is a typical large eccentric compression failure due to the combined action of lateral tensile force and vertical axial force. However, the left side column experienced narrower flexural cracks as the damage prone to concentrated in one side (relatively weak) although both sides have similar dimensions and reinforcement details.

**UPI Series**

UPI-0.4 has effective prestress of $0.4f_{pu}$. In addition, this specimen subjected to an interior-column-removal scenario and both side columns have overhanging beams. As shown in Fig. 4a, a roller support was applied at each overhanging beam to provide horizontal constraints and thus, compared to UPE-0.4 which has no overhanging beam, UPI-0.4 has a much stronger horizontal constraint at boundary. When MJD reached 10 mm, flexural crack or opening was observed in the beam-column interfaces. When the MJD reached 29 mm, the first peak load of 35 kN, which was 116.6 % of that of UPE-0.4, was measured. Further increase MJD to 110 mm, slight concrete crushing occurred at the middle column-beam interfaces. The flexural cracks first occurred at the right column at an MJD of 320 mm. Further increasing MJD, the opening at the beam-column interfaces became wider. With the increase of MJD to 631 mm, the fracture of one wire at the bottom tendon resulted in a sudden drop of load resistance. And the maximum opening width of 57 mm and 67 mm were measured at the middle column and side column
After that, the load resistance kept increasing with increase of MJD. The test was stopped at an MJD of 652 mm corresponding to the ultimate load capacity of 151 kN as the hydraulic jack reached its stroke capacity. The failure mode of UPI-0.4 is shown in Fig. 8. Wide opening with width about 60 mm was measured at the beam-middle column interface. For beam-side column interfaces, the beam and column were fully lost contact and only connected by tendons. Different to UPE-0.4, the cracks at the side columns were much thinner and no concrete crushing was observed.

Comparing to UPI-0.4, UPI-0.65 has higher effective prestress of 0.65 $f_{pu}$. The first peak load of 44 kN, which was 125.7% of that of UPI-0.4, was measured at an MJD of 39 mm. As shown in Fig. 5, the load resistance of UPI-0.65 is slightly higher than that of UPI-0.4 before MJD reached 303 mm due to higher effective prestress clamping the specimen tighter and greater compressive arch action was mobilized. The concrete crushing was first observed at the beam-middle column interface at an MJD of 70 mm which was earlier than that of UPI-0.4. The crack occurred at the side column at an MJD of 300 mm, which was also earlier than that of UPI-0.4. The ultimate load of 131 kN was obtained at an MJD of 542 mm. At this stage, some wires of the tendon were ruptured, and the load resistance suddenly dropped. Further increasing MJD, the load resistance almost kept constant. At an MJD of 628 mm, both tendons were fractured and the MJD suddenly increased to 641 mm with the loss of load resistance. And the maximum opening width of 55 mm and 60 mm were measured at the middle column and side column interfaces, respectively. The failure mode of UPI-0.65 was shown in Fig. 9. In general, it was very similar to that of UPI-0.4, except both tendons were fractured.

**Horizontal Reaction Force**

Fig. 10 shows the contribution of horizontal restraints to the total horizontal reaction at
right side. Negative values represent compressive force while positive values mean tensile force. As shown in Fig. 10(a), for UPE-0.65, at small deformation stage, the compressive reaction force mainly attributed into bottom pin connection. However, at large deformation stage, the tensile force is equally from top and bottom supports. Different to UPE-0.65, as shown in Fig. 10(b), the tensile reaction force of UPI-0.65 kept almost constant after MJD beyond 478 mm due to yielding of prestressing tendons. The drop of reaction force at MJD of 542 mm and 628 mm was due to the fracture of tendons suddenly.

**Deformation of Beams and Columns**

The deformation shape of double-span beams of UPI-0.4 is plotted in Fig. 11. It was found that the beam kept almost straightly during the test, which agreed well with the observations that no plastic hinges were formed at the beam ends. In general, similar phenomena were observed for all specimens. Fig. 12(a) shows the drift profile of side column of UPI-0.65. As shown in the figure, the column initially deformed outward (refer to negative value) with maximum outward movement of 0.5 mm at MJD of 100 mm, which was caused by compressive forces developed in the beams. Further increasing the MJD to 300 mm, the side column returned to its initial position. After that, inward movement was observed. The maximum inward movement of 5.1 mm was recorded at MJD of 500 mm due to catenary action developed by prestressing tendons and P-Δ effects. It should be noted that overhanging beams were designed beyond the side column. Fig. 12(b) illustrates the drift profile of right column of UPE-0.65. Similar to UPI-0.65, the maximum outward movement of 0.8 mm was measured at MJD of 100 mm. Then, the side column began to move inward. When the MJD reached 500 mm, the maximum inward movement of 48.1 mm was recorded at the beam axis. The larger inward movement in UPE-0.65 was mainly due to absence of overhanging beams, which resulted in less horizontal constraints for beams.
Moreover, when side column experienced large inward movements, the P-Δ effects due to applied axial force would aggravate the damage of side column and further increased the inward movements. The maximum inward and outward movements of the right column of UPE-0.4 were 0.6 mm and 39.9 mm, which were slightly less than that of UPE-0.65. Fig. 13 illustrates the relationship of total horizontal reaction versus horizontal drift at the center of beam-side column joint. At small deformation stage, the slopes (i.e., horizontal stiffness) of the curves are similar. However, the slopes of UPI series are much larger than that of UPE series at large deformation stage due to considerable constraint provided by the overhanging beams.

**Strain Gauge Reading**

Figs. 14 and 15 show the strain distribution along longitudinal reinforcement of typical specimens. For UPI-0.65, as shown in Fig. 14(a), compressive strain about -280 με was recorded in bottom longitudinal reinforcements after anchoring the tendons. However, when MJD reached 20 mm, some of the measuring point near the interface of middle column reduced to 0 με due to wide opening occurred there. With further increase of MJD up to 250 mm, the compressive strain kept increasing especially for points close to the side column.

However, further increasing the MJD to 500 mm, the compressive strain close to the side column began to reduce as entire section between beam and side column began to separate. For top rebar, as shown in Fig. 14(b), compressive strain about -280 με was also recorded. Conversely, the strain near the side column dropped to 0 με at MJD of 20 mm due to wide opening. Similarly, when MJD reached 500 mm, the strain along whole top rebar began to decrease because entire section between beam and side column began to loss contact or full depth opening. For UPI-0.4, similar results were recorded. The strain along the whole bottom and top rebar almost reduced to 0 με at the MJD of 500 mm due to the opening between the
beam and side column interfaces was wider. For UPE-0.65, as shown in Fig. 15, similar results were observed before the MJD reached 250 mm. However, when MJD achieved 500 mm, the compressive strain at the interfaces between beam and column kept increasing, rather than decreasing. This could be attributed to the large lateral deformation of the side columns allowing the beam and column to keep contact in compressive zone. Similar results were measured for UPE-0.4.

Variation of Prestressing Force in Tendons

Fig. 16 illustrates the various prestressing force in tendons with the increase of MJD. As shown in the figure, after post-tensioning, the total prestressing force of tendons in UPI-0.65, UPI-0.4, UPE-0.4, and UPE-0.65 were 237 kN, 150 kN, 153 kN, and 239 kN, respectively. The measured maximum force of the tendons was 329 kN, 323 kN, 269 kN, and 307 kN, respectively. Thus, only the tendons in UPI series were yielded. Comparing to UPI-0.65, the increase of prestressing force in tendons of UPI-0.4 was much faster. The tendons in UPI-0.65 were yielded at MJD of 322 mm, which was much earlier than that of UPI-0.4 (at MJD of 541 mm).

Discussion of the Results

The Effects of Effective Prestress

As shown in Fig. 5 and Table 3, the first peak load of UPE-0.4, UPE-0.65, UPI-0.4, and UPI-0.65 were 30 kN, 39 kN, 35 kN, and 44 kN, respectively. Thus, higher effective prestress could increase the first peak load by 30.0 % and 25.7 % for UPE and UPI series, respectively. Moreover, the ultimate load capacity of UPE-0.4, UPE-0.65, UPI-0.4, and UPI-0.65 were 73 kN, 66 kN, 151 kN, and 131 kN, respectively. Therefore, the higher effective prestress might aggravate the damage of side column of UPE series specimens and resulted in less ultimate load capacity. As shown in Figs. 7 and 8, the higher effective prestress resulted in the tendons of...
UPI-0.65 began to fracture at MJD of 542 mm, which was much earlier than that of UPI-0.4. Therefore, in general, lower effective prestress was preferred for PTPC frame to resist progressive collapse. Actually, similar suggestion was given by Cheok and Lew (1991) for seismic resisting design.

**The Effects of Boundary Conditions**

As shown in Table 3 and Fig. 5, comparing with UPE series specimens, UPI series specimens increased the first peak load and ultimate load capacity up by 16.7 % and 106.8 %, respectively. Therefore, stronger horizontal constraints might not increase the first peak load significantly. However, stronger horizontal constraints did enhance the ultimate load capacity at large deformation stage effectively. This is because the stronger horizontal constraints allowed full exploitation of the tendons at large deformation stage. Regarding failure modes, the failure of UPE series specimens was controlled by the large eccentric compression failure of the side column. However, the failure of UPI series specimens was controlled by the fracture of tendons.

**Dynamic Resistance of Specimens**

It is worth to note that progressive collapse normally is a dynamic problem. In other words, the column removal is generally in a sudden manner and thus, it is necessary to evaluate the dynamic resistance of the tested specimens via energy method proposed by Izzuddin et al. (2008). In their method, the external work was assumed to equal the strain energy stored in the frame when the kinetic energy was decreased to zero. Thus, the dynamic resistance of the specimens could be determined by Eq. (1).

$$P_d = \frac{1}{u_d} \int_0^{u_d} P(u)du$$  \hspace{1cm} (1)

where $P_d$ and $P(u)$ represent the pseudo-static resistance and the quasi-static resistance at the displacement demand $u_d$, respectively.
Fig. 17 illustrates the behavior of dynamic resistance of the tested specimens. The measured maximum dynamic ultimate load capacity of UPI-0.4, UPI-0.65, UPE-0.4, and UPE-0.65 were 71 kN, 67 kN, 49 kN, and 47 kN, respectively. Similar to the conclusions from non-linear quasi-static tests, the specimens with stronger horizontal constraints achieved larger dynamic ultimate load capacity. The specimens with lower effective prestress in tendons performed better. In DoD (2009), the dynamic increase factor (DIF) could be determined for RC frames by Eq. 2.

\[
DIF = 1.04 + 0.45 \times \frac{\theta_{pra}}{\theta_y} + \frac{l}{l_0}
\]  

(2)

where \( \theta_{pra} \) is the plastic rotation for collapse prevention; \( \theta_y \) is the rotation at yield.

It should be noted that for PTPC frames, beam reinforcements were not yielded during test and thus, Eq. 2 is not suited for PTPC frames. In the future, more dynamic tests and analysis should be carried out to give an equation for predicting DIF of PTPC frames and to refine the design guideline (DoD 2009).

**Variation of Bending Moment in Side Column of UPE Specimens**

The varying of bending moment of the side column of UPE specimens were determined by measured reaction forces to deep understand the failure mode of side columns of UPE specimens. Fig. 18 illustrates the force equilibrium diagram of the side column. The bending moment in section E-E can be determined by Eq. (3):

\[
M_E = H l_0 + V l
\]  

(3)

where \( H \) is horizontal reaction in top horizontal constraint; \( l_0 \) is distance from top horizontal constraint to section E-E; \( V \) is axial compression on side column; and \( l \) is horizontal movement in section E-E.

As shown in Fig. 18, the bending moment was negative (clockwise direction) at small
deformation stage whereas positive (counter-clockwise direction) bending moment was measured at large deformation stage. Compared to the negative bending moment, the positive one was much larger. The maximum positive bending moments of UPE-0.4 and UPE-0.65 were 83.6 kN·m and 85.2 kN·m, respectively. Fig. 19 gives the theoretical bending moment-axial force relationship curve of E-E section. As shown in the figure, the maximum bending moments in E-E section of UPE specimens reached tension failure (large eccentric compression failure), which agreed with the failure mode well.

**Discussion of Load Resisting Mechanisms**

As shown in Figs. 20 and 21, the load resisting mechanism of PTPC frames were different with conventional RC frames (Yu and Tan 2017) or PC frames with monolithic joints (Kang and Tan 2017). For conventional RC frames, the first onset load resisting mechanism is flexural action. Further increasing the displacement, if the beam ends have sufficient horizontal constraints, compressive arch action (CAA) may be triggered as the change of neutral axis may result in the beam end moved outward, which was restrained by, as shown in Fig. 20(a). It is vanished when concrete crushing occurred at the compressive zone. When the beams deformed over one-beam depth, penetrated deep cracks occurred at the beams and the concrete stops to contribute. Therefore, the load resistance is mainly attributed to the tensile force from beam reinforcements, which is called tensile catenary action (TCA), as shown in Fig. 20(b).

However, for PTPC frames, no beam reinforcements passed through the joints and the post-tensioning tendons are unbonded. Thus, no beam action is mobilized to resist progressive collapse. As shown in Fig. 21(a), the concrete suffered considerable initial pre-compressive stress due to post-tensioning. When the beams deformed, the rotation of the beam ends increased the compressive stress in the compressive zone and CAA is developed. However, it should be
emphasized that the cause of CAA in PTPC frame is different to that in RC frame. In PTPC frames, the CAA is actively applied due to post-tensioning tendons and thus, it will not vanish even concrete is crushed. Moreover, as the CAA in PTPC will keep working as long as the beam and column are still in contact and pre-compressive stress maintained. From this, when the MJD beyond one-beam depth, the contribution of CAA in PTPC became negative, as shown in Fig. 21(b). Furthermore, different to RC frames, the TCA of tendons is mobilized from the beginning of the test.

Finite Element Analysis

LS-DYNA (Hallquist 2008) was employed to develop a high fidelity finite element (FE) models to deep understand the test results and to quantify the effects of loading method and specimen design.

Establishment of FE Model

The concrete was modeled by an 8-node solid element with a reduced integration strategy. Reinforcements were modeled by a 2-node Belytschko-Schwer beam element. Unbonded tendon was modeled by 2-node spotweld beam. As shown in Fig. 22, a series of springs (relied on element Combin 165) were horizontally connected to the top of side column and overhanging beam (if any) to simulate the horizontal restraints while the bottom pin connection was modeled by keyword *CONSTRAINED_JOINT_REVOLUTE. Continuous surface cap model (CSCM) was used for concrete material due to its stability and accuracy (Yu et al. 2018, Yu et al. 2019). A bilinear elastic-plastic model *MAT_PLASTIC_KINEMATIC was used for reinforcements. The unbonded tendon was modelled by *MAT_SPOTWELD with proper definition of *INITIAL_AXIAL_FORCE_BEAM. As suggested by previous studies (Yu et al. 2018, Weng et al. 2019), perfect bond between reinforcement and concrete was assumed relied on *
The beam elements of tendon were embedded into concrete solid element by using *CONSTRAINED_BEAM_IN_SOLID whereas the constraint along the beam axis was released to consider unbonded feature between the tendon and concrete. *CONTACT_AUTOMATIC_SINGLE_SURFACE was defined well to simulate the interfaces between the beam and column surfaces. As shown in Fig. 23, based on sensitivity analysis, the beam ends with length of 100 mm from beam-column interface was meshed with size of 12.5 mm. However, the remaining regions were meshed with size of 25 mm because further mesh refining would not enhance the accuracy but increase the computational time significantly.

**FE Model Validations**

Figs. 24 and 25 illustrate the failure modes of UPE-0.65 and UPI-0.65. Comparing with Figs. 7 and 9, it was found that the openings at the beam-column interfaces, concrete crushing at the beam compressive toes, and cracks at side columns could be simulated well. However, for UPE-0.65, its left-side column achieved more severe damage than the right-side column, which was quite different with that from test observations. This could be explained that the damage will concentrate at one of side columns when first crack occurred there, which was random in reality. The failure mode of UPE-0.4 and UPI-0.4 was also well simulated. However, for the sake of brief, the failure mode of UPE-0.4 and UPI-0.4 was not presented herein.

Fig. 26 compares the vertical load-displacement curves while Fig. 27 compares horizontal reaction force-displacement curves. As shown in the figures, in general, the FE models could reproduce the vertical load-displacement curves and horizontal reaction force-displacement curves well. Therefore, the validated FE models were well validated and utilized to deeply understand the test results and to investigate the effects of parameters excluded in experimental program.
Effect of Concrete Compressive Strength

Fig. 28 shows vertical load-displacement curves of UPE-0.65 and UPI-0.65 with different concrete strength. The FPL of UPE-0.65 increased from 41 kN to 46 kN when the concrete compressive strength increased from 30 MPa to 50 MPa. Moreover, the UL increases from 75 kN to 83 kN as the higher concrete compressive strength increased lateral stiffness of the side columns. For UPI-0.65, its FPL increased from 43 kN to 48 kN when the concrete compressive strength increased from 30 MPa to 50 MPa while its UL decreased from 159 kN to 149 kN as the higher concrete strength increased the stiffness of the side column which reduced the deformation capacity of the specimen slightly.

Effect of Axial Compression Ratio on Side Column

Fig. 29 illustrates the effects of axial compression ratio on load resistance of UPE-0.65 and UPI-0.65. Fig. 29(a) indicated that the higher axial compression ratio on side columns has little effects on FPL of UPE-0.65. However, the UL of UPE-0.65 increased from 58 kN to 85 kN when the axial compression ratio increased from 0.0 to 0.4. This is because the higher axial compression force enhanced the lateral stiffness of side column. For UPI-0.65, conversely, higher axial compression force at side columns will decrease the UL in large deformation stage as the higher axial compression force increased the lateral stiffness of the side column, which leads to the tendon fractured earlier.

Effect of Boundary Condition

To further study the effect of boundary condition on the behavior of PTPC frame. A model named UPP-0.65 with asymmetric boundary was built. Compared with UPE-0.65, UPP-0.65 has one overhanging beam at the right side. As shown in Fig. 30, the left side column of UPP-0.65 suffered severe damage while the damage in right side column was milder. In general, as shown
in Fig. 31, the vertical load-displacement curve of UPP-0.65 was similar to that of UPE-0.65. Therefore, the additional overhanging beam on the right side will not affect the behavior of UPE-0.65 significantly since both UPP-0.65 and UPE-0.65 was failed due to large eccentric compression failure of the side column without overhanging beam.

**Effect of Loading Method**

In this study, concentrated load (CL) was applied at the lost column to investigate the load redistribution capacity of the specimens. However, gravity load is uniformly distributed along the beams in reality. Thus, it is necessary to study the difference between these two loading approaches. For this purpose, a multi-point load (ML) system was proposed in this numerical analysis. As shown in Fig. 32, the ML system consists of three load transfer beams, four steel plates, and a series of pin connections. Relying on the proposed ML system, the applied load can be almost equally divided into four point loads. The positions of the four steel plates were determined as shown in Fig. 33(a). As illustrated in Fig. 33(b), the ML system could produce similar bending moment diagram as uniformly distributed load.

Figs. 34 and 35 show the failure mode of UPE-0.65 and UPI-0.65 under ML approach. It was found that the beams did not keep straight, which was quite different from tested specimens. Fig. 36(a) shows comparison of the vertical load-displacement curves of UPI-0.65 from ML and CL approaches. It should be noted that the total load applied by ML approach should be divided by two for equivalently comparing with that from CL approach. At the beginning, the load resistance of UPI-0.65-ML (divided by two) was similar to that of UPI-0.65 measured from CL approach. However, the deformation capacity of UPI-0.65-ML was much lower than that of UPI-0.65-CL as the beams did not keep straight for UPI-0.65-ML. As shown in Fig. 36(b), the load resistance of UPE-0.65-ML (divided by two) was similar to that of UPE-0.65-CL even at
large deformation stage. This is because the failure of UPE-0.65 was controlled by the eccentric compression failure of the side column, rather than the fracture of the tendon. Similar results were observed in UPE-0.4. Therefore, it was concluded that multi-point or uniformly distributed load approach will not affect the failure mode and load resistance significantly, especially when the loss of a penultimate column was considered.

**Conclusions**

In this study, a series of four post-tensioned precast concrete (PTPC) beam-column sub-assemblages were tested under push-down loading procedure. Based on experimental results and analysis, the main conclusions were drawn:

1. As an innovative PC construction type, test results indicated that PTPC frame has excellent performance to mitigate progressive collapse. PTPC frame could develop desired large deformation capacity and ultimate load capacity in large deformation stage.

2. The experimental results and analysis indicated that the load resisting mechanisms mobilized in PTPC frames are quite different from conventional RC frames or PC frames with monolithic joints. The compressive arch action (CAA) in PTPC was generated actively due to pre-compressive stress by tendons. Thus, different to conventional RC frame, the contribution of CAA in PTPC was negative when the vertical displacement beyond about one-beam depth.

3. Different to RC frames, the tensile catenary action (TCA) by tendons is mobilized from the beginning of the test. In RC frames, the CAA and TCA are mobilized in sequence. However, in PTPC frames, the CAA and TCA are developed simultaneously from the beginning of the test.

4. Higher effective prestress could enhance the first peak load of the frame as the higher
effective prestress increased the pre-compressive stress in concrete. However, the higher
effective prestress may also result in the fracture of tendons earlier and reduce its
deformation capacity and ultimate load capacity. Thus, for PTPC frames considering the
risks of progressive collapse, it is suggested to design effective prestress less than 0.65$f_{pu}$.

5. Investigation on the effects of different column removal scenarios indicated that specimens
under the loss of an interior column performed best including the deformation capacity,
ultimate load capacity as well as first peak load capacity. This is because the overhanging
beams beyond the side columns could provide strong horizontal constraints to ensure the
tendon to fully develop its material properties. The failure of UPI series is controlled by
fracture of tendons. However, for UPE series, their failure was controlled by the large
eccentric compression failure of the side column.

6. Numerical results indicated that the concentrated loading approach may change the failure
mode and deformation capacity of the specimen, comparing to multi-point loading approach.
However, it will not affect the load resisting capacity of the specimen significantly.

Data Availability

Some or all data, models, or code generated or used during the study are available from the
corresponding author by request (list items).

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**Figure Captions**

**Fig. 1.** Typical PTPC connections: (a) unbonded connection; (b) partially bonded connection; (c) fully bonded connection

**Fig. 2.** Bending moment diagram of a typical frame after column removal: (a) interior column removal; (b) penultimate column removal

**Fig. 3.** Dimensions and reinforcement details of UPE-0.4 and UPI-0.4

**Fig. 4.** Test setup (a) photograph of UPI-series, (b) schematic view of UPI-series, and (c) UPE-series

**Fig. 5.** Load-displacement relationships of test specimens

**Fig. 6.** Failure mode of specimen UPE-0.4

**Fig. 7.** Failure mode of specimen UPE-0.65

**Fig. 8.** Failure mode of specimen UPI-0.4

**Fig. 9.** Failure mode of specimen UPI-0.65

**Fig. 10.** Contribution of the horizontal reaction at right column: (a) UPE-0.65; (b) UPI-0.65

**Fig. 11.** Deformation shape of double-span beam in UPI-0.4

**Fig. 12.** Horizontal movements in side column: (a) UPI-0.65; (b) UPE-0.65

**Fig. 13.** The relationship of horizontal reaction force v.s. lateral drift at the center of beam-side column joint

**Fig. 14.** Strain distribution along beam rebar of UPI-0.65: (a) bottom rebar; (b) top rebar
Fig. 15. Strain distribution along beam rebar of UPE-0.65: (a) bottom rebar; (b) top rebar

Fig. 16. Total prestressing force of tendons versus MJD

Fig. 17. Dynamic resistance of tested specimens

Fig. 18. The varying of bending moment in E-E section of side column

Fig. 19. Determination of the failure mode of UPE-series specimens

Fig. 20. Typical load resisting mechanisms in RC sub-assemblages: (a) compressive arch action; (b) tensile catenary action

Fig. 21. Schematic view of load resisting mechanisms in PTPC sub-assemblages: (a) relatively small deformation; (b) deformation larger than one-beam depth

Fig. 22. Geometrical model of UPI specimens

Fig. 23. Mesh size for beam end: (a) 8 mm; (b) 12.5 mm; (c) 25 mm

Fig. 24. Simulated mode of UPE-0.65

Fig. 25. Simulated failure mode of UPI-0.65

Fig. 26. Comparison of measured applied load-displacement curves with FE ones: (a) UPE-0.4 and UPI-0.4; (b) UPE-0.65 and UPI-0.65

Fig. 27. Comparison of measured horizontal reaction-displacement curves with FE ones: (a) UPE-0.4 and UPI-0.4; (b) UPE-0.65 and UPI-0.65

Fig. 28. Effect of concrete strength on the resistance: (a) UPE-0.65; (b) UPI-0.65

Fig. 29. Effect of axial compression ratio on the resistance: (a) UPE-0.65; (b) UPI-0.65

Fig. 30. Simulated failure mode of UPP-0.65

Fig. 31. Comparison of applied load-displacement curves of UPE-0.65 and UPP-0.65

Fig. 32. Multipoint loading system

Fig. 33. Determination of loading point position: (a) loading approach; (b) bending moment
Fig. 34. Observation and failure mode of UPE-0.65 under ML approach

Fig. 35. Observation and failure mode of UPI-0.65 under ML approach

Fig. 36. Applied load-displacement curves of under different loading approaches: (a) UPI-0.65; (b) UPE-0.65

Table 1. Specimen Properties

| Test ID     | Effective Axial Position of Span-to-depth Top and bottom Overhanging |
|-------------|----------------------|-----------------|----------------|-------------------------|
|             | prestress compression removed depth beam longitudinal beams       |
| UPE-0.4     | 0.4 $f_{pu}$ 0.2 Penultimate 12 0.66 NA                        |
| UPE-0.65    | 0.65 $f_{pu}$ 0.2 Penultimate 12 0.66 NA                        |
| UPI-0.4     | 0.4 $f_{pu}$ 0.2 Interior 12 0.66 Both sides                   |
| UPI-0.65    | 0.65 $f_{pu}$ 0.2 Interior 12 0.66 Both sides                   |

Note: $f_{pu}$ is the nominal ultimate strength of the post-tensioning tendons (1860 MPa).

Table 2. Material Properties of Reinforcement and Post-tensioning Tendons

<table>
<thead>
<tr>
<th>Item</th>
<th>Nominal diameter (mm)</th>
<th>Yield strength (MPa)</th>
<th>Ultimate strength (MPa)</th>
<th>Elastic modulus (GPa)</th>
<th>Elongation (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>R6</td>
<td>6</td>
<td>368</td>
<td>485</td>
<td>162</td>
<td>20.1</td>
</tr>
<tr>
<td>T12</td>
<td>12</td>
<td>462</td>
<td>596</td>
<td>171</td>
<td>14.7</td>
</tr>
<tr>
<td>T16</td>
<td>16</td>
<td>466</td>
<td>604</td>
<td>182</td>
<td>17.0</td>
</tr>
<tr>
<td>Tendons</td>
<td>12.7</td>
<td>1649</td>
<td>1970</td>
<td>213</td>
<td>6.3</td>
</tr>
</tbody>
</table>

Note: R6 represents plain bar with diameter of 6 mm; T12 and T16 represent deformed rebar with diameter of 12 mm and 16 mm, respectively.

Table 3. Test Results

<table>
<thead>
<tr>
<th>Test ID</th>
<th>MJD at FPL (mm)</th>
<th>MJD at UL (mm)</th>
<th>Resistance Re-ascending (kN)</th>
<th>FPL (kN)</th>
<th>UL (kN)</th>
<th>MHTF (kN)</th>
<th>MHCF (kN)</th>
</tr>
</thead>
<tbody>
<tr>
<td>UPE-0.4</td>
<td>45</td>
<td>540</td>
<td>200</td>
<td>30</td>
<td>73</td>
<td>139</td>
<td>-66</td>
</tr>
<tr>
<td>UPE-0.65</td>
<td>39</td>
<td>440</td>
<td>230</td>
<td>39</td>
<td>66</td>
<td>139</td>
<td>-70</td>
</tr>
<tr>
<td>UPI-0.4</td>
<td>29</td>
<td>652</td>
<td>159</td>
<td>35</td>
<td>151</td>
<td>324</td>
<td>-96</td>
</tr>
<tr>
<td>UPI-0.65</td>
<td>39</td>
<td>542</td>
<td>201</td>
<td>44</td>
<td>131</td>
<td>328</td>
<td>-84</td>
</tr>
</tbody>
</table>

Note: MJD represents middle joint displacement; FPL and UL represent first peak load and ultimate load, respectively; MHTF and MHCF represent maximum horizontal tensile force and maximum horizontal compressive force, respectively.
Figure 1

(a) Unbonded Tendon
(b) Spiral Hoop Grouting Pad
(c) Unbonded Length
Figure 3

(a) Detailing of UPI-0.4

(b) Exterior joint detailing of UPE-0.4

(c) Schematic of simplified boundary condition
1. Hydraulic Jack 1
2. Load Cell 1
3. Steel Assembly
4. Hydraulic Jack 2
5. Tension/Compression Load Cell
6. LVDT
7. Load Cell 2
8. Load Pin

(a) Self-Equilibrium System

(b) Self-Equilibrium System

(c) Self-Equilibrium System

Denotes LVDT
Figure 8
Figure 10
Figure 11

Click here to access/download;Figure;Figure_11.pdf
Figure 14

Click here to access/download;Figure;Figure_14.pdf
Figure 15

(a) Bottom Rebar Strain (με) vs. Distance from Middle Column Interface (mm) after Post-Tensioning for distances of 20 mm, 50 mm, 100 mm, 250 mm, and 500 mm. The strain decreases as the distance from the middle column interface increases.

(b) Top Rebar Strain (με) vs. Distance from Middle Column Interface (mm) after Post-Tensioning for distances of 20 mm, 50 mm, 100 mm, 250 mm, and 500 mm. The strain increases as the distance from the middle column interface increases.
ME = H₁l₀ + V₁

Figure 18

Click here to access/download;Figure;Figure_18.pdf
Theoretical M-N

- UPE-0.4
- UPE-0.65

Figure 19
Figure 21

(a) Interface of Side Column and Applied Vertical Load
(b) Opening and Tendon

Click here to access/download Figure 21.pdf
Figure 26: Diagrams showing applied load versus MJD for different UPE and UPI tests. The diagrams illustrate the comparison between test results and FEM simulations for UPE-0.4 and UPE-0.65, UPI-0.4, and UPI-0.65.
Figure 27
Figure 28

(a) Concrete Strength=30MPa
Concrete Strength=40MPa
Concrete Strength=50MPa

(b) Concrete Strength=30MPa
Concrete Strength=40MPa
Concrete Strength=50MPa

Click here to access/download;Figure;Figure_28.pdf
Figure 29

(a) 

(b)
Severe damage
Severe damage