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# New Client Puzzle Approach for DoS Resistance in Ad hoc Networks

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**Abstract**—In this paper we propose a new client puzzle approach to prevent Denial of Service (DoS) attacks in ad hoc networks. Each node in the network first solves a computational problem and with the solution has to create and solve a client puzzle. By combining computational problems with puzzles, we improve the efficiency and latency of the communicating nodes and resistance in DoS attacks. Experimental results show the effectiveness of our approach.

**Keywords**—Cryptographic Puzzles; Client Puzzles; Denial of Service (DoS); Distributed Denial of Service (DDoS)

## I. INTRODUCTION

DENIAL OF SERVICE ATTACKS (DoS) is considered to be one of the most important threats as well as one of the hardest problems in computer security nowadays. The main aim of a DoS attack is the interruption of services by attempting to limit access to a machine or service instead of subverting the service itself. This kind of attack aims at rendering a network incapable of providing normal service by targeting either the networks bandwidth or its connectivity. These attacks achieve their goal by sending at a victim a stream of packets that swamps his network or processing capacity denying access to his regular clients. In the not so distant past, there have been some large - scale attacks targeting high profile Internet sites [2]. In general, we can distinguish two different types of DoS attacks: logic attacks and flooding attacks. Until nowadays, there are many security vulnerabilities which an adversary can exploit to launch a DoS attack.

Unlike common wireless networks, ad-hoc networks are characterized by the absence of any existing network infrastructure or centralized administration (decentralized wireless network) as well as the ease and speed of deployment. Such networks are highly dynamic and each node participates in the basic functions of the network like packet forwarding and routing, since there are no routers or access points. Ad-hoc networks can operate in a stand-alone way or be attached to a larger network.

Protection against DoS attacks is a crucial component of any

security system. Traditional DoS attacks involve overwhelming a particular host. However, in ad hoc networks, mobility, limited bandwidth, routing functionalities associated with each node, etc, open many new opportunities for launching a DoS attack. These attacks might be at the routing layer or at the MAC layer [9].

### A. Our Contribution

In this paper we propose a new client puzzle to avoid DoS attacks in ad hoc networks, where nodes do not necessarily belong to a single authority and the topology can be altered dynamically. Our solution has the following four attributes:

- The creation of puzzles is not outsourced to a third entity (decentralized design).
- The connection initiator is responsible to create and solve the puzzle on the fly.
- Verifying a puzzle solution requires very little work for a node. More precise, the time needed is comparable with a simple table lookup.
- The difficulty of the puzzle is easy adjustable.

Lot of previous schemes involve puzzle distribution on central units or virtual channels. Our approach is decentralized since this is a fundamental property of ad hoc networks and especially for mobile ad hoc networks (MANETs). In our approach every node that is trying to contact another node has to solve two puzzles. The first one is a discrete logarithm problem (DLP) and the solution of this puzzle will help the connection initiator to create and solve the second puzzle which is considered to be the most difficult. Apart from that, even if a node does not solve correctly the DLP but just find the solution from a table lookup this will not make any harm to our network since the puzzle that will have to create and solve in the next step will be based not only to the solution of DLP but to another random number as well.

Every node needs to follow the same procedure even if it is legitimate or malicious, while the solution of the puzzle can become more difficult or easy depending on the trust

level and traffic congestion. Furthermore, DLP and our puzzle are combined with the best optimum approach for ad hoc networks.

## B. Organization

Following this introduction, the paper is organized as follows. In Section 2, we examine related works to prevent DoS attacks with the use of client puzzles. Section 3 describes our puzzle construction. Section 4 presents experimental results along with the advantages and disadvantages of our technique and Section 5 concludes the paper.

## II. RELATED WORK

Client puzzles approaches have been proposed by several researchers so as to avoid denial of service attacks. For example Juels and Brainard in [5] applied client puzzles to TCP SYN flooding, where they mention that also SSL encloses a parallel problem. In this paper, the authors proposed a cryptographically based countermeasure against connection depletion attacks. Connection depletion is a denial-of-service attack in which an attacker seeks to initiate and leave unresolved a large amount of connection requests to a server, exhausting its resources and rendering it unable to serve valid requests. TCP SYN flooding is a well-known example of such an attack. They introduced a countermeasure (a client puzzle protocol) which the basic scheme was as follows: When a server comes under attack, it distributes small cryptographic puzzles to clients making service requests. To complete its request, a client must solve its puzzle correctly.

An alternative method for implementing client puzzles techniques was proposed by Waters *et al.* [8]. This technique assumes that the client puzzle protocol is a three party protocol and builds a client puzzle based on the discrete logarithm problem for which authenticity and correctness can be verified using a Diffie-Hellman based technique. One of the main differences of this technique is that puzzle generation can be outsourced from the server to another external bastion host, yet verification of solutions can be performed by the server itself [10].

The attack and possible remedies were analyzed in detail by Schuba *et al.* in [6], where they contribute a detailed analysis of the SYN flooding attack and introduced a new solution, which offers protection against these types of attacks for all hosts that are connected to the same local area network and it's independent of their operating system or networking stack implementation.

Narasimhan *et al.* in [11] introduced the notion of hidden puzzle difficulty, where the attacker cannot determine the difficulty of the puzzle without expending a minimal amount of computational resources. Game theory was used to develop defense mechanisms.

Finally, a game based analysis of the client puzzle approach in order to defend DoS attacks have been introduced in [7], where the optimal strategy is derived for the attacked server in order to respond to DoS attacks effectively.

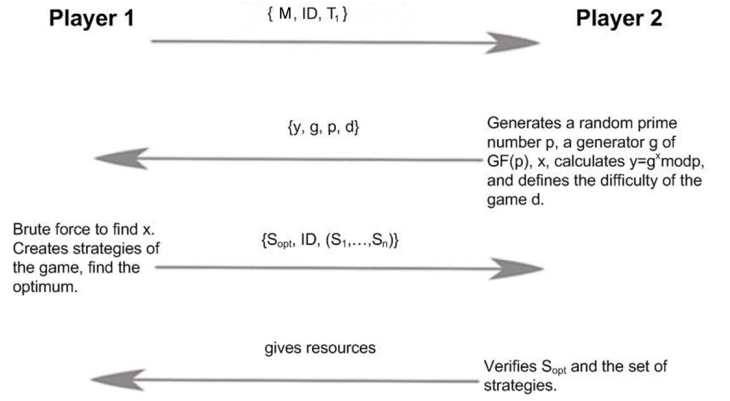


Fig. 1. Client Puzzle

## III. CONSTRUCTION OF THE PUZZLE

Our approach follows similar definitions used in game theory, where we have a set of players  $P_1, P_2 \in P$ , a set of possible strategies  $S_1, S_2, \dots, S_n \in S$  for every player and a payoff for each combination strategies.

Based on Figure 1 let's suppose that  $node_1$  which from now on will be referred as  $P_1$ , wants to communicate with  $node_2$  ( $P_2$ ).  $P_1$  sends to  $P_2$  his  $ID$ , a hello message  $M$  and time stamp  $T_1$ . When  $P_2$  receives these three parameters it first generates a random prime number  $p$ , a generator  $g$  of  $\mathbb{Z}_p^*$  and a random integer  $x$ . Then sets the difficulty level  $d$  of the puzzle that  $P_1$  will have to solve. Next,  $P_2$  calculates value  $y$  according to expression (1) as following:

$$y = g^x \text{ mod } p \quad (1)$$

and responds to  $P_1$  by sending  $g, y, p, T_2, d$ .

When,  $P_1$  receives  $g, y$  and  $p$  solves equation (1) over  $\mathbb{Z}_p^*$  by using the baby-step giant-step algorithm [12]. Next,  $P_1$  computes the integer division of  $x$  and  $d$  of the puzzle (i.e.  $x/d$ ) which is equal to number  $n$  that is needed to create the strategies of the puzzle. After finding  $n$ ,  $P_1$  is responsible for generating and solving the puzzle. This means that  $P_1$  will first need to calculate all strategies  $S$  and second to find the optimum strategy  $S_{opt}$ .

Each nodes strategy is defined as the sum of three positive integers  $(n_1, n_2, n_3)$  in a non-descending order such that:

$$n_1 + n_2 + n_3 = n, \quad (2)$$

where  $n = \lfloor \frac{x}{3} \rfloor$ .

The number of strategies that each puzzle will have, can be easily calculated from the expression (3) of Theorem 1.

*Theorem 1:* For all  $n \in \mathbb{Z}_+^*$  the number of strategies, is given by expression (3)<sup>1</sup>:

$$\Pi(n) = \frac{1}{2} \cdot \lfloor \frac{n}{3} \rfloor \cdot n + \frac{1}{8} \cdot (-1)^{n-3 \lfloor \frac{n}{3} \rfloor} + \frac{1}{8} \cdot (-1)^{1+n} - \frac{3}{4} \cdot \lfloor \frac{n}{3} \rfloor^2 \quad (3)$$

<sup>1</sup>The proof is omitted due to space constrains.

Since  $P_1$  can find all possible strategies of the puzzle, it can also find the optimum strategy ( $S_{opt}$ ). To calculate the optimum strategy,  $P_1$  will 'play' every strategy against all other strategies by using a utility function. However,  $P_1$  compares each strategy by itself and therefore the utility function will take as input two different strategies ( $S = (n_1, n_2, s_3), S' = (n'_1, n'_2, n'_3)$ ), until all possible combinations have been 'played'. The utility function  $U(S, S')$  will have the following three possible results:

- $S$ , if strategy  $S$  has at least two higher coordinates ( $n_i, i \in [1, 3]$ ) than the corresponding ones of strategy  $S'$ .
- $DRAW$ , if strategies  $S, S'$  have one equal coordinate (for example  $n_2 = n'_2$ ) and two different coordinates, but shared equally (for example  $n_1 > n'_1$  and  $n_3 < n'_3$ )
- $S'$ , if strategy  $S'$  has at least two higher coordinates ( $n'_i, i \in [1, 3]$ ) than the corresponding ones of strategy  $S$ .

When  $P_1$  finds  $S_{opt}$ , it sends back to  $P_2$  a set of all strategies  $S$ , optimum strategy  $S_{opt}$ , value of  $x$  and its  $ID$ . Upon reception,  $P_2$  verifies the strategies including the optimum and serves  $P_1$ . An example of how a puzzle can be solved, follows.

**Example 1:** Let's assume that  $n = 6^2$ .  $P_1$  needs to calculate all possible combinations in which  $n$  can be written as a sum of three positive integers in non-decreasing order, such that  $n_1, n_2, n_3 \in [1, n - 2]$ . From expression (3) the number of strategies when  $n = 6$  is  $\Pi(n) = 3$ . Hence,

$$6 = 1 + 1 + 4, 6 = 1 + 2 + 3, 6 = 2 + 2 + 2$$

which means that for this particular puzzle there are the following three strategies:

$$S_1 = (1, 1, 4), S_2 = (1, 2, 3), S_3 = (2, 2, 2). \quad (4)$$

Now  $P_1$  finds the optimum strategy  $S_{opt}$  by using the utility function (if the number of strategies is  $k$ ,  $P_1$  uses the utility function  $\frac{k \cdot (k-1)}{2}$  times). For strategies  $S_1, S_2, S_3$  we have:

$$\begin{aligned} u(S_1, S_2) &= u((1, 1, 4), (1, 2, 3)) \\ \Rightarrow u(S_1, S_2) &= (Draw, S_2, S_1) \\ \Rightarrow u(S_1, S_2) &= Draw \\ u(S_1, S_3) &= u((1, 1, 4), (2, 2, 2)) \\ \Rightarrow u(S_1, S_3) &= (S_3, S_3, S_1) \\ \Rightarrow u(S_1, S_3) &= S_3 \\ u(S_2, S_3) &= u((1, 2, 3), (2, 2, 2)) \\ \Rightarrow u(S_2, S_3) &= (S_3, Draw, S_2) \\ \Rightarrow u(S_2, S_3) &= Draw \end{aligned}$$

From the results above it's clear that the optimum strategy  $S_{opt}$  is  $S_3$  since it wins once and has two draws. Therefore,  $P_1$  sends to  $P_2$  the optimum strategy  $S_{opt}$ , the set of all strategies  $S$ , the value of  $x$  and its  $ID$ . Upon reception of the parameters,  $P_2$  first verifies that equation (III) holds for all

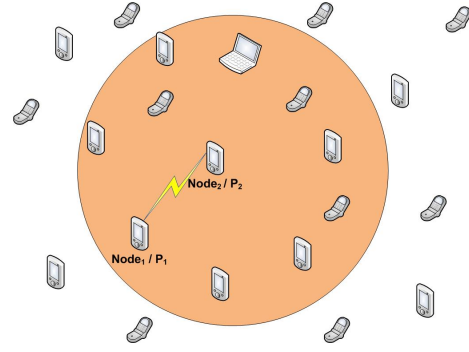


Fig. 2. Small scale ad hoc network.

possible strategies and second uses Algorithm 1 to guarantee that  $P_1$  has correctly found  $S$  and  $S_{opt}$ .

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**Algorithm 1:** Verification of finding  $S$  and  $S_{opt}$

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Input:  $V(S, S_{opt}), x, ID$ 
begin
  if ( $S_{opt}[0] > V_i[0]$  and ( $S_{opt}[1] > V_i[1]$  or
     $S_{opt}[2] > V_i[2]$ ) or ( $S_{opt}[1] > V_i[1]$  and
    ( $S_{opt}[0] > V_i[0]$  or  $S_{opt}[2] > V_i[2]$ )) then
    |  $optWins++$ ;
  end
  if  $V_{i-1}[1] < V_i[1]$  then
    |  $clientSum+ = V_i[0]$ ;
  end
  else
    |  $expectedSum+ = (V_i[1] - j) \cdot V_i[0]$ ;
    | if  $expectedSum == clientSum$  and  $optWins$ 
      |  $\geq \lceil \frac{\Pi(n)}{2} \rceil$  then
        | |  $giveResources$ ;
      end
    | else
      | |  $Drop\ Connection$ ;
    | end
  end
end

```

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#### IV. EXPERIMENTAL RESULTS & SECURITY DISCUSSION

In order to measure the effectiveness of our solution, we have used the Smart Dust simulator written in Java. Our testbed consists of a desktop computer with Xeon CPU at 2.80GHz, with 2.00 GB of RAM running Windows XP.

Our experiments were implemented in a small scale ad hoc network as seen in Figure 2. Every message of a node is broadcasting to each of its neighbors. When nodes wish to communicate with their neighbors, they broadcast a message. Upon reception of messages, nodes check whether a particular message is intended for them. If so, the node processes the request as we described in Section ?? else it drops the message.

<sup>2</sup>This is the smallest value that  $n$  can have, and the solution is trivial.

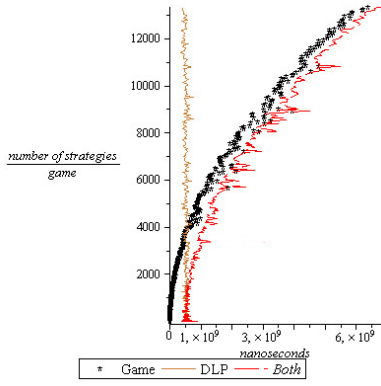


Fig. 3. Number of strategies with relation to time required for the puzzle, the DLP and combination of them.

Figure 3 shows how much time it takes to find  $x$  from (1), to solve only the puzzle (i.e. find  $S_i$  and  $S_{opt}$ ) and to combine both (i.e. client puzzle of Figure 1). Particularly, we tested our algorithm with different levels of difficulty (low, medium, difficult) and solved puzzles that had from 3 up to 13333 number of strategies. From the results we observe that for a puzzle with 13333 strategies the time needed  $P_1$  to solve the puzzle is 6.38 sec, while the time for both solving equation (1) by  $x$  and the puzzle is 6.81 sec, which is an efficient time even for mobile ad hoc nodes even if we consider that there are many puzzles with less number of strategies than 13333 and therefore less time to be solved. Table I, shows some representative values of Figure 3.

TABLE I  
RESULTS FROM FIGURE 3

Strategies	DLP Time(sec)	Puzzle Time(sec)	Combination Time(sec)
444	0.38	0.02	0.40
1976	0.50	0.66	0.89
6769	0.53	1.68	2.21
10034	0.59	3.50	4.10

For solving equation (1) we used the Baby-Step-Giant-Step algorithm which is a generic algorithm that falls into the class of square root algorithms (best possible performance without exploiting properties of a particular group with complexity  $O(\sqrt{n})$ ).

A very important property of client puzzles is the fact that verifying a puzzle solution should require very little work for a server. Considering that, we measured the time that  $P_2$  needs in order to generate the parameters of equation (1) and to verify the solution of the client puzzle. Also we found the time  $P_1$  needs to solve equation (1) and our client puzzle. As seeing in Figure 4, the computational cost of  $P_2$  who generates the DLP and verifies the puzzle, is significantly less than the

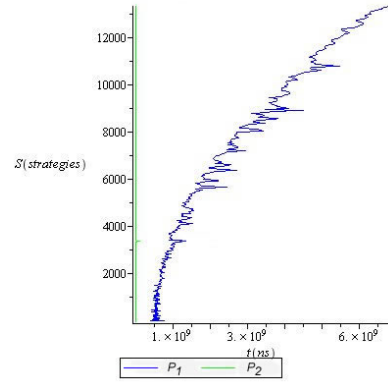


Fig. 4. Time required for  $P_1$  to solve the DLP and the puzzle and for  $P_2$  to verify the solution (Figure 1).

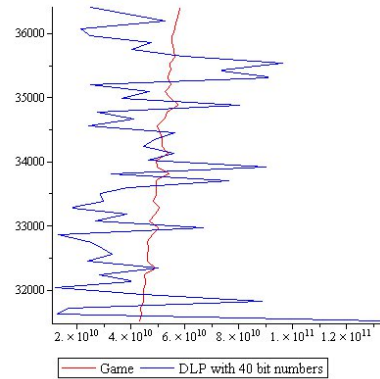


Fig. 5. Discrete Logarithm versus Our Puzzle with more strategies

computational cost of  $P_1$  who solves the puzzle and plays the game. Specifically, the minimum time that a node needs to generate the DLP and to verify the puzzle is 0.0007 secs, while the maximum time is 0.0075 secs (Table II).

TABLE II  
RESULTS FROM FIGURE 4

Strategies	Total Time (sec) for $P_2$	Total Time (sec) for $P_1$
444	0.0020	0.40
1976	0.0038	0.89
6769	0.0048	2.21
13333	0.0057	6.81

To prove the effectiveness of our approach we consider that  $P_1$  and  $P_2$  will solve only our puzzle. In order to achieve the same level of security as before, we increased the number of strategies from 13333 up to 36410. Furthermore, we increased the security level from  $2^{32}$  to  $2^{40}$  for the DLP and we measured the time that  $P_1$  needed to solve it. In this case, the average time was 44.88 secs, while for our puzzle was 50.53 secs.

We noticed that using DLP with 40 bit numbers is making the problem very difficult and thus it is not suitable for ad hoc networks, since every node would have to spend many computational resources and time until it finds the solution. Figure 5 illustrates equation (1) with 40-bits parameters and our puzzle based only on  $S$  and  $S_{opt}$ . As it is seen, there are cases where finding  $S$  and  $S_{opt}$  needs slightly more time than finding  $x$ , but in most cases finding  $x$  takes much more time.

Moreover, we have calculated the complexity of solving the DLP ( $O(\sqrt{n})$ ), of finding  $S$ ,  $S_{opt}$  ( $O(n)$ ) and of completing the client puzzle of Figure 1 ( $O(n\sqrt{n})$ ).

We have also made some attacks to our algorithm, in order to see how it handles malicious requests. Random nodes send requests to  $P_2$ . From the requesting nodes, some of them where malicious and tried to break the security of the system with one of the following ways: Sending strategies from a puzzle that was solved in the past (replay attack), sending the correct optimum strategy but the rest of the strategies was wrong, sending the correct optimum strategy but some of the rest strategies was wrong, sending a totally nonsense answer, sending the correct strategies but a wrong optimum strategy, sending all the strategies correct but did not send the optimum strategy at all and sending wrong  $x$  (did not solve the DLP correct) or fake  $d$ .

Each of the above attacks, the system realized that some of the expected data were wrong and thus the connection with the malicious node was dropped. Note that in our implementation we do not make use of any database to store information, instead only a vector is used where the node saves the id, the value of  $x$  and the difficulty  $d$ . Furthermore, the difficulty of the puzzle is increasing analogous to the requests that a node is receiving from its neighbors. If for example all neighbors send a request between a short time interval  $t$ , then the puzzle will be difficult for all of them. Apart from that, each node can only have a single open connection with each node. This means that multiple requests to the same node are not allowed.

Our approach can prevent TCP SYN flooding attacks, because as we described in Section 3 the node that is making the request has to perform complex computations than the one who is receiving the request. Our technique is based on the concept that we want to put a possible malicious node of an ad hoc network to perform expensive computations, in order to be able to use some of the resources of another node. This means that the resources of the first node will end before the other ones does. This assumption becomes even stronger in the case of ad hoc networks where nodes have limited resources and short battery life. Furthermore, legitimate users would experience just a negligible computational cost, except for the situation that a node is receiving plenty of requests at a specific time interval  $t$  (i.e all of his/her neighbors are sending request at the same time interval  $t$ ).

Attacks like teardrop, bonk and boink are beyond the scope of this paper and we assume that some of the existing techniques can be used in order to defeat them. Most systems knows how to deal with such attacks now and a firewall can drop fragmented packets in return for more latency on network

connections since this makes it disregard all broken packets.

Furthermore, in this paper we do not make use of client puzzle outsourcing techniques since we are referring to ad hoc networks without central authority. The existence of a central unit could lead to situations that malicious nodes could make directly attacks to this machine. Consider a situation where all the nodes in a network are overflowed. Then all the legitimate users will be left without offered services since there would be no one to create puzzles for them neither to verify solved puzzles.

For small smart devices like PDA's and mobile phones, we achieve DoS resistance. We have shown that using only the discrete logarithm problem with a marginary level of security, nodes do not have the necessary resources to solve it. In other words, by increasing the level of security in DLP, the solving time rapidly increases. On the contrary, by adding our puzzle and increasing the number of strategies, with lower level of security in DLP we achieve higher efficiency of computing resources.

## V. CONCLUSION

Unlike traditional networks ad hoc networks use dedicated nodes to support their basic functions like packet forwarding, routing, and network management[1]. In this paper we proposed a new client puzzle to prevent denial of service attacks in ad hoc network nodes. In our approach we do not use any central node that creates client puzzles and verifies the solutions. Instead every node in the network is responsible to generate puzzles and to avoid attacks that could take down the entire network. In our future work we are planning to create a reputation system for every node in a network, that will be based on the solution we presented in this paper. Finally, we are planning to extend our work by creating a distributed DoS defensive mechanism. To do that all nodes will be distributed in groups and they will have to take part to a multiplayer game in order for their requests to be processed.

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