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## ABSTRACT

Shafts are frequently constructed to allow access to subsurface infrastructure and the resulting excavation generally deep and narrow. Shafts may be constructed using a variety of methods and plan forms dependent on ground conditions and intended use. An axisymmetric (cylindrical) geometry is often preferred due to the relatively simple structural analysis, construction method and for a number of approaches that are available to estimate the ground movements around such an excavation. In certain cases, particularly when there is restricted space both above and below surface, non-circular shafts could be a preferred solution. The assessment of surface movements around non-circular shafts is difficult as little information exists and there are few empirical prediction methods available. In this study, a series of centrifuge tests have been conducted to investigate the effects of modifying the cross-sectional profile of a shaft (i.e. circular in plan compared with elliptical). Analysis of measurements obtained from centrifuge tests undertaken at City, University of London's geotechnical centrifuge facility are presented and compared with existing predictive methods. An addendum to the empirical equations and procedures for predicting surface settlements arising from circular shafts is presented to allow for the assessment of movements around elliptical shafts in clay.

## KEYWORDS

Shaft construction; Ground movements; Centrifuge modelling

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## LIST OF SYMBOLS

$a$	Constant indicates the depth at which maximum horizontal displacement occurs
$b$	Constant governs the height of the Gaussian curve
$d$	Distance from the shaft wall
$D$	Shaft diameter
$H$	Shaft depth
$K_0$	The ratio between horizontal and vertical effective stresses at rest
$OCR$	Overconsolidation ratio
$n$	Multiple of shaft depth, $H$ , to a distance, $d$ , from the shaft wall where settlement becomes zero
$PIV$	Particle Image Velocimetry
$PPT$	Pore Pressure Transducer
$S_v$	Vertical soil displacement
$S_h$	Horizontal soil displacement
$S_u$	Undrained shear strength of clay
$\alpha$	Empirical constant
$\phi'_c$	Critical state angle of shearing resistance
$\sigma'_h$	Horizontal effective stress
$\sigma'_v$	Vertical effective stress
$\sigma'_{v0}$	Maximum consolidation pressure for clay model in centrifuge test
$z$	Depth below soil surface

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## 1 INTRODUCTION

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3 In a developed urban environment the surface space is heavily utilised leading engineers to  
4 develop tunnelling solutions for housing transport links, water services, sewage services,  
5 communication networks and electrical lines. Access to these tunnelling systems can be a  
6 considerable challenge, particularly for transportation systems where easy access is required for  
7 thousands of people daily. There are many solutions to this problem of access including the  
8 sinking of shafts to intersect with tunnels or other structures (such as stations) below. The  
9 construction of a deep shaft will generate ground movements driven by reduction of horizontal  
10 stresses on the soil around the shaft and vertical stresses at the base but also influenced by other  
11 factors such as method of shaft construction, workmanship and dewatering. In a dense urban  
12 environment these movements have the potential to cause structural damage to existing surface  
13 and subsurface infrastructure and this must be, at the design stage, assessed.

14 The most common geometric form of a shaft is circular in plan cross-section. This shape is  
15 favoured due to the inherent advantage of radial symmetry. In this case the analysis of the lining  
16 can assume that loads are carried by the stiff hoop and that any ground movements generated  
17 during construction will be radially symmetric both above and below the ground surface. These  
18 assumptions do not, of course, account for variations in the soil around the shaft or construction  
19 methods and tolerances (potentially leading to non-uniform pressures being applied to the lining  
20 and non-uniform ground movement) or the presence of any existing buildings which would also  
21 contribute to asymmetric behaviour.

22 In theory a shaft can be sunk with any cross-sectional geometry. There are obvious  
23 disadvantages to certain shapes (e.g. a square or rectangular shaft would require a stiff design  
24 at the corners of the lining to counter the bending moments generated by the pressure acting on  
25 the sides) but there are advantages to an elliptical cross-section particularly in cases of restricted  
26 surface space (e.g. Feiersinger, 2011). Figure 1 shows a sketch of a hypothetical project to install  
27 two lifts for underground access to a metro station. The lifts are represented by the squares and  
28 the required circular or elliptical shaft to house them is shown. For this particular (notional)  
29 geometry the elliptical shaft has a plan area that is approximately 25% smaller which would have  
30 significant benefit in terms of removal of spoil from site. Additionally, the elliptical geometry could

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31 be aligned in such a way so as to avoid any surface or subsurface structures that may already  
32 exist. Taking into account these potential benefits, the objective of this paper is to provide  
33 experimental data on elliptical shaft construction in clay to support current design methodologies.

34

## 35 SHAFT DESIGN AND CONSTRUCTION

36

37 Construction of a shaft in clay can be carried using a number of methods dependent on the  
38 strength of the clay. Allenby & Kilburn (2015) discuss shaft-sinking techniques divided into two  
39 general categories; underpinning and caisson sinking however Schwamb (2014) also highlights  
40 the use of piling and diaphragm walling as viable construction techniques. In an urban  
41 environment where there are limitations on available space, noise and vibrations, shafts are  
42 usually constructed by underpinning (e.g. Morrison *et al.*, 2004). Underpinning is a construction  
43 technique which incrementally excavates the shaft followed by installation of a pre-cast concrete  
44 segmental lining and grouting behind the annulus (Allenby & Kilburn, 2015). There are also recent  
45 examples of shaft construction in stiff clays using a sprayed concrete lining (e.g. Rutty *et al.*, 2015)  
46 which also use an underpinning method. It is worth highlighting this technique as its flexibility  
47 would make it most suitable for construction of non-circular geometries. When utilising sprayed  
48 concrete, excavation is followed by construction of a primary lining (using sprayed concrete) which  
49 is then supplemented by a secondary lining constructed soon after (usually Cast-in-place or pre-  
50 cast concrete). The primary lining can be assumed to carry none of the load in the long term (as  
51 in Rutty *et al.*, 2015) or it can work with the secondary lining (as in Psomas *et al.*, 2019).

52 Modern geotechnical engineering practice aims to reduce ground movements arising from  
53 construction to a minimum. BS EN 1997-2:2007 (BSI, 2007) specifies that the design of a shaft  
54 (of any cross-section) must include detailed assessments of the adjacent ground movements in  
55 order to assess any impact on existing structures. There is little guidance available to aid with  
56 these assessments although, most notably, New & Bowers (1994) give a prediction method for  
57 surface settlements arising from circular shaft sinking in London clay (recently updated; New,  
58 2017). In this work it is asserted that predictions can only be made by referring to field data in  
59 similar soil conditions but these data are relatively limited in the literature, particularly so when  
60 compared with those of other geotechnical construction events (i.e. tunnelling). Le *et al.* (2019)

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61 extends this work to subsurface movements but again, the field data with which to validate these  
62 methods is limited.

63 When considering an elliptical shaft, it may be possible to adapt the work of New (2017) with  
64 additional modifications or assumptions in order to generate surface settlement predictions.  
65 Alternatively, finite element methods could be used to make predictions of ground movements  
66 (e.g. Pedro *et al.*, 2019) but observational data are vital for validating any numerical analysis of  
67 elliptical shaft excavations. There are very few published case studies reporting the construction  
68 of and the ground movements arising from elliptical shafts. Feiersinger (2011) reports the  
69 construction of a lift shaft at Green Park station in London using a sprayed concrete primary lining  
70 and cast-in-place secondary linings and whilst some information is given on instrumentation that  
71 was installed for surface movements, the measurements reported concentrate on the influence  
72 of the shaft on existing subsurface assets such as escalators and tracks. The shaft is  
73 approximately 27m deep with a major and minor axis of 8.6m and 5.6m respectively in the upper  
74 10m widening to a major and minor axis of 10m and 6.2m for the remaining depth. Topa Gomes  
75 *et al.* (2008) report a shaft construction based on two overlapping ellipses in a relatively  
76 uncongested urban space. Some subsurface movements are presented but relatively close to  
77 the shaft walls. In general, there is a lack of reported case data on which to base future  
78 assessments.

79

## 80 GROUND MOVEMENTS ARISING FROM SHAFT CONSTRUCTION

81

82 Ground movements generated by shaft construction will comprise vertical settlements and  
83 horizontal movements towards the shaft. These are primarily driven by reductions in horizontal  
84 and vertical earth pressures however, as Faustin (2017) identifies, there are many factors that  
85 contribute to the overall movements both in the short and the long term. These include (but are  
86 not limited to) the diameter and depth of the shaft, the construction method employed,  
87 workmanship, ground conditions and other processes such as dewatering or consolidation.

88 The vertical surface settlements arising from sinking a circular shaft in stiff London Clay during  
89 the Heathrow Express Trial Tunnel were reported by New & Bowers (1994) and used to establish

90 **Equation 1.**

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$$S_v = \alpha H \left(1 - \frac{d}{H}\right)^2 \quad (1)$$

91 Where  $S_v$  is the surface settlement at a distance,  $d$ , behind the wall.  $H$  is the depth of shaft and  
 92  $\alpha$  is an empirical constant that depends on ground conditions and construction method (in the  
 93 original work  $\alpha$  had a value of  $6 \times 10^{-4}$ ). The limitations of **Equation 1** are that the diameter of  
 94 excavation is not considered and there is a level of uncertainty surrounding the value of  $\alpha$ .  
 95 Subsequently, New (2017) documented field data from thirteen case studies with a wide range of  
 96 diameters (although predominantly in stiff London Clay). An amendment to **Equation 1** was  
 97 proposed with a new variable,  $n$ , controlling the extent of the vertical settlements around the  
 98 excavation (**Equation 2**).

$$S_v = \alpha H \left(1 - \frac{d}{nH}\right)^2 \quad (2)$$

99 Whilst there is still no explicit term considering the diameter of the shaft, the data presented by  
 100 New (2017) clearly shows that larger shafts produce (as might be expected) larger settlements  
 101 over a greater extent. It might also be logical that softer soils would produce larger movements,  
 102 an observation supported by the experimental data from Le *et al.* (2019).  
 103 As noted earlier, there is limited published data in the literature reporting either field  
 104 measurements, experimental data or numerical analyses of shaft construction. When considering  
 105 elliptical shafts the available literature is even more restricted however, Faustin *et al.* (2018) report  
 106 a series of centrifuge tests on model elliptical shaft excavations in sand. These tests modelled a  
 107 1:80 scale elliptical shaft excavation (with equivalent prototype dimensions of major axis length =  
 108 14.4m, minor axis length = 9.6m and excavation depth 15.4m) in Fraction E Leighton Buzzard  
 109 Sand with a stiff aluminium liner. The measurements during these tests were of the surface  
 110 settlement and lining strains. The surface settlement data was compared with those from tests  
 111 on circular shafts and showed that the maximum settlement was slightly higher in the elliptical  
 112 shaft excavation (0.028%H compared with 0.02%H). However, it should be noted that these  
 113 measurements may not be directly comparable as the plan area of the elliptical shaft modelled is  
 114 larger than that of the circular shaft. Faustin *et al.* (2018) also state that the extent of the surface  
 115 settlements is larger for the circular shaft when compared with the elliptical shaft (1.5H compared



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116 with 1.0H) however the data presented do not necessarily support this rather more measurements  
117 are reported for the circular tests at a greater distance from the shaft.

118 It is clear that, accepting that elliptical shaped shafts are likely to be utilised in future construction  
119 projects, there is a need to understand and predict the movements generated during their  
120 excavation. A series of centrifuge tests to examine this are now described.

121

## 122 CENTRIFUGE TESTING

123

124 Novel apparatus was developed to model the ground movements induced by a circular shaft  
125 excavation in overconsolidated clay (Divall & Goodey, 2016). In that work, good agreement was  
126 shown between the data collected from experiments using this apparatus and the prediction  
127 methods of New (2017). This apparatus does not model the soil-structure interaction between  
128 the soil and the shaft liner but rather it generates ground movements by allowing a small gap  
129 between the soil and a solid former to close, analogous to the volume loss that might be observed  
130 during tunnel excavation. The rationale for this experimental approach is to remove any influence  
131 of liner stiffness and concentrate solely on the patterns of ground movement. Based upon the  
132 designs described by Divall & Goodey (2016), modifications were made to the apparatus for  
133 modelling elliptical shafts whilst using an identical test procedure.

134

### 135 *Test apparatus*

136 A basic apparatus schematic of the shaft centrifuge models is given in Figure 2. In this series of  
137 experiments, all excavations are modelled as half-space simulations. This allows measurements  
138 of soil movement to be made using digital analysis of images taken of the experiment through a  
139 Perspex window on one side of the container. This would not be possible if the experiments  
140 utilised a full model of the shaft. The finished model comprises a consolidated clay sample with  
141 a pre-cut excavation, into which is placed an apparatus supporting that excavation during in-flight  
142 consolidation which then allows simulation of the shaft construction once the groundwater  
143 conditions are established.

144 The apparatus comprises a fully solid former enclosed within a latex bag. This solid former is  
145 used instead of a thin hollow liner to support the soil in its final position as, in these experiments

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146 where only half of the shaft is modelled, use of a thin liner would incorrectly represent the  
147 boundary condition at the edges in the plane of the cut. At the very base of the former, there is a  
148 small cavity which allows for basal heave to develop as the vertical stress is relieved during the  
149 excavation simulation. In this area the former is more representative of the real case but the wall  
150 is sufficiently thick to minimise bending. This apparatus is suspended from a stiff bracket attached  
151 to the upper surface of the box containing the experiment. The former is sized such that when  
152 installed within the pre-cut shaft excavation, there is a 4.5mm annular gap between the clay and  
153 the outer face of the former. The latex bag has a thickness of 1.5mm and, as such, when  
154 assembled there is a uniform 3mm gap around the annulus of the model. This gap can be  
155 considered to represent the amount of overcutting that might occur during excavation and the  
156 former to be the final position of the (e.g.) precast shaft lining. Thus, in the experiment,  
157 movements are driven by the closing of this annular gap. The amount of overcutting modelled  
158 here (300mm at prototype scale) is relatively large (100mm might be expected in practice). The  
159 choice of a 3mm gap is driven by the need to generate movements large enough to measure  
160 however the resulting measurements are normalised for comparison with other experiments or  
161 case studies. The void between former and latex bag (which includes the cavity at the base) is  
162 filled with a heavy fluid (sodium polytungstate) which has a bulk unit weight equivalent to that of  
163 the surrounding soil. This heavy fluid supports the clay both around the shaft and at the formation  
164 level during centrifuge flight whilst the pore pressures in the soil reached hydrostatic equilibrium  
165 with a water table set by a standpipe (at the ground surface) outside the model. Simulation of  
166 construction is then effected by draining the heavy fluid from the base of the latex bag which  
167 simultaneously reduces the horizontal stresses at the shaft perimeter and the vertical stress at  
168 formation level. Figure 3 shows the apparatus, how it sits within the clay model and how it  
169 attaches to the box within which it sits. More details of the model apparatus setup (for the  
170 reference case circular shaft geometry) are given in Le *et al.* (2019).

171 The two model elliptical shafts (shown in Figure 2) had plan cross-sectional areas equal to the  
172 circular shaft which is used as a reference case and is of the same dimensions as that described  
173 by Le *et al.* (2019) which is of 8m diameter and 20m depth at prototype scale, but had major and  
174 minor axes chosen to represent an approximately similar aspect ratio to the lower section of the  
175 elliptical shaft constructed at the Green Park underground station upgrade in London, UK

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176 (Feiersinger, 2011). The tests were conducted at 100g and thus the model elliptical shaft had a  
177 minor axis of 64mm, a major axis of 100mm and a depth of 200mm, the slight variation between  
178 this and the prototype size being due to the requirement of the plan area being the same as the  
179 circular reference case. It should be noted that both apparatus representing the elliptical shafts  
180 have the same dimensions but have their plane of symmetry (in the model) corresponding with  
181 either the major or the minor axis. This approach allows a modelling of models scenario and  
182 enables investigation of the two different ground movement measurement techniques (detailed  
183 later).

184

#### 185 *Test series*

186 A total of three tests were completed during this work. All three clay samples used in the tests  
187 were consolidated to 350kPa and swelled to 250kPa. All samples underwent further in-flight  
188 consolidation on the centrifuge resulting in samples that had varying strength and  
189 overconsolidation ratio with depth. The tests can be separated into two categories; CR, the  
190 reference circular shaft simulation and EL1 & EL2, the two different elliptical shaft simulations.  
191 Details of these test are summarised in Table 1. Where H is the depth of excavation, h is the  
192 horizontal axis length (i.e. the dimension across the box), v is the vertical axis length (the  
193 dimension into the box) and A is the cross-sectional area of the model shafts.

194

#### 195 *Test procedure and instrumentation*

196 The soil samples were created by mixing Speswhite kaolin powder, a clay whose engineering  
197 properties are well-established for centrifuge modelling (Grant, 1998), with distilled water to a  
198 form a slurry with a water content of 120% (twice the liquid limit). This slurry was placed within a  
199 soil container, known as a strongbox, and subjected to a vertical effective stress history as  
200 detailed previously. This process took approximately one week. During the swelling stage, two  
201 pore-water pressure transducers were installed via the back wall of the strongbox, the primary  
202 function of which is to ensure that pore water pressure within the soil achieves equilibrium with  
203 the standpipe during the in-flight consolidation phase.

204 Once the clay sample is prepared, the model making procedure would begin more details on  
205 which can be found in Le *et al.* (2019). The main aspects are briefly described below:

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- 
- 206 • The front wall of the strongbox was removed and the exposed surfaces of the clay sample  
207 were sealed with silicone oil to prevent drying out,
  - 208 • The soil sample was trimmed to the desired model height (275mm) and the semi-  
209 elliptical/circular cavity was manually cut into the front face of the clay sample using a  
210 specially constructed cutter and guide,
  - 211 • This front face of the model was sprayed with dyed blue Leighton Buzzard Sand (Fraction  
212 B) whereas the top of the model was sprinklered with Leighton Buzzard Sand (Fraction E)  
213 to create the texture necessary for post-test image analysis of soil movement,
  - 214 • The 83mm thick PMMA (Poly(methyl methacrylate)) window was bolted to the front of the  
215 strongbox which had the model shaft elements already attached,
  - 216 • The drainage channels were connected and the gantry necessary for 3D topography (Le  
217 *et al.*, 2016) was bolted to the top of the strongbox (Figure 3), and finally,
  - 218 • The latex bag was filled with the heavy fluid and all air bled out of the system.

219

220 The model was placed on the centrifuge swing (City, University of London has access to an  
221 Acutronic 661 and a description of the main features can be found in Panchal, 2018) and  
222 accelerated to 100g. The model was kept at this acceleration until the clay had reached  
223 hydrostatic equilibrium indicated by the stable readings from the aforementioned pore-water  
224 pressure transducers.

225 Simulation of the excavation process was achieved by draining the heavy fluid from the void  
226 between the former and latex bag. The rate of flow of the heavy fluid was set such that the entire  
227 process took approximately three minutes. Data from the surface displacements, subsurface  
228 displacements, pore-water pressure and heavy fluid pressure was taken at a rate of one per  
229 second. Once all ground movements had stopped the model was decelerated and hand shear  
230 vane readings were taken at various depths within the clay outside the zone of influence of the  
231 shaft. These readings could be used to determine the undrained shear strength,  $S_u$ , for each  
232 model. McNamara et al. (2011) demonstrated that, in this type of overconsolidated clay sample,  
233 post-test shear vane readings taken in the far field provided measurements of  $S_u$  directly  
234 comparable with in-flight measurements using a penetrometer and these readings are therefore

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235 considered representative of the initial undrained shear strength of the sample. These results can  
236 be found in Figure 4 along with the calculate variation in OCR.

237

## 238 RESULTS

239

### 240 *Correlation of test data*

241 Before any comparison of settlement data can be undertaken, it is necessary to ascertain the  
242 similarity between each model. Aside from the differences in geometry, there are other  
243 experimental factors that may influence the results obtained such as inconsistencies in undrained  
244 soil strength and initial fluid level within the excavation (i.e. the horizontal pressure supporting the  
245 soil around the shaft). The best fit lines to the measurements of undrained shear strength shown  
246 in Figure 4 indicate that Test CR and EL1 show very similar undrained strength profiles (with  
247 some expected scatter in the discrete readings) whereas Test EL2 is somewhat lower. For  
248 example, at a depth of 100mm (i.e. half the depth of the shaft) the undrained strength of EL2 is  
249 approximately 10% lower than CR and EL1. Pressure measurements within the heavy fluid also  
250 showed that the initial fluid level within the excavation was around 20% higher in Test EL2  
251 compared with that in Tests CR and EL1. These differences in initial conditions arise from the  
252 complex nature of the apparatus and model preparation process but will clearly have an effect on  
253 the measured results.

254 It is necessary to separate the effects on ground movements of these experimental variations  
255 from the differences that arise from changing the geometry of the shaft and a method was devised  
256 to account for the overall influence of the experimental variations. The presence of the stiff former  
257 implies that the end position of the soil is known i.e. once the fluid is drained, the soil moves  
258 (generally) horizontally until it comes into contact with the former. The effect of experimental  
259 differences can therefore be quantified by measuring the horizontal movement of the soil  
260 immediately adjacent to the shaft former as the fluid is drained. This movement must represent  
261 the distance between the soil's initial position and the former. Figure 5 shows this data, obtained  
262 from digital image analysis using geoPIV\_RG (Stanier *et al.*, 2015). It is clear that the horizontal  
263 movements in test EL2 are larger, indicating a bigger initial gap which is considered to be the  
264 dominant factor in the measured surface movements upon excavation. The area under each

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265 curve was obtained by numerical integration and it was found that (considering Test CR as the  
266 reference case) test EL1 had horizontal movements that were 3% lower than the reference case  
267 and test EL2 has movements that were 54% higher. This measurement can be considered to be  
268 analogous to the concept of volume loss used in tunnelling. The rate of excavation in the test is  
269 high and the event is essentially undrained. As such, the data for each test can be normalised to  
270 account for the fact that the movements driving the observed mechanisms (i.e. the initial gap  
271 between soil and former at the end of in-flight consolidation) are greater or smaller than the  
272 circular reference case.

273

274 *Accounting for the effect of friction at the clay model and PMMA window interface*

275 In this paper, measurements of soil movements are presented from various areas of the model  
276 and comprise surface settlement measurements obtained from 3D topography (Le *et al.*, 2016)  
277 and front face, subsurface measurements from geoPIV\_RG (Stanier *et al.*, 2015). Le *et al.* (2016)  
278 demonstrated that both of these techniques were capable of making measurements with  
279 comparable degrees of precision and accuracy. The (necessary) use of different measurement  
280 techniques means that some correlation must take place as front face measurements obtained  
281 from digital image analysis are influenced by friction between the soil and front window of the  
282 strongbox. Grant (1998) examined this phenomenon in a series of experiments using clay  
283 samples prepared in an identical manner to those in the current work and determined that an  
284 offset of -0.1 mm was evident in the region of interest when comparing results from LVDTs and  
285 image analysis. Put another way, Grant (1998) accounted for the friction at the clay-window  
286 interface by adding 0.1 mm to the settlements taken from digital image analysis.

287 In the current work, the region of interest is larger than that considered by Grant (1998); his work  
288 considered the movements immediately above a tunnel excavation. The application of an offset  
289 was therefore deemed inappropriate in this case. The reported 0.1 mm correction of Grant (1998)  
290 correlates to a scaling of around 10% and this scaling factor was therefore applied to  
291 measurements made at the clay-window interface in the work presented here.

292 To summarise, all results obtained (i.e. from both measurement systems at all locations) were  
293 scaled to account for variations in the experimental technique as previously detailed.

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294 Subsequently, measurements made at the front face of the model were increased by 10% to  
295 account for interface friction.

296

#### 297 *Surface settlement data*

298 Once the corrections detailed above have been applied to tests EL1 and EL2 it is possible to  
299 compare the surface settlements obtained parallel to the major and minor axes of the elliptical  
300 shaft and compare them with the (axisymmetric) settlements generated by the circular shaft.  
301 Figure 6 shows a sketch of the location of the measurement points and Figures 7a and 7b show  
302 the comparison along the major and minor axes respectively. In these figures it should be noted  
303 that those data labelled “P” (solid markers) are taken perpendicular to the front face of the  
304 centrifuge strong box using 3D topography and those labelled “F” (open markers) are taken at the  
305 front face both by geoPIV\_RG and 3D topography (hence the larger number of data points).

306 The dashed lines are least squares best fits of Equation 2 to the data from the circular reference  
307 test and the elliptical shaft tests. Data from the elliptical tests show good agreement independent  
308 of the measuring technique used. Settlements along the major axis are significantly smaller than  
309 those generated by the circular shaft excavation despite the major axis being 25% larger than the  
310 diameter of the circle (100mm vs 80mm). Conversely, settlements along the minor axis are  
311 comparable with those generated by the circular excavation despite the minor axis being 20%  
312 smaller than the diameter of the circle.

313

## 314 DISCUSSION

315

#### 316 *The nature of the modelled shaft*

317 It should be noted that the normalised settlements presented from the current tests are very much  
318 larger (by an order of magnitude) than those observed in the field (New, 2017). This arises from  
319 the fact that, in these tests, there is a 300mm overcut (at prototype scale) between the soil and  
320 the permanent former. As previously discussed, this is very much larger than that which might  
321 be encountered in practice where a 100mm overcut that is subsequently grouted might be more  
322 reasonable. The large overcut is an artifact of the experiments deliberately chosen to ensure  
323 consistent movements that can be reliably detected by digital image correlation.

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324 The heavy fluid within the excavation is drained via a pipe embedded within the soil attached to  
325 the base of the latex bag. It might be expected that the presence of this pipe would have some  
326 influence on the ground movements however it is located on the centreline of the excavation. As  
327 this is also aligned with a plane of symmetry, movements in this area would be expected to be in  
328 the form of vertical heave only and would be less influenced by the smooth pipe, in itself aligned  
329 with the direction of heave. Post-test inspection shows that the pipe and latex bag have very little  
330 effect on the heave at the formation and what influence there is occurs only when the soil is fully  
331 softened at the base i.e. some time after the end of excavation simulation.

332

### 333 *Comparison with empirical methods*

334 Figure 8 shows that the surface settlements generated by the elliptical shaft excavation could be  
335 represented by Equation 1 (New, 2017). A least squares best fit to the combined data (i.e. from  
336 all tests and measurement methods) is carried out to determine values of  $\alpha$  and  $n$ . Figure 8 shows  
337 the resulting curves and Table 2 gives the derived values of  $\alpha$  and  $n$ .

338

### 339 *Comparison with the results of Faustin et al. (2018)*

340 As detailed earlier there is one previously published set of experimental data detailing a centrifuge  
341 test on an elliptical shaft constructed in dense sand. Despite the differences between this and  
342 the current work, Equation 2 is utilised to examine the patterns of movement generated. Figure  
343 9 shows the results from Faustin *et al.* (2018) overlain with predicted curves generated by  
344 Equation 2. The curves are not mathematically fit to the data but rather placed to give an  
345 approximate upper bound to the data on the graph. The curve generated for the elliptical data  
346 has a value of  $\alpha$  that is 10% larger than that used for the circular curve (the value of  $n$  is constant  
347 at 1.5). This is commensurate with the observation that the plan area of the elliptical shaft is 10%  
348 larger in this work when compared with the circular. The curves give credence to the observation  
349 above that a suitable prediction can be generated for the maximum settlements caused by  
350 excavating an elliptical shaft from Equation 2 by considering a circular shaft of equivalent plan  
351 area. It should be noted that in the current work, the aspect ratio of the ellipse is 0.64 (and 0.67  
352 in Faustin *et al.*, 2018). Whether similar patterns of settlement would be observed for different  
353 aspect ratios remains a topic for future work.

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354

355 CONCLUSION

356

357 A practical solution to the problem of restrictions on available surface space coupled with  
358 increasingly congested underground space is the utilisation of elliptical shafts for access to  
359 underground infrastructure. It is clear that there is a requirement for estimating the ground  
360 movements resulting from such constructions and data from a series of well-controlled centrifuge  
361 tests carried out in overconsolidated clay have been presented in this paper.

362 The findings can be summarised below:

- 363 • The maximum settlements at the ground surface arising from elliptical shaft construction  
364 are apparent on line coincident with the minor axis of the ellipse. Conversely, the  
365 settlements generated on the line coincident with the major axis are significantly smaller  
366 in magnitude (in the order of 60% of the settlement seen on the minor axis, for the ratio  
367 in lengths of the minor to major axis of 0.64).
- 368 • For the purposes of assessing the movements that might be generated by a proposed  
369 elliptical shaft construction in clay, an upper bound to the surface settlements can be  
370 generated from Equation 2 by modelling a circular shaft of equivalent plan area. As with  
371 the original work of New & Bowers (1994) special consideration will still need to be given  
372 to an appropriate value of  $\alpha$ .

373

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375

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435 LIST OF FIGURES

436

437 **Figure 1:** Sketch showing required circular and elliptical plan geometry to enclose two adjacent  
438 lift mechanisms.

439 **Figure 2:** Photographs of apparatus showing: (top) assembly of former, latex bag and bracket,  
440 (middle) location of apparatus within the soil model, (bottom) attachment of the apparatus to the  
441 model box.

442 **Figure 3:** Schematic of centrifuge test apparatus.

443 **Figure 4:** Undrained shear strength with depth for CR, EL1 and EL2.

444 **Figure 5:** Horizontal displacement with depth for CR, EL1 and EL2 (L: results from left side of  
445 model, R: results from right side).

446 **Figure 6:** Sketch to show measurement locations.

447 **Figure 7a:** Comparison of surface settlements in elliptical shaft test (EL) along the major axis  
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450 direction with reference circular shaft data (CR).

451 **Figure 8:** Design lines for surface settlements arising for elliptical shaft construction in clay.

452 **Figure 9:** Comparison of Equation 2 with the results of Faustin (after Faustin *et al.*, 2018)

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1

Test ID	Maximum consolidation pressure (kPa)	Swelling pressure (kPa)	Excavation dimensions (mm or mm <sup>2</sup> )	Shaft liner dimension (mm or mm <sup>2</sup> )
CR (aspect ratio = 1.0)	350	250	h = v = 80 H = 200 A = 5027	h = v = 71 H = 200 A = 3959
EL1 (aspect ratio = 0.64)	350	250	h = 64 v = 100 H = 200 A = 5027	h = 55 v = 45.8 H = 200 A = 3959
EL2 (aspect ratio = 0.64)	350	250	h = 100 v = 64 H = 200 A = 5027	h = 91.6 v = 55 H = 200 A = 3959

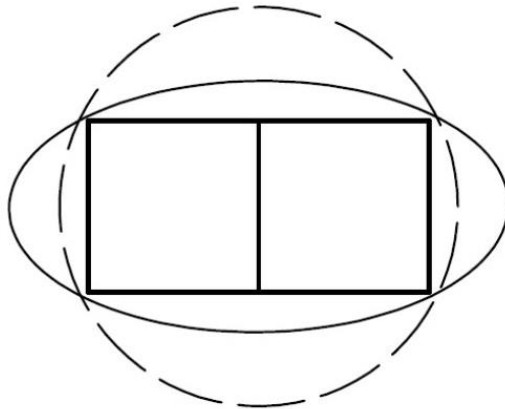
2 **Table 1:** Details of centrifuge tests

3

Test	CR	EL1	EL2 <sup>4</sup>
$\alpha$	$5.8 \times 10^{-3}$	$4.1 \times 10^{-3}$	$5.9 \times 10^{-3}$
n	1.5	0.94	1.33

6 **Table 2.** The values of  $\alpha$  and n derived from the tests.

7



**Figure 1:** Sketch showing required circular and elliptical plan geometry to enclose two adjacent lift mechanisms.

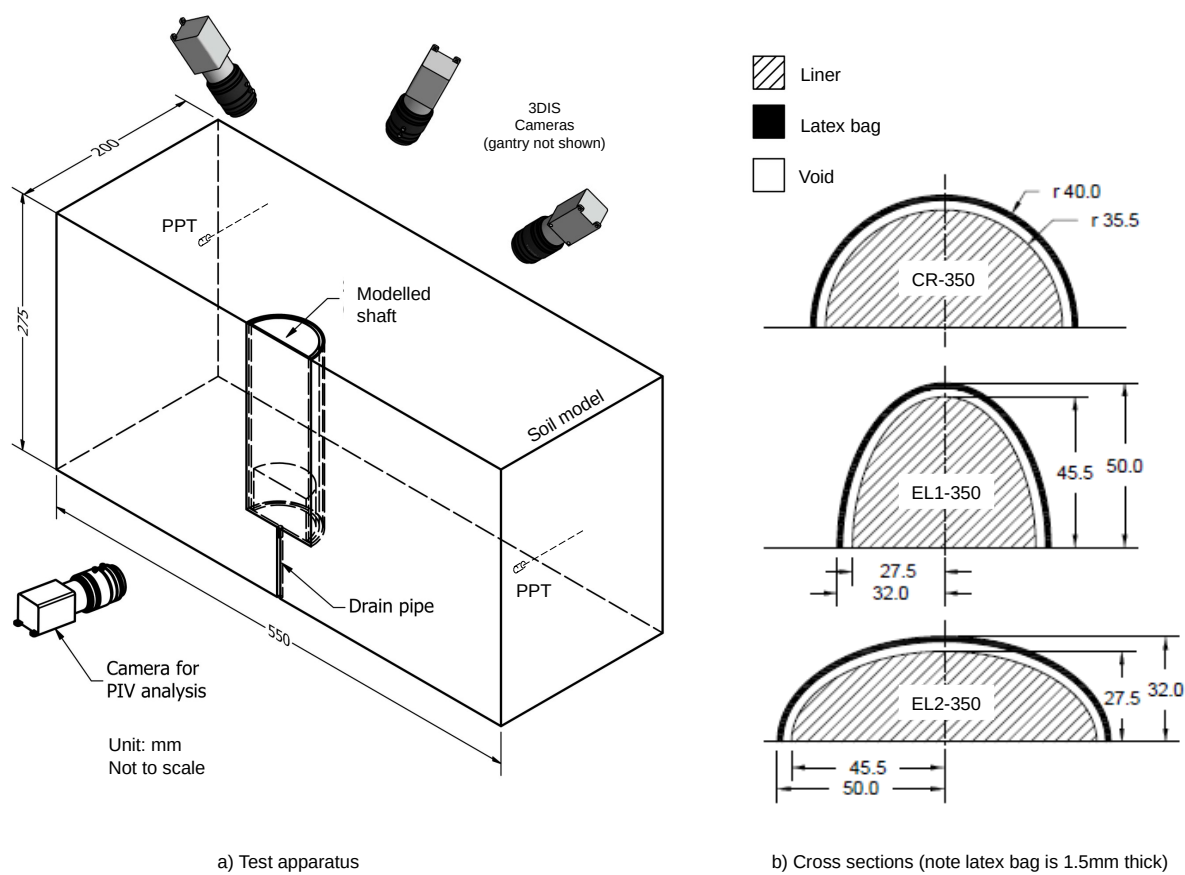
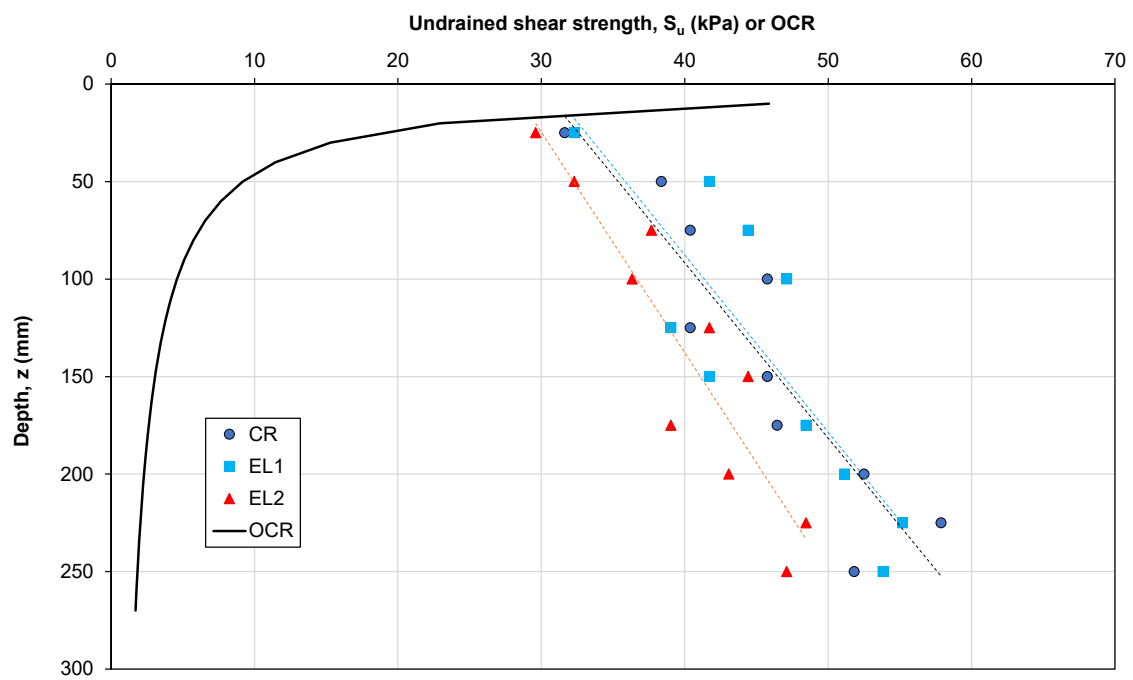


Figure 2: Schematic of centrifuge test apparatus.

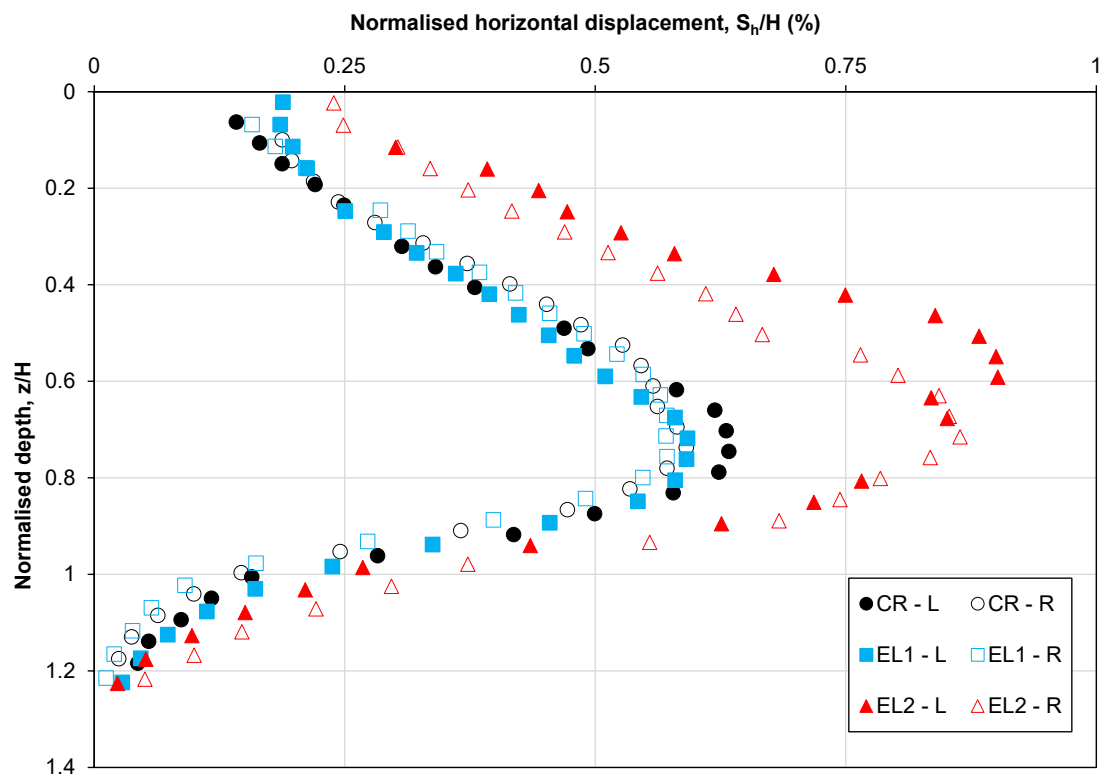


**Figure 3:** Photographs of apparatus showing: (top) assembly of former, latex bag and bracket, (middle) location of apparatus within the soil model, (bottom) attachment of the apparatus to the model box.

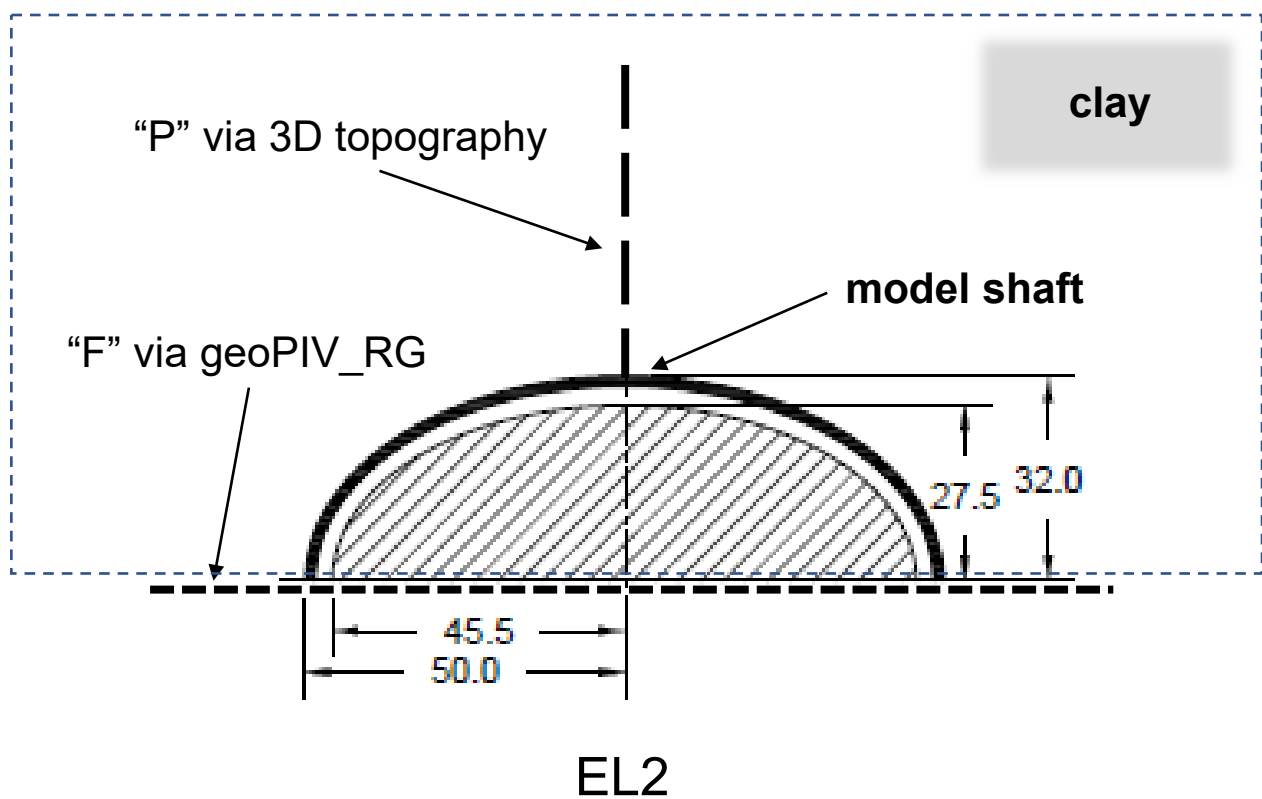
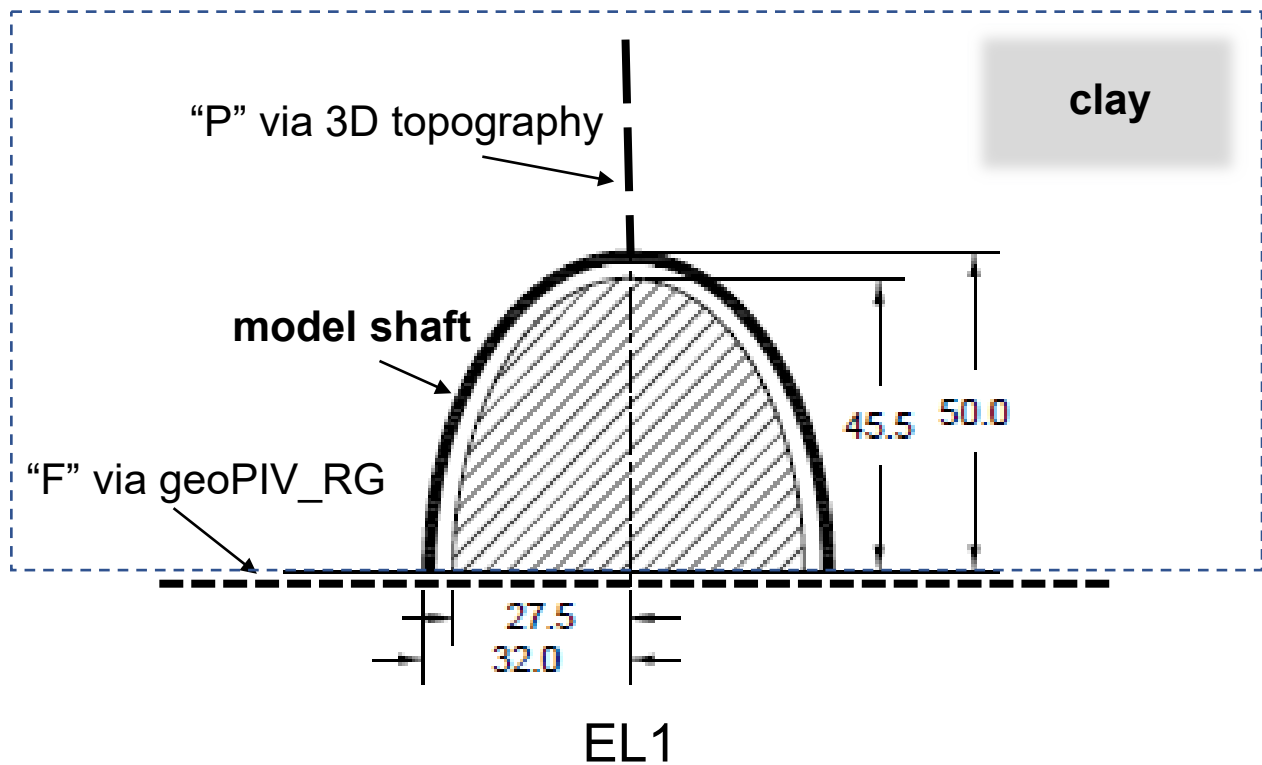




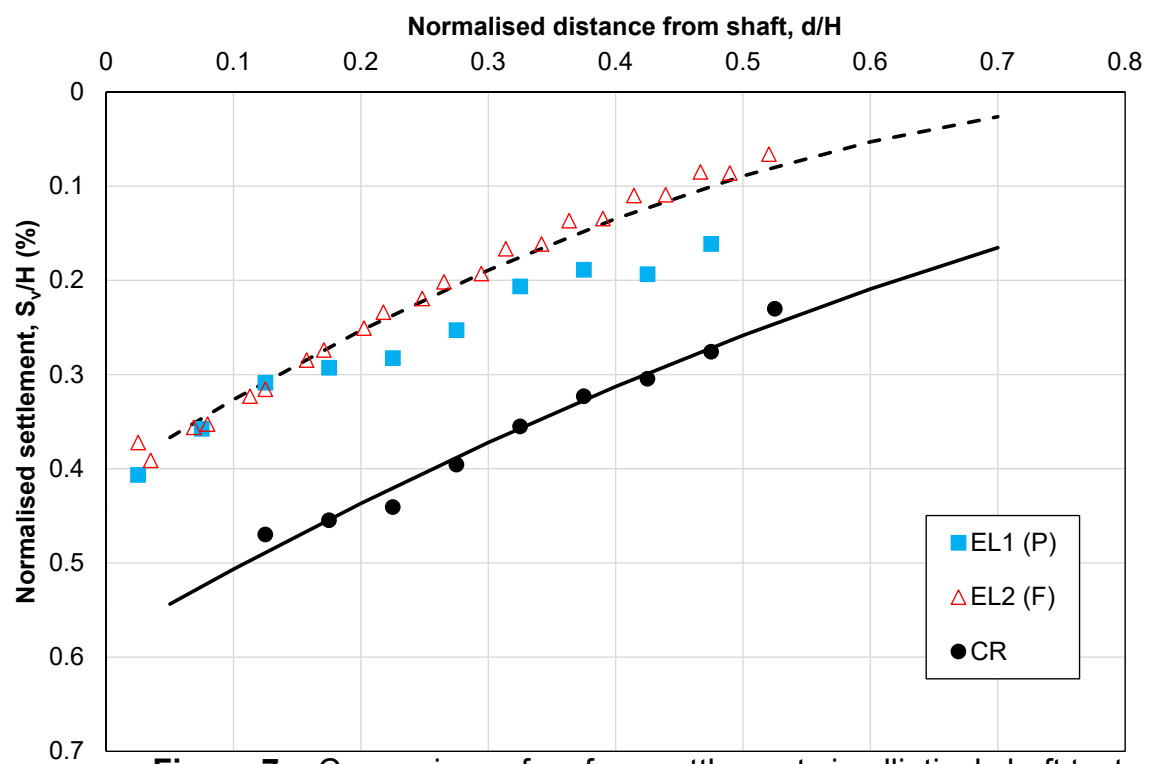
**Figure 4:** Undrained shear strength and OCR with depth for CR, EL1 and EL2.



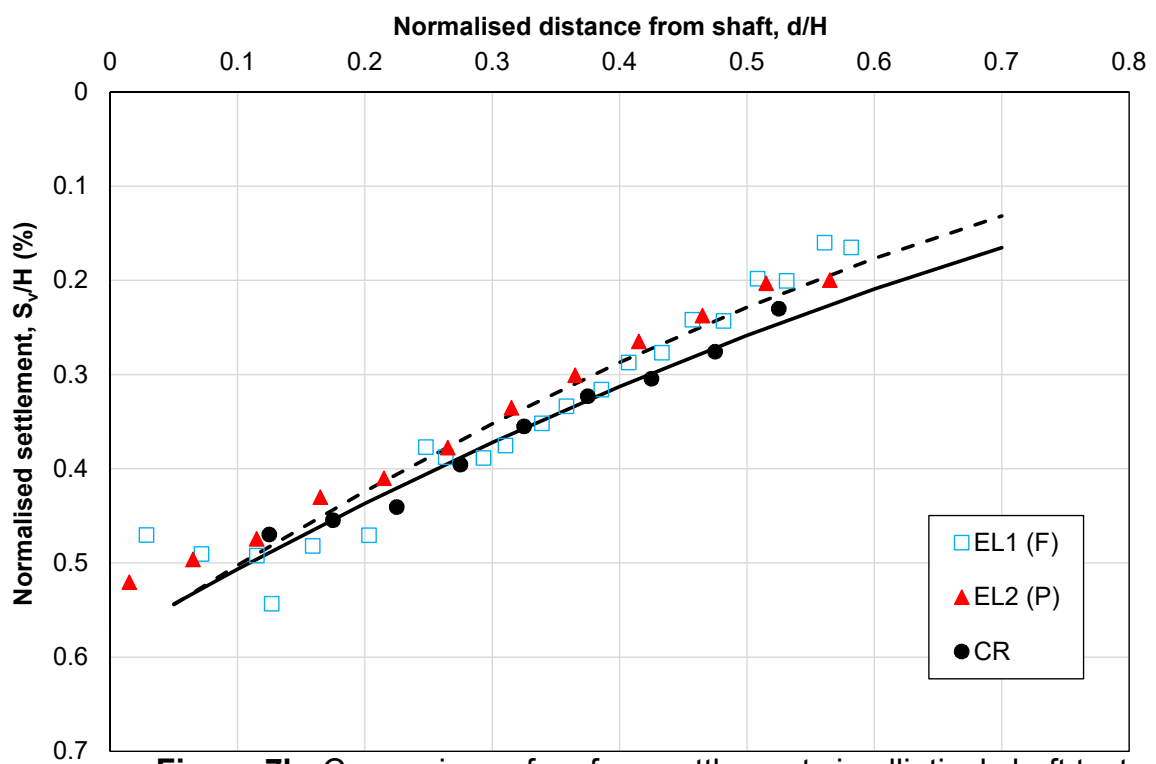
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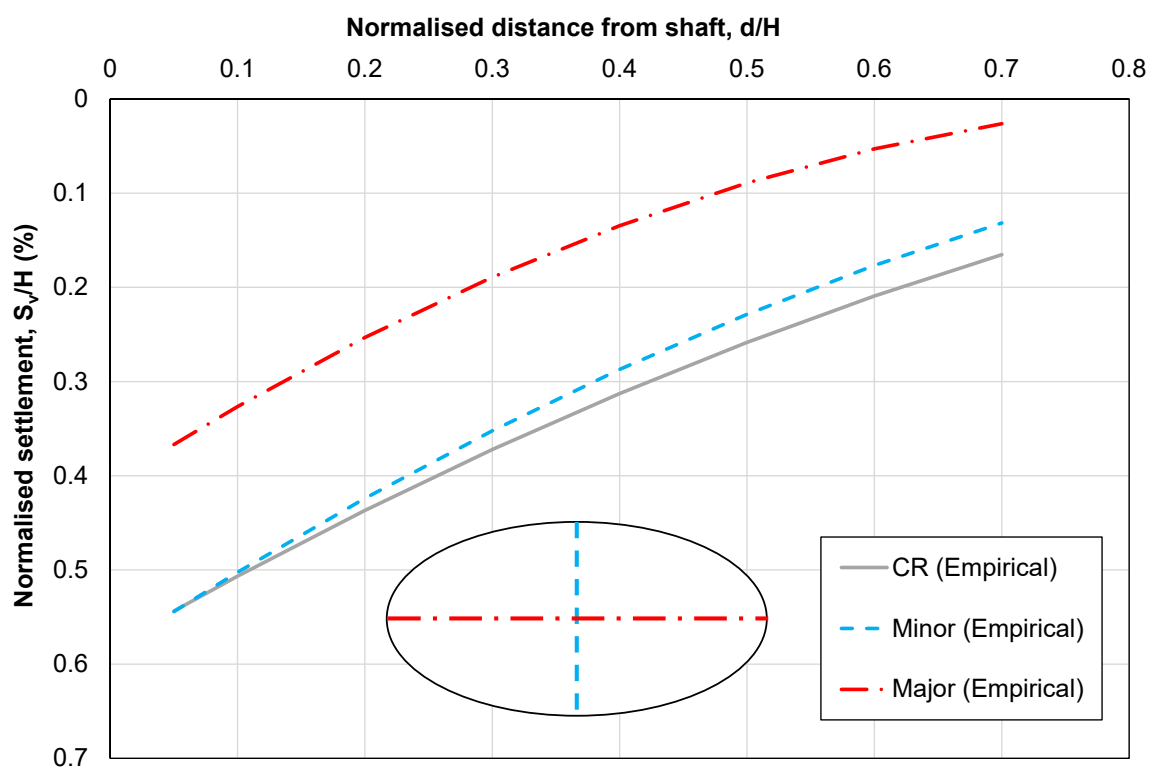
**Figure 6:** Sketch to show measurement locations



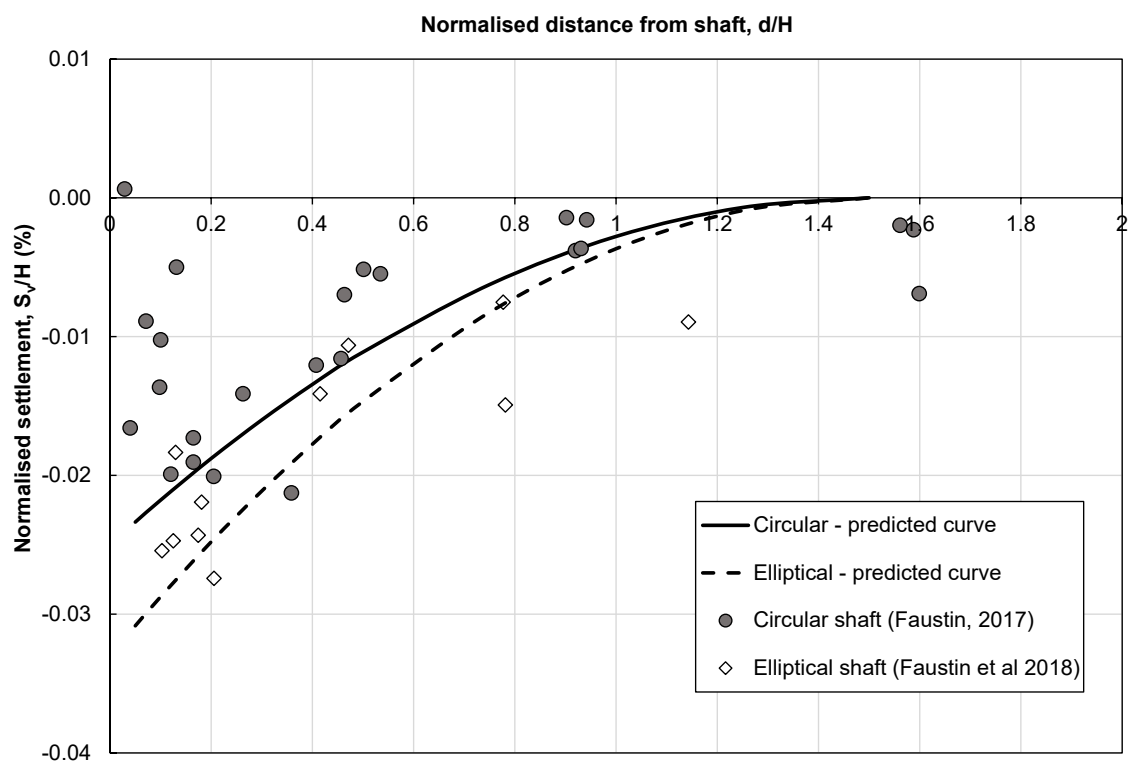
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