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## Skew wind actions on vehicles crossing bridges with solid parapets

Alfredo Camara<sup>a</sup>, Luis Fernandez Elvira<sup>b</sup>, Chrysanthi Stroumpouli<sup>b</sup>,  
Chetan Jagadeesh<sup>b</sup>

<sup>a</sup>*Department of Continuum Mechanics and Theory of Structures, Universidad  
Politécnica de Madrid, Calle Profesor Aranguren s/n, 28040 Madrid, Spain.*

<sup>b</sup>*Department of Civil Engineering, City, University of London. Northampton Square,  
London, EC1V 0HB, United Kingdom*

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### Abstract

This work focuses on the effect that the angle of incidence of the wind has on the flow around bridge decks with low-rise edge parapets, and how it affects the aerodynamic actions on vehicles. First, a generic deck model with different barrier configurations is studied using computational fluid dynamic (CFD) analysis, and it is observed that for very skew winds even relatively low barriers can deviate the flow to make it aligned with the direction of the deck, which is referred to as channelling effect in this study. The work continues with an extensive wind tunnel (WT) testing programme on a deck model that represents a realistic bridge with a conventional configuration of short side barriers. The flow visualisation and the aerodynamic forces measured on a high-sided vehicle show the existence of three different zones in terms of the skew angle of the wind, which are in agreement with the CFD results. It is concluded that skew winds can significantly increase the aerodynamic actions on the vehicles due to the reduction of the shielding area across the width of the deck, and also because of the along-deck wind channelling.

### *Keywords:*

Skew winds; wind tunnel testing; high-sided vehicles; bridge aerodynamics; CFD; aerodynamic coefficients

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*Email address:* alfredo.camara@upm.es (Alfredo Camara)

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1 **Nomenclature**

2	$\alpha^*$	Apparent wind incidence angle in the test with $x_v$ northbound.
3	$\alpha$	Angle between the horizontal mean wind speed and the deck.
4	$\bar{P}_i$	Time-averaged pressure at the $i$ -th pressure tap on the vehicle.
5	$\bar{U}$	Time-averaged wind speed.
6	$\beta$	Relative incidence angle between the wind and a moving vehicle.
7	$\gamma$	Inclination of the horizontal wind vector along the deck.
8	$\nu_a$	Kinematic viscosity of air.
9	$\psi$	Angle between the mean wind speed at the inlet and the horizontal
10		wind force resultant on the vehicle.
11	$\rho$	Density of air.
12	$\sigma_u$	Standard deviation of the stream-wise turbulence.
13	Re	Reynolds number.
14	$A_f$	Area of the rear face of the vehicle.
15	$A_i$	Tributary area corresponding to the $i$ -th pressure tap on the vehicle.
16	$C_j$	Aerodynamic coefficient of the vehicle, with $j = S, D, R, P, Y$ referring
17		to the side, drag, rolling, pitching and yawing, respectively.
18	$d$	Depth of the deck (without considering the barriers).
19	$f$	Frequency.
20	$F_j$	Drag ( $j = D$ ) and side ( $j = S$ ) force on the vehicle.
21	$h$	Vertical distance between the bottom of the vehicle and its centroid.
22	$h_f$	Height of the side barriers of the deck.
23	$H_v$	Total height of the vehicle.
24	$H_{obs}$	Depth of the deck including the side barriers.

- 25  $H_{vo}$  Height of the vortex generators in the wind tunnel.
- 26  $L_u$  Length scale of the stream-wise turbulence.
- 27  $L_v$  Total length of the vehicle.
- 28  $M_j$  Rolling, pitching and yawing moments on the vehicle, with  $j = R, P, Y$ ,  
29 respectively.
- 30  $n_i^{xv}, n_i^{yv}, n_i^{zv}$  Components of the vector normal to the surface of the vehicle  
31 in the  $i$ -th pressure tap.
- 32  $N_t$  Number of pressure taps in the vehicle.
- 33  $P_i$  Pressure at the  $i$ -th pressure tap on the vehicle.
- 34  $S_u$  Auto-spectral density of the stream-wise turbulence.
- 35  $t$  Time.
- 36  $U_h$  Magnitude of the horizontal component of the wind velocity vector.
- 37  $U_x$  Mean wind speed in the  $x$  direction (along-flow).
- 38  $U_z$  Mean wind speed in the  $z$  direction (across-flow horizontal).
- 39  $U_W$  Free-stream wind velocity in the wind tunnel.
- 40  $U_{x,\infty}$  Horizontal mean wind speed in the inlet.
- 41  $V$  Vehicle speed.
- 42  $W_v$  Total width of the vehicle.
- 43  $x_G, y_G, z_G$  Coordinates of the centroid of the vehicle in its local axes.
- 44  $x_i, y_i, z_i$  Coordinates of the  $i$ -th pressure tap in the local vehicle axes.
- 45  $x_v, y_v, z_v$  Local axes of the vehicle.
- 46  $z$  Height from the floor of the wind tunnel.

## 47 1. Introduction

48 Wind causes a large number of accidents and interruptions on road and  
49 railway networks, particularly on bridges because of their exposure [1, 2,  
50 3]. Understanding the aerodynamic actions on vehicles crossing bridges is  
51 essential to assess the risk of accidents and discomfort.

52 Many researchers have studied the on-bridge vehicle wind actions in  
53 bridges under purely crosswinds. Wind tunnel (WT) testing programmes  
54 have demonstrated the importance that the flow interference created by the  
55 shape of the deck and its furniture (parapets, wind barriers, etc.) have on  
56 trains [4, 5, 6] and road vehicles [3, 7, 8, 9, 10, 11]. Although these works  
57 consider the mean wind speed perpendicular to the deck, skew winds that  
58 form an angle  $\alpha \neq 90^\circ$  with respect to the deck are more likely to occur, and  
59 they are usually more dangerous from the point of view of the vehicle sta-  
60 bility [12, 13, 14, 15]. In addition, the combination of the vehicle speed ( $V$ )  
61 and the mean wind speed ( $U_{x,\infty}$ ) results in a relative yaw incidence angle  $\beta$   
62 as shown in Fig. 1(a), even for purely orthogonal winds. Indeed, Baker [16]  
63 demonstrated with a dynamic model of a 4-wheeled vehicle that yaw angles  
64 between  $\beta = 30^\circ$  and  $60^\circ$  (headwinds) are more dangerous for the driving  
65 stability of high-sided vehicles situated in homogeneous wind fields free from  
66 obstacles (i.e. in off-bridge conditions). The same conclusion was reached  
67 in the static analysis of different types of vehicles on a long-span bridge  
68 conducted by Kim *et al.* [17]. Recently, Camara [18] proposed a dynamic  
69 wind-vehicle-bridge interaction model that incorporated skew wind velocity  
70 histories and concluded that headwinds in the range between  $\beta = 40^\circ$  and  
71  $70^\circ$  maximise the risk of driving accidents. The previous studies are based  
72 on off-bridge aerodynamic vehicle coefficients, which are also used in many  
73 other works focusing on the driving safety and comfort in bridges under wind  
74 actions (e.g. [19, 20, 21, 22]). However, Han *et al.* [23] demonstrated the  
75 existence of significant flow interferences of the deck on the vehicle, and the  
76 importance of obtaining the on-bridge vehicle aerodynamic coefficients for a  
77 wide range of skew angles. Such disturbances may also deviate the projec-  
78 tion of the wind direction in the horizontal plane along the deck, as well as  
79 the resultant horizontal aerodynamic force on the vehicles, described by the  
80 angles  $\gamma$  and  $\psi$  in Figs. 1(b) and (c), respectively.

81 Cheli *et al.* [24] compared the off-bridge and on-bridge wind actions in  
82 WT experiments of a relatively shallow railway bridge without furniture,  
83 and they did not report significant variations of the results for different yaw

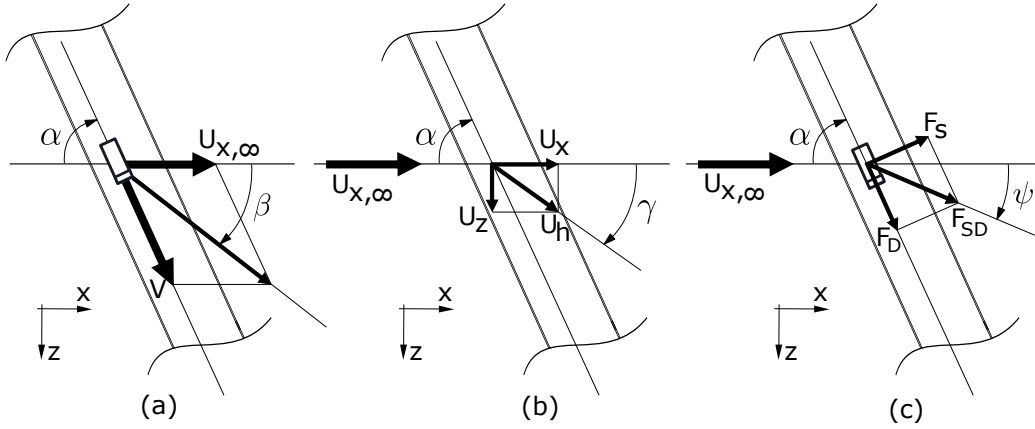


Figure 1: Definition and positive convention of representative angles in bridges under skew wind actions: (a) relative incidence angle  $\beta$  of wind on a moving vehicle, (b) inclination  $\gamma$  of the horizontal wind vector along the deck, (c) angle  $\psi$  between the mean wind speed and the horizontal wind force resultant.

84 angles. This is in agreement with the work of Dorigatti *et al.* [25], who  
 85 tested a typical long-span road bridge deck subject to a limited range of  
 86 wind skew angles from  $\alpha = 60^\circ$  to  $120^\circ$ . They considered a bridge deck  
 87 with relatively small parapets, in which the ratio of their height ( $h_f$ ) and  
 88 the depth of the deck ( $d$ ) is less than 0.25. However, in a different work  
 89 Cheli *et al.* [26] studied experimentally single- and double-deck road bridges  
 90 with larger railed parapets ( $h_f/d \approx 0.5$ ), and it was observed that the bridge  
 91 interference modifies the lateral force and rolling moment coefficients of the  
 92 vehicles, particularly when the skew angle is significant ( $\alpha = 45^\circ$ ) and the  
 93 width of the deck is narrow. Although it was not specifically explored by  
 94 these authors, their measurements could have been affected by the along-  
 95 deck wind flow deviated by deck and its furniture for skew angles, referred  
 96 to as ‘channelling effect’ in the present work. Relatively narrow bridges with  
 97 large solid windward barriers ( $h_f/d \approx 1.2$  and  $2$ ) were tested by Kozmar *et al.*  
 98 [27], and they argued that the skew angle of wind does not seem to affect  
 99 the flow field characteristics significantly. This could be attributed to the  
 100 lack of leeward barriers, which can redirect the wind flow along the deck as  
 101 it is demonstrated in the present work.

102 More recently, WT testing with scaled moving vehicles conducted at  
 103 Southwest Jiaotong University confirmed the strong influence of the skew  
 104 wind angle on the flow structures along different types of decks, including

105 a through-truss deck with significant wind shielding [28, 29], and a shallow  
106 box girder with or without windward barriers ( $h_f/d = 0.7$ ) [30, 31]. Despite  
107 the different levels of shielding considered in these studies it was concluded  
108 that the aerodynamic coefficients of the vehicles on the deck were not only  
109 affected by the relative incidence angle of the wind (or yaw angle  $\beta$ ), as it is  
110 the case in off-bridge conditions, but also by the skew wind angle ( $\alpha$ ) given  
111 its influence on the flow interferences introduced by the deck. The effect of  
112 the shape of the super-structure on the skew wind actions on the vehicles was  
113 also observed by other researchers experimentally [32, 33, 34] and numeri-  
114 cally with computational fluid dynamic (CFD) analysis [35, 36], but it has  
115 not been clearly connected with the parapets of the deck and their potential  
116 channelling effect.

117 Solid parapets are widely used for safety, construction and maintenance  
118 of bridges. The aim of this paper is to explore their effect on skew wind flows  
119 around the deck, and also on the resulting vehicle aerodynamic actions. To  
120 this end, the study combines CFD and WT testing on typical prestressed  
121 concrete bridge decks. First, an extensive three-dimensional CFD analysis is  
122 conducted on a highly idealised deck model to assess the influence that the  
123 skew angle  $\alpha$  has on the along-deck wind flow of the deck, considering different  
124 configurations of the edge barriers. The results indicate the existence of three  
125 distinct zones of influence of  $\alpha$  on the wind velocity vector along the deck,  
126 which is almost aligned with the deck within the height of the barriers when  
127  $\alpha < 60^\circ$  or  $\alpha > 120^\circ$ . This is due to the windward barrier and the results are  
128 in agreement with the WT testing conducted in a detailed scaled model of a  
129 real bridge. In these experiments, the flow visualisation and the study of the  
130 pressure maps and the resultant forces on the vehicles clearly indicate the  
131 importance of the wind skew angle on the driving safety due to the along-deck  
132 flow channelling effects.

## 133 2. Bridge cross-sections

134 Two different road bridge box girders are examined in this work: (1) a  
135 ‘generic’ idealised deck cross-section that is studied numerically using CFD,  
136 and (2) a ‘typical’ deck shape corresponding to a real bridge that is studied  
137 experimentally in a WT. Both cases are illustrated in Fig. 2, in which the  
138 dimensions have been normalised with respect to the depth of the deck ( $d$ ).  
139 In order to minimise local flow perturbations, and to focus on the effect of the  
140 bridge furniture on the wind field above the deck in the generic bridge model

141 of Fig. 2(a), it has been simplified to a single box girder, a top slab with  
 142 uniform thickness ( $0.09d$ ) and two edge parapets. The deck cross-section in  
 143 Fig. 2(b) represents a typical prestressed concrete bridge with double box  
 144 girder. Its detailed dimensions are taken from the midspan cross-section of  
 145 the Orwell Bridge (UK, 190-m main span) and it has 4 lanes (L1 - L4), two  
 146 of them in the upwind girder (UG) and the other two in the downwind girder  
 147 (DG). The solid parapets in both cross-sections have a height of  $h_f = d/3$ ,  
 148 which is representative of many long-span bridges with concrete barriers, or  
 149 with edge parapets formed by a concrete plinth and metal railing on top [37].

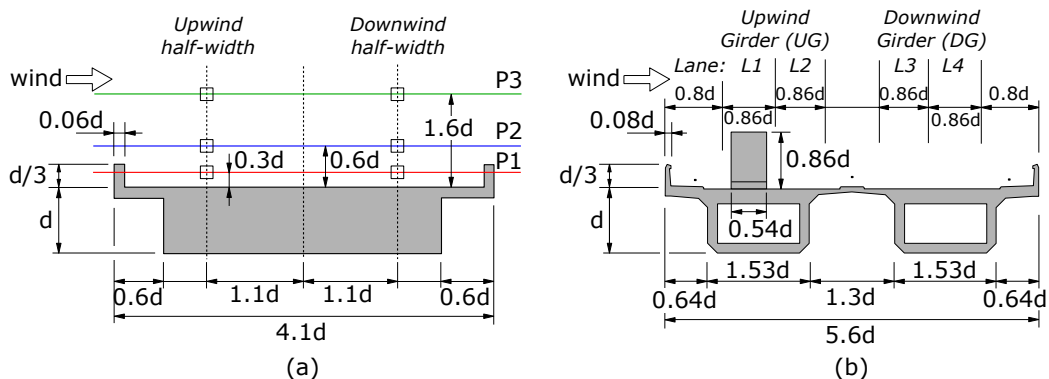


Figure 2: Dimensions of the bridge cross-sections in terms of their depth  $d$ : (a) idealised generic bridge, (b) typical bridge with a high-sided vehicle.

### 150 3. Numerical study of deck channeling effects

151 The aim of this section is to characterise the diverting effect of the deck  
 152 and its parapets on the mean wind field across its width. To this end, series  
 153 of three-dimensional (3D) CFD finite volume analyses were conducted in  
 154 OpenFOAM [38] considering the idealised deck model presented in Fig. 2(a).  
 155 In this model we chose  $d = 154$  mm to assimilate it to the WT experiments  
 156 presented later. Vehicles are not included in the numerical model to focus  
 157 on the flow around the deck.

158 In the CFD analysis the Reynolds-averaged Navier–Stokes (RANS) equa-  
 159 tions and the standard  $k - \epsilon$  turbulence model [39] are solved in steady state.  
 160 This is deemed appropriate considering that the goal of the CFD analysis in  
 161 this research is to visualise the global wind flow around the deck for different  
 162 skew angles, and not to calculate the transient aerodynamic actions. For this

163 reason, wall functions that incorporate the linear (laminar) and logarithmic  
 164 (turbulent) law-of-the-wall are implemented close to the deck surface with  
 165  $y^+ \approx 50$  in the first grid cell, spanning the inner region between the wall and  
 166 the fully developed turbulence region. The pressure-velocity coupling of the  
 167 fluid motion equations is solved with the semi-implicit algorithm SIMPLE  
 168 [40].

169 The 3D fluid domain around the deck model is described in Fig. 3(a)  
 170 in terms of the depth of the deck plus the side barriers ( $H_{obs} = d + h_f =$   
 171  $4d/3$ ). Sensitivity analysis were performed to validate the width of the fluid  
 172 domain and its near-wall refinement. The shape of the fluid cells is hexaedral  
 173 (structured) in the whole domain, establishing 7 inflation layers around the  
 174 perimeter of the deck that have a thickness of 1 mm in the first layer and grow  
 175 with an expansion rate of 1.2. A detail of the mesh close to the perimeter  
 176 of the deck cross-section is included in Fig. 3(b). The values of the skew  
 177 wind angle considered range from  $\alpha = 20^\circ$  to  $90^\circ$ , typically with increments  
 178 of  $10^\circ$ . As a reference, the model with purely orthogonal wind ( $\alpha = 90^\circ$ ) and  
 179 both edge barriers has approximately 4 million cells in the fluid domain. The  
 180 different wind incidence angles are achieved by rotating the deck with respect  
 181 to the  $y$  axis and maintaining the orientation of the boundary conditions  
 182 of the flow. This implies that the mesh varies from case to case, but its  
 183 resolution is maintained and it has been verified that re-meshing for different  
 184 wind skew angles does not affect significantly the results.

185 Fig. 3(a) also includes the reference axes of coordinates and the boundary  
 186 conditions applied to all the faces, with a uniform wind flow of  $U_{x,\infty} = 10$   
 187 m/s in the  $x$  direction imposed at the inlet ( $Re = U_{x,\infty}d/\nu_a \approx 1.5 \times 10^5$ , with  
 188  $\nu_a = 1.48 \times 10^{-5}$  m<sup>2</sup>/s being the kinematic viscosity of air). Several variations  
 189 of the barrier configuration presented in Fig. 2(a) are introduced to study  
 190 their effect on the flow, resulting in the following cases: (1) original model  
 191 with the two edge parapets, (2) model with only the windward parapet, and  
 192 (3) model with no parapets. The three deck cross-sections are shown in Fig.  
 193 4.

### 194 3.1. Across-flow horizontal wind field

195 Fig. 4 presents the across-flow horizontal wind field ( $U_z$ ) in the vertical  $x$ –  
 196  $y$  midplane of the model illustrated in Fig. 3(a). The results are normalised  
 197 with respect to the inlet wind speed  $U_{x,\infty} = 10$  m/s to show the important  
 198 influence of the angle between the deck and the mean wind speed on the  
 199 deviation of the flow. When the wind direction is purely orthogonal to the

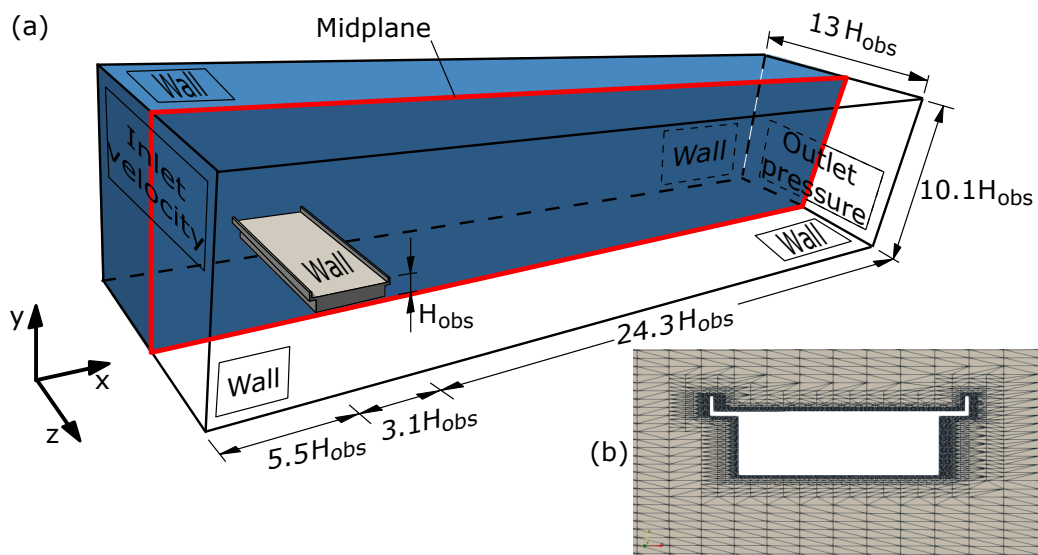


Figure 3: (a) Geometry and boundary conditions of the CFD study in the generic bridge section.  $H_{obs} = 4d/3$  is the total depth of the deck, including the edge barriers. The blue shaded region represents half of the wind domain, the other half is removed for visualisation purposes. (b) Detail of the mesh around the cross-section of the deck. The two views correspond to the case with  $\alpha = 90^\circ$  and both barriers.

200 deck the across-flow component of the wind field ( $U_z$ ) is negligible, regardless  
 201 of the barrier arrangement above the deck slab, as it is observed in Figs. 4(a)  
 202 - (c). However, skew winds forming an angle of  $\alpha = 45^\circ$  with the deck are  
 203 partly diverted when they reach the vertical faces of the girder, which creates  
 204 a  $U_z$  component of the wind velocity vector that is up to 70% of the inlet  
 205 speed. This effect is observed along the depth of the deck (d) regardless of  
 206 its barriers, but the presence of a windward edge parapet extends it above  
 207 the pavement and reach the region used by the vehicles. This is shown in  
 208 Figs. 4(d) and (e), which also indicate that the leeward parapet does not  
 209 contribute to the diversion of the wind flow in the carriageways.

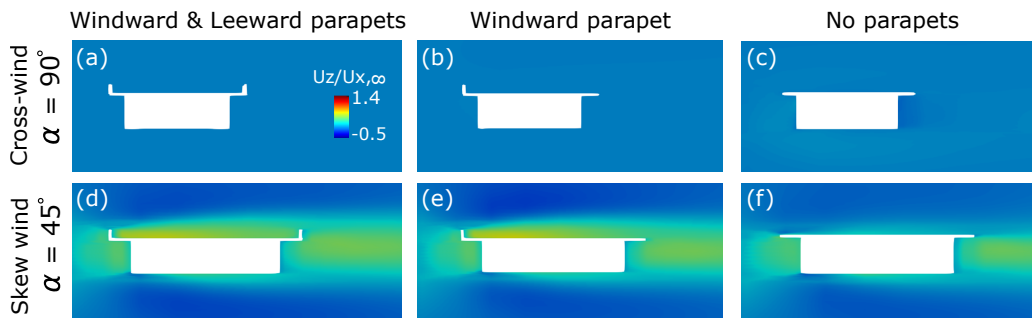


Figure 4: Normalised across-wind velocity fields ( $U_z/U_{x,\infty}$ ) for different wind incidence angles and geometries of the generic bridge cross-section.

### 210 3.2. Deck channelling effects

211 The across-wind velocity field  $U_z$  included in Fig. 4 is strongly influenced  
 212 by the distance above the deck in which it is measured. In order to explore  
 213 this effect and the orientation of the wind flow along the deck, the wind speed  
 214 is obtained in the horizontal  $x-z$  planes P1, P2 and P3 described in Fig. 2(a).  
 215 Each of these planes contain the interpolated CFD results corresponding to  
 216 the fluid cells that they intersect. Ignoring the  $y$ -component of the wind  
 217 velocity gives a grid of points in each horizontal plane with velocities in  
 218 the  $x$  and  $z$  directions ( $U_x$  and  $U_z$ , respectively). We define the along-deck  
 219 horizontal inclination of the wind field shown in Fig. 1(b) as:

$$\gamma = \arctan \left( \frac{U_z}{U_x} \right). \quad (1)$$

220 The angle of wind above the deck  $\gamma$  is calculated along two lines parallel to  
 221 the bridge that are located at the centres of the upwind and the downwind  
 222 halves of its width, as shown in Fig. 2(a). This is done for each of the  
 223 planes P1-P3, and the arithmetic average of  $\gamma$  along these lines is calculated  
 224 discarding the points close to the  $x - y$  boundary faces. Fig. 5(a) shows the  
 225 averaged  $\gamma$  in the plane P1 of the model with two edge barriers. The results  
 226 indicate that purely cross-winds with  $\alpha = 90^\circ$  lead to  $\gamma = 0^\circ$ . This means  
 227 that the streamlines are contained in vertical  $x - y$  planes, and it is visualised  
 228 in the quiver plot presented in Fig. 5(b) when  $\alpha = 90^\circ$ , in which the size of  
 229 the vectors represents the magnitude of the horizontal wind component (i.e.  
 230  $U_h = \sqrt{U_x^2 + U_z^2}$  in Fig. 1(b)), and their inclination is given by  $\gamma$ . Fig. 5(b)  
 231 also shows the small magnitude of the horizontal wind velocity within the  
 232 edge parapets due to their shielding effect for purely cross-winds. However,  
 233 for non-orthogonal winds the horizontal inclination of flow along the deck  
 234 within the height of the parapets is significant, and its relationship with the  
 235 incidence angle  $\alpha$  can be divided in three zones represented in Fig. 5(a):

- 236 • Zone I - Initiation of channelling. This region corresponds to nearly-  
 237 orthogonal winds with  $75^\circ < \alpha < 90^\circ$ , for which the angle of wind along  
 238 the deck ( $\gamma$ ) is very sensitive to  $\alpha$ . As the wind incidence angle is more  
 239 skewed with respect to the deck the wind field across its width rapidly  
 240 becomes more aligned with the direction of its edge barriers, particu-  
 241 larly in the upwind half of the deck. Fig. 5(c) shows the horizontal  
 242 wind field for a representative incidence angle in this region.
- 243 • Zone II - Transition. When  $60^\circ < \alpha < 75^\circ$  the inclination of wind along  
 244 the deck is almost insensitive to variations of the skew wind angle. In  
 245 this region, as the incident wind becomes more parallel to the deck (i.e.  
 246  $\alpha$  is reduced) the flow within the height of the edge barriers is almost  
 247 aligned with them, as shown in Fig. 5(d) .
- 248 • Zone III - Full channelling. If the wind is significantly skewed, with  
 249  $\alpha < 60^\circ$ , the windward barrier diverts the streamlines and creates a  
 250 strong wind flow parallel to the girder in the first half of the deck,  
 251 introducing a full channelling effect for which  $\gamma \approx \alpha$ . This effect is  
 252 less pronounced in the downwind half of the deck after the streamlines  
 253 reattach, as it is illustrated in Fig. 5(e). The quiver plot also shows  
 254 that the magnitude of the horizontal wind field along the deck for very  
 255 skew winds is larger than for orthogonal flows, suggesting the loss of

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the shielding effect of the edge barriers in Zone III. The limit case in which  $\alpha = 0^\circ$  has not been analysed due to modelling difficulties, but in this case the deck is parallel to the wind flow and therefore it would lead to  $\gamma = 0^\circ$  across its width.

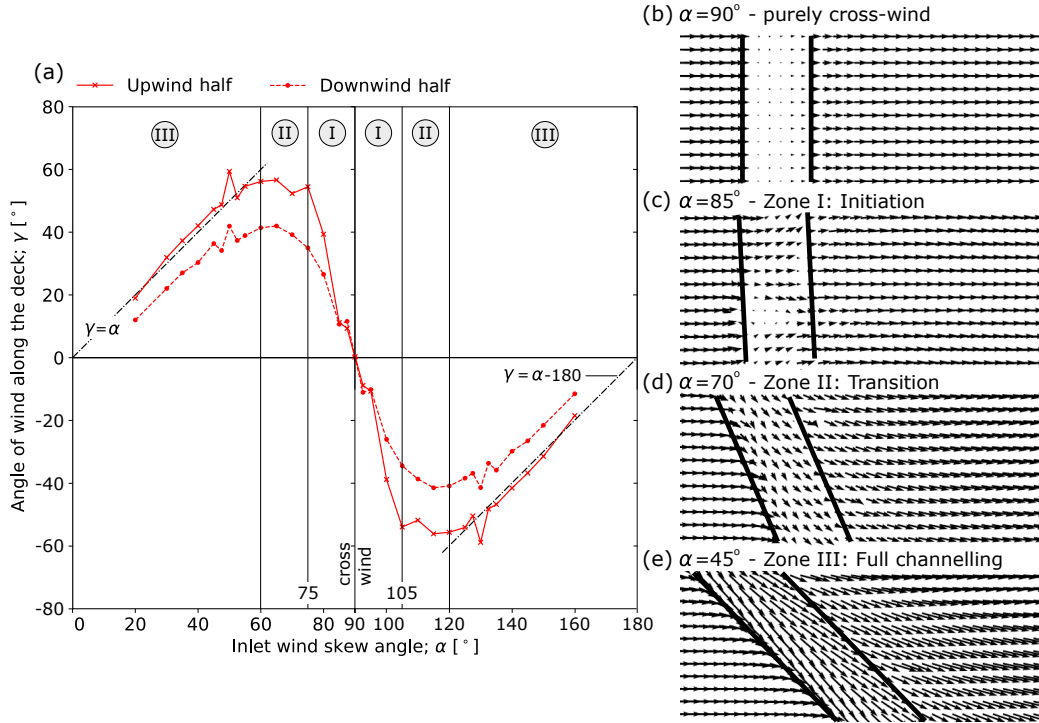


Figure 5: (a) Horizontal inclination of the wind velocity vector along the deck ( $\gamma$ ) for different wind incidence angles  $\alpha$  in the plane P1, within the height of the barriers. Figures (b)-(e) include quiver plots with the horizontal wind vector orientation around the deck, with the thick black lines indicating its edge barriers (plan view of the deck). CFD results in the generic bridge with both edge barriers.

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If the wind skew angle is  $\alpha > 90^\circ$  the values of the angle  $\gamma$  are anti-symmetric with respect to the axis  $\alpha = 90^\circ$ , and the full channelling region is described by  $\gamma \approx \alpha - 180^\circ$ , as it is indicated in Fig. 5(a).

The above zonation refers to the plane P1 in the bridge with both edge barriers. Fig. 6 compares the averaged wind inclination  $\gamma$  in different planes and deck cross-sections. The angle  $\gamma$  in the plane closer to the upper slab of the bridge (P1) obtained for the case with the two edge barriers is almost

267 identical to the case with only the windward parapet, distinguishing the  
 268 three regions of channelling previously discussed (Figs. 6(a) and Fig. 6(b)).  
 269 However, the deviation of the wind field above the deck is small when there  
 270 are no barriers on the deck ( $\gamma \approx 0$  for any value of the skew wind angle  $\alpha$ ),  
 271 even in the plane P1 as shown in Fig. 6(c). On the other hand, the influence  
 272 of the furniture of the bridge above the deck is less significant as the distance  
 273 from the pavement level increases. Certain flow channelling is observed in  
 274 the downwind half of the bridge with barriers in the intermediate plane P2,  
 275 but this effect disappears in plane P3, which corresponds to height of the top  
 276 of typical high-sided vehicles, regardless of the presence of parapets.

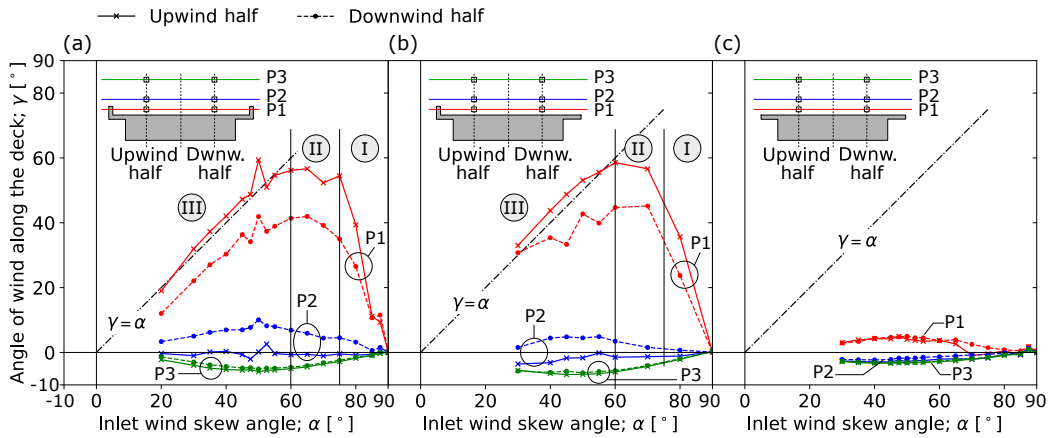


Figure 6: Horizontal inclination of the wind velocity vector along the deck ( $\gamma$ ) for different wind incidence angles  $\alpha$  in the bridge section with (a) both edge parapets, (b) windward parapet, and (c) no parapets. CFD results in different horizontal planes (P1-P3) of the generic bridge.

277 The magnitude of the horizontal wind field is also affected by the flow  
 278 channelling in the models with windward barriers, as it is shown in the along-  
 279 deck average of  $U_h$  presented in Figs. 7(a) and (b). This is appreciable in the  
 280 plane P1, where the velocity magnitude is reduced due to the protection of  
 281 the barriers if the wind is nearly orthogonal to the deck (Zone I), and it gets  
 282 closer to the inlet wind speed as the wind incidence angle is more skewed  
 283 (Zones II and III). The channelling effect in terms of  $U_h$  is smaller in plane  
 284 2 (but higher than in terms of  $\gamma$  at this position), and it vanishes in plane  
 285 P3. The influence of  $\alpha$  in the velocity magnitude is also weak in the bridge  
 286 without parapets described in Fig. 7(c), regardless of the position above the  
 287 deck where it is measured.

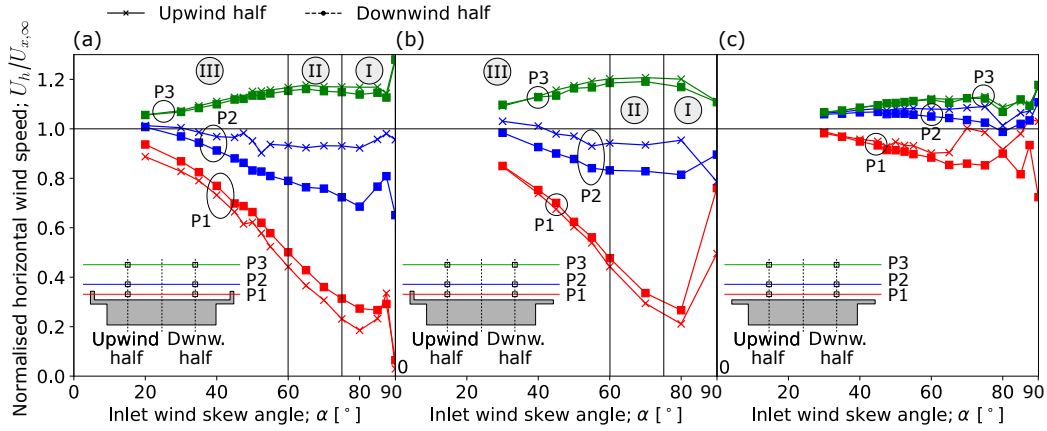


Figure 7: Horizontal wind speed magnitude along the deck ( $U_h$ ) normalised with respect to the inlet wind speed ( $U_{x,\infty}$ ) for different wind incidence angles  $\alpha$  in the bridge section with (a) both edge parapets, (b) windward parapet, and (c) no parapets. CFD results in different horizontal planes (P1-P3) of the generic bridge.

#### 288 4. Experimental testing of a typical deck with a high-sided vehicle

289 The purpose of the WT testing is to study the wind flow around the  
 290 deck of a typical bridge and the aerodynamic forces on high-sided vehicles  
 291 for different wind incidence angles. To this end, a 1/50 scale model of the  
 292 midspan segment of the bridge deck included in Fig. 2(b) was built and  
 293 tested in the closed-return environmental WT at City, University of London.

##### 294 4.1. Preliminary considerations

295 The working zone of the WT is 3-m wide x 1.5-m high x 8.1-m long.  
 296 A castellated barrier and four elliptical vortex generators with a height of  
 297  $H_{vo} = 1.2$  m were fitted at the upstream end of the working zone to generate  
 298 simulated atmospheric shear flows. These were described in detail by Sykes  
 299 [41]. In addition, the floor between the vortex generators and the 2.8-m  
 300 diameter turning table was covered by near-cylindrical roughness elements,  
 301 with height of 70 mm ( $0.058H_{vo}$ ) and mean diameter of 55 mm.

302 First, the wind field at the centre of the rotary table was measured with-  
 303 out the deck model, with a free-stream wind speed of  $U_W = 9$  m/s. The  
 304 measurements were obtained in 248 points equally-spaced in the vertical di-  
 305 rection ( $z$ ) using a pressure scanner mounted on an adjustable rake. The  
 306 sampling time and frequency was 600 s and 100 Hz, respectively. Fig. 8(a)  
 307 shows the profiles of the time-averaged horizontal (stream-wise) velocity and

308 turbulence intensity, normalised with respect to the height of the vortex gen-  
 309 erators ( $H_{vo}$ ) and the free-stream wind speed ( $U_W$ ). The measured boundary  
 310 layer can be described by the power law

$$\frac{\bar{U}}{U_W} = \left( \frac{z}{H_{vo}} \right)^{0.25}, \quad (2)$$

311 with  $\bar{U}$  representing the time-average of the wind speed and  $z$  the distance  
 312 from the tunnel floor. This work is mostly interested in the wind flow around  
 313 the deck of the bridge, where the boundary layer also matches the profile  
 314 given by EN1991-1-4 [42] for a terrain of type II.

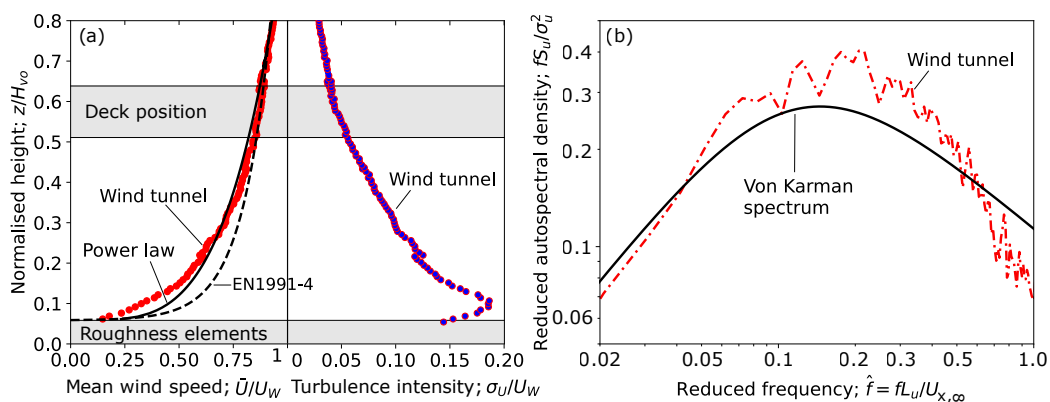


Figure 8: Stream-wise wind flow properties in the WT without deck model: (a) mean wind speed and turbulence intensity profiles, (b) frequency spectrum of the wind velocity record at the height  $z = 0.58H_{vo}$ , normalised with respect to the mean speed at the same point ( $U_{x,\infty}$ ).

315 The frequency content of the stream-wise turbulence measured at the  
 316 height corresponding to the centroid of the vehicle model ( $z = 0.58H_{vo}$ ) is  
 317 consistent with the corresponding Von Karman spectrum shown in Fig. 8(b),  
 318 which is described as

$$\frac{fS_u}{\sigma_u^2} = \frac{4\hat{f}_u}{\left(1 + 70.8\hat{f}_u^2\right)^{5/6}}, \quad (3)$$

319 where  $S_u$  and  $\sigma_u$  are the auto-spectral density and the standard deviation of  
 320 the turbulent component,  $f$  is the frequency and  $\hat{f}_u = fL_u/U_{x,\infty}$  its reduced  
 321 expression. It refers to the recorded flow velocity at the level of deck in the

322 study of the wind field of the empty tunnel, for which the mean wind speed  
323 is  $U_{x,\infty} = 7.9$  m/s, and the along-flow turbulence length-scale is measured as  
324  $L_u = 0.84$  m.

325 The dimensions of the typical deck cross-section tested in the WT are  
326 included in Fig. 2(b), with  $d = 85$  mm to give a scale factor of 1/50 with  
327 respect to the midspan segment of the Orwell Bridge deck. In order to  
328 inform the design of the tunnel setup, a series of 3D CFD simulations were  
329 conducted in OpenFOAM [38] using the same numerical scheme described  
330 previously. The simulations showed that even with a relatively long deck  
331 of 2.4 m the wake of the upwind edge under the most inclined wind tested  
332 ( $\alpha = 45^\circ$ ) affected the vehicle located at its centre, particularly in Lane 4  
333 (downwind) as shown in Fig. 9(a). Therefore, it was decided to place the  
334 vehicle at the quarter-span of the deck, 0.6 m away from its downwind end,  
335 where such effect is reduced (Fig. 9(b)). Three different end plates were  
336 built in plywood to adjust to the upwind end of the deck model at skew  
337 wind angles of  $\alpha = 45^\circ$ ,  $60^\circ$  and  $75^\circ$ . In order to prevent clashing with the  
338 road furniture a small gap was left between the edge barriers and the plate,  
339 and it was covered by a small flexible screen to avoid the wind flow through  
340 the plate. The CFD results showed that the plate was not needed at the  
341 downwind end of the deck to explore the wind flow around the vehicle. The  
342 influence of the upwind end plate in the experimental results is considered  
343 further in Section 4.4. Regardless of the use of end plates, the CFD analysis  
344 also suggested that very skew incidence angles, with  $\alpha < 45^\circ$  (or  $\alpha > 135^\circ$ )  
345 cannot be tested accurately in the current setup because the flow disturbances  
346 originated at the upwind end of the deck propagate to the vehicle.

347 The stiff timber deck model includes all the relevant details of the para-  
348 pets and barriers with a tolerance of  $\pm 1$  mm. The bridge model was mounted  
349 on the tunnel's turntable using two vertical metal struts bolted to the un-  
350 derside of the model. These props have a small cross-section to minimise the  
351 obstruction to the wind flow because they are only used to hold the deck  
352 with vehicles at a height of approximately 600 - 800 mm from the tunnel's  
353 floor, and not to represent the actual piers of the bridge. The blockage ratio  
354 of the model in the WT is approximately 6%. Fig. 10 shows the test setup.

355 The WT is operated with an incoming wind speed at the level of the deck  
356 of  $U_{x,\infty} \approx 8$  m/s, resulting in a Reynolds number  $Re \approx 2.5 \times 10^5$ . This is lower  
357 than the expected  $Re$  numbers in actual bridges, but it has a small effect in  
358 the results according to other WT studies on scaled vehicle-bridge models  
359 that reached  $Re$  values in the same order of magnitude (e.g. [25, 43, 44]).

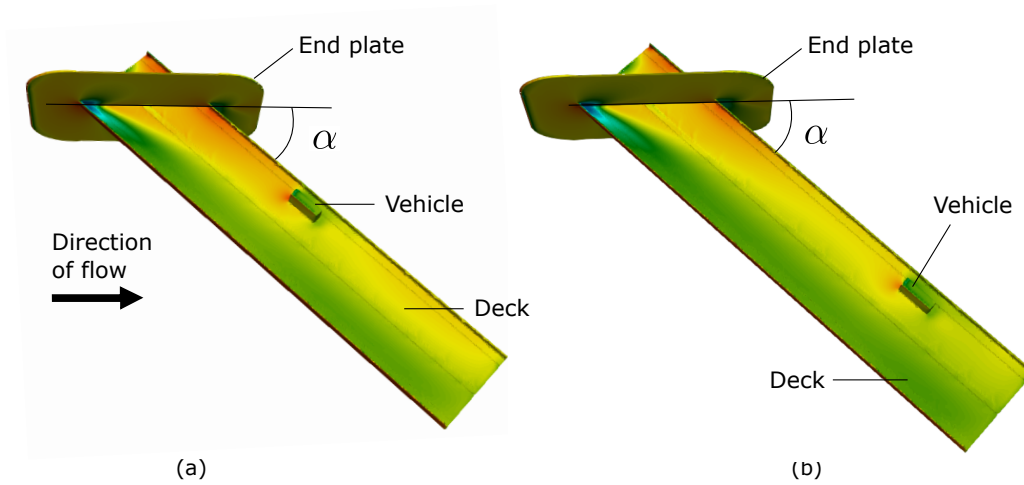


Figure 9: Normalised pressure contour map in the 2.4-m long deck model with an idealised vehicle on the leeward lane: (a) vehicle at midspan, (b) vehicle at downwind quarter-span. Both cases consider skew wind with  $\alpha = 45^\circ$ , going from left to right. The red and blue colour indicates the regions with highest and lowest pressures.

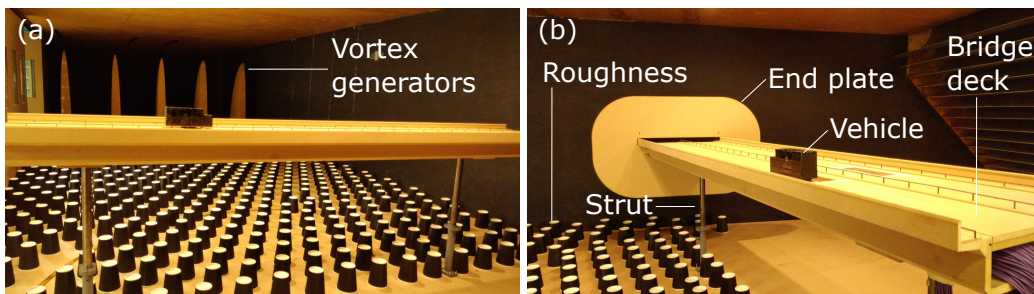


Figure 10: Setup of the model in the WT: (a) view of the model with the vortex generators behind, (b) view of the deck cross-section with the pressure tap tubes going to the vehicle, and the plate at the upwind end of the deck.

360 *4.2. Vehicle model*

361 The vehicle in this study is a 1/50-scale model of a typical rigid truck  
 362 with a simplified shape to facilitate manufacturing and maintain generality  
 363 in the results. The dimensions of the vehicle are included in Fig. 11(a),  
 364 along with its reference local axes ( $x_v, y_v, z_v$ ) and the position of its centroid.  
 365 This point is not the actual centroid of the physical model of the vehicle, but  
 366 it represents a conventional location of the centroid of unladen rigid trucks  
 367 reported in literature [16, 45]. The wheels are simplified as 6-mm thick timber  
 368 segments that represent the equivalent blockage of typical wheels to cross  
 369 winds. A 64-channels pressure scanner is used to calculate the aerodynamic  
 370 actions on the vehicle.

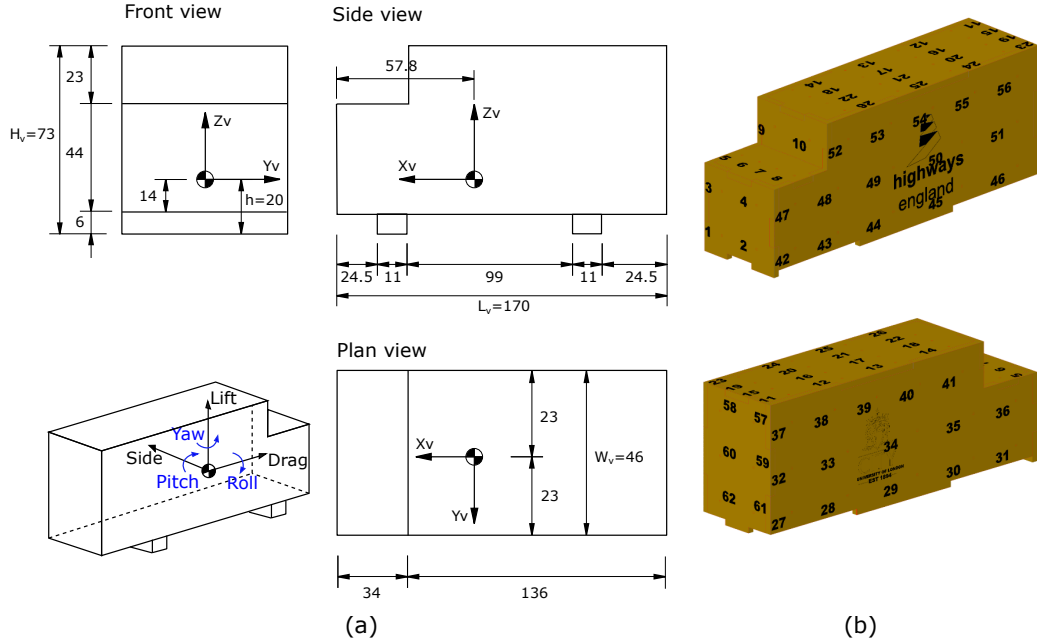


Figure 11: High-sided vehicle model used in the WT testing: (a) views with dimensions in mm, (b) distribution of pressure taps.

371 The vehicle model is made of acrylic plastic elements that are interlocked  
 372 and glued together to form all its faces. They have a total of 62 pressure  
 373 taps that were laser-cut. The distribution of these sensors in the vehicle  
 374 is designed to capture the pressure gradients for different wind incidence  
 375 angles, using as a reference the pressure maps obtained from the 3D CFD.  
 376 The distribution and the numbering of the pressure taps on the faces of the

377 vehicle is included in Fig. 11(b). The wheels of the vehicle are screwed to  
 378 a sliding plate that fits in the upper slab of the deck model. It allows the  
 379 vehicle to be placed on the centreline of the road lanes (L1 - L4) of the deck.  
 380 The tubes that connect the pressure taps on the vehicle with the pressure  
 381 scanner are mounted inside the hollow deck girders to avoid interference with  
 382 the air flow. It is noted that the lift forces on the vehicle are not obtained  
 383 because of the lack of pressure taps at its bottom face.

384 The side and drag forces ( $F_S$  and  $F_D$ ), as well as the rolling, pitching and  
 385 yawing moments ( $M_R$ ,  $M_P$  and  $M_Y$ ) are calculated at every instant from the  
 386 time-history recording of the pressure at each of the  $N_t = 62$  taps shown in  
 387 Fig. 11(b):

$$F_S(t) = \sum_{i=1}^{N_t} P_i(t) A_i n_i^{y_v} \quad (4a)$$

$$F_D(t) = \sum_{i=1}^{N_t} P_i(t) A_i n_i^{x_v} \quad (4b)$$

$$M_R(t) = \sum_{i=1}^{N_t} P_i(t) A_i n_i^{y_v} (z_i - z_G) + P_i(t) A_i n_i^{z_v} (y_i - y_G) \quad (4c)$$

$$M_P(t) = \sum_{i=1}^{N_t} P_i(t) A_i n_i^{z_v} (x_i - x_G) + P_i(t) A_i n_i^{x_v} (z_i - z_G) \quad (4d)$$

$$M_Y(t) = \sum_{i=1}^{N_t} P_i(t) A_i n_i^{y_v} (x_i - x_G) + P_i(t) A_i n_i^{x_v} (y_i - y_G), \quad (4e)$$

392 where  $P_i(t)$  and  $A_i$  are the instantaneous pressure and contributing area of  
 393 the  $i$ -th tap;  $(n_i^{x_v}, n_i^{y_v}, n_i^{z_v})$  are the three components of the vector normal  
 394 to the surface of the vehicle at the pressure tap  $i$ , in the Cartesian coordi-  
 395 nate system of the vehicle  $(x_v, y_v, z_v)$  shown in Fig. 11(a);  $(x_i, y_i, z_i)$  are the  
 396 coordinates of the  $i$ -th pressure tap in these axes; and  $(x_G, y_G, z_G)$  are the  
 397 local coordinates of the centroid of the vehicle, which are  $(0,0,0)$  in this case  
 398 because it coincides with the origin of the vehicle coordinate system. The  
 399 convention for positive pressures is that they point inside the vehicle, and  
 400 the positive normal vector at the surfaces also points inside the volume of the  
 401 vehicle. During the WT testing the instantaneous pressure  $P_i(t)$  is recorded  
 402 for 180 s with an adquisition frequency of 10 Hz.  
 403

404 We obtained the time-averaged aerodynamic coefficients from the time-  
 405 history results given in Eq. (4). The quasi-steady force coefficients are

$$C_j = \frac{F_j}{0.5\rho U_{x,\infty}^2 A_f}, \quad (5)$$

406 with the subindex  $j = S, D$  referring to the side and drag forces, respectively.  
 407  $A_f = 3082 \text{ mm}^2$  is the area of the back face of the vehicle, and  $\rho \approx 1.2$   
 408  $\text{kg/m}^3$  is the density of the air measured during the experiment. Similarly,  
 409 the quasi-steady moment coefficients are

$$C_j = \frac{M_j}{0.5\rho U_{x,\infty}^2 A_f h}, \quad (6)$$

410 in which  $j = R, P, Y$  represent the rolling, pitching and yawing moments,  
 411 respectively, and  $h = 20 \text{ mm}$  is the vertical distance from the wheel/deck  
 412 interface and the centroid of the vehicle (Fig. 11(a)).

#### 413 4.3. Test programme

414 The experimental programme aims to cover a wide range of combinations  
 415 of the wind incidence angle ( $\alpha$ ) and the position of the vehicle across the  
 416 width of the deck, which is always centered on one of the four road lanes  
 417 shown in Fig. 2(b). To facilitate the comparison of the results, the vehicle  
 418 is orientated southbound (with the local vehicle axis  $x_v$  pointing at the bot-  
 419 tom) regardless of the lane occupied and the wind incidence angle, as it is  
 420 illustrated in Figs. 12(a) and (b). The incidence angles range from  $\alpha = 45^\circ$   
 421 to  $\alpha = 135^\circ$ , with an interval of  $5^\circ$ . As it was observed in the CFD simula-  
 422 tion, if the wind incidence angle is between  $\alpha = 45^\circ$  and  $\alpha = 90^\circ$  the upwind  
 423 side of the deck model (which is the northbound one in Fig. 12(a)) does not  
 424 affect the wind flow around the vehicle. However, when  $\alpha > 90^\circ$  the upwind  
 425 end of the deck becomes the southbound one, and the test would require to  
 426 move the end plate and the vehicle to the opposite side of the bridge, or to  
 427 disassemble the whole bridge and rotate it  $180^\circ$  to reach the setup in Fig.  
 428 12(b). Symmetry is exploited to avoid this difficulty, and the vehicle is ro-  
 429 tated to face to the northbound end of the deck for the tests with  $\alpha > 90^\circ$ .  
 430 This leads to the configuration described in Fig. 12(c), which is equivalent  
 431 to Fig. 12(b) with  $\alpha = \alpha^* + 90^\circ$ , and  $\alpha^*$  being the apparent wind incidence  
 432 angle in the test with  $x_v$  northbound. Hereinafter, no mention is made to  
 433 the orientation of the vehicle in the test and only the wind incidence angle  
 434  $\alpha$  is reported.

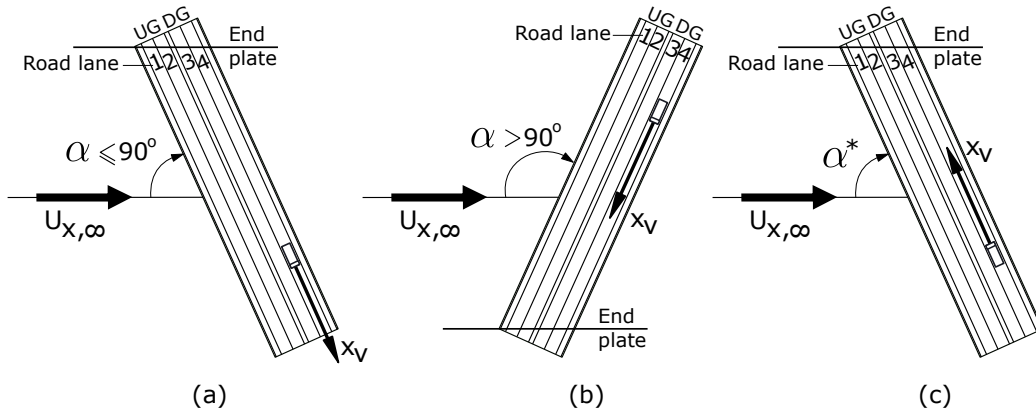


Figure 12: Plan view of the test configurations (looking from above) with wind incidence angles: (a)  $\alpha \leq 90^\circ$ , (b)  $\alpha > 90^\circ$ , and (c)  $\alpha > 90^\circ$  with opposite vehicle orientation ( $x_v$ ) to make it equivalent to (b). Note that the vehicle is static during testing. UG and DG refer to the upwind and downwind girders of the bridge, respectively.

435 In total, 76 different wind-vehicle configurations have been tested without  
 436 end plates, and 24 additional cases are repeated with these elements for angles  
 437  $\alpha = 45^\circ, 60^\circ, 75^\circ, 105^\circ, 120^\circ$  and  $135^\circ$  to explore their influence in the results.

#### 438 4.4. Results of the wind tunnel testing

439 The time-averaged pressure ( $\bar{P}_i$ ) measured on the faces of the vehicle when  
 440 it occupies different lanes and it is subject to purely cross wind ( $\alpha = 90^\circ$ ) is  
 441 presented in Fig. 13. The tributary area of each tap is coloured according  
 442 to its pressure, intentionally avoiding the use of smoothing interpolators to  
 443 show the actual test data. Regardless of the lane occupied by the vehicle, the  
 444 results in Fig. 13 show negative pressure (suction) in all its faces apart from  
 445 the windward side when  $\alpha = 90^\circ$ , and this is because of the separation of the  
 446 flow around the sharp corners of the vehicle faces. On the other hand, the  
 447 windward side of the vehicle presents a characteristic gradient of pressures  
 448 that goes from negative at the bottom to positive at the top due to the  
 449 diversion of the wind flow exerted by the upwind edge barrier of the deck.  
 450 This effect increases the rolling moment and it is most significant when the  
 451 vehicle is closer to the barrier (lane 1), reducing its importance as the vehicle  
 452 moves to the downwind edge. In order to visualise the flow, a stream of  
 453 smoke was introduced upstream of the deck, at the level of its barrier. Fig.  
 454 14 shows two frames of the visualised smoke, which indicate that the flow is  
 455 diverted by the barrier and thereafter impacts the top of the vehicle.

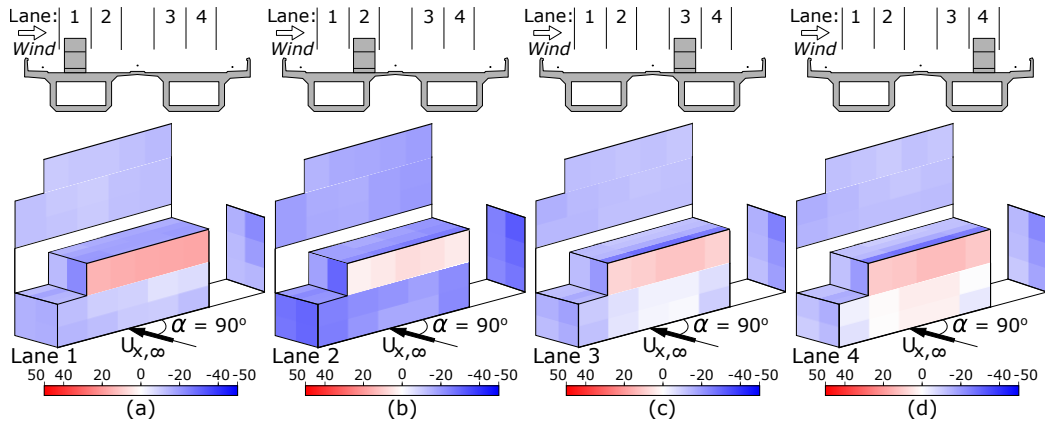


Figure 13: Time-averaged pressure distribution on the vehicle located in: (a) lane 1, (b) lane 2, (c) lane 3, and (d) lane 4. Purely cross wind  $\alpha = 90^\circ$ . The red and the blue colours indicate positive and negative pressures, respectively. Units in Pa.

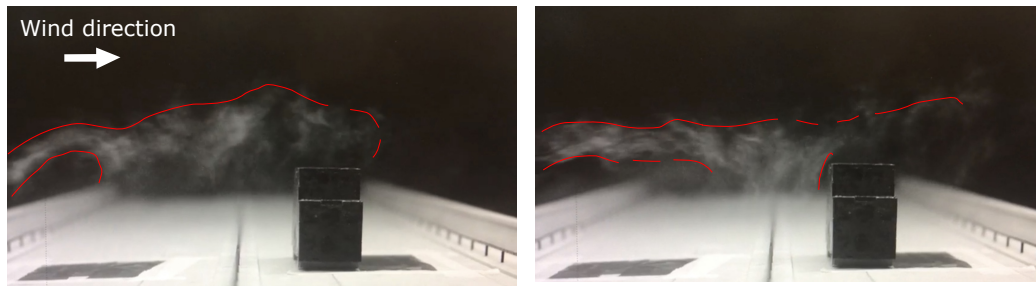


Figure 14: Two frames of the smoke flow recorded by a high-speed camera in the WT testing of the typical bridge, with the vehicle located on lane 3. Purely cross wind ( $\alpha = 90^\circ$ ) going from left to right.

456 The wind flow and the pressure distribution on the vehicle changes sig-  
 457 nificantly with the incidence angle, as illustrated in Figs. 15 and 16 for skew  
 458 wind angles with  $\alpha = 45^\circ$  and  $\alpha = 135^\circ$ , respectively (without end plate).  
 459 This is particularly true in the downwind lanes and it is attributed to (1) the  
 460 flow reattachment in this part of the deck due to the increased along-wind  
 461 width of the deck for skew incidence angles, and (2) the flow channelling  
 462 effects discussed previously. The latter affects the vehicle as a combination  
 463 of flow diversion ( $\gamma$ ) within the height of the parapets (plane P1, see Fig.  
 464 6(a)), and the increment in the velocity magnitude ( $U_h$ ) in the full height  
 465 of the vehicle (planes P1 and P2, Fig 7(a)). With  $\alpha = 45^\circ$  and  $\alpha = 135^\circ$ , the  
 466 shielding effect of the edge parapet is only visible in the windward side face  
 467 of the vehicle located on the upwind girder (lanes 1 and 2). When it is on the  
 468 downwind girder (lanes 3 and 4) most of this face is under positive pressure,  
 469 with an along-deck gradient that contributes to the yawing moment in the  
 470 vehicle. This effect is also present in the suction measured on the leeward  
 471 face of the vehicle, which contrasts with the approximately uniform suction  
 472 observed on this face under cross-winds, as seen in Fig. 13.

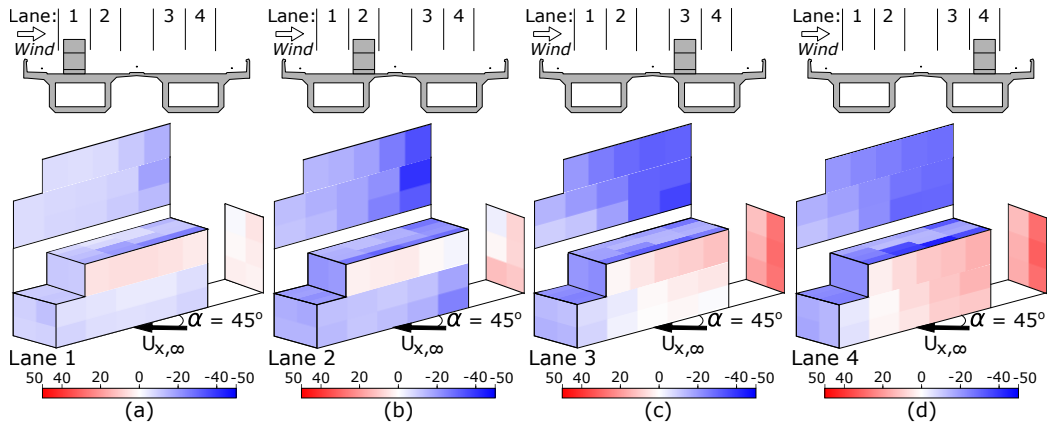


Figure 15: Time-averaged pressure distribution on the vehicle located in: (a) lane 1, (b) lane 2, (c) lane 3, and (d) lane 4. Skew wind  $\alpha = 45^\circ$ . The red and the blue colours indicate positive and negative pressures, respectively. Units in Pa.

473 The skew wind angles  $\alpha = 45^\circ$  and  $\alpha = 135^\circ$  fall within the full-channelling  
 474 Zone III identified in the CFD analysis of Section 3, and its characteristic  
 475 along-deck diversion of the flow contribute to the vehicle pressure maps  
 476 recorded in Figs. 15 and 16. Under very skew tail-winds ( $\alpha = 45^\circ$ ) the pressure  
 477 at the rear face of the vehicle is higher than at its windward side, which

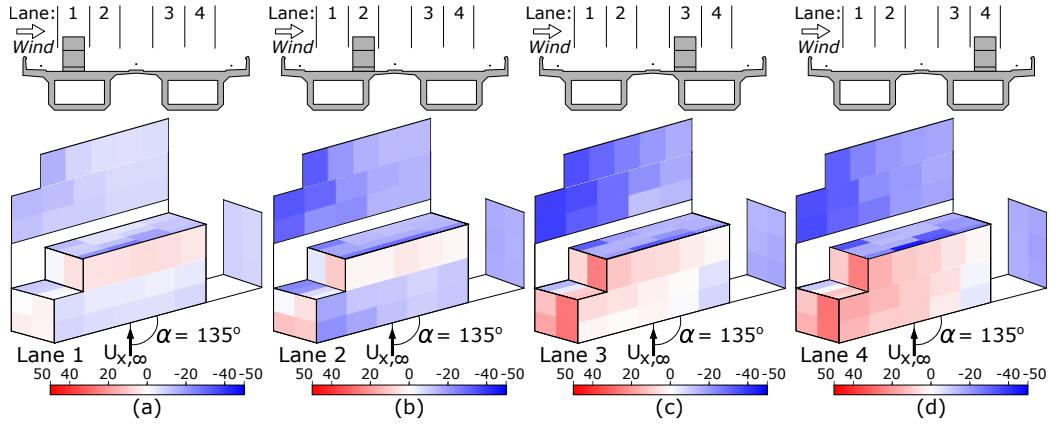


Figure 16: Time-averaged pressure distribution on the vehicle located in: (a) lane 1, (b) lane 2, (c) lane 3, and (d) lane 4. Skew wind  $\alpha = 135^\circ$ . The red and the blue colours indicate positive and negative pressures, respectively. Units in Pa.

478 affects the vehicle drag and it is attributed to the along-deck wind flow on  
 479 the deck, particularly in lanes 3 and 4 (Figs. 15(c) and (d)). The same effect  
 480 is observed in the case with skew head-wind  $\alpha = 135^\circ$ , but in this case the  
 481 large positive pressure is recorded at the front vehicle face (Figs. 16(c) and  
 482 (d)). We also note that the increment of suction at the windward edge of the  
 483 vehicle top for very skew winds was also reported by [46] testing a similar  
 484 vehicle in an open flat surface (off-bridge), which suggests that it is due to  
 485 the wind incidence angle and not to the wake of the parapets.

486 Following the study of the pressure distribution on the vehicle, the discus-  
 487 sion now focuses on the resultant wind effects. Fig. 17 presents the side  
 488 coefficient ( $C_S$ ) of the vehicle located in both girders, and compares it with  
 489 the off-bridge coefficient given by Baker [16] to highlight the important dif-  
 490 ferences with the on-bridge aerodynamic effects for a wide range of wind  
 491 incidence angles. The zonation of skew winds observed in the CFD anal-  
 492 ysis of Section 3 is also included, which is proven to have an important effect  
 493 in the results obtained experimentally. The side coefficient for winds in Zone  
 494 I (small incidence angles) is reduced by approximately 42%, 83%, 66% and  
 495 53% in lanes 1, 2, 3 and 4, respectively, with respect to the corresponding  
 496 off-bridge reference value. This indicates that the shielding of the upwind  
 497 edge barrier reduces the side force significantly for purely or nearly-cross  
 498 winds, especially in lane 2 because it is where the region of low wind speeds  
 499 across the deck (referred to as ‘protective bubble’) created by the windward

500 barrier is higher. However, this effect diminishes as the vehicle moves to the  
 501 downwind lanes. On the other hand, the side force is reduced by increasing  
 502 the wind incidence angle in the transition Zone II when the vehicle is in lane  
 503 1, but it is almost insensitive to changes of  $\alpha$  within this Zone when the  
 504 vehicle is in other lanes. The picture changes significantly under large skew  
 505 wind angles in Zone III, where the side force on the vehicle increases with  
 506  $\alpha$  in Zone III for all the road lanes, but particularly in the downwind girder  
 507 lanes 3 and 4 (Fig. 17(b)), for which  $C_S$  rises by up to 80% when  $\alpha$  varies  
 508 only 25% (from 60° to 45°). This is attributed to the reattachment of the  
 509 wind flow on the downwind girder for very skew wind angles in Zone III.

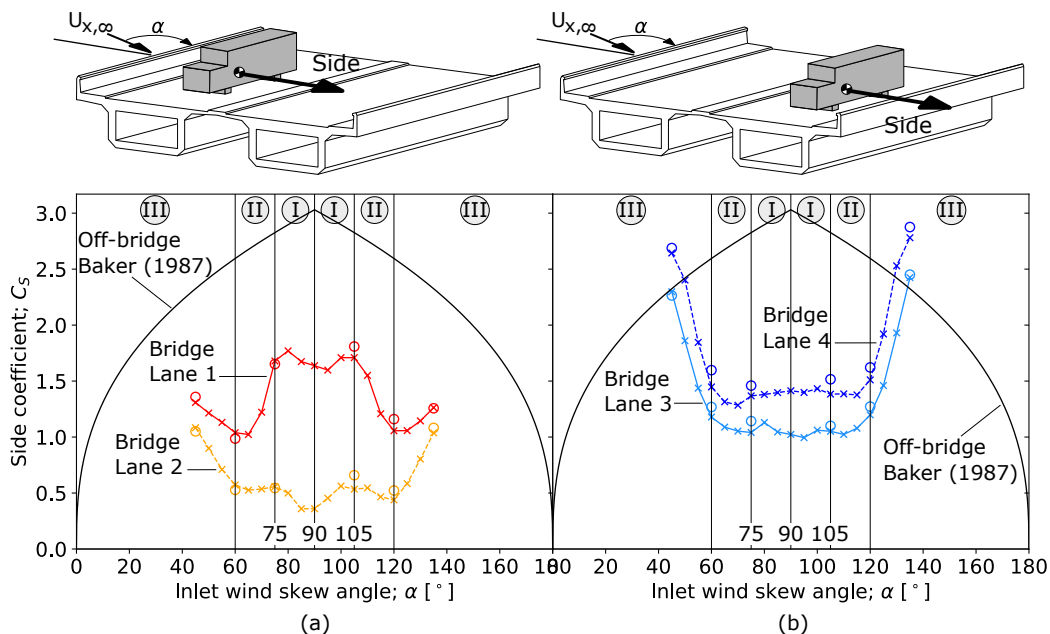


Figure 17: Side coefficient of the vehicle in: (a) upwind girder, and (b) downwind girder. The off-bridge side coefficient given by Baker [16] is included for comparison. The cross markers connected with lines refer to the tests without end plate, whilst the circular markers indicate the results with end plate. The positive convention for side forces in the vehicle is included.

510 The drag coefficient ( $C_D$ ) is included in Fig. 18, and it also shows its  
 511 dependency with the skew wind zonation and the position of the vehicle  
 512 across the width of the deck. The drag increases more with  $\alpha$  in Zone I than  
 513 in Zone II, which can be connected with the smaller change of the inclination  
 514 angle of the horizontal wind along the deck ( $\gamma$ ) in Zone II, as it was described

515 in Fig. 5(a). However, when the wind flow is fully channelled in Zone III the  
 516 drag coefficient grows at a higher rate with the wind incidence angle. This is  
 517 observed in all the lanes, but the influence of  $\alpha$  is stronger in the downwind  
 518 girder (Fig. 18(b)) resulting in drag coefficients in lanes 3-4 that are larger  
 519 than those in lanes 1-2, also exceeding the reference values for the vehicle in  
 520 open terrain. This is explained by the large wind pressure in the rear or front  
 521 vehicle faces for tail- or head-winds, respectively, as shown in Figs. 15(c)-(d)  
 522 and 16(c)-(d), which is attributed to the flow channelling in Zone III.

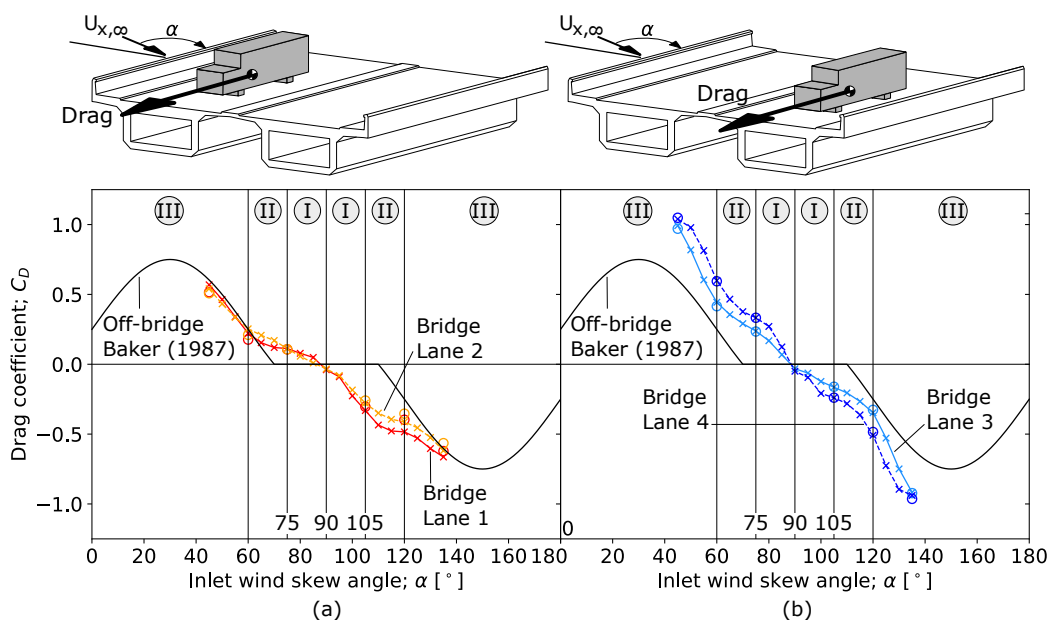


Figure 18: Drag coefficient of the vehicle in: (a) upwind girder, and (b) downwind girder. The off-bridge side coefficient given by Baker [16] is included for comparison. The cross markers connected with lines refer to the tests without end plate, whilst the circular markers indicate the results with end plate. The positive convention for drag forces in the vehicle is included.

523 Fig. 19 shows that the influence of the wind incidence angle  $\alpha$  on the  
 524 rolling moment of the vehicle ( $C_R$ ) is closely related to that on the side force.  
 525 The exception is mainly in Lane 1 for highly skew winds, in Zone III, where  
 526 the rolling coefficient is strongly reduced. This is because the vertical pressure  
 527 gradient observed in the windward vehicle face for cross-winds gives way to  
 528 a more uniform pressure distribution in the vertical direction when  $\alpha < 60^\circ$   
 529 (Fig. 15(a)) or  $\alpha > 120^\circ$  (Fig. 16(a)). However, the same range of skew  
 530 angles in Zone III increases the rolling moment in the downwind girder even

531 beyond the off-bridge reference value (Fig. 19(b)), both for tail- and head-  
 532 winds. This may be due to the larger positive and negative pressures recorded  
 533 at the top of the vehicle's windward and leeward side faces, respectively, when  
 534 it is in lanes 3 and 4 and the incidence angle of the wind is in Zone III (see  
 535 Figs. 15(c)-(d) and 16(c)-(d)), in combination with the relatively low position  
 536 of the centroid of the vehicle.

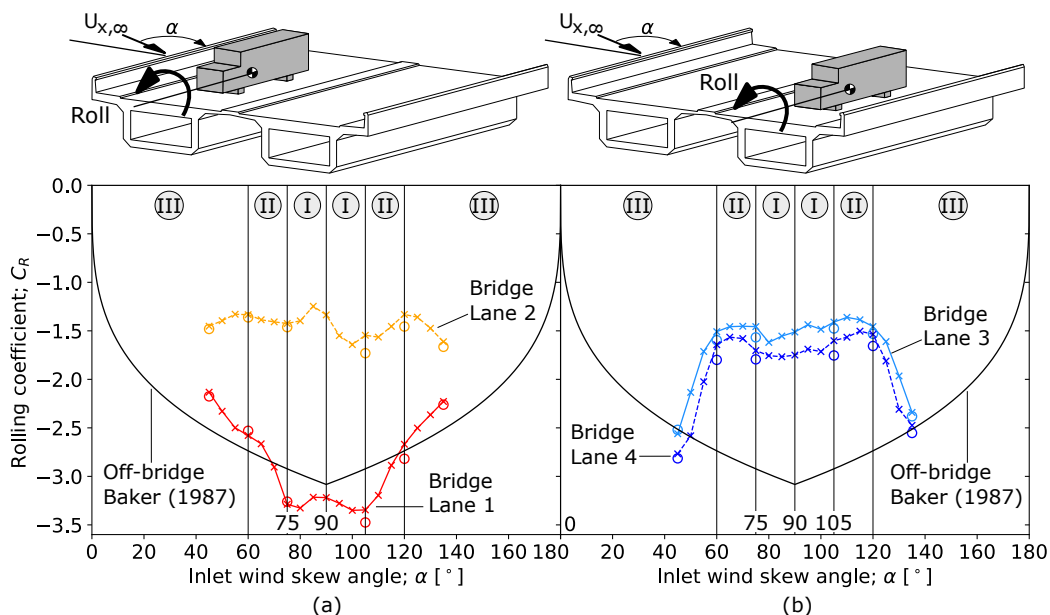


Figure 19: Rolling coefficient of the vehicle in: (a) upwind girder, and (b) downwind girder. The off-bridge side coefficient given by Baker [16] is included for comparison. The cross markers connected with lines refer to the tests without end plate, whilst the circular markers indicate the results with end plate. The positive convention for rolling moments in the vehicle is included.

537 The pitching and the yawing moment coefficients of the vehicle ( $C_P$  and  
 538  $C_Y$ ) are included in Figs. 20 and 21, respectively. The apparent asymmetry of  
 539 these two actions with respect to the cross-wind angle of incidence  $\alpha = 90^\circ$   
 540 contrasts with the other aerodynamic coefficients, particularly due to the  
 541 large increments of  $C_P$  and  $C_Y$  for Zone III head-winds ( $\alpha > 120^\circ$ ) in lanes  
 542 1 and 2, and for tail-winds ( $\alpha < 60^\circ$ ) in lanes 3 and 4. The pitching moment  
 543 is larger than the off-bridge vehicle reference value in the upwind girder,  
 544 especially in lane 1, when  $\alpha > 120^\circ$  (Fig. 20(a)). This is attributed to  
 545 the pressure imbalance at the top vehicle face shown in Figs. 15 and 16,  
 546 and it also appears on its side faces (windward and leeward) to contribute

547 to the yawing moment presented in Fig. 21. Lane 1 shows values of  $C_Y$   
 548 that are similar to those in the off-bridge vehicle for all the angles tested  
 549 apart from skew headwinds with  $\alpha > 120^\circ$  that fall in Zone III, for which  
 550 the yawing moment increases significantly. The same happens in Lane 2,  
 551 which is significantly shielded until  $\alpha > 120^\circ$ . The effect is more significant  
 552 in the downwind girder, in which the yawing moment is relatively low for  
 553 angles in Zones I and II, but increases significantly in Zone III, particularly  
 554 for tailwinds with  $\alpha < 60^\circ$ . Indeed, when  $\alpha = 45^\circ$  the value of  $C_Y$  is more  
 555 than 5 times higher than with  $\alpha > 60^\circ$ . This is explained by the horizontal  
 556 pressure gradient increasing towards the windward face of the vehicle for  
 557 very skew tailwinds when it is in the downwind girder, favoured by the flow  
 558 channelling in Zone III as depicted in Figs. 15(c) and (d). The effect is  
 559 stronger under tailwinds because the distance between the centroid of the  
 560 vehicle and its rear side is larger than to its front side (Fig. 11(a)).

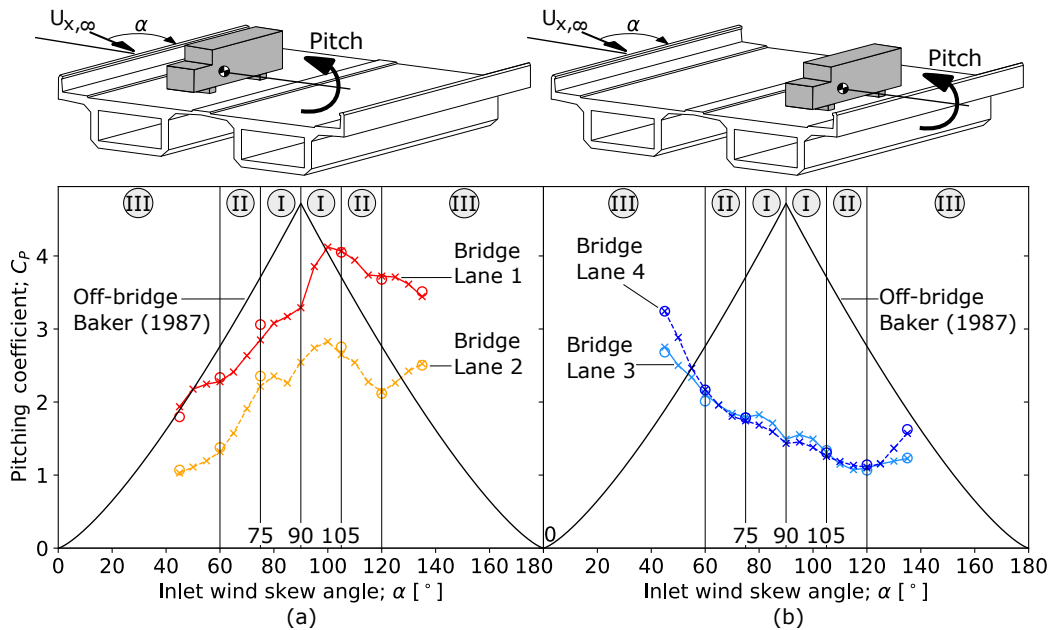


Figure 20: Pitching coefficient of the vehicle in: (a) upwind girder, and (b) downwind girder. The off-bridge side coefficient given by Baker [16] is included for comparison. The cross markers connected with lines refer to the tests without end plate, whilst the circular markers indicate the results with end plate. The positive convention for pitching moments in the vehicle is included.

561 It is observed in Figs. 17 - 21 that the results with the end plate installed

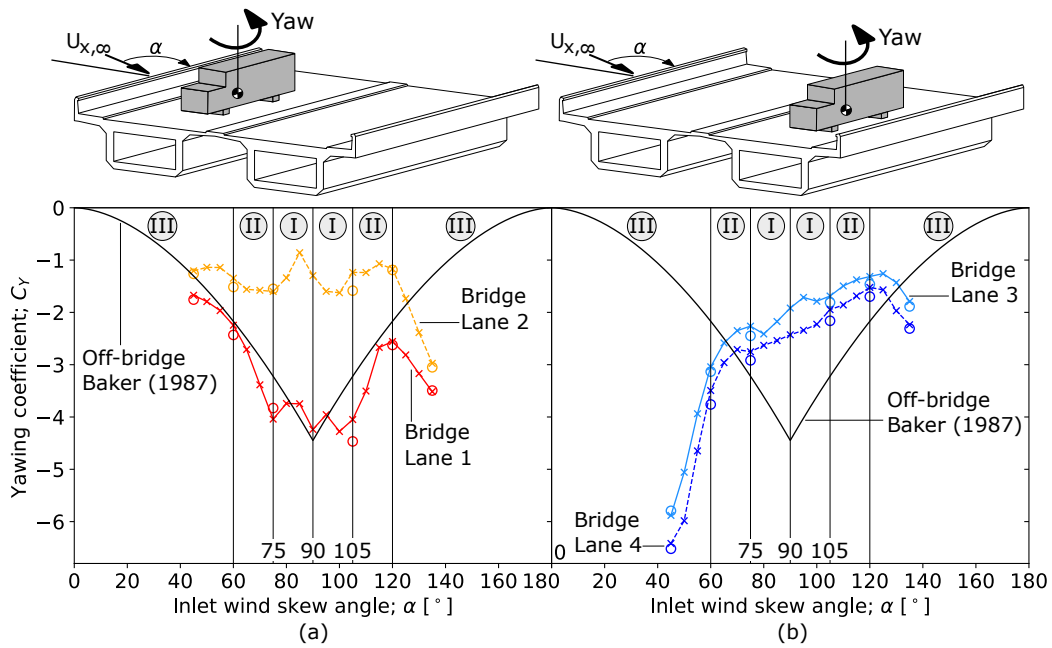


Figure 21: Yawing coefficient of the vehicle in: (a) upwind girder, and (b) downwind girder. The off-bridge side coefficient given by Baker [16] is included for comparison. The cross markers connected with lines refer to the tests without end plate, whilst the circular markers indicate the results with end plate. The positive convention for yawing moments in the vehicle is included.

562 in the bridge model are very similar to the corresponding cases without this  
563 element, with a maximum difference in the order of 10%. This indicates that  
564 under non-orthogonal winds the upwind end of the model does not affect  
565 significantly the flow around the vehicle thanks to the length of the deck  
566 model, and it validates the use of the results without end plate for all the  
567 wind incidence angles tested. In the following, the WT test results correspond  
568 to cases without this element.

#### 569 4.5. Further considerations on wind channelling effects

570 The along-deck channelling of the wind field is explored further consid-  
571 ering the horizontal vehicle aerodynamic force vector that results from the  
572 combination of the side and the drag forces in the horizontal plane ( $x - z$ ),  
573 as shown in Fig. 1(c). The magnitude of this vector,  $F_{SD} = \sqrt{F_S^2 + F_D^2}$ ,  
574 is normalised with respect to the projected area of the vehicle in the wind  
575 direction:

$$C_{SD} = \frac{F_{SD}}{0.5\rho U_{x,\infty}^2 L_p H_v}, \quad (7)$$

576 this is to avoid distorting the results because the area of the vehicle's side  
577 face is larger than the rear one. In Eq. (7)  $H_v = 73$  mm is the height of  
578 the vehicle and  $L_p$  is the projected length of the vehicle plan in the wind  
579 direction:  $L_p = L_v \sin(\alpha) + W_v \cos(\alpha)$ , with  $L_v = 170$  mm and  $W_v = 46$  mm  
580 being the length and the width of the vehicle, respectively (see Fig. 11(a)).

581 The results of the combined side-drag coefficient are obtained in each  
582 time frame during testing and their average values are presented in Fig. 22.  
583 The horizontal force exerted by the wind on the vehicle is almost insensitive  
584 to changes in the wind incidence angle when it is moderately skewed, in  
585 Zones I and II, for all the lanes with the exception of the upwind one (lane  
586 1). However, the transition to Zone III marks a strong increment of the  
587 horizontal wind force as it becomes more inclined with respect to the deck,  
588 particularly in lanes 3-4 as shown in Fig. 22(b). This is attributed to the  
589 along-deck channelling of the wind field within the height of the barriers,  
590 combined with flow reattachment in the downwind girder.

591 The angle  $\psi$  between the horizontal aerodynamic force on the vehicle and  
592 the inlet wind direction that was described in Fig. 1(c) is:

$$\psi = \arctan \left[ \frac{F_D \cos(\alpha) + F_S \sin(\alpha)}{F_D \sin(\alpha) - F_S \cos(\alpha)} \right], \quad (8)$$

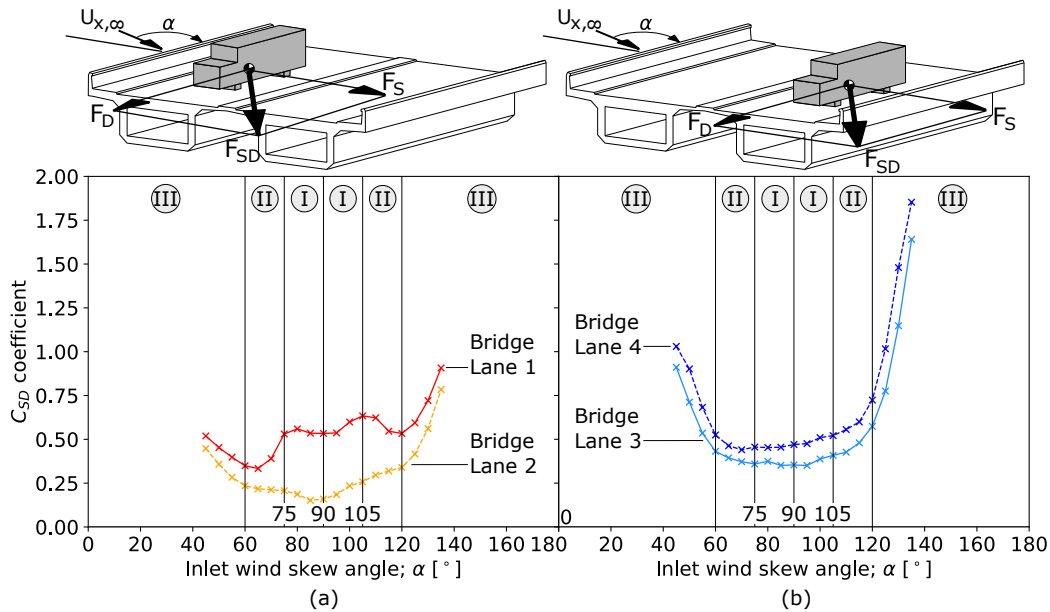


Figure 22: Combined side-drag aerodynamic coefficient  $C_{SD}$  of the vehicle in (a) upwind girder, and (b) downwind girder. The positive convention for side and drag forces in the vehicle is included.

593 which is averaged in Fig. 23 from the instantaneous values measured in the  
 594 WT. The results indicate that the deviation of the side-drag force resultant  
 595 with respect to the wind incidence angle is relatively small (within  $\psi \pm 10^\circ$ )  
 596 in Zones I and II, with the exception once again of Lane 1 and  $\alpha < 75^\circ$  due  
 597 to the large wind exposure in this part of the deck. The small value of  $\psi$   
 598 in Zones I and II indicates that for moderate-to-low wind incidence angles  
 599 the horizontal force  $F_{SD}$  on the vehicle is almost aligned with the inlet wind  
 600 direction. However, large deviations between the direction of wind and  $F_{SD}$   
 601 appear in Zone III due to the flow channelling along the deck, particularly  
 602 in the downwind girder.

603 However, there are significant differences between the angle  $\psi$  measured  
 604 in the WT and the direction of wind within the height of the barriers ( $\gamma$ ),  
 605 because the former is affected by the aerodynamic pressure on the vehicle  
 606 above the barriers. For this reason additional WT tests with light-weight  
 607 woolen tufts distributed along the centre of the four lanes were conducted  
 608 to visualise the orientation of the wind flow along the deck, close to the  
 609 pavement surface. One end of these tufts was fixed to the model and they

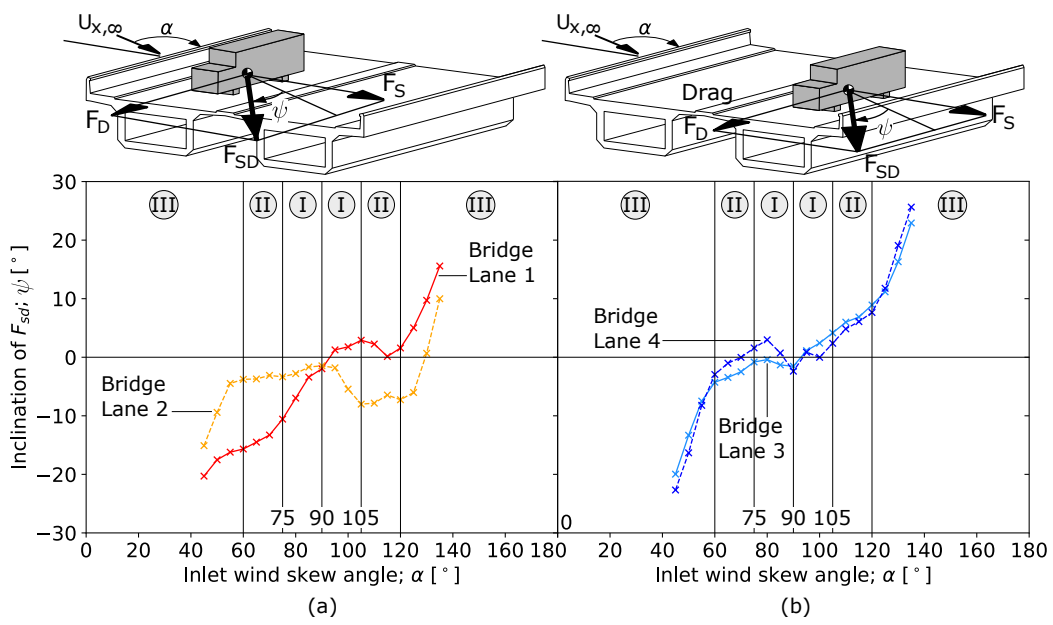


Figure 23: Angle  $\psi$  between the inlet mean wind speed direction and the horizontal side-drag resultant force  $F_{SD}$  in (a) upwind girder, and (b) downwind girder. The positive convention for the angle  $\psi$  is included.

610 are shown as black lines in the plan views of the testing included in Fig.  
 611 24, where the numbers 1, 2, 3 and 4 refer to the corresponding road lanes.  
 612 During testing, a high-speed camera mounted above the model was used to  
 613 study the movement of the tufts. The orientation of the wind flow at the  
 614 pavement level,  $\gamma$  (Fig. 1(b)), was estimated by identifying which tufts were  
 615 actively moving during the tests and averaging the angle that they formed  
 616 with the horizontal line. The lines in Fig. 25 show the angle of wind along  
 617 the deck, after averaging separately the values of  $\gamma$  in the active wool strips  
 618 of the lanes in the two girders. The figure also includes shaded bands that  
 619 represent one standard deviation of  $\gamma$  above and below the mean value.

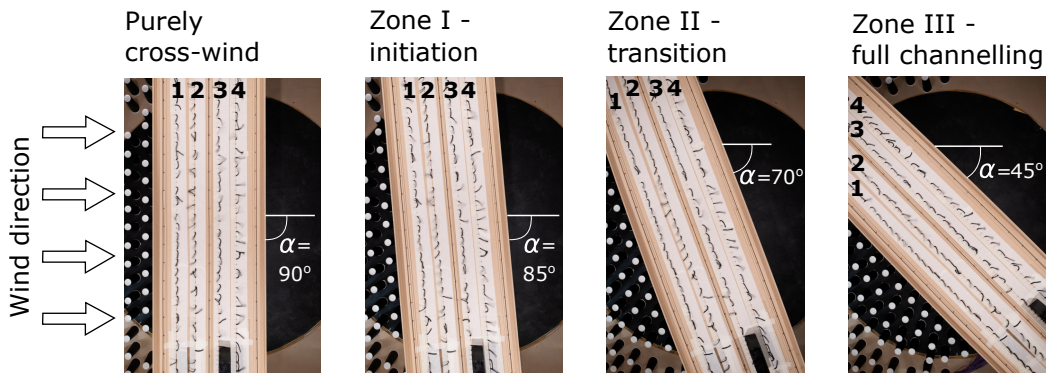


Figure 24: Plan view of the experimental measurement of the along-deck wind inclination ( $\gamma$ ) in the WT for wind incidence angles ( $\alpha$ ) that are representative of different flow regions.

620 The experimental results in Fig. 25 are compared with those obtained  
 621 from the CFD analysis of the wind flow within the height of the barriers  
 622 (Plane 1) in the generic bridge deck discussed in Section 3. The results of  
 623 both studies are consistent, even though the experimental testing and the  
 624 CFD results refer to slightly different deck cross-sections (see Fig. 2). The  
 625 differences between CFD and WT testing are higher for wind flows that are  
 626 fully or nearly perpendicular to the deck, because the larger shielding effect of  
 627 the barriers reduces significantly the mean wind speed close to the pavement  
 628 level (also observed in the CFD results of Fig. 5(b)-(c)), and the movement of  
 629 the tufts is more chaotic as it can be observed in the large standard deviation  
 630 of the angle  $\gamma$  across the deck in Zone I. However, the influence of the skew  
 631 angle  $\alpha$  on the wind flow in the downwind region of the deck agrees well with  
 632 the three different zones described in the CFD study. As it was observed  
 633 in the numerical analysis, the WT testing shows that  $\gamma$  is smaller than  $\alpha$

634 in the downwind girder. The larger differences between the inclination of  
 635 the wind flow in the upwind girder of the tested bridge, compared with the  
 636 CFD results, are attributed to a stronger recirculation effect, observed in the  
 637 inclination of the tufts in lanes 1 and 2 in Fig. 24. Nevertheless, for very  
 638 large skew angles in Zone III the experimental results indicate that the flow  
 639 in these lanes is almost aligned with the deck, resulting in a fully channelled  
 640 flow.

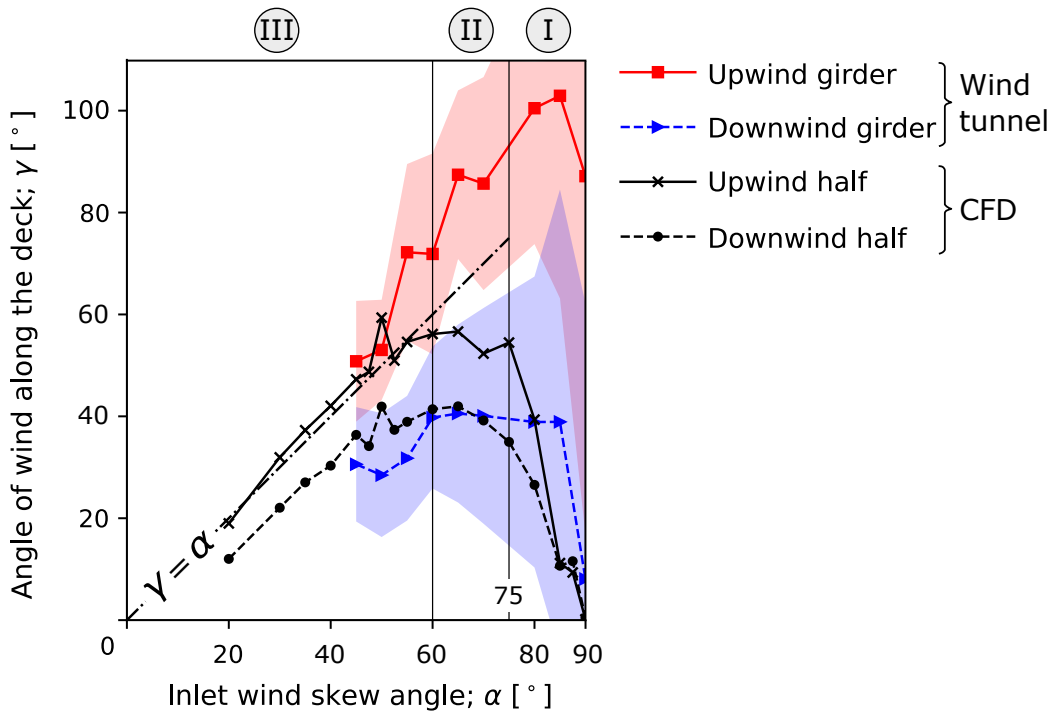


Figure 25: Comparison of the along-deck wind inclination ( $\gamma$ ) obtained with WT testing in the typical bridge, and with CFD in Plane P1 of the generic bridge.

## 641 5. Conclusions

642 This work studied the effect of the angle of incidence of the wind on the  
 643 flow around bridge decks with low-rise edge parapets ( $h_f/d = 1/3$ ), and how  
 644 it affects the aerodynamic forces and moments on vehicles. To this end, a  
 645 generic (idealised) deck model with different barrier configurations is studied  
 646 using computational fluid dynamic (CFD) analysis. The work continues with

647 an extensive wind tunnel (WT) testing programme on a deck model that  
648 represents a real bridge with a conventional configuration of relatively short  
649 side barriers. The following conclusions are drawn:

- 650 • The CFD analysis of the generic deck model showed that a low-rise  
651 windward edge parapet is able to introduce a significant diversion of  
652 the wind velocity field along the deck for skew incidence angles. This  
653 flow diversion mainly occurs within the height of the barriers.
- 654 • The effect of the wind skew angle ( $\alpha$ ) on the horizontal angle of inclina-  
655 tion of the wind velocity along the deck ( $\gamma$ ) is studied experimentally  
656 and numerically. In the region of the deck within the height of the barri-  
657 ers both methods show that for small incidence angles ( $75^\circ < \alpha < 105^\circ$ )  
658  $\gamma$  rapidly changes to get closer to  $\alpha$  (Zone I - Initiation); for interme-  
659 diate skew angles  $\gamma$  is relatively insensitive to  $\alpha$  (Zone II - Transition);  
660 and for very skew winds ( $\alpha < 60^\circ$  or  $\alpha > 120^\circ$ ) the wind flow is almost  
661 aligned with the deck (Zone III - Full channelling). The deviation of  
662 the wind velocity field by the deck is negligible above the parapets,  
663 regardless of the skew angle.
- 664 • The pressure maps on the vehicle faces obtained in the WT testing  
665 indicate that under purely cross-winds the low-rise parapets are able  
666 to shield significantly high-sided vehicles across the width of the deck,  
667 particularly in its centre and towards the windward side. However, the  
668 parapets direct the wind to the top of the vehicle, increasing the rolling  
669 moment in the most upwind lane.
- 670 • The skew wind angle affects significantly the pressure distribution and  
671 the resultant aerodynamic coefficients on the vehicle, which exceed the  
672 reference off-bridge values if  $\alpha$  is in Zone III due to the along-deck flow  
673 and its reattachment in the downwind girder.

674 One limitation of this work is that it considers the vehicle as static in  
675 the wind tunnel testing. However, its relevance lies in the observation of sig-  
676 nificant flow disturbances around conventional bridge decks with relatively  
677 short edge parapets, which are widely used for the safety of traffic but rou-  
678 tinely ignored in the aerodynamic actions on vehicles. More importantly,  
679 it is demonstrated that the wind field around vehicles changes significantly  
680 with the incidence angle. This suggests that the widely spread use of aerody-  
681 namic vehicle coefficients calculated from numerical or experimental models

682 in which the vehicle is static are not entirely valid in further wind-vehicle-  
683 bridge interaction analyses. This is because as the vehicle moves in this type  
684 of studies the relative angle of incidence of wind changes ( $\beta$  in Fig. 1(a)),  
685 and this cannot be directly related to the angle  $\alpha$  used in the test with a  
686 static vehicle, as it was also argued by [28, 29] in railway bridges. [Therefore, additional WT testing with moving vehicles for different wind incidence](#)  
687 [angles is needed.](#)  
688

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693 of the actual conditions in the Orwell Bridge.

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