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**Citation:** Aqel, O., White, M. & Sayma, A. I. (2023). Loss Analysis in Radial Inflow Turbines for Supercritical CO<sub>2</sub> Mixtures. In: Proceedings of the ASME Turbo Expo. . New York, USA: ASME. ISBN 9780791887110 doi: 10.1115/GT2023-102556

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## LOSS ANALYSIS IN RADIAL INFLOW TURBINES FOR SUPERCRITICAL CO<sub>2</sub> MIXTURES

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### ABSTRACT

Recent studies have indicated the potential of CO<sub>2</sub>-mixtures to lower the cost of concentrated solar power plants. Based on aerodynamic and cost considerations, radial inflow turbines (RIT) can be a suitable choice for small to medium sized sCO<sub>2</sub> power plants (about 100 kW to 10 MW). The aim of this paper is to quantify the effect of doping CO<sub>2</sub> on the design of RITs. This is achieved by comparing the 1D mean-line designs and aerodynamic losses of pure sCO<sub>2</sub> RITs with those of three sCO<sub>2</sub> mixtures containing tetrachloride (TiCl<sub>4</sub>), sulphur dioxide (SO<sub>2</sub>), and hexafluorobenzene (C<sub>6</sub>F<sub>6</sub>).

Results show that the optimal turbine designs for all working fluids will have similar rotor shapes and velocity diagrams. However, factors such as the clearance-to-blade-height ratio, turbine pressure ratio, and the difference in the viscosity of the fluids cause variations in the achievable turbine efficiency. Once the effects of these factors are eliminated, differences in the total-to-static efficiency amongst the fluids may become less than 0.1%. Moreover, if rotational speed limits are imposed, then greater differences in the designs and efficiencies of the turbines emerge amongst the fluids. It was found that limiting the rotational speed reduces the total-to-static efficiency in all fluids; the maximum reduction is about 15% in 0.1 MW CO<sub>2</sub> compared to the 3% reduction in CO<sub>2</sub>/TiCl<sub>4</sub> turbines of the same power.

Among the mixtures studied, CO<sub>2</sub>/TiCl<sub>4</sub> achieved the highest performance, followed by CO<sub>2</sub>/C<sub>6</sub>F<sub>6</sub>, and then CO<sub>2</sub>/SO<sub>2</sub>. For example, 100 kW turbines for CO<sub>2</sub>/TiCl<sub>4</sub>, CO<sub>2</sub>/C<sub>6</sub>F<sub>6</sub>, CO<sub>2</sub>/SO<sub>2</sub>, and CO<sub>2</sub> achieve total-to-static efficiencies of 80.0%, 77.4%, 78.1%, and 75.5% respectively. Whereas, the efficiencies for 10 MW turbines are 87.8%, 87.3%, 87.5%, and 87.2%, in the same order.

**Keywords:** sCO<sub>2</sub> power cycle, radial inflow turbine, loss analysis, sCO<sub>2</sub> mixtures

### NOMENCLATURE

#### Roman letters

$p$	Pressure [Pa]
$T$	Temperature [K <sup>-1</sup> or °C]
$h$	Specific enthalpy [J kg <sup>-1</sup> ]
$t$	Blade thickness [m]
$Z_n$	Sator blade count [no]
$Z_r$	Rotor blade count [no]
$N$	Rotational speed [RPM]
$\dot{m}$	Mass flow rate [kgs <sup>-1</sup> ]

#### Greek letters

$\alpha$	Absolute flow angle [°]
$\beta$	Relative flow angle [°]
$\eta$	Efficiency
$\phi$	Flow coefficient
$\psi$	Loading coefficient
$\xi$	Meridional velocity ratio
$\epsilon$	Clearance gap height
$\nu$	Kinematic viscosity [mm <sup>2</sup> s <sup>-1</sup> ]

#### Dimensionless groups

$N_s$	Specific speed
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#### Superscripts and subscripts

tt	Total-to-total
ts	Total-to-static
s	Isentropic value
sh	value at the rotor shroud
h	value at the rotor hub

### 1. INTRODUCTION

Recent research has shown the advantage of CO<sub>2</sub>-mixtures over pure CO<sub>2</sub> and state of the art steam Rankine cycles when used in power blocks of concentrated solar power (CSP) plants. Studies under the umbrella of the SCAREBEUS project have posited that mixtures of CO<sub>2</sub>/TiCl<sub>4</sub>, CO<sub>2</sub>/SO<sub>2</sub>, and CO<sub>2</sub>/C<sub>6</sub>F<sub>6</sub> may achieve cycle efficiencies above 50% depending on the cycle layout, turbine inlet temperature, and minimum cycle temperature; which may be as high as 60°C in the case of CO<sub>2</sub>/SO<sub>2</sub>

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Documentation for asmeconf.c.l.s: Version 1.32, February 24, 2023.

[1–4]. Most recently, it was found that mixtures outperform pure sCO<sub>2</sub> or steam cycles in both energy and exergy efficiencies, a difference which increases at higher ambient temperatures [5].

Another line of CO<sub>2</sub>-mixture research is being pursued by Valencia-Chapi and co-authors. In a group of 4 studies, they investigated 16 mixtures for CSP power blocks. All of their studies show the increase in cycle efficiency compared to pure sCO<sub>2</sub>. Similar to the SCARABEUS project, they found that the gains in efficiency depend on the choices of dopant, cycle layout, heat sink temperature, and mode of cooling [6–9]. Research into CO<sub>2</sub>-mixture power blocks has also been gaining momentum with other research groups, some of which attest to the potential benefits of the technology for plants with elevated cooling temperatures [10–16]. Overall, this technology seems promising for CSP plants with relatively high heat sink temperatures (above 40 °C).

According to the criteria presented by Di Marcoberardino et al. [17], the dopants for CSP applications must be able to create mixtures with critical temperatures above 85 °C (0.9 of the critical temperature), and maintain thermal and chemical stability at high temperatures (700 °C) and pressures (25 MPa).

Having established the latent advantages of CO<sub>2</sub> mixture working fluids, a component-level design study becomes justified. Owing to its relative infancy, research into CO<sub>2</sub> mixture turbines is limited. Although there is an existing body of literature on turbines operating with organic mixtures for organic Rankine cycles, they do not encounter the same technical challenges as those facing CO<sub>2</sub> turbines; namely aerodynamic and rotordynamic constraints imposed by a high-power density and high operating temperatures. Nonetheless, there have been many investigations into pure supercritical CO<sub>2</sub> turbines, of which only those pertaining to radial inflow turbines (RIT) are relevant to this paper.

The largest RIT thus far was investigated by El Samad et al. [18] who assessed the performance of a 100 MW utility scale RIT operating within an Allam cycle. Depending on the pressure ratio, the designed turbine may achieve total-to-static efficiencies of up to 86%, with lower pressure ratios improving efficiencies. A similar observation was made by Uusitalo et al. [19]. In that study, the turbine efficiency ranged between 80% to 87% for 0.1 MW and 3.5 MW capacity RIT. Moreover, passage and exit losses had the greatest adverse effect on turbine efficiency.

By mapping the design space of radial turbines of different power outputs (100 kW and 200 kW), Qi et al. [20] demonstrated how recommended parameter constraints limit an RIT design space. According to that paper, total-to-static efficiencies in the range of 72% to 82% were possible. However, those efficiencies were likely underestimated by at least 2% because the authors of that paper had doubled the passage losses based on an erroneous implementation of the passage loss model.

There have been some studies addressing aerodynamic losses in sCO<sub>2</sub> RITs. Zhou et al. [21] pointed out the vulnerability of sCO<sub>2</sub> RIT to tip clearance due to their relatively compact size. They demonstrated this by analysing a 1 MW RIT using computational fluid dynamics (CFD). An increase in the dimensionless tip clearance of 6% (from 2% to 8% of the leading edge height)

was shown to decrease efficiency by 3.84%. They also showed that the addition of a volute may reduce efficiency by 2%.

Lv et al. [22] analysed loss correlations using 1D generated designs and CFD simulation results. Based on their analysis, a specific set of nozzle and rotor loss models was recommended. An even more comprehensive rotor loss assessment study, including 30 different models (some of which with their own variations), was conducted by Persky and Sauret [23]. Both studies agree that the best choice of passage loss model is that developed by Wasserbauer and Glassman [24] at NASA; however, Persky and Sauret noted that the CETI model, presented by Moustapha et al. [25], is more accurate in estimating design-point efficiency. On the other hand, a study by Uusitalo and Grönman [19] concluded that the CETI model was a better option for modelling passage loss in sCO<sub>2</sub> turbines, specifically for specific speeds in the range of 0.4–0.65. Alternatively, Ventura et al. [26] used a combination of both approaches and averaged their results.

Thus far, many questions about the effect of doping CO<sub>2</sub> on the design of radial inflow turbines remain unanswered: will the shape and dimensions of the turbine change? Will certain mixtures produce better performing turbines? What will be the similarities and differences between the mixtures? Will differences remain if the turbines operate within similar boundary conditions? And, does the scale of the turbine effect mixtures to the same degree? In this paper, these questions are answered by analysing and comparing the design of radial inflow turbines for CO<sub>2</sub>, CO<sub>2</sub>/TiCl<sub>4</sub>, CO<sub>2</sub>/SO<sub>2</sub>, and CO<sub>2</sub>/C<sub>6</sub>F<sub>6</sub> working fluids. Firstly, RITs are designed for the four working fluids under three design scenarios at three power scales. Then, the contribution of losses in each case is reasoned and compared amongst the fluids; followed by a mathematical treatment of loss models to ascertain the effect of each of their parameters. The similarities and dissimilarities between the working fluids are then summarised based on the preceding analyses. Finally, practical rotational speed limitations are imposed to reveal its discrepant effect on the fluids. Ultimately, this study aims to better understand the consequences of doping CO<sub>2</sub> by explaining the root cause of the differences between radial inflow turbine designs for CO<sub>2</sub> mixtures.

## 2. METHODOLOGY

### 2.1 Cycle model

A simple recuperated transcritical cycle was chosen for the purpose of this study. A schematic of the cycle and its Temperature-Entropy (T-s) diagram are shown in Fig. 1. Turbine boundary conditions, including dopant fraction, are derived from an optimisation study conducted by the authors in a previous study [27]; the results of which are shown in Table 1.

TABLE 1: TURBINE BOUNDARY CONDITIONS

Variable	CO <sub>2</sub> /TiCl <sub>4</sub>	CO <sub>2</sub> /SO <sub>2</sub>	CO <sub>2</sub> /C <sub>6</sub> F <sub>6</sub>	CO <sub>2</sub>
Dopant [%]	17	26	17	0
$T_{in}$ [°C]	700	700	700	700
$P_{in}$ [MPa]	25	25	25	25
$P_{in,t}/P_{out,s}$	2.50	3.39	3.25	3.42

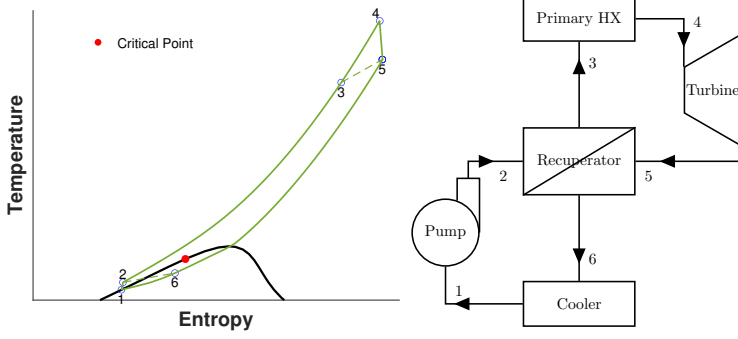


FIGURE 1:  $T$ - $s$  DIAGRAM AND SCHEMATIC OF A SIMPLE RECUPERATED  $\text{CO}_2$  CYCLE

## 2.2 Turbine model

Conventionally, radial inflow turbines are designed by assuming a set of geometric and kinematic parameters, the values of which are based on recommendations from the literature. At first, the rotor geometry and kinematics are defined, which in turn inform the nozzle and volute designs. Most literature follow one of the three most popular design methodologies introduced by: (1) Aungier [28]; (2) Moustapha et. al. [25]; and (3) Whitfield and Banies [29]. Lee and Gurgenci [30] compared the three against experimental data and studied their consequences on rotor design. All three methods yield turbine efficiencies within 2% of each other, with the latter method resulting in the lowest efficiency due to faster flow velocities.

In this study, the flow coefficient ( $\phi$ ), the loading coefficient ( $\psi$ ), and the meridional velocity ratio ( $\zeta$ ) are used to determine the velocity triangles, following the method suggested by Mustapha et al. [25]. They are defined as:

$$\phi = \frac{C_{5m}}{U_4} \quad (1)$$

$$\psi = \frac{\Delta h_0}{U_4^2} \quad (2)$$

$$\zeta = \frac{C_{5m}}{C_{4m}} \quad (3)$$

, where  $\Delta h_0 [J/kg]$  is the total-to-total enthalpy drop across the turbine, and the velocities  $U_4$ ,  $C_{4m}$  and  $C_{5m}$  are indicated in Fig.3. Additionally, the hub-to-shroud ( $r_{5h}/r_{5s}$ ) and the outlet-to-inlet ( $r_5/r_4$ ) radius ratios are used to control the turbine shape. In Fig. 2, key dimensions of the turbine rotor are shown, whereas the velocity triangles and labeling convention of the tangential and meridional directions are shown in Fig. 3.

The turbine design and performance evaluation process is initiated by specifying the turbine boundary conditions, design variables, and fixed parameters which are then used to generate the rotor geometry and flow kinematics. Subsequently, aerodynamic losses are computed using a set of loss models. Table 2 lists the loss mechanisms considered, along with an abbreviation of the correlations chosen to represent each of the losses, and a reference to the source where the complete forms of the correlations can be found.

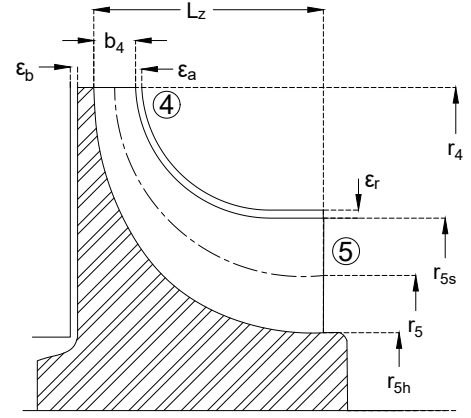


FIGURE 2: RADIAL INFLOW TURBINE MERIDIONAL GEOMETRY

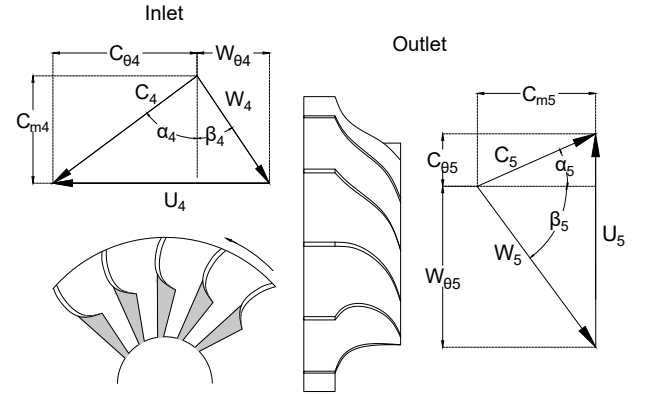


FIGURE 3: RADIAL INFLOW TURBINE VELOCITY DIAGRAMS

The nozzle loss was chosen because it relates the loss to geometry and flow parameters. The passage and clearance losses, which typically comprise more than 60% of the total loss, were chosen based on their accuracy in predicting design-point efficiency [23]. The same study recommends the incidence and trailing edge losses in Equations 9 and 12. The choice of windage loss is less consequential as it contribute little to the total loss in efficiency.

The total enthalpy loss in the turbine is equal to the arithmetic sum of individual aerodynamic losses:

$$\Delta h_{\text{loss}} = \Delta h_n + \overbrace{\Delta h_i + \Delta h_p + \Delta h_c + \Delta h_{te}}^{\Delta h_{\text{rotor}}} + \Delta h_e \quad (4)$$

Total-to-static and total-to-total efficiencies are calculated as:

$$\eta_{ts} = \frac{h_4 - h_5}{h_4 - h_{5s}} \quad (5)$$

$$\eta_{tt} = \frac{h_4 - h_5}{h_4 - h_{05s}} \quad (6)$$

Unlike other losses, the enthalpy drop due to windage is subtracted from the total enthalpy drop when calculating the power:

$$W = \dot{m}(\Delta h_{tt} - \Delta h_w) \quad (7)$$

Therefore, it is not considered as an internal loss in the rotor and does not contribute to the entropy generation between the rotor inlet and outlet.

### 2.3 Model verification and validation

The process of verification aims to confirm the sanctity of the 1D mean-line model by demonstrating that it generates results consistent with other 1D mean-line models. This may be achieved by simulating existing 1D turbine designs and comparing the results with the that of the source. Model verification is made complicated because it is uncommon to find existing works which use an identical mean-line design approach to the one used here. Alternatively, a sensible approach to verification is to tailor the mean-line model to match the assumptions of the existing models whilst maintaining core features intact.

Validation, on the other hand, proves the accuracy of the 1D model, not it's consistency. Validation is necessary because the loss equations used in the mean-line design model were originally created for air turbines. Therefore, it is imperative to confirm their accuracy in the design of non-air gas turbines before interpreting the results of the mean-line model. Ideally, the mean-line model results would be benchmarked against experimental data points. However, in the absence of experimental data, a numerical model, such as CFD, is commonly used in lieu of experiments. Fortunately, LV et. al. [22] validated their mean-line model with CFD simulations. Therefore, verification of the current 1D model against that study would validate it by corollary. To ensure a fair comparison, the 1D mean-line model was temporarily modified to neglect blade blockage at both the leading and trailing edges of the rotor, as was the case in the source study [22].

Two versions of the 1D model are compared in Table 4: one that neglects blade blockage in accordance with the source study; the other accounts for blockage. The former is a temporary modification to the model which is used exclusively for comparison, but is discarded otherwise.

With the regards to the modified model, although blockage is not accounted for, there are differences in most parameters, the greatest of which is in the leading edge height  $b_4$  with a deviation of -11% from the source. This is because the modified model produces a greater inlet radius  $r_4$ , which is a consequence of the greater tip speed  $U_4$ . The higher tip speeds are attributed to the overestimation of the inlet velocity  $C_4$ . Ultimately, all these differences originate from the enthalpy loss through the stator; the model estimates lower loss compared to Ref. [22].

The same may be inferred with respect to the current model which accounts for blade blockage, as listed in the last column of Table 4. However, the differences in the geometric parameters are greater because the passage is partly blocked by the blades, thus larger radii are required to maintain the same passage areas.

Overall, the discrepancies culminate in an efficiency difference of ~1%. A loss breakdown of the current turbine design and that as reported by Ref. [22] is shown in Fig. 4. The loss profiles are well aligned apart from small differences in the passage and

clearance losses, which are likely due to the deviations in velocities. The greatest difference is in the stator loss. This is expected because the source study uses a different stator loss model that only depends on the flow velocity and a loss coefficient, unlike the model used here in Eq. 8, which also accounts for the angle of the flow and the viscosity of the fluid.

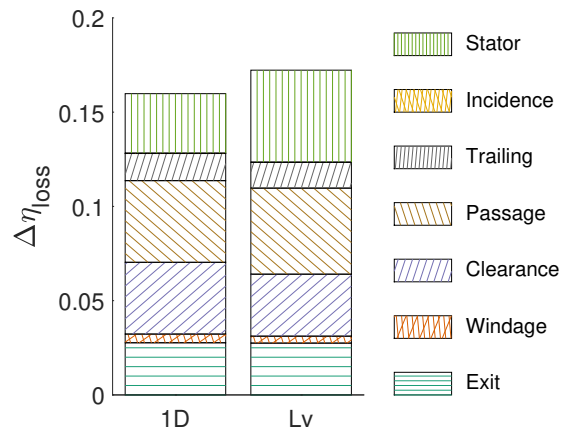


FIGURE 4: LOSS COMPARISON WITH REF [22]

The meanline model is further validated for all the working fluids using CFD for one of the design cases discussed in Section 3, namely the 1 MW turbine of Case-A with the rotational speed limit imposed. A comparison of key variables of the meanline and CFD simulations are listed in Table 3.

The 3D geometry of the rotor blade was built in ANSYS BladeGen using the blade inlet and outlet geometries generated by the mean-line model. The stator was designed according to the method detailed by [28], then built in SolidWorks and imported into ANSYS DesignModeler. The 3D rotor and stator blades and their passages were meshed using ANSYS TurboGrid. The mesh resolution was determined from mesh-dependence study for both the rotor and stator, the results of which are shown in Fig 5. The final mesh was composed of approximately 770 thousand nodes in the rotor, and 460 thousand nodes in the stator.

Simulations were then conducted using ANSYS CFX solver. The Reynolds-averaged Navier-Stokes (RANS) equations were closed with the  $k - \epsilon$  turbulence model. Boundary conditions were imposed as total conditions at the inlet and static pressure at the exit of the domain. Solution convergence was achieved if the root mean square residuals for mass, momentum, and turbulence

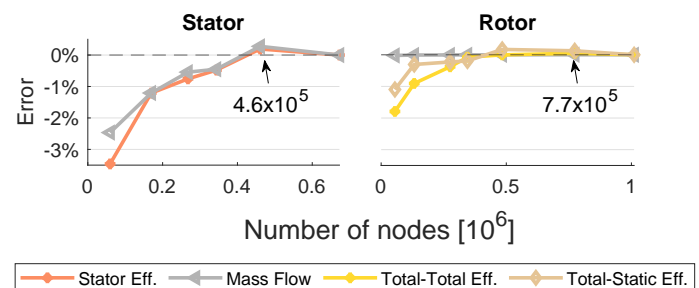


FIGURE 5: GRID INDEPENDENCE STUDY FOR ROTOR AND STATOR

TABLE 2: LOSS EQUATIONS USED IN THE 1D MEAN-LINE MODEL

Loss mechanism	Correlation	Eq.	Reference
Nozzle	$\Delta h_n = \frac{C_4^2}{2} \frac{0.05}{Re_N^{0.2}} \left( \frac{3 \tan \alpha_4}{s/c} + \frac{s \cos \alpha_4}{b_4} \right)$	(8)	[31]
Incidence	$\Delta h_i = \frac{W_4^2}{2} (\sin(\beta_4 - \beta_{4,opt}))^2$	(9)	[24]
Passage	$\Delta h_p = m_f \left[ \frac{L_h}{D_h} + 0.68 \left( 1 - \left( \frac{r_5}{r_4} \right)^2 \right) \frac{\cos \beta_5}{b_5/c} \right] \frac{W_4^2 + W_5^2}{2}$	(10)	[25]
Clearance	$\Delta h_c = \frac{Z_r U_4^3}{8\pi} (K_a \epsilon_a C_a + K_r \epsilon_r C_r + K_{ar} \sqrt{\epsilon_a \epsilon_r C_a C_r})$	(11)	[25]
Trailing edge	$\Delta h_{te} = \left( \frac{Z_t t_5}{\pi (r_{5s} + r_{5h}) \cos \beta_5} \right) \frac{W_5^2 Y_5}{2}$	(12)	[32]
Exit	$\Delta h_e = \frac{C_5^2}{2}$	(13)	
Windage	$\Delta h_w = 0.25 C_w \rho_4 \omega^2 r_4^5$	(14)	[33]

TABLE 3: MEAN-LINE MODEL VERIFICATION AGAINST CFD

Fluid	Variable	Model	CFD	dev[%]
CO <sub>2</sub> /TiCl <sub>4</sub>	$\eta_{tt}$ [%]	88.94	91.57	-2.63
	$\eta_{ts}$ [%]	87.02	86.88	0.14
	$\dot{m}$ [kg/s]	23.98	24.13	-0.63
	Power [MW]	10.003	10.086	-0.82
CO <sub>2</sub> /SO <sub>2</sub>	$\eta_{tt}$ [%]	88.91	90.79	-1.88
	$\eta_{ts}$ [%]	86.95	85.95	1.00
	$\dot{m}$ [kg/s]	17.14	17.40	-1.50
	Power [MW]	10.003	10.008	0.05
CO <sub>2</sub> /C <sub>6</sub> F <sub>6</sub>	$\eta_{tt}$ [%]	88.87	91.55	-2.68
	$\eta_{ts}$ [%]	87.12	85.66	0.16
	$\dot{m}$ [kg/s]	22.82	22.96	-0.62
	Power [MW]	10.007	10.006	-0.54
CO <sub>2</sub>	$\eta_{tt}$ [%]	88.23	91.44	-2.68
	$\eta_{ts}$ [%]	85.66	85.57	0.1
	$\dot{m}$ [kg/s]	15.32	15.65	-2.13
	Power [MW]	10.0	10.2	2.08

had reduced to at least  $10^{-5}$ . Thermodynamic and transport properties were supplied to the CFD solver by a lookup table created with properties calculated by Simulink Thermodynamics software package. The size of the lookup table was 200X200 and spans the range of  $7 < P < 30$  MPa and  $700 < T < 950K$ . The table resolution was determined based on a sensitivity study; the results of which indicated that increasing the resolution beyond 200 would have an insignificant effect on the efficiency or mass flow (less than 0.01%).

## 2.4 Turbine design optimisation

In the following study, radial inflow turbines are designed for four working fluids under three scenarios and three power capacities. In all instances, the turbines are assumed to operate under similar inlet conditions, namely total temperature and pressure; but, the static outlet pressure and mass flow rate depend on the scenario and the power capacity, respectively.

In cases B and C, a gradient-method optimisation algorithm is used with Eq. 5 as the objective function; hence the turbines are optimised to maximise the total-to-static efficiency. Moreover, a global optimum solution is ensured by initiating the optimiser ten times, each time from a randomly chosen initial point. The number of initiation points was determined by a sensitivity study through which the optimal solution remained unchanged above five initiation points; twice that number was used for the sake of certainty.

**2.4.1 Case-A: Fixed design and pressure ratio.** In the first instance, all design parameters are selected and fixed based on common recommendations in the literature, which are listed in Table 5. This exercise aims to study the effectiveness of the standard approach in choosing an efficient design for each of the working fluids. Moreover, the pressure ratio are also fixed according to the cycle conditions under which each working fluid is designed to operate, as listed in Table 1. Although these pressure ratios may not maximise turbine performance, they are the typical conditions under which the turbines are expected to operate.

**2.4.2 Case-B: Optimised design at fixed pressure ratio.** Next, the pressure ratios are maintained according to the cycle, but the input design parameters are optimised within the constraints shown in Table 5. The range of each of these parameters that yields good turbine performance is well-established in the literature and will be used to confine the turbine design space. This iteration represents a thorougher design approach than Case-A because more effort is required to find the optimal design rather than relying on a one-size-fits all approach.

TABLE 4: MEAN-LINE MODEL VERIFICATION AGAINST REF [22]

Input	[22]	Model <sub>no blockage</sub>	Model		
$\dot{m}$ [kg/s]	1.80	1.80	1.80		
$T_{04}$ [K]	943	943	943		
$p_{04}$ [bar]	106.9	106.9	106.9		
$p_6$ [bar]	77.7	77.7	77.7		
$N$ [krPM]	80.0	80.0	80.0		
$Z_r$	14.0	14.0	14.0		
$Z_n$	21.0	21.0	21.0		
$\epsilon$ [mm]	0.30	0.30	0.30		
$t_4$ [mm]	0	0	<b>1.24</b>		
$t_{5s}$ [mm]	0	0	<b>0.31</b>		
$t_{5h}$ [mm]	0	0	<b>0.62</b>		
$\phi$	0.88	0.88	0.88		
$\psi$	0.28	0.28	0.28		
$\xi$	1.14	1.14	1.14		
$r_5/r_4$	0.48	0.48	0.48		
$r_{5h}/r_{5s}$	0.50	0.50	0.50		
$\alpha_4$ [°]	76.5	76.5	76.5		
Results			dev[%]	dev[%]	
$r_4$ [mm]	27.3	27.8	2	31.0	14
$r_{5s}$ [mm]	17.5	16.9	-3	18.9	8
$r_{5h}$ [mm]	8.69	8.38	-4	9.36	8
$b_4$ [mm]	4.48	3.99	-11	3.93	-12
$\beta_4$ [°]	28.5	-29.6	4	-29.6	4
$\beta_{5,rms}$ [°]	58.7	-63.4	8	-63.4	8
$U_4$ [m/s]	228	233	2	232	2
$C_4$ [m/s]	208	211	1	210	1
$W_4$ [m/s]	55.6	56.5	2	56.5	2
$C_6$ [m/s]	55.3	56.0	1	55.9	1
$W_6$ [m/s]	123	125	2	125	2
$\eta_{ts}$ [%]	<b>83.1</b>	<b>84.2</b>	<b>1.1</b>	<b>84.0</b>	<b>0.9</b>
$\eta_{tt}$ [%]	<b>85.4</b>	<b>86.6</b>	<b>1.2</b>	<b>86.4</b>	<b>1</b>

**2.4.3 Case-C: Optimised design and pressure ratio.** Finally, the pressure ratios are optimised along with the input parameters of Case-B. The change in pressure ratio is balanced by a change in mass flow rate to maintain a prescribed power output. This scenario decouples the turbine pressure ratio from that of the cycle pressure ratio. This exercise aims to determine whether the turbines will converge on a common pressure ratio, whether the differences between the fluids are caused by the turbine boundary conditions rather than intrinsic differences between the fluids themselves, and it will also indicate the potential benefit of multi-staging in each of the working fluids.

**2.4.4 Power scaling.** Large scale designs may suppress the differences among the working fluids. Therefore, the three aforementioned cases are simulated for turbines with power outputs

TABLE 5: TURBINE OPTIMISATION PARAMETERS

Variable	Type	Case-A	Cases B & C	Ref
$\phi$	Variable	0.23	0.2 - 0.3	[25]
$\psi$	Variable	0.93	0.85 - 1.0	[25]
$\xi$	Variable	1.0	1.0 - 1.5	[34]
$r_5/r_4$	Variable	0.5	0.3 - 0.7	[31, 35]
$r_{5h}/r_{5sh}$	Variable	0.45	0.4 - 0.7	[35]
$\alpha_4$ [°]	Constraint		68 - 76	[36]
$\beta_4$ [°]	Constraint		-20 - -40	[25]
$r_{5sh}/r_4$	Constraint		< 0.7	[31]
$\alpha_5$ [°]	Input	0	0	[25]
$\epsilon_{a,r}$ [mm]	Input	0.4	0.4	[31]
$L_z/b_5$	Input	1.50	1.50	[28]
$t_4/r_4$	Input	0.04	0.04	[34]
$t_{5h}/r_4$	Input	0.02	0.02	[34]
$t_{5sh}/r_4$	Input	0.01	0.01	[34]

of 0.1 MW, 1 MW, and 10 MW. Ultimately, power scaling will reveal whether certain mixtures have an inherent advantage at smaller scales.

### 3. RESULTS AND DISCUSSION

This section explores turbine designs for pure and mixed CO<sub>2</sub> working fluids under the three design approaches across power scales. Firstly, the performance of all the cases are discussed in terms of total-to-static efficiency. Secondly, the loss break-down of Case-B against Case-C is presented to explain the observed trends. Next, particular interest is given to clearance loss owing to its importance at smaller scales. Lastly, similarities and dissimilarities between the fluids are highlighted.

#### 3.1 Performance trends

The following discussion refers to the total-to-static efficiencies presented in Fig. 6.

**3.1.1 Power Scaling.** Regardless of the working fluid, the gain in efficiency from 0.1 MW to 1 MW is always greater than the gain from 1 MW to 10 MW. Apart from a few cases, the former is more than double the latter. Among the fluids, the increase in efficiency with power scaling is greatest for CO<sub>2</sub>, regardless of the design approach (Case A, B, or C). At its greatest, the gain in efficiency is 12% between 0.1 MW and 10 MW for Case-A of CO<sub>2</sub>. The smallest gains are ~5.4% between 0.1 MW and 10 MW for Case-C of CO<sub>2</sub>/TiCl<sub>4</sub> and CO<sub>2</sub>/C<sub>6</sub>F<sub>6</sub>.

The power a turbine generates scales with the radius squared, but the leakage flow scales linearly with the radius [37]. Therefore, avoiding leakage losses is easier in large turbines, but will be difficult in small-scale turbines. Ultimately, the clearance gap to blade height ratio is the best indicator of the loss in efficiency due to leakage.

The consequence of the clearance to blade height ratio is best understood through Fig. 7, in which designs according to Case-A are presented. Case-A was chosen because the discrepancies

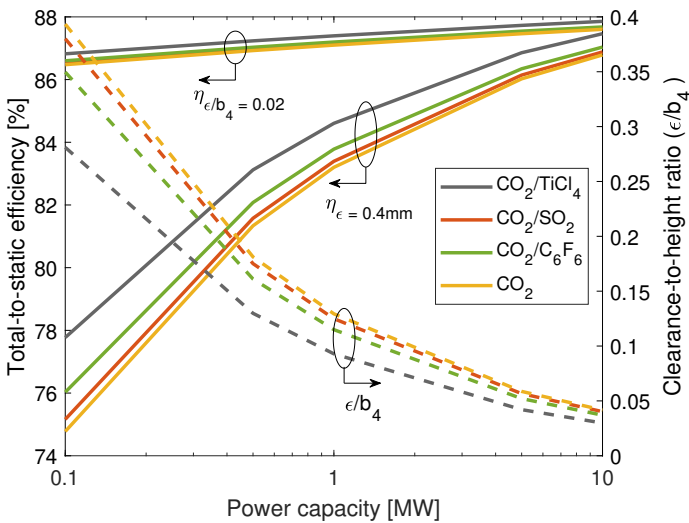
	$\text{CO}_2/\text{TiCl}_4$			$\text{CO}_2/\text{SO}_2$		
10 MW	87.5	87.8	88.4	86.9	87.3	88.3
1 MW	84.6	85.4	86.7	83.4	84.2	86.6
0.1 MW	77.8	80	83	75.2	77.4	82.6
	A	B	C	A	B	C

	$\text{CO}_2/\text{C}_6\text{F}_6$			$\text{CO}_2$		
10 MW	87	87.5	88.3	86.8	87.2	88.3
1 MW	83.8	84.6	86.9	83.2	84	86.4
0.1 MW	76	78.1	82.9	74.8	75.5	82.2
	A	B	C	A	B	C

**FIGURE 6: TOTAL-TO-STATIC EFFICIENCY OF THE THREE CASES AT DIFFERENT POWER CAPACITIES**

between the fluids are most pronounced, whereas the differences are lessened by the optimisation in Cases-B and C. There is a direct but inverse correlation between the total-to-static efficiency and the clearance-to-height ratio; the greater the ratio, the lower the efficiency. Because  $\text{CO}_2/\text{TiCl}_4$  can maintain the lowest  $\epsilon/b_4$  across scales, it has the highest turbine efficiency amongst the fluids, which is confirmed by Fig. 6. Conversely,  $\text{CO}_2$  has the greatest ( $\epsilon/b_4$ ), thus the lowest efficiency.



**FIGURE 7: LEFT AXIS: CHANGE IN EFFICIENCY ACROSS POWER SCALES AT CONSTANT  $\epsilon = 0.4\text{mm}$ , AND AT CONSTANT CLEARANCE-TO-HEIGHT RATIO  $\epsilon/b_4 = 0.02$ . RIGHT AXIS: THE CHANGE IN  $\epsilon/b_4$  WHEN  $\epsilon = 0.4\text{mm}$**

Although the trends in efficiency and  $\epsilon/b_4$  are observably correlated, they do not necessarily prove causation. However, causation is demonstrated in the same figure by the parallel lines of efficiency at the top of the figure. These lines were produced

by running similar scenarios as in Case-A; but with a constant clearance to blade height ratio  $\epsilon/b_4 = 0.02$ . This assumption is for illustrative purposes and may not be feasible as the clearance gap may be as low as  $22\ \mu\text{m}$  in 0.1 MW turbines. Although narrower gaps have been cited in the literature [20], their feasibility was not physically demonstrated.

This hypothetical example demonstrates that if  $\epsilon/b_4$  is assumed constant, the change in efficiency across scales becomes uniform for all fluids, thus negating the positive effect wider blade heights have on efficiency. It also indicates the potentially significant gain in efficiency if shrouded rotors are used, especially at small scale. Of course, the use of shrouds will be accompanied by greater windage loss; nonetheless, the potential gains due to the reduction in clearance loss will likely outweigh the penalties of windage loss. The factors limiting the use of closed rotors are likely to be mechanical. Firstly, the structural limits placed on the blade tip speeds are more stringent when closed shrouds are used. Generally, tip speeds should be lower with closed rotors. Moreover, the manufacturability of the closed rotor passages at such small scales is a key hindrance, as well as the increased mass and the effect this might have on rotordynamics - particularly at the smaller scales.

The larger blade heights in  $\text{CO}_2/\text{TiCl}_4$  turbines is a consequence of the lower specific work of the turbine, which causes higher mass flow rates to maintain the same power output. Evidently, this is due to the difference in the inlet density of the fluid and, to a lesser degree, its adiabatic coefficient, as explained in an earlier publication [38]. Although the difference in the blade heights is exacerbated by the difference in the pressure ratio between the working fluids, it is not eliminated even if a uniform pressure ratio is applied to all fluids, as is discussed in the following section.

**3.1.2 Design scenarios.** The merits of design optimisation are evident in all fluids and for all power capacities. As stated earlier, Case-A assumes both fixed design parameters and pressure ratios, whereas Case-B optimises the design variables but maintains the same pressure ratios. Therefore, any differences between the two approaches will be a result of the change in turbine design parameters. Overall, Case-B improves the performance of all turbines, indicating that optimisation converges on design parameters that are more suitable than those assumed in Case-A.

A greater gain in the efficiency of Case-B indicates a greater inadequacy of the assumptions of Case-A. This is most apparent at small scales where the differences between the two cases are the greatest. Therefore, small turbines require a different set of design parameters than those assumed in Case-A. For example, the smallest gain in design parameter optimisation is 0.3% for 10 MW  $\text{CO}_2/\text{TiCl}_4$ , and the greatest is 2.2% for 0.1 MW  $\text{CO}_2/\text{SO}_2$ . For all fluids, as the turbines are scaled up towards 10 MW, the differences between Case-A and Case-B decrease, thus indicating that the assumption of Case-A are better suited to 10 MW turbines.

The turbine is decoupled from cycle conditions in Case-C by optimising the static pressure at the outlet, thus the turbine pressure ratio is optimised. Case-C also optimises design parameters. Therefore, performances differences between Case-C and

Case-B are derived from pressure ratio optimisation even if the design parameters are different.

For all working fluids, the optimisation algorithm converges on the minimum limit of the pressure ratio (1.5) by maximising the outlet pressure. This is an expected outcome because lower pressure ratios induce lower flow velocities and, consequently, lower aerodynamic losses; which is true across power capacities. Here, as in Case-B, small turbines benefit the most from pressure ratio optimisation. The greatest increase in efficiency for Case-C compared to Case-B is 6.7% with 0.1 MW CO<sub>2</sub> turbine, and the smallest increase is 0.6% with 10 MW CO<sub>2</sub>.

Among the fluids, the smallest gain in pressure ratio optimisation is for CO<sub>2</sub>/TiCl<sub>4</sub>. This is because the pressure ratio set by cycle conditions, as used for Cases A & B, is lower than those of the other fluids, as listed in Table 1. Therefore, the change in the pressure ratio for CO<sub>2</sub>/TiCl<sub>4</sub> is 1.0 compared to 1.75, 1.89, and 1.92 for CO<sub>2</sub>/SO<sub>2</sub>, CO<sub>2</sub>/C<sub>6</sub>F<sub>6</sub>, and CO<sub>2</sub>, respectively. This suggests that CO<sub>2</sub>/TiCl<sub>4</sub> will benefit less from multi-staging compared to the other fluids when operating within pressure ratios dictated by their respective cycles.

Generally, the benefits of scaling is greatest for Case-A, followed by Case-B and the Case-C, regardless of the working fluid. Therefore, the differences in the efficiencies of the cases for a given power capacity decreases at higher power scales. For example, the efficiency of Case-C is 7.4% higher than that of Case-A for 0.1 MW CO<sub>2</sub>/SO<sub>2</sub>, but this difference shrinks to 1.4% at a scale of 10 MW. A similar trend is observed in all fluids, but to varying degrees. The cause of the dissimilar trends in performance across power scales is the drastic change in the height of the clearance gap at the blade with respect to the height of the blade, as was explained through Fig. 7.

An apt comparison of fluids, cases, and power scales may be made through a classical specific speed and efficiency chart. In Fig 8, all turbines discussed thus far are plotted with respect to the curve produced by Balje [39]. The benefits of optimisation are evident in Case-B and Case-C where the efficiency is higher than Case-A, especially in 0.1 MW turbines. Moreover, the higher flow coefficients result in higher specific speeds in Cases-B and C. Overall, designs fall in the range of  $0.3 < N_s < 0.5$ .

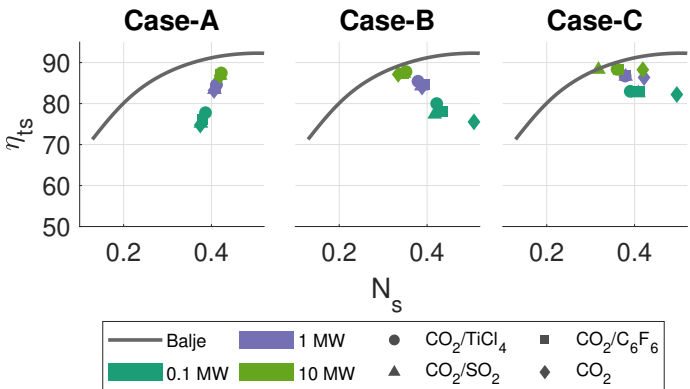


FIGURE 8: SPECIFIC SPEED AND EFFICIENCY COMPARISON

### 3.2 Loss Analysis

The loss profiles of the optimal RIT designs according to Case-B are presented in Fig 9. Overall, the contributions of losses are similar for all fluids, with the rotor passage loss having the greatest weight in 10 MW turbines, clearance and passage equally contributing to losses in 1 MW turbines, and clearance as the predominate loss in 0.1 MW turbines. Among all losses, however, the clearance loss is the most salient variance across power scales. In the proceeding analysis, the similarities across the working fluids are explained, followed by a discussion on the variance across power scales.

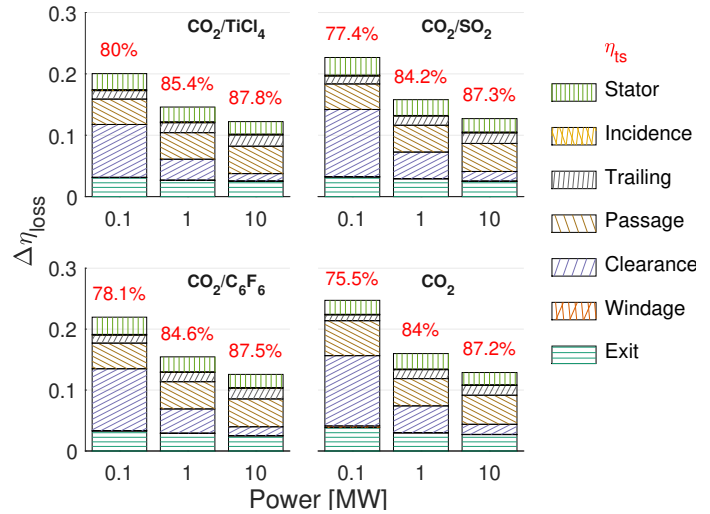


FIGURE 9: LOSS CONTRIBUTIONS FOR CASE-B

Stator and exit losses mainly depend on the absolute inlet and outlet velocities, respectively. Therefore, the stator and exit losses are almost uniform among the fluids at the same power scale owing to the similar velocity diagrams at inlet and outlet, an example of which is shown in Fig. 10. The sizes of the triangles scale with the specific work of the turbine, but the shapes are determined by  $\psi$ ,  $\phi$  and  $\zeta$ . Although stator loss is also dependent on the kinematic viscosity of the working fluid, as seen in Eq. 8, it will be shown in Section 3.3 that this dependency is weak.

Across power scales, however, there is an increase in the stator loss and a more notable increase in the exit loss. Velocity diagrams may also be used to explain these increases. An example is shown in Fig 13 for CO<sub>2</sub>/SO<sub>2</sub>, in which the outlet velocity is greater in small turbines, which is driven by the increase in the flow coefficient ( $\phi$ ). This trend is observed in all working fluids and is the response of the optimisation algorithm to the increasing clearance. According to the clearance loss model in Eq. 11, losses will decrease with increasing meridional velocities  $C_{4m}$  and  $C_{5m}$ . Therefore, as the significance of clearance loss amplifies at smaller scales, optimisation favors designs that have higher flow coefficients. This is an attempt to abate the increase in clearance loss because of its increasing importance at small scale; which is not prevalent in larger turbines where the increase in the passage loss due to higher flow velocities outweighs the decrease in clearance loss, thus lower flow coefficients are preferred. Moreover, the inlet radius reduces in order to reduce the clearance/blade height, which would further increase the rotational speed at small

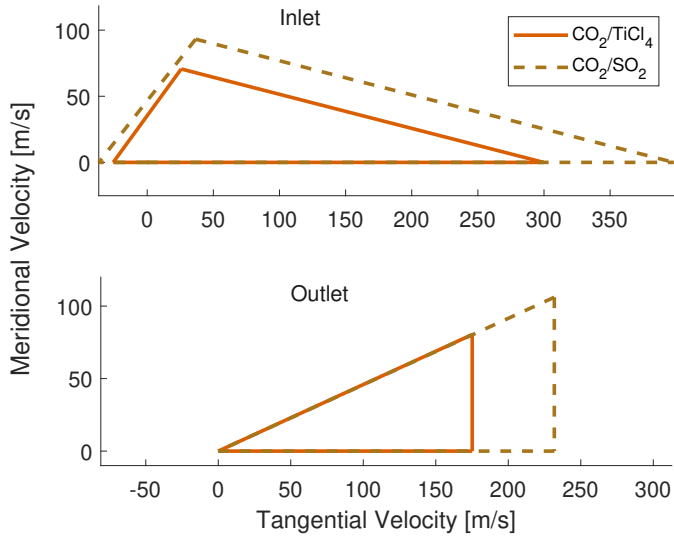


FIGURE 10: VELOCITY TRIANGLES FOR 0.1 MW  $\text{CO}_2/\text{TiCl}_4$  AND  $\text{CO}_2/\text{SO}_2$  TURBINES FROM CASE-B

scale; this is evident in the increase in the blade width to radius ratio ( $b_4/r_4$ ) shown in Table 7.

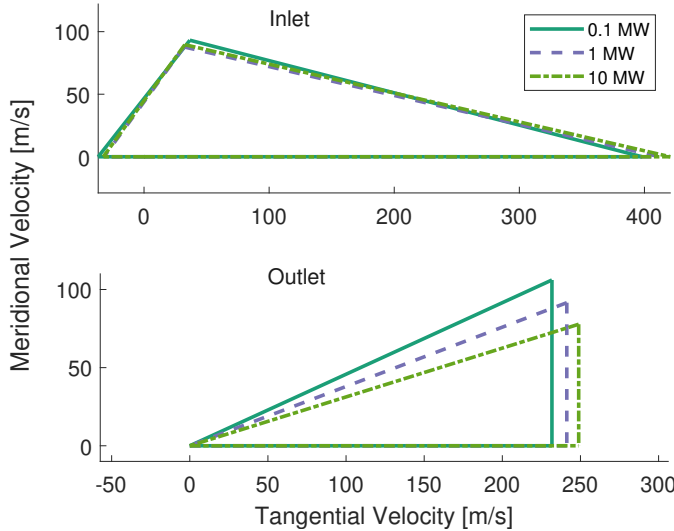


FIGURE 11: VELOCITY TRIANGLES ACROSS POWER SCALES FOR  $\text{CO}_2/\text{SO}_2$  FROM CASE-B

Like the exit loss, the trailing edge loss is also influenced by the velocity triangle at the outlet, namely by  $w_5$  and  $\beta_5$ , and to a lesser degree, by the outlet blade dimensions and the blade count. Therefore, the similar outlet velocity triangles and proximate blade counts render the trailing edge loss contributions comparable for all fluids at the same power scale. Unlike clearance loss, the trailing edge loss is less important in small turbines compared to large turbines owing to the decrease in the relative velocity at outlet  $w_5$  and the decrease in the blade count in some fluids like  $\text{CO}_2/\text{TiCl}_4$  and  $\text{CO}_2$ . Both incidence and windage

losses are negligible for all fluids. The former is suppressed by the constraint of  $-40 < \beta_4 < -20$  imposed on the optimisation, which maintains favourable flow angles into the rotor and keeps the loading coefficient  $\psi$  close to 0.9.

Instead of presenting an additional loss profile chart for Case-C, Fig. 12 shows the difference in each loss contribution with respect to the baseline Case-B. Compared to Case-B, both passage and clearance losses are lower in Case-C for all turbines across all power scales, while trailing edge losses are higher. This is because the lower pressure ratios of Case-C compared to Case-B require turbines that are less loaded. According to Euler's equation, the specific work of a turbine with zero exit swirl ( $\alpha_5 = 0$ ) is defined as:

$$w = U_4 C_{4\theta} \quad (15)$$

Therefore, to decrease the specific work ('unload' the turbine), the blade tip speed and or the inlet tangential velocity must be decreased. In Case-C, both  $U_4$  and  $C_{4\theta}$  reduce in concert to maintain a favorable absolute inlet flow angle within the limits of Table 5.

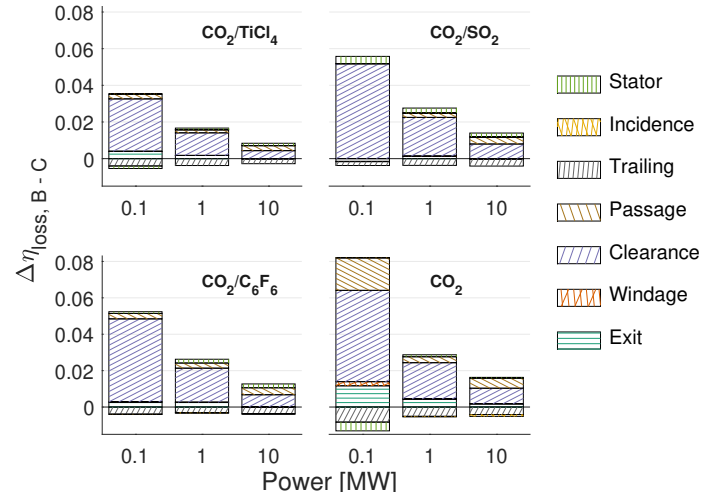


FIGURE 12: DIFFERENCE IN LOSS CONTRIBUTIONS BETWEEN CASE-B AND CASE-C

Concurrently, to maintain the prescribed power capacity at a lower specific work, the mass flow rate must increase. With slower flows and greater flow rates, the passage areas must enlarge, leading to wider blades. Ultimately, the wider blades lower clearance losses by decreasing the clearance gap to blade height ratio  $\epsilon/b_4$  in both the axial and radial direction at the inducer and exducer, respectively. Moreover, slower internal flows in the rotor decrease friction and its associated passage loss. On the other hand, the wider blades at the outlet induce higher trailing edge losses, as observed for all turbines.

### 3.3 Loss model sensitivity

The purpose of the following analysis is to examine and explain the sensitivity of the loss models to changes in the geometric and kinematic features of the RIT, and in the viscosity of the fluid. The ranges of the input variables are set based on the expected turbine design space, and are shown in Table 6, in which the limits of some parameters are set as a fraction of the base value,

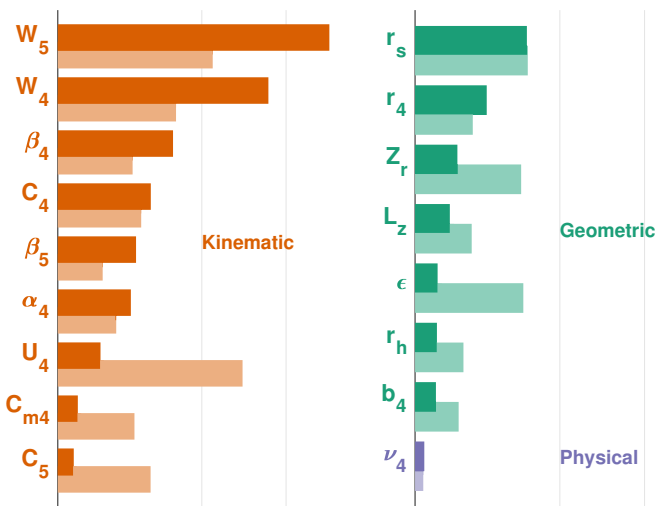
while the limits for others are set in absolute value. The base values are taken from 0.1 MW and 10 MW CO<sub>2</sub> turbines from Case-B as examples. Moreover, the exit loss is not considered in the analysis because of its direct and quadratic correlation with  $C_5$ , which will cause  $C_5$  to overwhelm all other parameters in Fig 13.

This analysis is purely mathematical and assumes that all terms are mutually exclusive, and thus can be changed independently of each other; which is not physically possible. However, loss models are ultimately mathematical formulas and will be treated as such for the purposes of this analysis. By understanding the effect each term has on turbine losses the optimal turbine designs presented in the preceding sections may be justified.

**TABLE 6: RANGE OF PARAMETERS FOR LOSS SENSITIVITY STUDY**

	Lower	Upper		Lower	Upper	Unit
Fractional limits			Absolute limits			
$b_4$	0.75	1.25	$W_4$	50	250	[m/s]
$r_{5s}$	0.75	1.25	$W_5$	50	250	[m/s]
$r_{5h}$	0.75	1.25	$C_4$	150	450	[m/s]
$r_4$	0.75	1.25	$C_{4m}$	50	250	[m/s]
$L_z$	0.75	1.25	$C_5$	50	150	[m/s]
$\epsilon$	0.5	1.5	$Z_r$	12	32	
$\nu_4$	0.5	1.5	$\alpha_4$	40	80	[°]
			$\beta_4$	-40	40	[°]
			$\beta_5$	-85	-45	[°]

In Fig. 13, the qualitative significance of a parameter is indicated by the length of its bars, the color of the bar indicates the nature of the parameter (kinematic, geometric, or physical), and the contrast of the color indicates the power scale: dark for 10 MW; light for 0.1 MW.



**FIGURE 13: LOSS SENSITIVITY: THE LENGTH OF THE BARS INDICATES THE QUALITATIVE EFFECT A PARAMETER HAS ON THE TOTAL LOSS. DARK BARS ARE FOR 10 MW; LIGHT FOR 0.1 MW**

A perceptible feature of Fig. 13 is the uneven influence of parameters, which is dependent on the significance of the losses to which it contributes. For example, the most influential parameters at the 10 MW scale are those which affect passage loss because, as seen earlier in Fig. 9, the passage loss is predominant in large turbines. Among the kinematic parameters, the relative flow velocities  $w_4$  and  $w_5$  have the greatest effect. The relative outlet velocity  $w_5$  is more significant because, in addition to passage loss, it affects the trailing edge loss as well. On the other hand, small-scale turbines are penalised more by clearance loss. Therefore, the efficiency is expected to become increasingly sensitive to parameters that contribute to clearance loss as the turbine is scaled down to 0.1 MW. This is confirmed by Fig. 13, in which the significance of terms that appear in Eq.11, such as  $\epsilon$ ,  $U_4$ , and,  $Z_r$ , is amplified in the 0.1 MW turbine. Overall, geometric parameters become more important in 0.1 MW turbines, as observed in the general trend in right side plot of Fig. 13.

The effect of the physical properties of the fluid, represented by the kinematic viscosity, is the smallest at both scales. Therefore, the differences in the viscosity of the fluids has little sway on turbine performance; in other words, the loss models are fluid-agnostic. It must be emphasised that this conclusion is strictly based on the mathematical nature of the loss models used here, and may not accurately represent the effect that each of these parameters has on the physical flow in the rotor. Indeed, Keep and Jahn [40] conducted a numerical loss investigation of a 300 kW low-specific speed RIT operating with CO<sub>2</sub> and concluded that endwall viscous losses in the stator are more significant than predicted using gas turbine derived preliminary design methods. Moreover, viscous stresses are stronger at low Reynolds number. Accordingly, losses are likely to have increased sensitivity to the viscosity of the fluid at low Reynolds number, which is not the case here as  $Re \gg 10^6$ . However, the trends shown in Fig. 13 justify the convergence of the 1D model on a similar turbine design regardless of the fluid. Ultimately, it's the flow and shape characteristics of a turbine that determine its performance, not the characteristics of the working fluid.

### 3.4 Similarities and dissimilarities

The designs of the turbines from Case-B are compared in Table 7 and Fig. 15. For a given power capacity, the turbines have similar shapes, which may be attributed to the consistency in the design parameters ( $N_s$ ,  $\phi$ ,  $\psi$ ,  $\xi$ ,  $r_5/r_4$ ,  $r_{5h}/r_{5s}$ ,  $L_z/b_5$ ). Therefore, a consistent rotor shape optimises aerodynamic performance regardless of the working fluid. There are a few likely reasons for this. First, all working fluids behave very close to ideal gases throughout the expansion process; they have compressibility factors close to unity. This is confirmed in Fig. 14 where the expansion process with respect to compressibility contours on reduced pressure-temperature axes are depicted. All the working fluids studied here have compressibility values in the range of 0.97 to 1.04 throughout the expansion process. The process shown in Fig. 14 is for 10 MW Case-B turbines; however, the compressibility factors are within the same range in all cases at all power-scales.

Second, the loss models presented in Table 4 mainly depend on kinematic and geometric features of the turbine, which are

TABLE 7: DESIGN DATA FOR OPTIMAL CASE-B RIT

Parameter	0.1 MW				10 MW			
	CO <sub>2</sub> /TiCl <sub>4</sub>	CO <sub>2</sub> /SO <sub>2</sub>	CO <sub>2</sub> /C <sub>6</sub> F <sub>6</sub>	CO <sub>2</sub>	CO <sub>2</sub> /TiCl <sub>4</sub>	CO <sub>2</sub> /SO <sub>2</sub>	CO <sub>2</sub> /C <sub>6</sub> F <sub>6</sub>	CO <sub>2</sub>
$\psi$	0.9	0.91	0.91	0.88	0.92	0.92	0.92	0.86
$\phi$	0.26	0.27	0.28	0.3	0.23	0.23	0.23	0.23
$\xi$	1	1.17	1.18	1	1	1	1	1.04
$r_5/r_4$	0.6	0.58	0.58	0.47	0.6	0.6	0.6	0.59
$r_h/r_s$	0.69	0.62	0.62	0.32	0.67	0.68	0.68	0.67
$N_s$	0.4	0.42	0.43	0.49	0.39	0.38	0.38	0.41
$b_4/r_4$ [%]	8.0	9.1	9.2	9.0	8.1	6.8	6.7	6.9
$\eta_{tt}$ [%]	80	77.4	78.1	75.5	87.8	87.3	87.5	87.2
$\eta_{ts}$ [%]	82.6	79.9	80.7	78.6	90.1	89.5	89.7	89.6
$p_{06}/p_5$	2.5	3.39	3.25	3.42	2.5	3.39	3.25	3.42
$\Delta h_{tt}$ [kJ/kg]	103	186	138	212	103	186	138	212
$N$ [kRPM]	192.7	314.1	252.7	396.3	20	30.6	24.2	35.8
$\alpha_4$ [°]	73.7	75.6	75.6	71.2	76	76	76	75.6
$\beta_4$ [°]	-20	-20.3	-20.8	-22.6	-20	-20	-20	-31.3
$\beta_5$ [°]	-66.2	-64.8	-64.6	-57.6	-69	-69.1	-69.1	-68.8
$U$ [m/s]	302	397	344	427	314	421	363	462

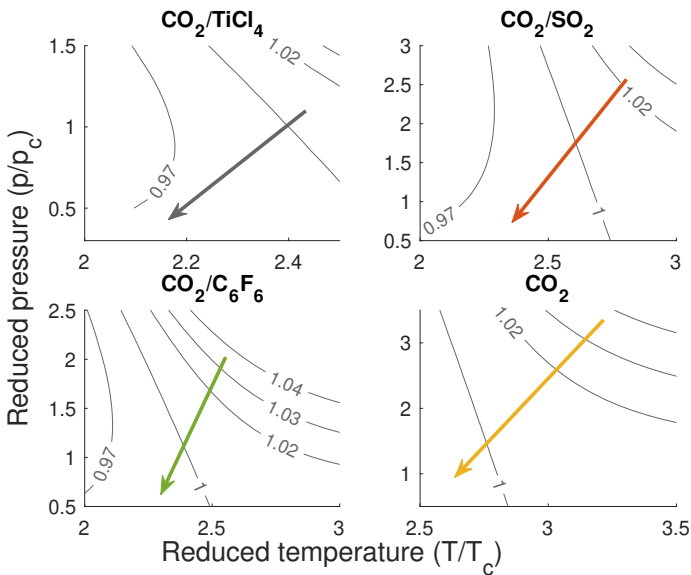


FIGURE 14: EXPANSION PROCESS WITH RESPECT TO COMPRESSIBILITY CONTOURS FOR 10 MW CASE-B

set by the aforementioned design parameters, and not on the thermophysical properties of the fluid, as explained in Section 3.3.

Based on the analysis presented thus far, the differences in turbine performance are attributed to two main aspects: pressure ratio and clearance-to-height ratio. Fluids which operate in cycles with lower pressure ratios are able to achieve higher turbine efficiencies. Moreover, fluids that have turbines with shorter blades are penalised more by clearance loss. However, as seen in Fig. 13, kinematic viscosity may contribute to the performance

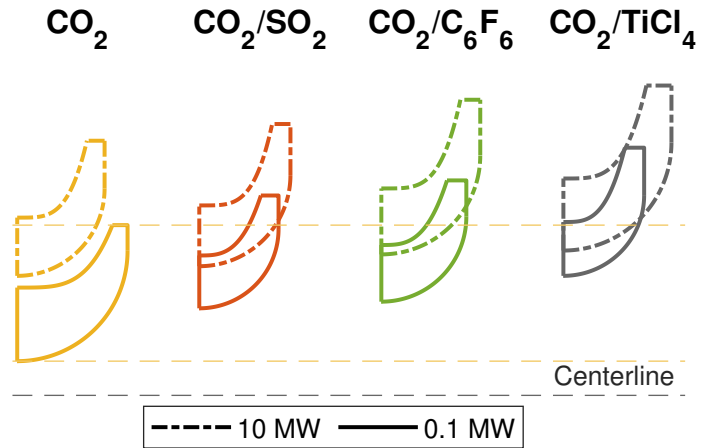


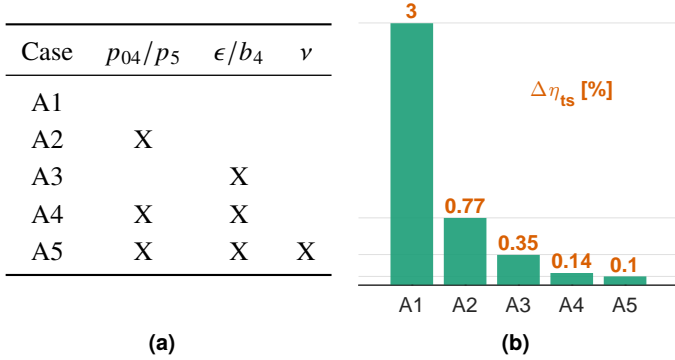
FIGURE 15: ROTOR MERIDIONAL PROFILE. DIMENSIONS OF 10 MW TURBINES HAVE BEEN SCALED DOWN

differences of the turbines, although slightly.

In the following analysis, Case-A designs of 0.1 MW CO<sub>2</sub>/TiCl<sub>4</sub> and CO<sub>2</sub> turbines are revisited to understand the dissimilarities between the fluids by quantifying the influence of pressure ratio, clearance-to-height ratio, and kinematic viscosity. Five sub-cases are devised with a combination of fixed parameters as marked in Fig. 16a. To eliminate the effect of viscosity, a fixed viscosity of 4mm<sup>2</sup>/s was assumed for both fluids in Case-A5.

According to the results in Fig. 16b, the clearance-to-height ratio is the biggest contributor to the difference in performance, followed by the pressure ratio; however, the clearance-to-height ratio will likely be less important in larger turbines. On the other hand, a common viscosity reduces the difference by a mere

0.4%. If pressure ratio, clearance-to-height, and viscosity are all assumed equal, then the difference between the efficiency of the two fluids will be 0.1%, namely due to windage loss differences. A similar analysis at the 10 MW scale yields a difference of 0.05%. Therefore, the uneven performance metrics of the fluids stem from the pressure ratio imposed by the cycle, and by the minimum allowable clearance gap; otherwise, there is no intrinsic aerodynamic advantage of any single mixture over the others.



**FIGURE 16: (A) PARAMETERS ASSUMED FIXED IN EACH SUB-CASE. (B) DIFFERENCE IN EFFICIENCY BETWEEN  $\text{CO}_2/\text{TiCl}_4$  AND  $\text{CO}_2$  0.1 MW TURBINES FOR EACH SUB-CASE**

Doping  $\text{CO}_2$  will produce working fluids that are inherently different, despite their ideal gas behaviour in the vicinity of the turbine. Although the thermophysical differences do not manifest in different aerodynamic designs, they affect extensive features of the turbine such as size, thrust, torque, and rotational speed.

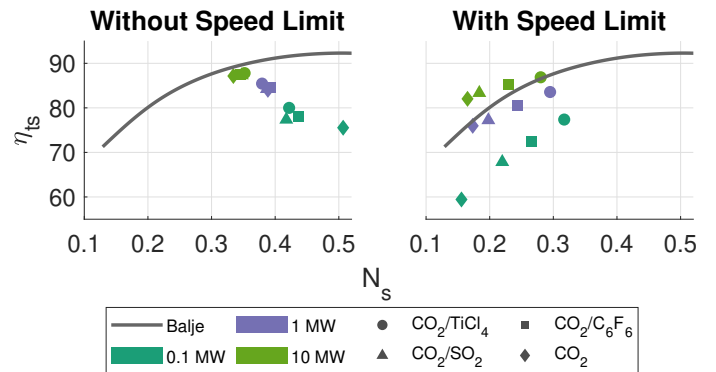
For a given power capacity and pressure ratio, the level of specific work possible depends on the fluid. Therefore, the mass flow required by the fluids will differ; and so will the size of their respective turbines. Additionally, doping  $\text{CO}_2$  changes its density. In the case of the dopants studied here, which were selected to increase the critical temperature, the resulting mixtures have densities that are higher than pure  $\text{CO}_2$ .

What has been shown thus far is that optimisation produces similar turbine designs, in terms of the shape of the rotor and the shape of the velocity diagrams; but the sizes of the turbines will be different, and so will the sizes of their velocity diagrams. For example, owing to its high specific work  $\text{CO}_2/\text{SO}_2$  turbines have considerably higher tip speeds than the other two mixtures. Likewise, pure  $\text{CO}_2$  turbines may have double the rotational speed of  $\text{CO}_2/\text{TiCl}_4$  turbines. Although the consequences on aerodynamic performance is minute, increased rotational speeds entail more demanding bearing selection requirements. Moreover, axial thrust is expected to be greater in turbines with heavier working fluids such as  $\text{CO}_2/\text{TiCl}_4$  or  $\text{CO}_2/\text{C}_6\text{F}_6$ , which may alter the thrust balancing requirements depending on the dopant.

Although this study is focused on the aerodynamic characteristics of radial inflow turbines for  $\text{CO}_2$ -based mixtures, it would be good to discuss some of the mechanical implications of these designs, most potent of which is the rotational speed. An overview of the practical limits of designing  $\text{CO}_2$  was presented by Mcclung et. al. [41], in which an empirical chart was used to determine the practical rotational speed limit of a generator for a

given power output. According to that study, the rotational speed limits for 0.1 MW, 1 MW, and 10 MW turbines are 151 kRPM, 46.4 kRPM, and 14.3 kRPM, respectively. Compared to these limits, the rotational speeds quoted in Table 7 are impractical; for all fluids. The turbines that are the furthest from the practical rotational speed limits are those of  $\text{CO}_2$  with rotational speeds about 270% of the speed limit. It is expected that applying the rotational speed limit would penalise the efficiency of all turbines; but to what degree? To answer this question, the optimisation in Case-B is repeated under the aforementioned rotational speed constraints.

Predictably, limiting the rotational speed had a significant influence on the total-to-static efficiency and the specific speeds of the turbines, which are shown in Fig. 17.



**FIGURE 17: SPECIFIC SPEED AND EFFICIENCY COMPARISON OF CASE-B WITH AND WITHOUT A LIMIT OF ROTATIONAL SPEED**

The greatest drop in efficiency is 15% for the 0.1 MW  $\text{CO}_2$  turbine; the lowest is 1% for the 10 MW  $\text{CO}_2/\text{TiCl}_4$  turbine. Not only does the efficiency drop, but the differences between the turbine designs of the fluids are exacerbated by the practical speed limit, which is notable in the reduction in the specific speed of all designs. The range of specific speeds reduces from  $0.3 < N_s < 0.5$  to about  $0.15 < N_s < 0.3$ . The restriction of  $\text{sCO}_2$  radial inflow turbines to low specific speeds was already noted by Keep [42], and it seems that the same applies to  $\text{CO}_2$  mixtures; however, higher specific speeds are possible in mixtures owing to the lower specific work imposed by their cycles. To maintain favourable specific speeds, and thus good efficiency, multi-staging will be required; more so for  $\text{sCO}_2$  and  $\text{SO}_2$  than for  $\text{TiCl}_4$  and  $\text{C}_6\text{F}_6$ .

Ultimately, the rotational speed limit is yet another practical limit on turbine design which causes the turbine designs of the fluids to diverge. It is expected that the designs will diverge even further as more design limits are imposed (as was seen with the clearance gap and rotational speed).

#### 4. CONCLUSION

In this paper, the design of small- to medium-scale radial inflow turbines under multiple design assumptions were analysed with the aim of discerning the effects of doping  $\text{CO}_2$ . Results indicate that the aerodynamic behaviour of the working fluids is similar. Therefore, turbine designs for all working fluids converge

on similar rotor shapes and velocity diagrams. However, not all turbines achieve the same performance.

Among the mixtures studied, CO<sub>2</sub>/TiCl<sub>4</sub> achieved the highest performance, followed by CO<sub>2</sub>/C<sub>6</sub>F<sub>6</sub>, and then CO<sub>2</sub>/SO<sub>2</sub>. For example, 100 kW turbines for CO<sub>2</sub>/TiCl<sub>4</sub>, CO<sub>2</sub>/C<sub>6</sub>F<sub>6</sub>, CO<sub>2</sub>/SO<sub>2</sub>, and CO<sub>2</sub> achieve total-to-static efficiencies of 80.0%, 77.4%, 78.1%, and 75.5% respectively. Whereas, the efficiencies for 10 MW turbines are 87.8%, 87.3%, 87.5%, and 87.2%, in the same order.

Variations in the achievable efficiency amongst the fluids stem from variations in their clearance-to-blade height ratio, their pressure ratios, rotational speed limits, and, to a lesser degree, differences in their viscosity. In conclusion, although doping CO<sub>2</sub> has little effect on the aerodynamic performance of the turbine, it is the consequence of the change in cycle conditions along with the design limitations of radial inflow turbines that lead to differences in the performance of the turbines amongst the fluids.

The differences in performance amongst the fluids are greatest in small scale turbines; with fluids that produce turbines of greater blade heights having the highest efficiency. The effect of clearance loss is attenuated with design optimisation by allowing greater flow coefficients, which increase velocities and reduce tip clearance loss. Consequently, the specific speed of the turbines increases at smaller power scales.

The study reveals that loss models are not sensitive to the working fluid. Moreover, the influence of geometric and kinematic parameters changes with power scale. Multi-staging of CO<sub>2</sub>, CO<sub>2</sub>/SO<sub>2</sub>, and CO<sub>2</sub>/C<sub>6</sub>F<sub>6</sub> turbines is more beneficial than for CO<sub>2</sub>/TiCl<sub>4</sub> because of the high pressure ratio cycle within which they operate. Additionally, the size of the rotor and the magnitude of the velocities depends on the working fluid, which may entail different mechanical requirements, such as bearing selection and rotordynamics.

It is recommended that future work builds on the findings of this paper by completing a comprehensive mechanical design of the turbines, including bearing selection, rotordynamics, and structural analysis, to ascertain the consequences of doping CO<sub>2</sub> on the full design of the turbine.

## ACKNOWLEDGMENTS

This work was supported by the European Union's Horizon 2020 research and innovation programme under grant agreement No. 814985.

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