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Seismic retrofitting of URM masonry piers with helical steel reinforcement

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Abstract: Past earthquakes revealed that the brittle nature of unreinforced masonry (URM) structural walls often leads to extensive cacking and shear damage, which can seriously affect the structural integrity and thus compromise the safety of the entire building. Hence, finding an effective seismic retrofitting solution that can increase the safety of existing masonry building stock is of great importance. This paper explores the potential of alternative seismic retrofitting solutions for URM masonry walls - near-surface mounted austenitic stainless-steel helical bars. Being cold rolled from a plain round wire and subsequently tensioned through a free-twisting process, such a reinforcement can not only offer high durability, but also superior mechanical and bond properties, as well as effective redistribution of loads through the retrofitted masonry. In addition, the relatively high flexibility of the bars allows them to be mounted continuously along the joints of the wall, leaving the aesthetic of the retrofitted masonry intact. A total of nine single-leaf clay brick walls were tested under cyclic displacement reversals to examine the seismic performance of the reinforcement in terms of increasing in-plane shear capacity and ductility. Test specimens comprised cantilever walls with various retrofitting patterns, including flexural and shear helical reinforcements installed in the mortar joints or into the vertical slots cut into the masonry. The results showed considerable improvements in the ductility and energy dissipation of the walls after the retrofitting. For most of the retrofitted walls the value of q factors exceeded 4.0, which is greater than the typical q factors for reinforced masonry, thus indicating that large increases in ductility were achieved. The paper highlights the potential of helical stainless-steel bars as a seismic retrofitting reinforcement capable of preserving the structural integrity of masonry structures at increasing displacement demands without affecting the aesthetic of the surface of the walls.

Keywords: Helical stainless-steel reinforcement, twisted bars, seismic retrofitting, masonry, in-plane damage, shear

1. Introduction

48 Unreinforced masonry (URM) buildings constitute more than 70% of the existing building
49 stock worldwide and make up the vast majority of the world's cultural and architectural heritage
50 [1]. Although masonry buildings have proven to be highly durable structures, much of the
51 existing building stock comprises non-engineered URM buildings, often built using weak
52 materials and designed according to simple principles with little or no seismic provisions. The
53 in-plane behaviour of URM walls has been studied experimentally by many researchers, whose
54 work largely contributed to the current state-of-the-art [2-6]. Owing to its inherent non-
55 homogeneity, the seismic behaviour of masonry under combined shear and compression loads
56 is different from that of homogeneous materials. In general, the failure mode of URM walls
57 subjected to in-plane seismic excitations depends on wall aspect ratio and axial load and is
58 characterised as either flexure controlled or shear controlled [6, 7]. For slender walls, with
59 relatively low axial loads, failure is usually governed by flexure and their strength is limited by
60 rocking or crushing of the bricks. For stockier walls, shear behaviour usually dominates in the
61 form of shear sliding or diagonal cracking failure mode, either at the mortar joint interfaces or
62 through the brick units. Shear failures are characterised by more brittle behaviour, which can
63 lead to catastrophic collapses of buildings. In turn, damage in URM buildings during past
64 earthquakes, often associated with brittle in-plane shear failure of masonry walls, has resulted
65 in numerous casualties and severe economic losses [8]. Only in 2023, two high-magnitude
66 earthquakes (Turkey-Syria and Marrakesh-Safi) devastated countries with large stocks of URM
67 buildings killing more than sixty thousand people and causing large-scale damage to
68 households and infrastructure, with very high economic losses. In light of the above, finding an
69 effective seismic retrofitting solution, which will increase the deformability and thus the safety
70 of existing URM structures in seismic-prone areas is of fundamental importance.

71 To date, several different retrofitting systems designed to improve the in-plane behaviour of
72 URM masonry walls have been investigated experimentally. These include repairs with
73 external steel strips [9-10], steel reinforced concrete and ferrocement jackets [11-13], shotcrete

74 [14-15], centercore technique [16] as well as externally bonded advanced composites such as
75 fibre-reinforced polymers (FRP) [17-19] or textile-reinforced mortars [20-24]. These
76 strengthening methods proved to be effective in improving the overall shear behaviour of walls;
77 however, they are usually expensive, require a great deal of preparation time and affect the
78 appearance of masonry, which in case of heritage structures is often unacceptable. Refined
79 retrofitting methods, which provide more balanced options without changing the aesthetics of
80 masonry include structural repointing interventions where steel [25-26] or FRP [27-30]
81 reinforcement is mounted near to the surface of the wall (NSMR). This method can be
82 particularly useful as it allows strengthened walls to perform akin to reinforced masonry (RM),
83 and thus be designed using standard provisions for new RM structures. Such solutions can
84 enhance the in-plane behaviour of masonry; however, these systems also have some limitations
85 in relation to the installation and their performance. Due to the lack of flexibility in either
86 regular steel bars or FRP bars, the installations can only be performed in the bed joints, and on
87 regular masonry. Without affecting the appearance of the structure. In addition, these systems
88 seem to improve the cracking behaviour primarily at low displacement demands, but show
89 reduced performance at the stage of severe damage in masonry. In fact, with increasing
90 horizontal displacement demands, the bond and the composite action between regular steel/FRP
91 reinforcement and masonry degrades and in turn the ductility and energy dissipation capacity
92 are limited. However, it is often the ductility that helps to prevent brittle collapse of the structure
93 during strong earthquakes [31-32].

94 An alternative to FRP or regular steel bars can be stainless steel helical reinforcement, which is
95 widely used as masonry connectors and reinforcement for various structural repairs of masonry.
96 Alongside being used as wall ties or connectors, helical bars can be also installed as near-surface
97 mounted reinforcements, fitted into slots cut into mortar joints, bonded using cement or
98 polymer-based grout and finished with colour matching mortar. Being cold rolled from a plain
99 round wire and subsequently tensioned through a free-twisting process, such reinforcement

100 offers high durability and superior mechanical properties when compared to alternatives due to
101 its increased strength and its helical shape, which offers additional mechanical interlock in the
102 masonry. As such, the helical shape of the bar ensures a desirable balance between flexibility,
103 strength, and bond, enabling reinforced masonry to reach larger deformability levels compared
104 to regular steel bars. Moreover, the flexibility of stainless-steel helical bars makes it possible to
105 bend them by hand and place them into both bed and head joints, and hence, the retrofitting can
106 be carried out without any major changes to the appearance of the masonry.

107 Although research on stainless steel helical bars is very limited, recent studies have indicated
108 that such reinforcement could be used for seismic retrofitting applications. Pull-out tests of
109 helical connectors from masonry substrates [33-34] generally showed good performance related
110 to bond strength, anchorage length, and mitigation of strength degradation during cyclic
111 loading, which highlights the potential for this reinforcement in seismic retrofitting
112 applications. Experimental investigations of helical bars in tension [35] revealed a good level
113 of ductility (extended the yielding plateau at ultimate load) and a minor effect of cycling on
114 strength. The effectiveness of helical reinforcement for shear strengthening of masonry walls
115 has been investigated experimentally [36] and numerically [37] on masonry wallets subjected
116 to diagonal tension; significant gains in shear strength and ductility were observed in the
117 retrofitted walls compared to URM walls. Recent research on the performance of masonry T-
118 connection joints [38] retrofitted with helical bars used as connectors subjected to cyclic out-
119 of-plane loads indicated that such reinforcement can significantly increase the energy
120 dissipation capacity.

121 Although initial test results on the performance of helical bars indicate that they can be used for
122 seismic retrofitting applications, to date this has not been experimentally verified in masonry
123 piers subjected to shear – critical structural members resisting earthquakes. The previous studies
124 [32, 33] involved monotonic loading of walls under diagonal compression without including

125 the effect of vertical stress and cyclic loading thus offering only limited information on the
126 seismic performance.

127 The present study, for the first time investigates the use of helical bars for seismic retrofitting
128 of URM masonry walls through full-scale tests on masonry walls subjected to cyclic quasistatic
129 in-plane loads representing seismic actions. Moreover, some novel retrofitting patterns of
130 helical bars are explored, in addition to ‘traditional’ ones involving repointing of bed joints.
131 The Section 2 outlines the experimental program and the methodology as well as provides the
132 details of the test specimens and the materials employed in this study. The Section 3 discusses
133 the hysteretic responses of the walls as well as their failure behaviour. The main quantitative
134 results are also presented and discussed. In the Section 4, the experimental capacities are
135 compared to the theoretical Eurocode-based predictions.

136 The results of this experimental study will contribute towards developing novel ductile
137 retrofitting systems for URM walls in seismic prone areas, thus improving the safety of masonry
138 buildings during earthquakes and increasing their resilience to seismic activities.

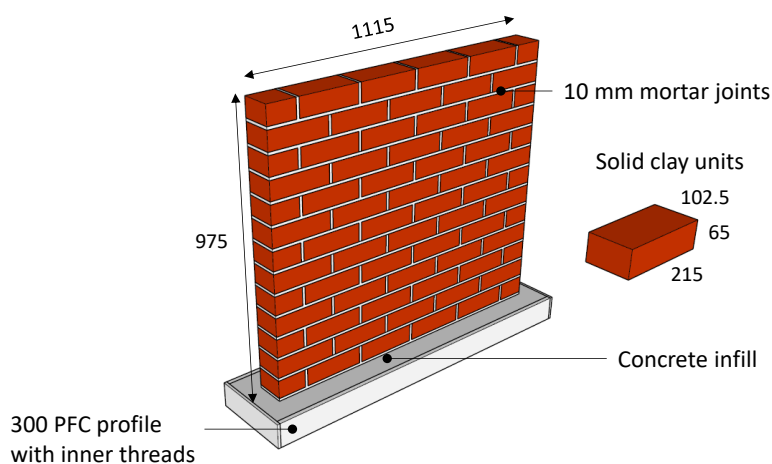
139 **2. Experimental programme**

140 The main testing programme comprised in-plane cyclic shear tests on cantilever masonry walls
141 subjected to different levels of axial loading and retrofitted with various patterns of helical bars.
142 A total of nine tests were carried out: two on URM walls and seven on retrofitted walls using
143 two levels of axial load. The different reinforcement patterns aimed to investigate the
144 contribution of the reinforcement to the strength, ductility, and energy dissipation capacity of
145 the masonry walls. In addition to reinforcement patterns used in previous studies, by taking
146 advantage of the flexibility of the helical bars, a unique retrofitting configuration was explored
147 where the reinforcement was placed into the mortar joints chasing bed joints and head joints
148 without cutting through brick units (a “wiggled” pattern). One of the URM walls was tested
149 under a low axial load, and after the testing, was repaired and re-tested to attest to the practical

150 aspects of the application. The tests were complemented by material tests on masonry brick
 151 units, mortar, and grout samples as well as helical bars, to evaluate materials' strength.

152 *2.1. Wall specimens*

153 All wall specimens were built as single-leaf masonry walls using solid fired clay masonry units
 154 laid in a running stretcher bond with a half brick overlap maintaining approximately 10 mm
 155 thick horizontal and vertical mortar joints (Fig. 1). The overall dimensions of the wall
 156 specimens were 1115×975 mm resulting in an aspect ratio of 0.87. The nominal thickness of
 157 the wall was equal to the thickness of one brick, i.e. 102.5 mm. The walls were built onto
 158 adapters fabricated using parallel flange channels (PFC) with steel rebars welded inside and
 159 then infilled with concrete (40 MPa), with cast-in inner threads welded to the bottom of the
 160 PFC to enable a connection to the steel test frame. Prior to being infilled with concrete, a number
 161 of the adapters were fitted with helical bars, which would later form vertical reinforcement to
 162 the wall specimens to ensure good anchorage to the base. Such arrangements were only made
 163 for the test purposes. For interventions on real structures, anchorage of the helical bars into the
 164 foundation, or into the elements of the adjacent stories, would not be difficult to achieve even
 165 if the existing foundation is shallow as the bars can easily be bent at an angle or extended deeper
 166 into the adjacent structural elements until the required anchorage length is achieved.



167

168

Fig. 1. Geometry of the wall specimens (dimensions in mm)

169 The properties of the wall specimens are listed in Table 1. Two levels of axial stress were
 170 investigated, equal to 0.6 MPa and 1.0 MPa. These stress levels correspond to about 7 % and
 171 12 % of the masonry compressive strength and can represent typical stress levels in masonry
 172 buildings. Similar stress range was also adopted in the past research studies on URM [5, 39].
 173 One reference URM specimen and six retrofitted specimens were tested with an applied axial
 174 stress equal to 1.0 MPa, and two wall specimens (one URM and one retrofitted) were tested
 175 with an axial stress of 0.6 MPa. The two tests with the lower axial stress were carried out on
 176 the same specimen. Firstly, the URM wall was tested to failure and then it was retrofitted with
 177 helical bars and retested under the same axial stress of 0.6 MPa.

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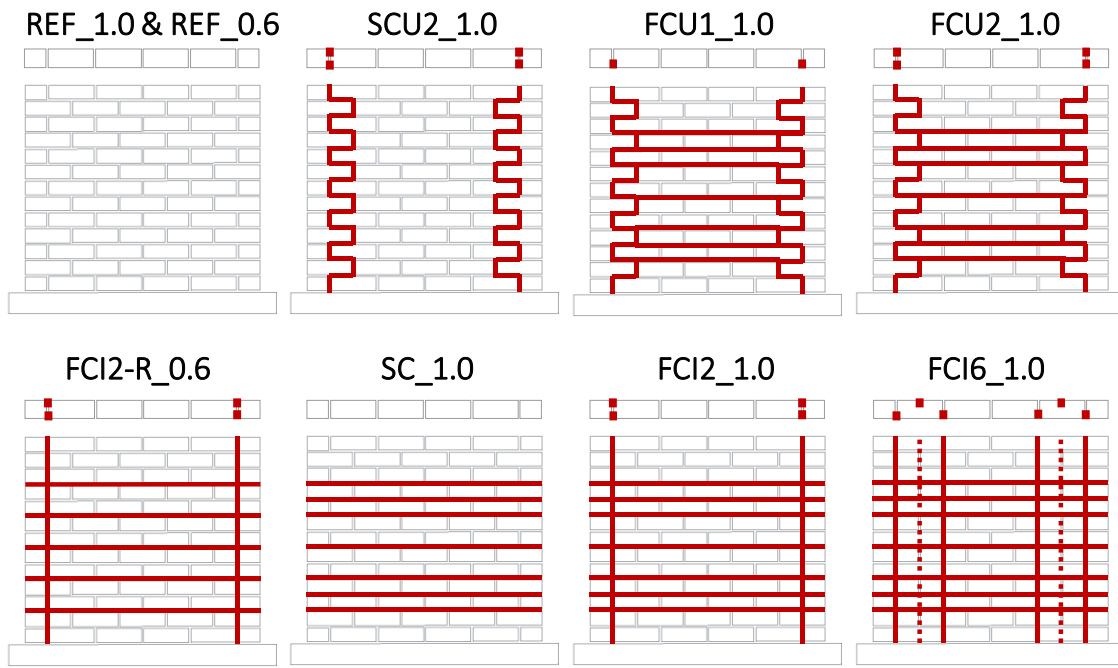
Table 1. Test specimens and retrofitting patterns.

	ID tag	Vertical load (MPa)	Vertical reinforcement		Horizontal reinforcement	
			type	no. per testing direction	type	no. per wall
1	URM_1.0	1.0	-	-	-	-
2	FCU1_1.0	1.0	wiggled	1	bed joint	7
3	FCU2_1.0	1.0	wiggled	2	bed joint	14
4	SC_1.0	1.0	-	0	bed joint	14
5	SCU2_1.0	1.0	wiggled	2	-	0
6	FCI2_1.0	1.0	straight	2	bed joint	14
7	FCI6_1.0	1.0	straight	6	bed joint	14
8	URM_0.6	0.6	-	-	-	-
9	FCI2-R_0.6	0.6	straight	2	bed joint	10

180

181 The reinforcement patterns for all walls are shown in Fig. 2. Three of the retrofitted specimens
 182 had “wiggled” helical bars (alternating in the horizontal and vertical direction in each course)
 183 as reinforcement, installed without cutting through the brick units, while three had vertical
 184 helical vertical bars installed into straight slots cut into the brick units. All retrofitted walls had
 185 helical bars placed into horizontal mortar joints in patterns as per Fig. 2. SC_1.0 and SCU2_1.0
 186 had only one type of reinforcement (horizontal or vertical bars, respectively) to investigate the
 187 individual contribution of this reinforcement to overall capacity. FCU1_1.0 and FCU2_1.0 had
 188 the same reinforcement pattern (“wiggled” vertical bars and horizontal bars) with the latter
 189 having twice the amount of reinforcement to investigate how the reinforcement ratio affects the

190 global response of the wall. FCI2_1.0 had the same pattern as FCU2_1.0, but straight bars were
 191 used instead of wiggled bars to investigate the difference in performance of these two
 192 reinforcement patterns. FCI6_1.0 had six helical bars installed vertically on both sides of the
 193 wall in a staggered pattern, representing walls with a high vertical reinforcement ratio.



194

195 *Note that all vertical bars were fitted into the PFC adapter prior casting concrete infill to achieve full anchorage
 196 in the base.

197 **Fig. 2.** Reinforcement patterns for all wall specimens.

198

199 2.2. Materials

200 The mechanical properties of the materials used to build and retrofit the walls were determined
 201 experimentally prior to the main testing programme. The experimental characteristics of the
 202 materials were then used to estimate the theoretical capacity of the walls. The material tests
 203 comprised compression tests on bricks and masonry prisms to determine the compressive
 204 strength and modulus of elasticity; bending tests on brick assemblages to determine the flexural
 205 strength of the bricks; compressive and flexural tests on the masonry mortar and grout; and
 206 tensile tests on helical bars to determine the mechanical properties of the reinforcement.
 207 Standardised shear tests on brick triplets were also carried out to estimate the initial shear
 208 strength and friction coefficient for the masonry joints.

209 2.2.1. Brick units

210 Standard solid clay masonry units were used in the present study with overall nominal
211 dimensions of 102.5×215×65 mm (tolerance: length, ± 4 mm; width, ± 3 mm; height, ± 2 mm)
212 and a nominal density of 1830 kg/m³. The compressive strength of the brick units was
213 determined according to RILEM provisions [40]. The tests were performed on two sets of brick
214 units, with three units per set to account for the variability in the materials: (i) with the load
215 applied normal to the brick headers; (ii) with the load applied normal to the beds. The loaded
216 surfaces had a 5 mm gypsum capping to ensure that load will be distributed uniformly across
217 the loading area. The average compressive strength was equal to 23.8 MPa (COV 9 %) for the
218 direction normal to the headers and 28.9 MPa (COV 7 %) for the direction normal to the beds.
219 The Young's modulus was measured during the compressive strength tests, where the units
220 were tested in an upright (soldier) orientation, based on the readings of two LVDTs attached to
221 the stretchers (Fig. 3). The base length of the gauges was set at 150 mm and a constant
222 displacement rate of 0.2 mm/min was used. The elastic modulus was estimated between the
223 stress levels corresponding to 30-60% of the failure stress as an average across the three
224 specimens. The mean value of the experimental elastic modulus of the bricks was equal to
225 5691.1 MPa (COV 20%) with a maximum mean strain of 0.0039 (COV 6 %).

226



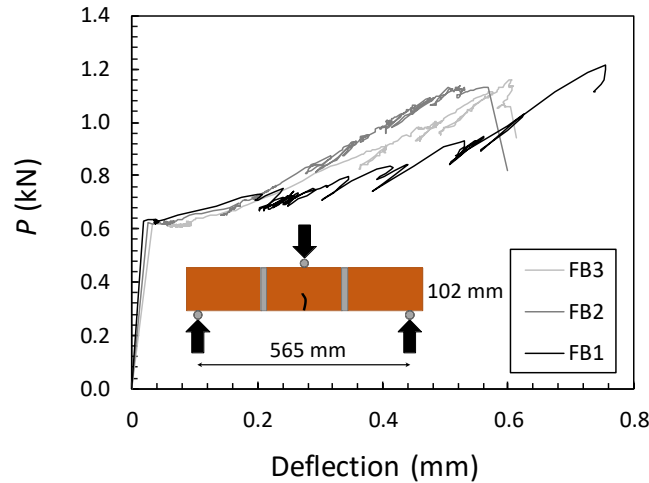
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228 **Fig. 3.** Masonry unit tested under compression before and after failure.

229

229 The tensile properties of the masonry units were also estimated in line with RILEM provisions
230 [40]. A typical specimen consisted of three bricks bonded together header-to-header using a

231 very strong binder (with 1 day compression strength equal to 40 MPa), thus enforcing the failure
 232 in the masonry unit, under the loading point of a 3-point bending configuration over a 565 mm
 233 clear span (Fig. 4). The flexural tensile strength was determined from the tests as the maximum
 234 stress at failure and was equal to 1.43 MPa (COV 2 %).



235

236 **Fig. 4.** Three-point bending test on brick-mortar assemblages.

237

238 2.2.2. Compressive strength of masonry and mortar

239 The mortar mix used to build the walls comprised cement-lime-sand composition with the ratio
 240 by volume equal to 1:2:8, respectively. The compressive and flexural strength of mortar was
 241 determined according to EN 1052-11 [41] on standard 40×40×160 mm prisms. The average
 242 values of compressive and flexural strengths were 5.1 MPa (COV 3 %) and 1.1 MPa (COV 6
 243 %), respectively.

244 The compressive strength (perpendicular to the bed joints) and elastic modulus of masonry were
 245 estimated according to EN 1052-1 [42] on four identical brick and mortar assemblages tested
 246 at a displacement rate of 0.2 mm/s. The stress-strain responses for all four specimens are shown
 247 in Fig. 5. The tests revealed an average compressive strength of 8.6 MPa (COV 5%) with a
 248 corresponding peak strain of 0.0068 (COV 11%). The average experimental modulus of
 249 elasticity was estimated as 1772.1 MPa (COV 8 %).

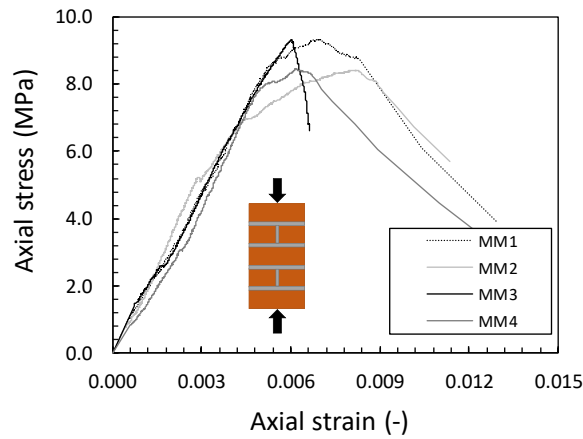


Fig. 5. Compressive characteristics of masonry brick-mortar assemblages.

2.2.3. Initial shear strength

The initial shear strength and the coefficient of friction were estimated according to EN 1052-3 [43] using the test setup shown in Fig. 6. The shear stress was determined at three different precompression levels, i.e. 0.2 MPa, 0.6 MPa, and 1.0 MPa. Three tests were carried out at each precompression level, totalling nine samples. The coefficient of friction was estimated as 0.6 and initial bond strength as 0.59 MPa.

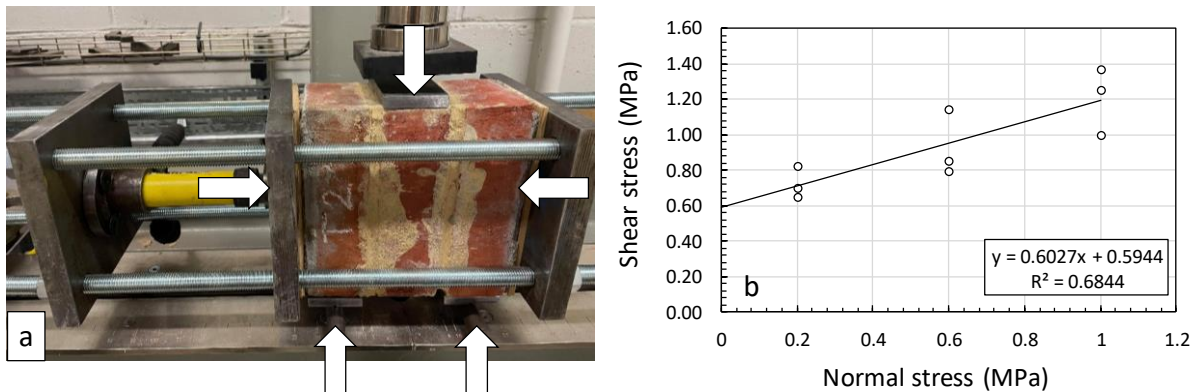


Fig. 6. Initial shear strength – test rig and results: a) test rig; b) test results for all 9 triplets

2.2.4. Helical bars and grout

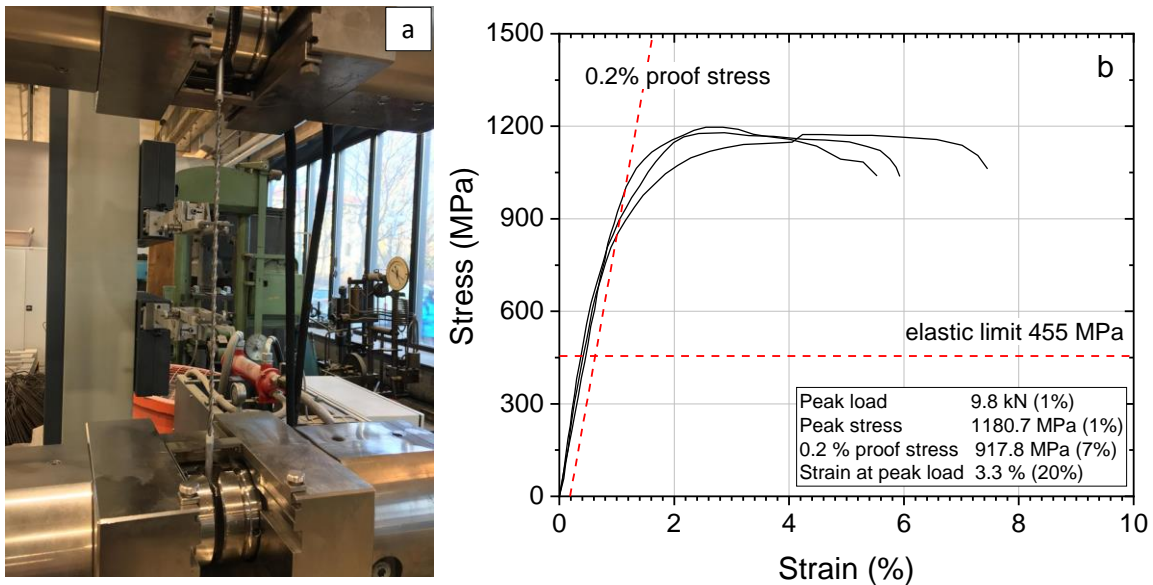
The retrofitting system consisted of helical bar with an overall diameter of 6 mm (Fig. 7) and a cement-based pumpable and thixotropic bonding agent (grout). The shape of the helical bar offers great flexibility, thus allowing for easy bending and installation in masonry joints. The mechanical properties of the helical bars were determined with standard tensile tests on three bar samples using the provisions set out in ISO 6892 [44].



Fig. 7. Geometry of the helical bars

266
267
268 Strain was measured using an external extensometer with a base length of 100 mm, spanning
269 the centre of the sample. Due to the specific helical shape of the bars, direct tensile tests could
270 not be performed without risking damage to the helical fins near to the grip jaws of the machine.
271 Therefore, the bar ends were anchored within aluminium tubes of 10 mm internal diameter and
272 filled with resin grout, which enabled a larger surface area of the helix to be gripped. In turn,
273 all tested samples exhibited a rupture within the extensometer's measuring range, which is the
274 intended failure mode for this test. The test setup and the stress-strain response for all three
275 samples is shown in Fig. 8. The average tensile load measured during the test was 9.8 kN (COV
276 1 %); with a cross-sectional area equal to 8.3 mm^2 , such load resulted in an average stress of
277 1180.7 MPa (COV 1%). Based on the test results, it was determined that the response of the
278 helical bar was close to elastic up to a stress level of about 455 MPa, which seems to agree with
279 the estimates from other tests on helical bars [34-35]. The results indicated that such
280 reinforcement reaches higher stress levels at larger displacements and does not exhibit clear
281 yielding point as in the case of mild steel reinforcement; hence, the 0.2 % proof stress value
282 was also determined, which for three tests revealed a mean value of 917.8 MPa (COV 7%). The
283 Young's modulus of the helical bars was estimated as secant modulus at the stress level
284 corresponding to the elastic range (455 MPa, see Fig. 8b) was equal to 110.8 GPa (COV 9%).
285 As can be seen, the elastic modulus is much lower than the modulus of normal steel but at the
286 same time much greater stress levels can be attained in comparison to mild steel reinforcement.
287 The cement-based grout, which is an integral part of this retrofitting system was tested using
288 the same provisions as for the masonry mortar. The mean compressive and flexural strengths

289 after 28 days of curing were equal to 40.4 MPa (COV 4 %) and 4.1 MPa (COV 11%),
 290 respectively.



291

Fig. 8. Tensile testing: a) test setup; b) stress-strain response

292

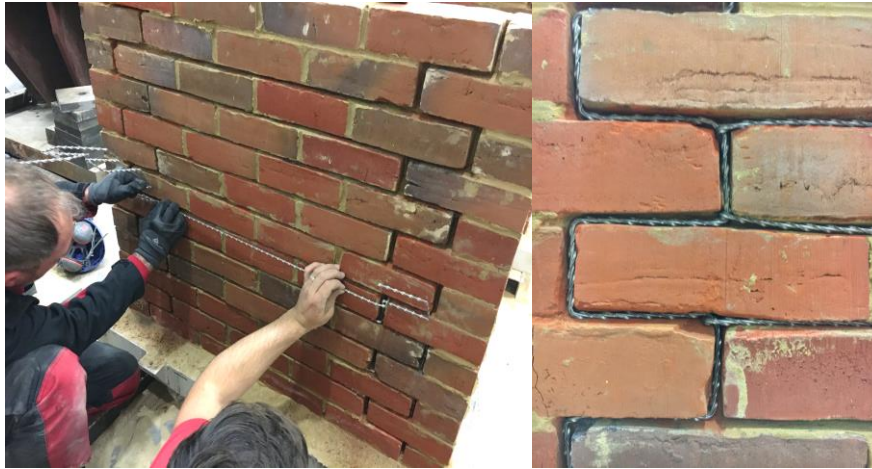
293 2.3. Retrofitting with helical bars

294 The retrofitting was carried out on the masonry walls after a minimum of 6 weeks of curing at
 295 room temperature. All walls were retrofitted with the helical bars from the same batch with the
 296 same diameter of 6 mm. The following procedure was applied to carry out the installation:

- 297 • The existing mortar was raked out to a depth of approximately 25 mm, and then the slot
 298 was cleaned using compressed air and water. Straight slots were cut into both the mortar
 299 joints and masonry units for the specimens requiring straight vertical reinforcements.
- 300 • Helical bars were bent where necessary and cut to length to suit the slot.
- 301 • After ensuring that the cut slots were free from dust and debris, and were dampened, the
 302 grout was pumped into the back of the slot to fill approximately half of the depth. The
 303 procedure was carried out separately for vertical reinforcement and bed joint
 304 reinforcement.
- 305 • The vertical reinforcements were pressed into the grout first, followed by the bed joint
 306 reinforcements with the latter anchoring to the vertical reinforcement (Fig. 9).

307 • The final layer of grout was applied, providing about 15mm of cover to the helical bars.

308



309

310 **Fig. 9.** Retrofitted helical bars, wiggled to both bed joints and head joints.

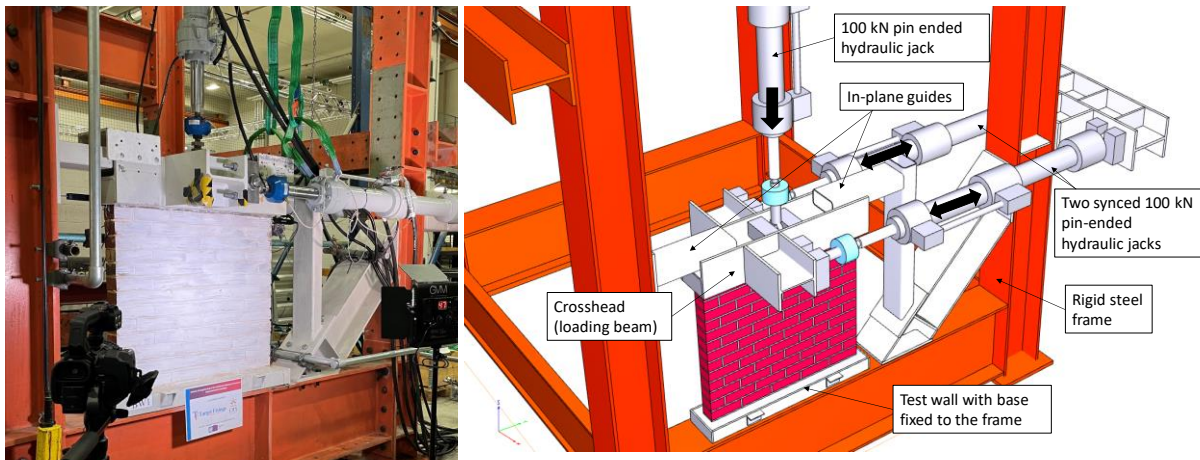
311

312 It should be noted that this type of retrofitting also applies to double leaf walls or the walls
313 thicker than 215 mm, however, according to the manufacturer, in such cases the bars should be
314 always installed on both faces of the wall and additional perpendicular tying of the wythes
315 should be considered where necessary.

316 *2.4. Test setup and methodology*

317 The test setup used for all in-plane cyclic shear tests is shown in Fig. 10. All walls were tested
318 as cantilevers, representing the lower half of a typical pier with an aspect ratio of around 1.75
319 fixed between the openings [45]. The bottom (300 mm PFC profile at the base of each
320 specimen) was connected to the self-reacting test frame via 12 M24 bolts, thus being
321 constrained against any displacement or rotation. The horizontal load was applied via a
322 crosshead beam, which was free to rotate and translate in the in-plane direction. The bottom of
323 the crosshead was filled with concrete and bonded to the top of the masonry wall using high
324 strength grout, hence ensuring a strong bond between the two elements. The horizontal load
325 was applied through two synchronised pin-ended hydraulic actuators, each with a nominal
326 capacity of 100 kN. The vertical load was applied via a similar hydraulic pin-ended actuator,

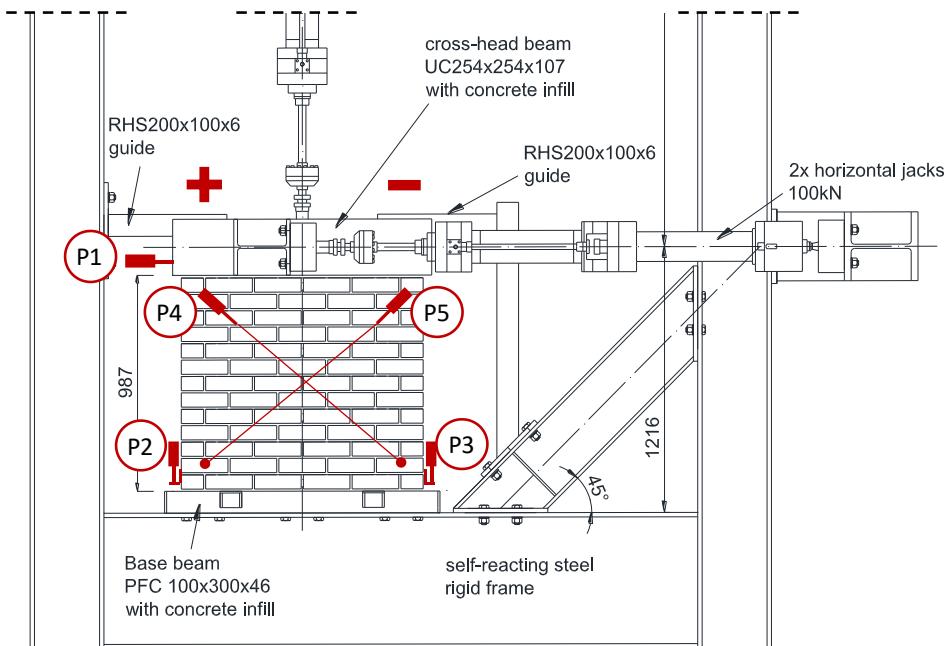
327 maintaining the design stress level. Additional in-plane guides were provided to ensure that any
 328 out-of-plane movements of the wall during the tests are prevented.



329

330 **Fig. 10.** Typical test setup for in-plane testing with cyclic reversals.

331 The experimental load was measured by two load cells built into the actuators; the horizontal
 332 shear capacity was taken as the sum of the loads recorded by the two horizontal actuators. The
 333 external instrumentation is shown in Fig. 11. The net displacement of the wall was measured
 334 by an LVDT (P1) placed on top of the wall. Uplift was measured by LVDTs P2-P3, and the
 335 shear deformations were measured by wire gauges P4-P5.

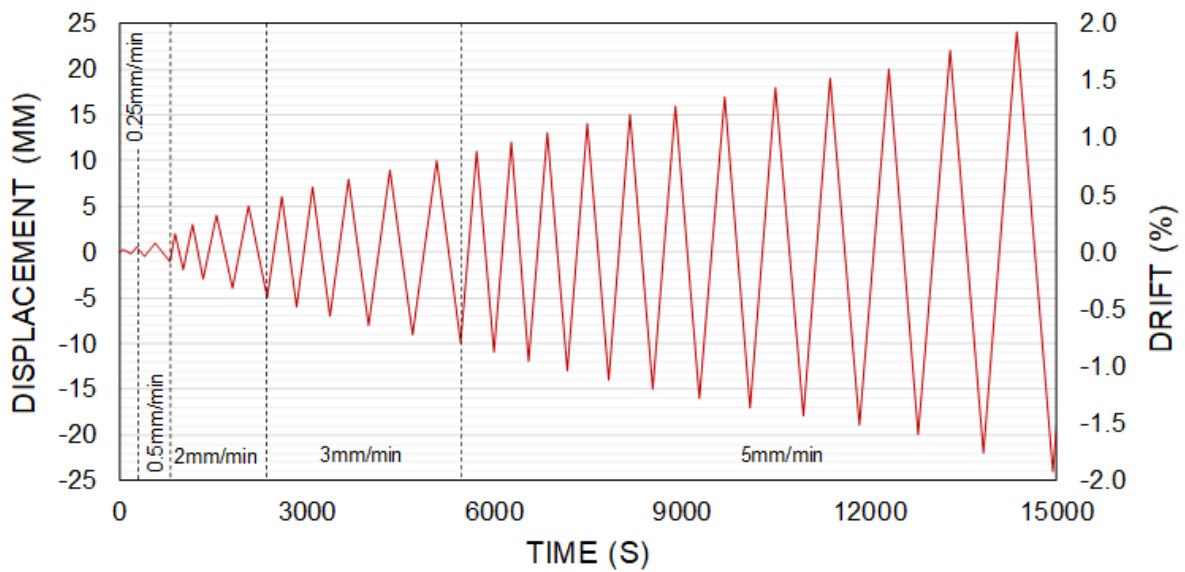


336

337 **Fig. 11.** Test setup and instrumentation – frontal elevation. Note that diagonal gauges were
 338 installed on the back side of the wall. The signs “+” and “-“ indicate directions of loading –
 339 push and pull, respectively.

340

341 The in-plane loading was applied in displacement control under quasi-static conditions to
 342 capture the post-peak softening stage and associated damage accumulation. The vertical stress
 343 was applied with a load-controlled regime. All wall specimens were subjected to the same in-
 344 plane reverse cyclic loading history shown in Fig. 12. The first two cycles were performed at
 345 target displacements of ± 0.25 and ± 0.50 mm to capture the elastic response of the wall
 346 specimen, while the subsequent cycles were performed at increasing target displacement
 347 amplitudes of ± 1 mm. The tests were terminated once a strength degradation of about 25% was
 348 observed, which is close to the level at which the element was considered to have reached its
 349 near-collapse limit state [46].



350

351 **Fig. 12.** Loading protocol adopted for the in-plane cyclic shear testing.

352

353 3. Test results and discussion

354 The main results for “push” (+) and “pull” (-) directions are summarised in Table 2. The
 355 reported values include the experimental horizontal shear capacity, V_{max} , taken as the sum of

356 the loads measured by the two horizontal actuators and the experimental drift levels (computed
 357 based on the P1 readings), δ_{Vmax} and δ_{max} , representing the drift of the wall at the peak horizontal
 358 load and the maximum recorded drift (corresponding to about 25 % load drop), respectively.
 359 The reported displacement values represent readings from LVDT P1, measuring the net
 360 displacement of the specimen.

361

362

Table 2. Main results of the in-plane cyclic shear tests

ID tag	σ_n (MPa)	V_{max} (kN)		δ_{Vmax} (%)		δ_{max} (%)	
		Push	Pull	Push	Pull	Push	Pull
URM_1.0	1.0	+68.5	-69.4	+0.76	-0.67	+0.98	-0.88
FCU1_1.0	1.0	+65.3	-67.2	+0.80	-0.70	+1.87	-1.69
FCU2_1.0	1.0	+69.6	-69.1	+0.95	-0.82	+1.42	-1.39
SC_1.0	1.0	+66.5	-67.0	+0.67	-0.59	+1.05	-0.97
SCU2_1.0	1.0	+69.8	-71.1	+0.92	0.97	+1.59	-1.52
FCI2_1.0	1.0	+70.0	-67.5	+0.50	-0.54	+1.27	-1.25
FCI6_1.0	1.0	+68.5	-73.5	+0.50	-0.60	+0.95	-1.03
URM_0.6	0.6	+42.8	-45.1	+0.95	-0.90	+1.26	-1.00
FCI2-R_0.6	0.6	+45.8	-43.7	+0.79	-0.71	+1.75	-1.84

363

364 3.1. Failure modes and hysteretic response

365 The failure modes and cyclic in-plane responses for all walls are shown in Fig. 13 and Fig 14.
 366 Owing to their nature, the URM cantilever walls developed mixed failure modes involving
 367 various degrees of flexural and shear damage. Both URM walls initially developed flexural
 368 cracks in the horizontal mortar bed joint at the bottom of the wall, which kept opening until
 369 shear cracks started to appear and eventually led to brittle shear failure. The walls with near-
 370 surface mounted helical reinforcement developed different cracking behaviour, and, in turn,
 371 brittle shear failure was avoided, thus allowing for a more limited degradation of the in-plane
 372 load compared to the URM specimen. Although the natural variability of masonry led to some
 373 differences in the failure patterns on the left and right sides of the wall, a fairly symmetrical in-
 374 plane cyclic behaviour has been recorded up to the peak load capturing similar values of shear
 375 capacity and drift for both push and pull directions (Table 2). The difference between the
 376 maximum shear capacities recorded in the two loading directions was not more than about 7 %
 377 (5 kN, FCI6_1.0) whereas the difference across the drifts δ_{Vmax} was about 16 % (0.13 %,)

378 FCU2_1.0). After reaching the peak load, and due to the different level of damage in the
379 masonry per loading direction, the difference in the maximum drift values δ_{max} became more
380 significant; up to 28 % (0.26%, URM_0.6).

381 Overall, the hysteretic response of the walls was characterised by a linear behaviour until the
382 first cracks appeared at the base of the wall, followed by a progressive deterioration of lateral
383 stiffness, indicating involvement of the mechanisms of rigid body motion (such as rocking of
384 the pier). The cyclical response of the walls retrofitted with helical bars did not show any major
385 increase in the in-plane strength; however, the walls exhibited a different post peak response
386 and some of the reinforcing patterns offered a more controlled failure mode and led to a larger
387 displacement capacity. The next sections offer a more in-depth analysis of the results describing
388 the failure mechanisms and hysteretic responses of each wall separately. It will be shown that
389 certain combinations of helical bars can not only change the failure mode from brittle to ductile
390 but can also lead to larger energy dissipation compared to a URM counterpart wall.

391 3.1.1. Test wall URM_1.0

392 The first cracks initiated in the mortar joint at the base of the wall at the interface between the
393 masonry and the footing at a drift level of about 0.15 %. This was expected as the bending
394 moment in this section was the highest and mortar joints form the weakest link in the masonry.
395 With increasing lateral load, the cracks propagated from the edges towards the centre of the
396 wall until they formed one crack across the full length of the wall. This was associated with
397 increased rocking of the wall and progressive degradation of the in-plane stiffness in the
398 hysteretic load vs. drift response (Fig. 14a). Just before reaching the peak shear load, two shear
399 cracks appeared (Fig 13a). The first crack occurred in the “push” direction and was shallow
400 reaching only above the third course and represented the peak shear load. In the following cycle,
401 in the pull direction, a steeper shear cracked formed, which was associated with a sudden drop
402 in the stiffness and large in-plane displacement (Fig. 13a). Both cracks occurred at the masonry
403 mortar interface with some cracks developing through the brick units, in the vicinity of the

404 corners of the wall. The peak shear force attained by URM_1.0 was +68.5/-69.4 kN with the
405 corresponding drift of +0.76/-0.67 %.

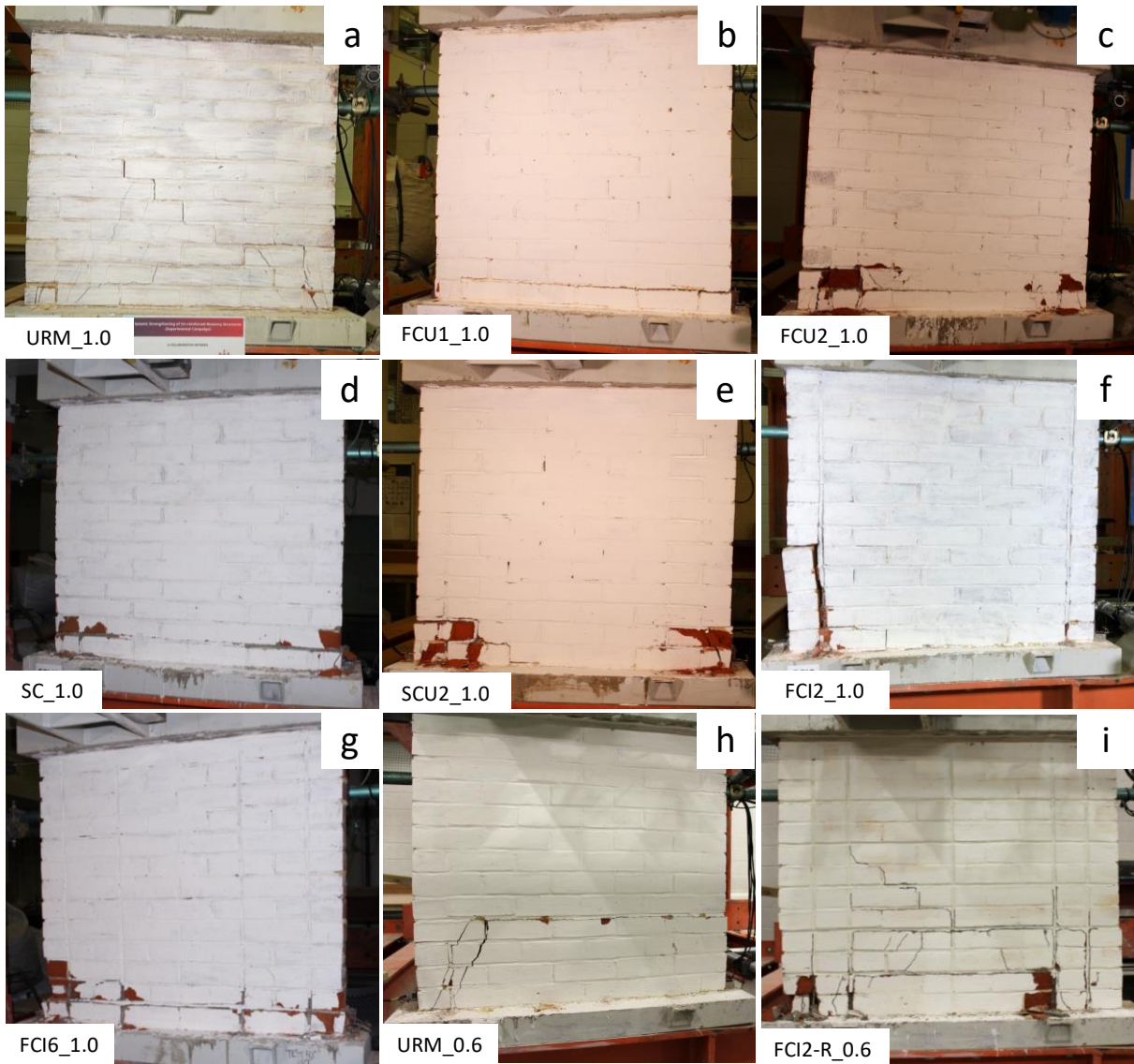
406 3.1.2. Test wall FCU1_1.0

407 After the first loading cycles, horizontal cracks started to develop along the interface with the
408 concrete adapter at a drift of about 0.1 %, just slightly less than it was observed for the
409 unreinforced counterpart indicating a minor contribution to the in-plane stiffness at the early
410 stages of loading. However, the vertical portion of the “wiggled” reinforcements between the
411 concrete base and the first course effectively bridged the crack, which led to the redistribution
412 of the loads and some horizontal cracks appeared between the first and the second course from
413 the bottom bed joint where wiggled bars were chased into the bed joints (Fig 13b). As the
414 loading progressed, the width of the crack further increased, which eventually led to
415 compression crushing at the bottom corner bricks of the wall. These cracks coincide with
416 reaching the maximum capacity of the specimen +65.3/-67.2 kN and the subsequent onset of
417 strength loss. The wall did not lose strength rapidly with increasing displacement but exhibited
418 an ability to maintain a residual strength capacity of about 75 % for the pull and 67 % for the
419 push directions, at a large drift of +1.87/-1.69 %. It is evident that the two “wiggled” bars
420 installed into the joints, combined with bed joint bars, somewhat contributed to the wall’s
421 structural response; although not being able to increase the lateral load capacity of the wall, still
422 managed to provide a better controlled post peak strength degradation and prevented shear
423 cracking and a brittle collapse.

424 3.1.3. Test wall FCU2_1.0

425 The second wall with an increased number of the “wiggled” bars showed similar initial response
426 to its counterpart wall FCU1_1.0. As in the previous test, the cracks developed at the second
427 from bottom course, but overall, more damage was present after the onset of cracking and as
428 the load progressed (Fig 13c, Fig. 14c). The beneficial effect of the increased reinforcement
429 ratio on the global response of the wall was a higher drift capacity at peak load, equal to +0.95/-

430 0.82 %, as well as the increased area of hysteresis loops, manifesting an increased energy
 431 dissipation capacity. On the other hand, the larger drifts resulted in increased compression in
 432 the toe regions of the wall and hence caused more damage to the brick units compared to its
 433 counterpart wall FCU1_1.0, and the result was that a non-symmetric post-peak response was
 434 achieved with failure in the push direction, where significant toe crushing developed.

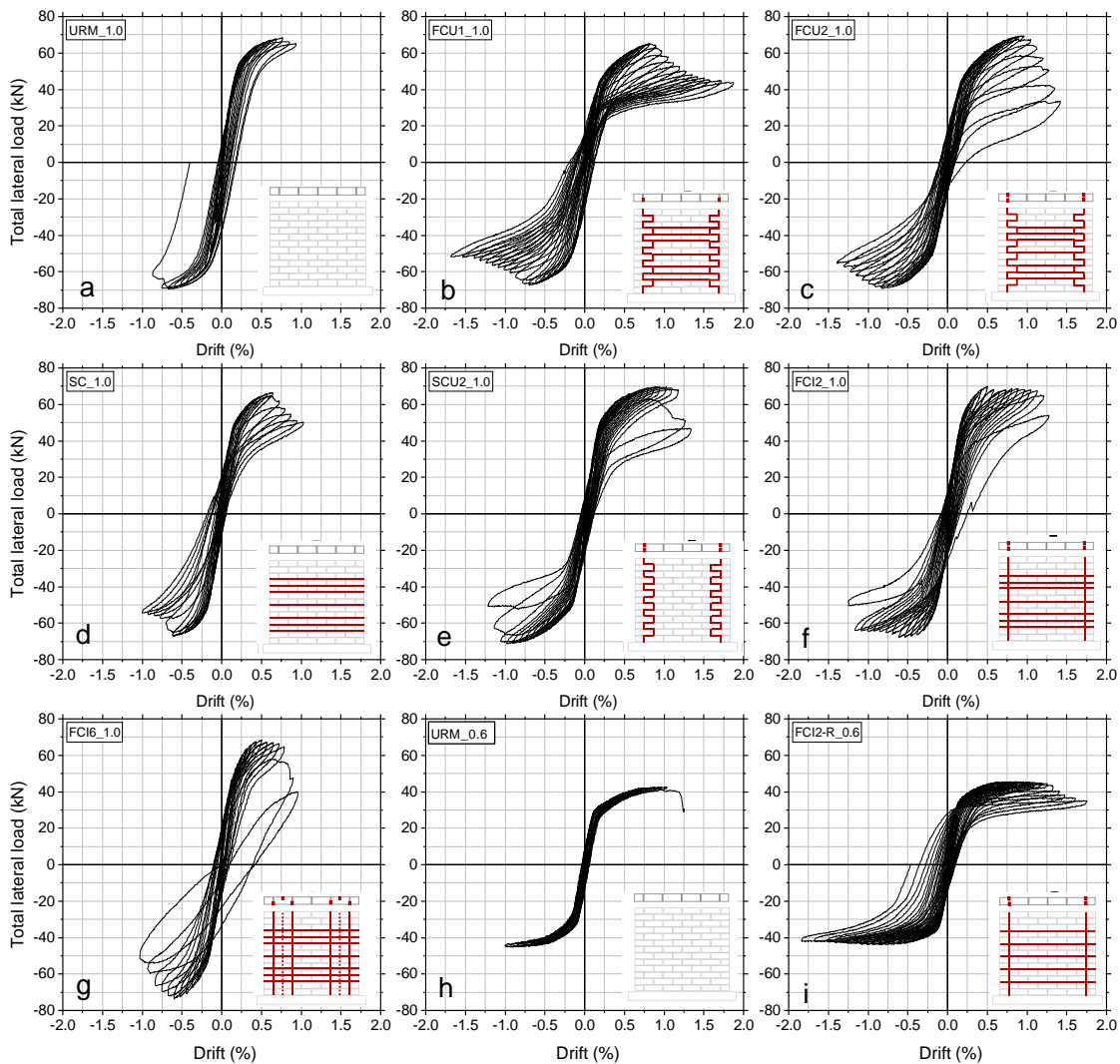


435

436

Fig. 13. Failure patterns for all walls.

437



438

439

Fig. 14. Load-drift hysteresis loops for all walls.

440

441 3.1.4. Test wall SC_1.0

442 The wall retrofitted only with bed joint reinforcement showed at initial stages a behaviour
 443 similar to the corresponding URM wall, but this behaviour changed with increasing
 444 displacement demands and a more ductile response was achieved at the ultimate stage and
 445 beyond the peak. The first cracks developed in the push direction (Fig. 13d) in the second from
 446 bottom course at about 0.15 % drift – the same drift level as in the case of URM_1.0. At the
 447 peak load of +66.5/-67.0 kN, a drift of +0.66/-0.59 % was attained exhibiting almost the same
 448 load path as the URM wall. However, after reaching the maximum load, shear cracks did not
 449 occur but failure was induced in the toe regions leading to a compression failure of the two

450 bottommost corner bricks. This manifested on the hysteretic response as a sudden load drop at
451 the end of the cycle, and triggered a progressive loss of strength. With further increase of the
452 load, it stabilised, maintaining more than 75 % of the peak lateral capacity before the test was
453 terminated. Although strength of the wall did not increase (indicating that lateral load capacity
454 was governed by flexure/rocking rather than by shear strength) the use of bed joint bars alone
455 allowed to avoid shear cracking and enabled a more controlled failure of the wall.

456 3.1.5. Test wall SCU2_1.0

457 As expected, at a drift level of 0.15 % cracking developed in the bed joint, which was not
458 reinforced as in FCU2_1.0, however, as the displacement increased, the cracks did not progress
459 from both sides as in the case of FCU2_1.0. Although “wiggled” reinforcement has been
460 somewhat engaged, and even slightly increased the wall’s capacity reaching a peak of +69.8/
461 71.1 kN was recorded, the high demand put on the vertical wiggled bars led to separation of the
462 two toes from the wall just below the third course where the bar had its second bend (Fig. 13e).
463 This caused a rapid loss of strength and led to a global failure of the wall without any capacity
464 to preserve residual strength. Although the presence of the “wiggled” reinforcement (as
465 expected) did not lead to higher lateral load capacity, it improved the hysteretic energy
466 dissipation, albeit not to the extent that it did in the specimen (FCU2_1.0) with a combination
467 of “wiggled” and horizontal bars.

468 3.1.6. Test walls FCI2_1.0 and FCI6_1.0

469 The wall specimens with straight vertical reinforcement installed into slots cut through the
470 bricks and the mortar head joints recorded comparable performance levels to the walls with
471 “wiggled” bars up to the peak load, however, they showed limited capability to control the
472 failure of the wall. FCI2_1.0 cracked at a drift of 0.12% at slightly higher load level than the
473 URM wall. It is noted that although vertical bars were anchored into the footing, the wall did
474 not seem to behave as a proper reinforced masonry wall, with increase in lateral load capacity
475 proportional to the vertical reinforcement added. The wall developed a slightly stiffer response

476 compared to the URM members in the push direction, and almost an identical load path in the
477 pull direction. At a drift of about 0.5 %, cracks along the vertical reinforcement appeared and
478 this effectively stopped the load from further increasing. Despite this, the wall maintained most
479 of its capacity until reaching a drift of about 1.1-1.2 % when a large part of the masonry
480 separated from the wall (Fig. 12f) and triggered the failure. In an attempt to avoid such a failure,
481 the wall FCI6_1.0 had installed more straight bars installed in a staggered pattern (front/rear,
482 see Fig. 2), hence having the vertical reinforcement closer to the centre of the wall specimen.
483 The wall cracked at a low drift level of about 0.1 %, indicating a stiff response. Separation of
484 the masonry cover was avoided but having more flexural reinforcement led to similar lateral
485 load and displacement capacities and eventually a more brittle post peak degradation (Fig. 12g).

486 3.1.7. Test walls URM_0.6 and FCI2-R_0.6

487 The test on the second URM wall with a lower axial stress of 0.6 MPa showed a different failure
488 mode compared to URM_1.0. Initial cracks were observed at a drift of 0.1 % in the horizontal
489 bottommost mortar joint, and with increasing amplitudes these cracks propagated through the
490 bed joint and connected to form one continuous crack about which the wall rocked. The wall
491 rocked in-plane showing nonlinear elastic behaviour and no loss of strength without any signs
492 of sliding or crushing until reaching a drift of about 0.75 %. Just before reaching the peak load
493 in the pull direction, a diagonal crack formed on the left side of the pier, and, with increasing
494 displacement, the crack changed to horizontal above the fourth course (Fig. 13h), which
495 propagated through the entire bed joint ultimately leading to a sliding shear failure.

496 After the test, any damaged bricks were replaced, and the wall was retrofitted “as it stands”
497 using straight vertical and horizontal helical bars (see reinforcement patterns in Fig. 2). The
498 grout was allowed approximately 28 days to cure at room temperature, and then the same wall
499 was then tested as FCI2-R_0.6. Since some of the damage was already accumulated in the wall,
500 the initial stiffness did not increase significantly; the old cracks opened, and some new cracks
501 developed at a drift level of 0.15 % in both loading directions. The horizontal crack appeared

502 again; however, sliding was effectively resisted by the vertical bars resulting in an enhanced
503 rocking capacity and much greater energy dissipation. The in-plane capacity was reached when
504 toe-crushing failure was observed; however, the strength decay was gradual and smooth
505 enabling reaching a 20 % strength loss at +1.75/-1.84 % drift level despite a shear stepped crack
506 developing in the pull direction Fig 13i, Fig.14i).

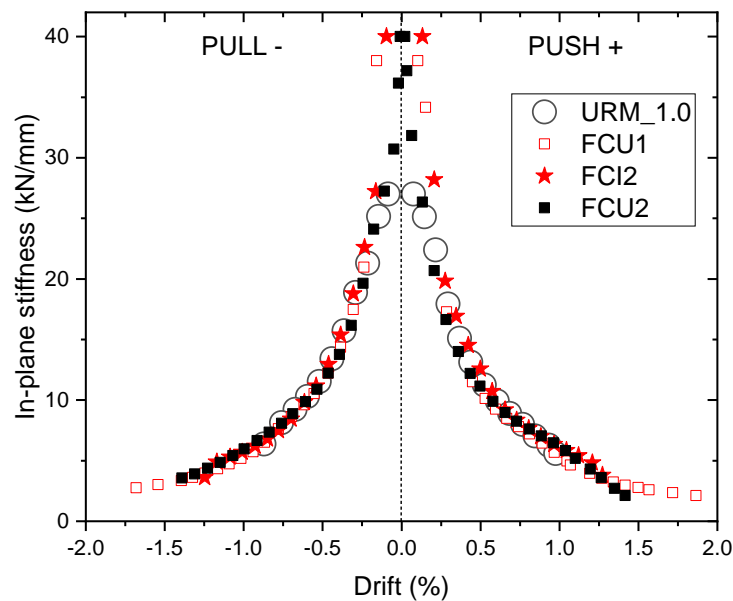
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508 Whilst none of the retrofitting patterns have visibly contributed to the lateral in-plane capacity,
509 the different reinforcing patterns affected the overall cyclic response and post-peak behaviour
510 of the walls. In general, lightly reinforced specimens performed better and showed a more
511 gradual degradation of the lateral capacity. This was seen particularly in the lightly reinforced
512 specimens FCU1_1.0 and FCI2-R_0.6, which exhibited the most gradual failures. Having more
513 reinforcement, specimens FCU2_1.0, FCI2_1.0 and FCI6_1.0 showed more rapid strength
514 degradations, which led to masonry crushing; however, these specimens were still able to attain
515 large drift levels before failure. A more brittle behaviour was recorded for the specimens with
516 only one type of reinforcement SC_1.0 (bed joint) and SCU2_1.0 (vertical), and whilst both
517 specimens exhibited the ability to prevent shear failure, their hysteretic responses clearly show
518 lower energy dissipation capacities.

519 *3.2. In-plane stiffness*

520 The experimental secant stiffness was estimated as the ratio of the total lateral force per
521 direction to the corresponding displacement amplitude. All retrofitted walls exhibited a similar
522 degradation of lateral stiffness, hence, only four specimens are shown for brevity (URM and
523 three RM specimens, Fig. 15). As can be seen, the addition of helical reinforcement somewhat
524 increased the initial in-plane stiffness; however, it did not substantially change the post-
525 cracking stiffness compared to URM_1.0 wall regardless of the retrofitting pattern, and both
526 the “wiggled” and the straight flexural bars yielded a similar response. Although stiffness did

527 not increase, the helical bars allowed for extending the stiffness degradation path and enabled
 528 larger drift levels to be achieved.



529

530 **Fig. 15.** Typical degradation of in-plane stiffness.

531

532 3.3. Definition of yield displacement and ductility factor

533 Owing to their inherent heterogeneity and low deformability, masonry members are
 534 characterised by nonlinear response and lack of a clear yielding point, thus making it difficult
 535 to distinguish elastic and plastic stages of the structural response. Various mathematical
 536 simplifications were proposed and introduced into design codes to simplify the analysis and
 537 idealise the real response using linear approximations, assuming elastic, homogenous and
 538 isotropic global properties of masonry. Current design procedures for masonry members often
 539 recommend using a bilinear elasto-plastic idealisation, which is deemed capable of adequately
 540 representing the simplified response of masonry [6, 47-48]. The bilinear force-displacement
 541 relationships (a typical one is shown in Fig. 16) were obtained from experimental envelopes,
 542 using average values of initial stiffness and ultimate post-peak displacement Δ_{max} corresponding
 543 to about a 25 % loss of strength. Knowing the two mentioned values, the ultimate resistance
 544 V_{ult} can be computed as:

$$V_{ult} = K_e \left(\Delta_{max} - \sqrt{\Delta_{max}^2 - \frac{2A_{env}}{K_e}} \right) \quad (1)$$

545 The elastic stiffness K_e was determined based on experimental data and was taken as a ratio
 546 between the measured experimental lateral load at onset of cracking, V_{cr} , and the corresponding
 547 displacement at cracking, Δ_{cr} . The value A_{env} is the average area under the experimental
 548 envelope curves and represents the total energy dissipated during the test per direction. The
 549 shape of the idealised bilinear response (red curve in Fig. 16) was determined by imposing that
 550 the total energy of the experimental response is equal to the total energy of the bilinear response.
 551 The experimental and idealised characteristics of the in-plane responses are listed in Table 3.
 552 The values obtained from this analysis seem to be consistent with the literature and close to
 553 current design recommendations. The average experimental crack limit was $0.69V_{max}$ (COV 12
 554 %), which is in very good agreement with the limit proposed by Tomažević [6] ($0.70V_{max}$) and
 555 is less conservative than the 40% to 60 % crack limit provisions proposed in key design codes
 556 (EC8 [47], FEMA [48], ASTM [49]). The ratio between the idealised and experimental
 557 maximum shear resistance V_{ult}/V_{max} oscillated around 0.9 (0.89, COV 6 %), which is in line
 558 with the findings of previous studies ([5-6], [12],[50]) and thus attests the validity of the
 559 analysis.

560 The idealised values of the yield displacement, Δ_{el} , and the displacement corresponding to the
 561 25 % lateral load drop, Δ_{ult} , were used to assess the ability of the tested walls to withstand post
 562 elastic deformations. Key structural factors, such as global ductility factors (μ) and behaviour
 563 factors (q) were computed as:

$$\mu = \frac{\Delta_{ult}}{\Delta_{el}} \quad (2)$$

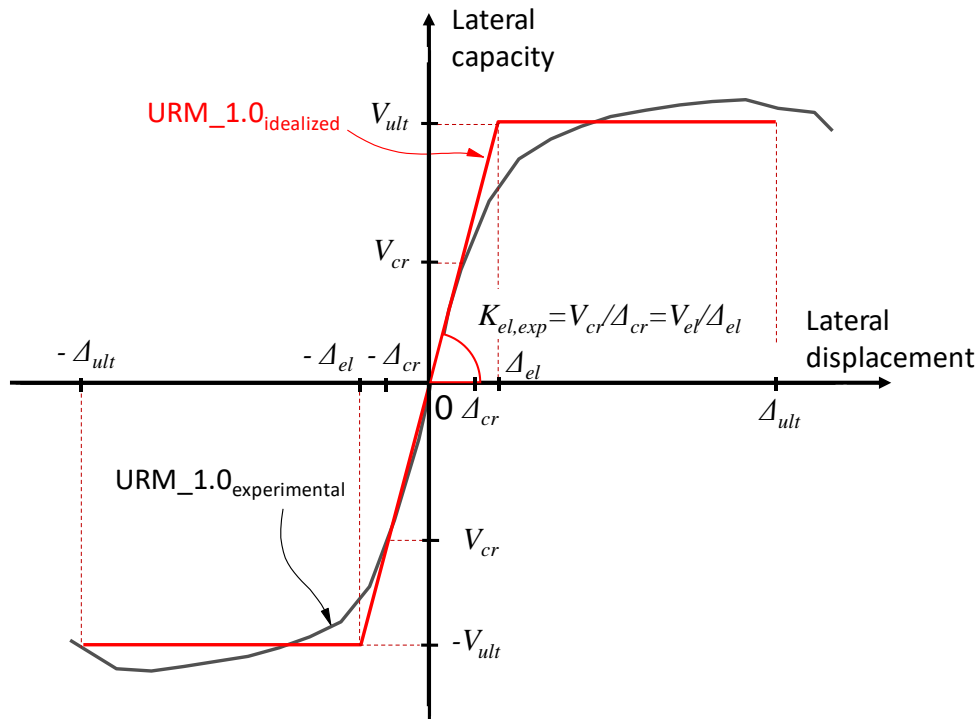
$$q = \sqrt{2\mu - 1} \quad (3)$$

564 Eq. 3 assumes that the fundamental period of the masonry building is in the equal energy region
 565 of the response spectrum. The computed values demonstrate significant improvements in post-

566 peak behaviour (Table 3). For the URM wall, with larger vertical stress, the force reduction
 567 factor was equal to 2.6, which is close to the upper limit for URM walls in accordance with
 568 Eurocode 8. For most of the retrofitted walls the value of q factors exceeded 4.0, which
 569 represents a reduction factor greater than that proposed for reinforced masonry 2.5-3.0, thus
 570 indicating that large gains in ductility have been achieved. Both the test and re-test of the wall
 571 with lower stress level exhibited q factor larger than 4.0 with factors for the re-test equal to 4.5.

572 **Table 3.** Parameters of the idealised elastic and post-elastic behavior; ductility factor and
 573 behavior factor.

ID tag	$K_{el,exp}$ (kN/mm)	V_{ult} (kN)	V_{ult}/V_{max}	crack limit	Δ_{el} (mm)	Δ_{ult} (mm)	μ	q
URM_1.0	27	65.0	0.94	0.65 V_{max}	2.4	9.1	3.8	2.6
FCU1_1.0	38	57.9	0.88	0.60 V_{max}	1.5	14.1	9.3	4.2
FCU2_1.0	40	63.7	0.92	0.69 V_{max}	1.6	13.8	8.7	4.0
SC_1.0	28	61.8	0.93	0.71 V_{max}	2.2	8.6	3.9	2.6
SCU2_1.0	33	63.3	0.90	0.73 V_{max}	1.9	13.2	6.9	3.6
FCI2_1.0	45	63.6	0.92	0.85 V_{max}	1.4	13.3	9.4	4.2
FCI6_1.0	50	56.9	0.80	0.73 V_{max}	1.1	10.7	9.4	4.2
URM_0.6	25	34.7	0.79	0.68 V_{max}	1.4	11.9	8.6	4.0
FCI2-R_0.6	24	42.4	0.95	0.54 V_{max}	1.8	19.1	10.8	4.5

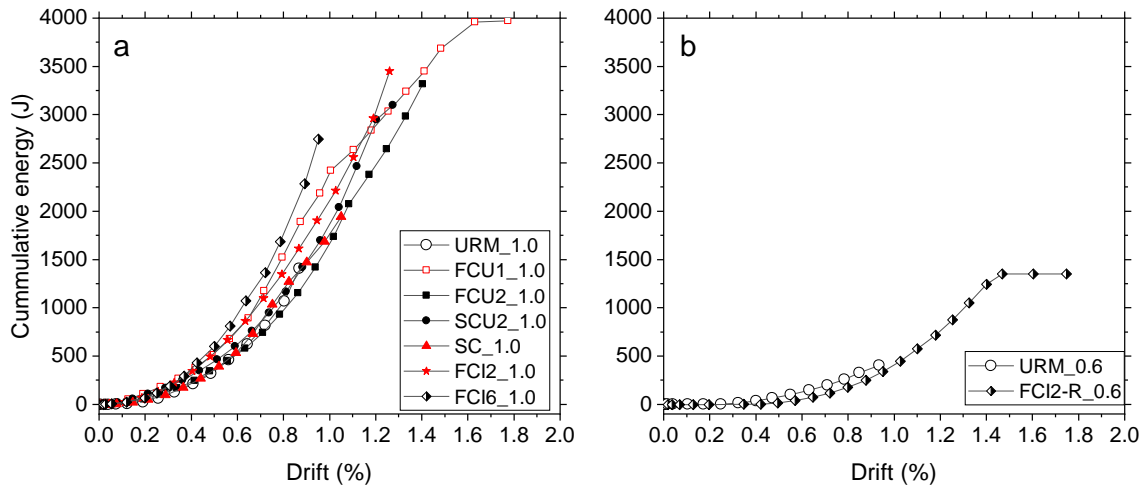


574

575 **Fig. 16.** Typical bilinear idealisation of force-displacement response.

576 3.3. Energy dissipation capacity

577 The cumulative energy dissipated during in-plane testing plotted against average drift in push
578 and pull directions is illustrated in Fig 17. As can be seen, similar energy dissipation capacities
579 were achieved for the walls with a larger axial stress up to drift levels of about 0.4 %, with the
580 poorest energy characteristics exhibited by the URM_1.0 (Fig. 17a). However, as the drift levels
581 increased, the walls with the straight vertical reinforcements (FCI2_1.0 and FCI6_1.0), as well
582 as the wall lightly reinforced with “wiggled” reinforcement FCU1_1.0, showed improved
583 energy dissipation performance compared to the URM wall. Compared to the latter, at a drift
584 of 0.9 %, FCI6_1.0 dissipated about 50 % more energy and about 15 % more was dissipated by
585 FCI2_1.0. At approximately the same drift level, FCU1_1.0 dissipated about 24 % more energy
586 compared to the reference wall, and at ultimate showed the largest energy dissipation capacity.
587 The remaining walls SC_1.0 and SCU2_1.0 showed similar, however, extended energy
588 dissipation paths compared to URM_1.0, indicating that such retrofitting layouts might be less
589 efficient during events like earthquakes, however, can still prolong the structure’s integrity. The
590 repaired and retested wall FCI2-R_0.6 showed more than a twofold increase in energy
591 dissipation at ultimate than during the first test (Fig.17b). Based on the results it can be
592 concluded that up to the maximum drift levels seen in URM, straight bars have a higher
593 potential to dissipate energy than the wiggled bars, however both types of bars are able to
594 prevent brittle collapse of the structure and are able to contribute to the total energy dissipation
595 even beyond the peak lateral load. It is also worth noting that although a limited number of
596 walls was tested, the bars turned out to be more effective in the elements axially loaded to 1.0
597 MPa and dissipated more energy than the walls loaded to 0.6 MPa. The equivalent viscous
598 damping ratio for the retrofitted walls was up to 10% (Fig. 18). As the figure shows, the
599 hysteretic energy dissipation was higher in the case of specimens characterised by higher
600 ductility, i.e., FCU1_1.0, FCI2_1.0, and FCI6_1.0.

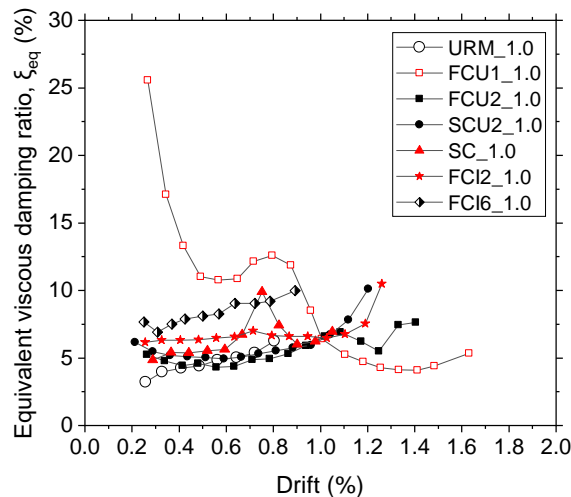


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602 **Fig. 17.** Energy dissipation for increasing drift levels: a – walls specimens with an axial stress

603

level of 1.0 MPa; b – walls with an axial stress level of 0.6 MPa.



604

605 **Fig. 18.** Equivalent viscous damping ratio for walls specimens with an axial stress level of 1.0

606

MPa

607

608 **4. Analytical predictions**

609 The theoretical values of lateral load capacities associated with various failure modes (flexural,

610 shear sliding, diagonal shear) were assessed using Eurocode 6 [51], which also has provisions

611 for steel reinforcement, and hence can be used to estimate, by analogy, the contribution of

612 helical bars to the total lateral load capacity. In the following sections, the contributions of the

613 masonry and reinforcement were determined separately and were then compared with the

614 experimentally derived peak load capacity. For comparing with test results, the safety factors
 615 were not taken into account in the code equations and the measured values of materials
 616 properties reported in section 2.2. were utilised.

617 4.1. Calculations for unreinforced masonry

618 4.1.1. Shear sliding

619 The model adopted in Eurocode 6 code is an extension of the Mohr-Coulomb criterion with an
 620 upper cap. The shear strength of unreinforced masonry is defined as the sum of the initial shear
 621 strength (shear bond at zero compression) and the contribution of the compressive stress
 622 perpendicular to the shear direction through friction. The characteristic shear strength of
 623 masonry at the critical section can be determined from:

$$\tau_{vk,1} = (\tau_{vk0} + \mu\sigma_d) \leq 0.065f_u \quad (4)$$

624 Where τ_{vk0} is the initial shear strength, μ is the coefficient of friction and σ_d is the design
 625 compressive stress. Eurocode 6 recommends $\mu = 0.4$, and, if no experimental data is available,
 626 τ_{vk0} can be assumed from tabulated values between 0.15 MPa and 0.3 MPa, or as recommended
 627 by the appropriate National Annex. The value of τ_{vk} is also limited to 6.5% of the compressive
 628 strength of the masonry unit, f_u , to avoid compression failure in the corners. The associated
 629 horizontal load (shear capacity) can be calculated as:

$$H_{sl} = t \cdot l_c \cdot \tau_{vk,1} \quad (5)$$

630 The experimental shear strength should be determined by taking into account only the length
 631 of the compressed part of the wall, neglecting the part in tension. The length l_c was calculated
 632 assuming linear distribution of compressive stresses (e.g. in [50]) resulting from the
 633 experimental loads. The value t represents the thickness of the wall. Verification of the
 634 experimental and theoretical shear capacities has been carried out using the material
 635 characteristics reported in section 2.2, using experimental values of τ_{vk0} and μ in lieu of the
 636 values recommended by Eurocode 6.

637 4.1.2. Diagonal cracking

638 The approach adopted in Eurocode 6 considers the shear strength of masonry as a main design
 639 parameter, and thus implicitly considers shear sliding as a failure mode that governs the global
 640 shear resistance of the members being designed. Although the procedure for estimating
 641 diagonal cracking is not given in the main sections of the document, such provisions can be
 642 found in the National Annex DIN EN 1991 1-1/NA [52] and this criterion is based on Mann-
 643 Müller model [53]. According to the National Annex, the diagonal cracking strength can be
 644 estimated from:

$$\tau_{vk,2} = 0.45 f_{bt,cal} \sqrt{1 + \frac{\sigma_d}{f_{bt,cal}}} \quad (6)$$

645 Where $f_{bt,cal}$ represents the tensile strength of masonry units. The tensile strength of the units
 646 was not determined experimentally but derived from the flexural tests on masonry (see section
 647 2.2.1). The tensile strength of brick units was calculated as the average reported flexural
 648 strength divided by 1.5, similar as in [54]. As such, $f_{bt,cal}$ was taken as $1.43\text{MPa}/1.5=0.9\text{MPa}$.
 649 As can be seen, this approach assumes that tensile strength governs shear behaviour of the walls
 650 and this model is a variation of the model established by Turnšek and Čačovič [55], which
 651 assumes that URM masonry behaves as an elastic, homogeneous and isotropic material.

652 The horizontal load associated with diagonal cracking strength was calculated as:

$$H_d = t \cdot l \cdot \tau_{vk,2} \quad (7)$$

653 4.1.3. Flexural resistance

654 The flexural resistance was determined based on force equilibrium. The bending moment was
 655 calculated as:

$$M_{Ru} = \frac{\sigma_d t L^2}{2} \left(1 - \frac{\sigma_d}{f_m} \right) \quad (8)$$

656 Where L is the length of the wall, t is the thickness of the wall and f_m is the experimental
 657 masonry strength. The lateral load corresponding to the flexural capacity was calculated as:

$$H_f = \frac{M_{Ru}}{h\alpha} \quad (9)$$

658 where h is the height of the wall and α is 1.0 (for cantilevers).

659 4.2. Calculations for reinforced masonry

660 4.2.1. Steel reinforcement contribution to shear resistance

661 According to Eurocode 6, the reinforcement contribution to shear capacity only comes from
662 bed joint reinforcements, and can be calculated as:

$$H_{str,h} = 0.9A_{sh}f_{yh} \quad (10)$$

663 Where A_{sh} is the total cross-sectional area of horizontal reinforcement and f_{yh} is the allowable
664 stress in the helical steel reinforcement. A_{sh} was assumed as the area of one helical bar (8.3
665 mm²) multiplied by the number of horizontal bars crossing the diagonal crack. Based on the
666 tensile tests, the allowable stress in the helical bars was as the maximum stress at the elastic
667 range, which was limited to 455 MPa (see Fig. 8).

668 4.2.1. Contribution to flexural resistance

669 The lateral flexural capacity was estimated using standard verification Eurocode procedure for
670 reinforced concrete masonry members assuming rectangular stress distribution. The ultimate
671 bending moment was computed as:

$$M_{Ru,v} = A_{sv}f_yz \leq 0.4f_m tL^2 \quad (11)$$

672 Where z is the lever arm of the internal forces. The area A_{sv} represented the total area of the
673 vertical reinforcement installed on one side of the wall. The horizontal load associated with the
674 moment was calculated as:

$$H_{str,v} = \frac{M_{Ru,v}}{h\alpha} \quad (12)$$

675 4.3. Summary of predictions and discussion

676 Results of the predictions are illustrated in Fig. 19, with the experimental-to-theoretical ratios
677 listed in Table 4. Given that mixed failure modes were observed during testing, the contribution
678 of bare masonry was verified against the models for flexural capacities and the two shear
679 capacities (sliding/diagonal cracking) separately. The capacities of the wall specimens

680 retrofitted with helical reinforcement were estimated as the sum of the contributions of
 681 unreinforced masonry and contribution of helical reinforcement. As such, for the flexure-
 682 controlled estimate, the total lateral in-plane capacity consisted of the flexural contribution of
 683 the bare masonry wall (Eq. 9) and the contribution of the vertical helical bars (Eq. 12). The
 684 shear controlled-estimate comprised the component associated with shear resistance of bare
 685 masonry (either Eq. 5 or Eq. 7, depending on the failure mode observed during the experiment)
 686 and the contribution of the horizontal helical bars (Eq. 10).

687

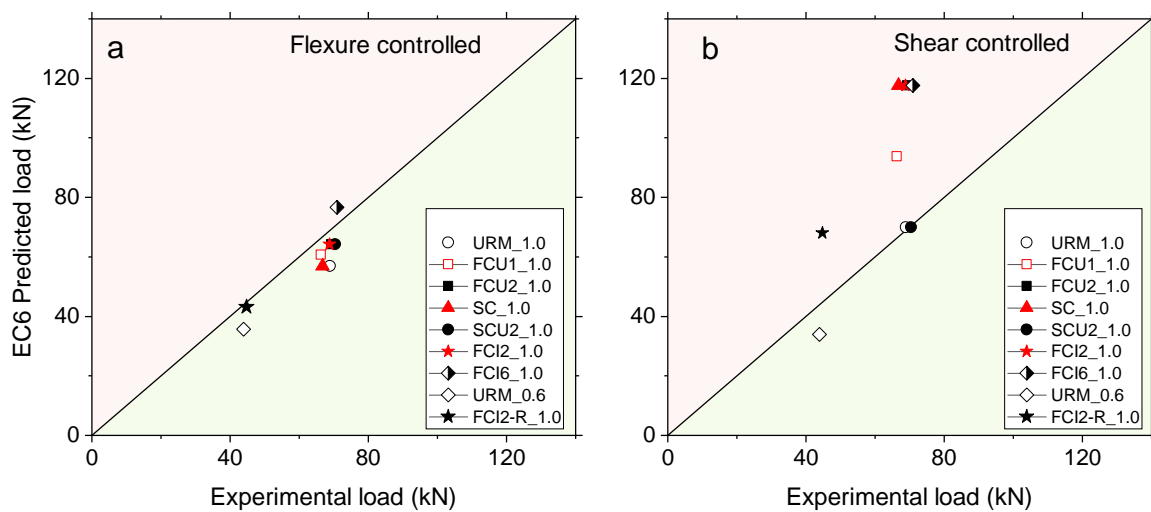
688 **Table 4.** Predictions of lateral load capacity: experimental-to-theoretical ratios

ID tag	V_{max} (kN)	URM			RM	
		Sliding	Diagonal	Flexure	Shear-controlled*	Flexure-controlled
		$V_{max}/Eq.5$	$V_{max}/Eq.7$	$V_{max}/Eq.9$	$V_{max}/(Eq.7+Eq.10)$	$V_{max}/(Eq.9+Eq.12)$
URM_1.0	68.9	1.21	0.99	1.21	-	-
FCU1_1.0	66.2	-	-	-	0.71	1.09
FCU2_1.0	69.3	-	-	-	0.59	1.08
SC_1.0	66.7	-	-	-	0.57	1.17
SCU2_1.0	70.4	-	-	-	1.01	1.10
FCI2_1.0	68.7	-	-	-	0.58	1.07
FCI6_1.0	71.0	-	-	-	0.60	0.93
URM_0.6	43.9	1.29	0.71	1.23	-	-
FCI2-R_0.6	44.7	-	-	-	0.67	1.07

689 * for the walls with vertical stress 0.6 MPa for Eq.5 was used instead of Eq.7, as shear sliding was observed during
 690 the experiments.

691

692



693

694 **Fig. 19.** Predictions of lateral load capacity: a – Predictions associated with flexural failure; b

695

– predictions associated with shear failure.

696 4.3.1. Contribution of masonry

697 Based on the experimental observations on the URM walls, it is evident that both developed
698 extensive flexural damage, which was followed by a shear failure. URM_1.0 failed due to
699 development of a diagonal stepped crack (whilst also exhibiting some cracks through the
700 masonry units), whereas URM_0.6, after significant rocking, eventually failed due to shear
701 sliding. It is worth noting that if rocking occurs first, there are no hardening mechanisms left,
702 which can substantially increase the lateral capacity. Yet, the tests have shown that shear
703 failures followed the rocking response, which indicates that shear resisting mechanisms have
704 been already degraded due to cyclic loading, and hence, the initial shear resistance of the wall
705 degraded too, and shear failure ensued. In turn, although both the URM walls exhibited shear
706 failures, the initial flexural damage effectively limited the lateral in-plane capacity of the test
707 walls, and thus, both checks (flexural and shear) should be carried out. As can be seen, flexural
708 and shear predictions can give reasonable estimates of the in-plane lateral load capacity and
709 confirm the experimental observations. For the failure modes corresponding to experimental
710 observations, the predictions of shear resistance yielded ratios equal to 0.99 for diagonal
711 cracking (URM_1.0) and 1.29 for shear sliding (URM_0.6). The prediction of flexural
712 resistance yielded experimental-to-theoretical ratios equal to 1.21 and 1.23 for URM_1.0 and
713 URM_0.6, respectively. Based on the predictions, it can be concluded that the theoretical shear
714 capacities of the unreinforced cantilever walls were estimated reasonably well using Eurocode
715 6 provisions and the predictions are in a good agreement with the experimental behaviour.

716 4.3.2. Contribution of helical bars

717 As discussed before, helical bars prevented a brittle shear failure and led to the flexural failure
718 associated with significant rocking and toe crushing. The flexure-controlled estimate,
719 combining flexural contribution of bare masonry and the contribution of vertical reinforcement
720 produced consistent and accurate predictions of the total lateral capacity, with average
721 experimental-to-theoretical ratios equal to 1.07 (COV 8 %). It is also worth noting that almost

722 all theoretical predictions (apart from FCI6_1.0, which was slightly overestimated) were on the
723 safe side, even though safety factors were omitted in the calculations. On the other hand, if the
724 walls were deemed shear-critical, and shear contribution of masonry is coupled with
725 contribution of the bed joint bars, the EC6 provisions led to overestimation of the total lateral
726 load capacity with average experimental-to theoretical ratios equal to 0.67 and large scatter in
727 the predicted values (COV 26 %). This can be mainly attributed to the lack of extensive diagonal
728 cracking in the retrofitted specimens and thus lower engagement of the bed joint reinforcement
729 during the tests. The addition of helical reinforcement prevented shear failure; however, flexural
730 failure occurred shortly thereafter without any significant contribution to the lateral capacity.
731 Such mixed failure modes are typical for cantilevered masonry structures, therefore, for design
732 purposes, verification of the lateral resistance in reinforced cantilever walls should be carried
733 out analysing both shear and flexural behaviour and the minimum resistance should be used in
734 the design.

735 It becomes evident that, despite having a beneficial effect on the ductility, helical bars did not
736 substantially contribute to the lateral load resistance of cantilever masonry walls; similar results
737 have been reported in other studies [26] dealing with near-surface mounted bed joint steel
738 reinforcement. However, the presence of vertical “wiggled” or straight bars or even bed joint
739 bars alone was sufficient to effectively control shear cracking in the walls and prevent brittle
740 failure, which can greatly improve the safety of the masonry structures during seismic events.
741 Due to their flexibility and relatively high tensile capacity, the use of helical bars improved the
742 post-peak in-plane behaviour allowing reinforced masonry to undergo larger drift levels and
743 dissipate more hysteretic energy. Being able to accommodate larger displacement demands the
744 retrofitted walls showed that ductility improved by up to 146 % compared to the reference
745 walls. This also resulted in behaviour factors larger than 4.0, which exceeds typical factors for
746 reinforced masonry and seem to be in similar range to the factors derived for retrofitted masonry

747 (e.g. [22]), however, this observation should be treated with caution as this very much depends
748 how the yield displacement of the wall is defined.

749 **5. Conclusions**

750 The paper investigated, for the first time, the potential of helical bars as seismic reinforcement
751 for unreinforced masonry piers. A total of nine masonry cantilever walls were subjected to
752 quasi-static cyclic loading until failure or a load drop associated with about 25 % load drop.
753 Various retrofitting layouts were investigated, exploring the use of horizontal and vertical
754 straight and vertical “wiggled” bars (a novel type of combined horizontal and vertical
755 reinforcement feasible due to the flexibility of the helical bars) as well as bed joint bars. The
756 experimental results were assessed in terms of strengthening efficiency, ductility, and energy
757 dissipation; and were verified using Eurocode 6 provisions for masonry structures. Based on
758 the experiments and analysis discussed above, the following conclusions can be drawn:

- 759 • Tensile tests showed that 6 mm helical bars have different characteristics than regular
760 steel bars. Due to the specific production process, helical reinforcement can undergo
761 larger deformations whilst maintaining relatively large stress levels, and the stress-strain
762 relationship is characterised by a not well-defined yield point. The tests revealed an
763 average tensile strength equal to 1181 MPa, 0.2% proof strength of 917 MPa and elastic
764 range limit at a level of about 455 MPa. This greatly exceeds the typical stress levels in
765 standard 6 mm steel rebars, which usually start yielding at stress levels around 500 MPa
766 at 0.2 % deformation.
- 767 • Having initially experienced rocking at the base, the cantilever URM walls subsequently
768 failed in shear and the hysteretic response showed a very limited capacity to dissipate
769 energy. The wall with higher vertical stress level exhibited diagonal shear cracks in both
770 loading directions, whereas the wall with lower stress level, after significant rocking,
771 failed by shear sliding (showing also signs of diagonal cracking). The walls retrofitted
772 with helical bars did not exhibit shear failure, but a more controlled flexural failure

773 related to rocking, which was terminated by compressive capacity of the bricks in the
774 toe regions.

775 • Although the retrofitting with helical bars prevented brittle shear failure, the walls failed
776 in flexure at similar lateral load levels to the URM counterparts indicating that helical
777 bars did not contribute much to the overall strength of the walls. However, the post peak
778 performance of the retrofitted walls was significantly improved, and some residual
779 lateral load capacity was maintained.

780 • The primary contribution of the helical reinforcement was to the deformation capacity;
781 the walls reinforced with helical bars exhibited larger ductility than the URM walls and
782 developed a more controlled and gradual failure. The behaviour factors for most of the
783 retrofitted walls exceeded 4.0, which is significantly greater than typical q factors for
784 URM walls specified in Eurocode. Hence, such a retrofitting system has the potential to
785 offer additional deformation capacity to the masonry and maintain the integrity of the
786 walls, even when severe in-plane damage is developed. Concluding, the use of helical
787 bars has the potential to increase the life-safety performance of the masonry structures
788 during seismic actions without much interference in the aesthetics of masonry.

789 • The Eurocode 6 provisions and experimentally-derived material characteristics were
790 sufficient to reasonably predict the lateral load capacity of URM and retrofitted walls.
791 The diagonal cracking and shear sliding failures were predicted with experimental-to-
792 theoretical ratios equal to 0.99 and 1.29, respectively. The flexural failure of retrofitted
793 walls was estimated considering flexural contributions of masonry and helical
794 reinforcement and resulted in an average ratio of 1.07 suggesting that Eurocode 6
795 provisions can be directly applied for load capacity estimations, although they do not
796 explicitly account for the effects of cyclic degradation.

797

798

799 **6. Future research**

800 It is believed that the true potential of stainless-steel helical bars for as a seismic
801 reinforcement was not fully explored in this study due to the fact that only cantilevers were
802 investigated, and such structures do not usually show extensive shear cracking, and
803 therefore, do not fully engage horizontal reinforcement. Past research studies on masonry
804 wallettes with bed joint helical bars [36-37, 54] demonstrated that helical bed reinforcement
805 can be very effective in bridging diagonal cracks and can lead to a substantial increase in
806 shear strength and in-plan deformation capacity. It is deemed that future research on the use
807 of helical reinforcement for seismic retrofitting should focus on cyclic static and dynamic
808 tests on masonry piers and spandrels with fixed-fixed boundary conditions, which more
809 accurately represent shear-critical masonry piers during earthquakes. In such tests, a more
810 pronounced diagonal cracks can be developed, and hence, a better engagement, and thus, a
811 higher utilisation of bed joint helical reinforcement is expected. Nevertheless, helical
812 reinforcement has a clear potential to preserve integrity of the structure and increase safety
813 of masonry buildings during earthquakes with minimum installation efforts and without
814 changing visual aesthetics of the walls.

815

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820

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