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We performed large-eddy simulations of the flow over a series of three-dimensional (3D) dunes at laboratory scale. The bedform three-dimensionality was imposed by shifting a standard two-dimensional (2D) dune shape in the streamwise direction according to a sine wave. The turbulence statistics were discussed in Part 1 of this article [M. Omidyeganeh, U. Piomelli, J. Fluid Mech. 721, pp. 454–483, (2013)]. Coherent flow structures and their statistics are discussed concentrating on two cases with the same crestline amplitudes and wavelengths but different crestline alignments: in-phase and staggered. The present paper shows that the induced large-scale mean streamwise vortices are the primary factor that alters the features of the instantaneous flow structures. Wall turbulence is insensitive to the crestline alignment; alternating high- and low-speed streaks appear in the internal boundary layer developing on the stoss side, whereas over the node plane (the plane normal to the spanwise direction at the node of the crestline), they are inclined towards the lobe plane (the plane normal to the spanwise direction at the most downstream point of the crestline) due to the mean spanwise pressure gradient. Spanwise vortices (rollers) generated by Kelvin-Helmholtz instability in the separated shear-layer appear regularly over the lobe with much larger length scale than those over the saddle (the plane normal to the spanwise direction at the most upstream point of the crestline). Rollers over the lobe may extend to the saddle plane and affect the reattachment features; their shedding is more frequent than in 2D geometries. Vortices shed from the separated shear-layer in the lobe plane undergo a three-dimensional instability while advected downstream, and rise toward the free surface. They develop into a horseshoe shape (similar to the 2D case) and affect the whole channel depth, whereas those generated near the saddle are advected downstream and toward the bed. When the tip of such a horseshoe reaches the free surface, the ejection of flow at the surface causes “boils” (upwelling events on the surface). Strong boil events are observed on the surface of the lobe planes of 3D dunes more frequently than in the saddle planes. They also appear more frequently than in the corresponding 2D geometry. The crestline alignment of the dune alters the dynamics of the flow structures, in that they appear in the lobe plane and are advected towards the saddle plane of the next dune, where they are dissipated. Boil events occur at a higher frequency in the staggered alignment, but with less intensity than in the in-phase alignment.

1. Introduction

The stable, unidirectional flow over mobile sand river beds usually results in large-scale bed deformations called dunes (Yalin 1964; Allen 1968; van Rijn 1984). Dunes
have a crestline, generally normal to the flow direction, followed by a steep downward slope (the lee side), and then by a more gradual upward slope (the stoss side). Although two-dimensional transverse dunes (in which the crestline is straight and normal to the flow) regularly exist in pure oscillatory flows (Allen 1968), they appear occasionally in unidirectional flows in rivers and laboratory flumes for a short period of time (Venditti et al. 2005); most dunes generated in unidirectional flows have sinusoidal or irregular crestlines (Ashley 1990). The flow separates at the crest and reattaches at the beginning of the stoss side (Kostaschuk 2000). Note that in large sand-bed alluvial channels dunes may possess low-angle lee side and intermittent separation of the flow at the crest (Roden 1998; Best & Kostaschuk 2002); here we study typical dune models with an angle of repose slip face where the flow permanently separates at the crest (Roden 1998; Kostaschuk 2000). In the first part of this paper (Omidyeganeh & Piomelli 2013), the past research on two- and three-dimensional dunes was reviewed, and thus here we limit ourselves to a brief summary.

The main features of the flow over dunes are flow separation at the crest and the resulting separated shear-layer, the recirculation region, and the downstream developing internal boundary layer. Each of these generates a variety of coherent structures with a broad range of length- and time-scales. Detailed investigation of the turbulent structures has revealed the importance of Kelvin-Helmholtz instability of the shear layer, which causes large-scale eddies (with length-scales comparable to the river depth; Kostaschuk & Church (1993); Bennett & Best (1995); Omidyeganeh & Piomelli (2011)). Very large structures contribute significantly to the transport of mass and momentum (Babakai & Hickin 1996; Lapointe 1996; Best et al. 2001). Correlations between the ejection events over the lee side of dunes and suspended sediments, measured in the experiments (Lapointe 1996; Schmeeckle et al. 1999; Shugar et al. 2010), showed the contribution of separated vortices to the sediment transport. Lapointe (1996) showed that most of the sediment suspensions in rivers are due to turbulent ejection events.

These large eddies are often associated with “boils”, i.e., upwellings at the water surface that occur when a horizontally oriented vortex reaches the surface (Matthes 1947). Various conjectures were advanced to explain their occurrence (Jackson 1976; Müller & Gyr 1986; Nezu & Nakagawa 1993; Kadota & Nezu 1999; Best 2005a); Omidyeganeh & Piomelli (2011) confirmed the conjectures by Müller & Gyr (1986) and Best (2005a) and showed that they are due to horseshoe vortices of size comparable to the flow depth originating in the separated-shear layer.

While much research has concentrated on 2D dunes, fewer investigations have considered the effects of crestline three-dimensionality. The mean flow has been studied experimentally (Allen 1968; Maddux et al. 2003b,a; Venditti et al. 2005; Venditti 2007) and numerically (Omidyeganeh & Piomelli 2013). Although some features of the flow are common with the flow over 2D dunes (e.g., the separation at the crest, reattachment on the bed, and deceleration/acceleration over the lee/stoss side), the 3D mean flow significantly alters the turbulence characteristics. Secondary vortices with sizes comparable to the flow depth are generated, and observations of these motions have been reported over the last century (Gibson 1909; Vanoni 1946; Karcz 1966; Kinoshita 1967). These secondary vortices have been related to the surface concentration of suspended sediment, which varied in the spanwise direction, with higher concentrations in the upwash regions of these vortices (Karcz 1966). Two counter-rotating streamwise vortices occur next to each lobe (the most downstream point on the crestline), and direct low-momentum fluid near the bed upwards and high-momentum fluid over the saddle (the most upstream point on the crestline) downwards. These motions are generated by the spanwise gradient of the pressure on the bed (secondary currents of Prandtl’s first kind (Bradshaw

Characteristics of the secondary currents and their impact on the channel resistance, water surface response, and turbulence statistics were investigated by Maddux et al. (2003b,a) for crestlines that are staggered (i.e., each lobe is followed by a saddle, and vice-versa), and by Venditti (2007) for in-phase crestlines.

Omidyeganeh & Piomelli (2013) compared in-phase and staggered alignments, and also considered different amplitudes and wavelengths of the crestlines. They studied the sensitivity of the flow field to the crestline parameters (deformation amplitude, wavelength, and alignment) by performing a numerical study of 3D dunes created by shifting a standard 2D dune shape (Omidyeganeh & Piomelli 2011) in the streamwise direction according to a sine wave. The statistics of the flow were discussed. The three-dimensional flow separation at the crestline was found to alter the distribution of wall pressure; near the bed, fluid is directed from the saddle toward the lobe and near the flow surface the direction of flow is reversed. This results in the counter-rotating streamwise vortices straddling the lobe plane. These features of the mean flow are shown in Figure 2 and are discussed briefly in Results. For crest wavelengths smaller than the flow depth, however, the secondary flow exists only near the bed and the mean flow away from the bed resembles the two-dimensional case. Staggering the crestlines alters the secondary motion; the fastest flow occurs between the lobe and the saddle planes, and two pairs of streamwise vortices appear (a strong one, centred about the lobe, and a weaker one, coming from the previous dune, centred around the saddle). The sensitivity of the average reattachment length, which depends on the induced secondary flow, the streamwise and spanwise components of the channel resistance (the skin friction and the form drag), and the contribution of the form drag to the total resistance were also studied: the three-dimensionality of the bed increases the drag in the channel; the form drag contributes more than in the two-dimensional case to the resistance, except for the staggered-crest case. Turbulent-kinetic energy is increased in the separated-shear layer by the introduction of three-dimensionality. The upward flow on the stoss side and higher deceleration of flow on the lee side over the lobe plane lift and broaden the separated shear-layer, respectively, affecting the turbulent kinetic energy.

Turbulent structures are responsible for sediment transport over bedforms (Lapointe 1996; Schindler & Robert 2005); their importance in an open channel flows with smooth and rough beds on the sediment transport mechanism has been discussed in the literature (Sutherland 1967; Jackson 1976; Best 1992; Kaftori et al. 1995a,b; Nino & Garcia 1996). Ejections may persist for a long time and lift up the sediment. If the wall-shear stress increases, more particles are entrained in the outer region of the flow, especially over rough beds (Nino & Garcia 1996). The inrush of high-momentum fluid into the bed (sweep events) coalescing with surrounding events, on the other hand, may cause a small defect on the bed (Best 1992) and grow to a large-scale deformation. Despite the importance of wall-turbulence and of sweeps and ejections near the bed, and their impact on the bed deformation, their dynamics have not yet been studied in depth.

The field observations of Parsons et al. (2005) highlight the importance of 3D bedforms for flow structures and sediment transport; secondary flows over saddle- or lobe-shaped crestlines were observed to direct the downstream bed morphology and sediment-suspension mechanism in the flow. Moreover, the distribution of coherent structures in the bulk flow, especially horseshoe vortical structures that interact with the free surface and cause strong boil events and their statistics have to be studied.

The importance of 3D dunes in controlling flow resistance, sediment transport, and turbulent structures demands further investigation of the flow mechanics. The effects of their geometry on the dynamics of vortical structures responsible for important events such as boils are not completely understood. In addition to the relation between boundary
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shear stress and turbulence statistics with three-dimensionality of dunes, the relation of instantaneous features of vortical structures to the geometrical parameters of 3D dunes must be studied to explore the geometry mechanics and channel resistance in rivers, and to understand bed deformation mechanism (Best 2005a). In the first part of this article (Omidyeganeh & Piomelli 2013), we performed a controlled investigation of simple sinuous crestline deformations and analyzed the effect of geometrical parameters of the crestline on the mean-flow characteristics. Here, in the second article, we study the effect of the three-dimensionality on the turbulent structures near the bed, in the separated-shear layer, and in the bulk flow. The present qualitative and quantitative analysis on these coherent structures will provide insights on the boil events at the free surface.

In the following, we begin by reviewing the numerical model. We then present visualizations and statistical measures of turbulent eddies, first in the near-wall region, then in the separated shear layer. A discussion of the effect of crestline deformation on the generation of boils will follow. Finally, we will draw some conclusions and make recommendations for future work.

2. Problem formulation

In large-eddy simulations, the velocity field is separated into a resolved (large-scale) and a subgrid (small-scale) field, by a spatial filtering operation (Leonard 1974). The non-dimensional continuity and Navier-Stokes equations for the resolved velocity field are

\[
\frac{\partial \overline{u_i}}{\partial x_i} = 0
\]

\[
\frac{\partial \overline{u_i}}{\partial t} + \frac{\partial \overline{u_i u_j}}{\partial x_j} = -\frac{\partial \overline{P}}{\partial x_i} - \frac{\partial \tau_{ij}}{\partial x_i} + \frac{1}{Re_b} \frac{\partial^2 \overline{u_i}}{\partial x_i \partial x_j}
\]

where \(Re_b = U_b H_b / \nu\), \(H_b\) is the average channel depth, and \(U_b\) is the bulk velocity at the streamwise location where the channel depth is equal to the average channel depth \((x \approx 14h)\). \(x_1\), \(x_2\) and \(x_3\) are the streamwise, vertical and spanwise directions, also referred to as \(x\), \(y\) and \(z\). The velocity components in these directions are, respectively, \(u_1\), \(u_2\) and \(u_3\) (or \(u\), \(v\) and \(w\)). An overline denotes a filtered quantity, and \(\tau_{ij} = \overline{u_i u_j} - \overline{u_i} \overline{u_j}\) are the subgrid stresses, which were modeled using an eddy-viscosity assumption

\[
\tau_{ij} - \delta_{ij} \tau_{kk}/3 = -2\nu_T \overline{S_{ij}} = -2C \frac{\overline{S}}{\overline{S}} \overline{S_{ij}}.
\]

Here, \(\overline{S} = 2 (\Delta x \Delta y \Delta z)^{1/3}\) is the filter size, \(\overline{S_{ij}} = (\partial \overline{u_i} / \partial x_j + \partial \overline{u_j} / \partial x_i) / 2\) is the resolved strain-rate tensor and \(|\overline{S}| = (2 \overline{S_{ij} \overline{S_{ij}}})^{1/2}\) is its magnitude. The coefficient \(C\) is determined using the dynamic model (Germano et al. 1991) with the Lagrangian averaging technique proposed by Meneveau et al. (1996), and extended to non-Cartesian geometries by Jordan (1999) and Armenio & Piomelli (2000).

The governing differential equations (2.1) and (2.2) are discretized on a non-staggered grid using a curvilinear finite-volume code. The method of Rhie & Chow (1983) is used to avoid pressure oscillations. Both convective and diffusive fluxes are approximated by second-order central differences. A second-order-accurate semi-implicit fractional-step procedure (Kim & Moin 1985) is used for the temporal discretization. The Crank-Nicolson scheme is used for the wall-normal diffusive terms, and the Adams-Bashforth scheme for all the other terms. The pressure is obtained from the solution of a Poisson equation, which is discussed in Omidyeganeh & Piomelli (2013). The code is parallelized using the Message-Passing Interface and the domain-decomposition technique, and has been

Figure 1. (a) Sketch of the physical 3D dune configuration. The sine function that is superimposed into 2D dune configuration is $A \sin(2\pi z/\lambda)$, where $\lambda$ is the wavelength (here $\lambda = 16h$) and $A$ is the amplitude (here $A = 2h$), and (b) bed geometry.


A full description of the geometry and 3D parameters of the crestline (amplitude $A$ and wavelength $\lambda$) can be found in Omidyeganeh & Piomelli (2013). The computational configuration is sketched in Figure 1. Periodic boundary conditions are used in the streamwise ($x$) and spanwise ($z$) directions. The flow is driven by a pressure gradient that maintains a constant streamwise flow-rate in time. The top surface is assumed to be rigid and free of shear stress: the vertical velocity is set to zero, as are the vertical derivatives of the streamwise and spanwise velocity components. The surface deformation is reported to be small, less than 2% of the flow depth in experiments (McLean et al. 1994; Kadota & Nezu 1999; Maddux et al. 2003a,b) and simulations (Yue et al. 2006; Stoesser et al. 2008) of 2D and 3D dunes, and it was shown that the free surface response to the 3D dune bed is 2D (Maddux et al. 2003b; Omidyeganeh & Piomelli 2013). Therefore, the free-slip condition is expected to have small effects on the statistics and on the evolution of significant structures. The Reynolds number is $18,900$ based on the $H_b \simeq 3.5h$ and $U_b$ defined above.

An orthogonal mesh in the $xy$–plane is generated using a hyperbolic grid-generation technique. This mesh is then repeated in the spanwise direction with non-uniform spacing, superimposed with a sine function shift, $A \sin(2\pi z/\lambda)$, in the streamwise direction. We modified the Poisson solver to address the curvature of grid lines in the spanwise direction as discussed in Omidyeganeh & Piomelli (2013).

Omidyeganeh & Piomelli (2013) showed that the crestline alignment significantly alters the physics of the flow, such as the secondary streamwise vortices, while different amplitudes and wavelengths of the crestline only quantitatively change the characteristics, except for crestline wavelengths lower than the flow depth in which the secondary currents are confined to the near bed area. Hence, in the present study we concentrate on three cases: two have different crestline alignments but the same amplitude and wavelength, the third has a much lower wavelength. Table 1 lists these test cases; their names are equivalent to Table 1 in Omidyeganeh & Piomelli (2013). Case 11, however, is a
Table 1. Properties of the test cases. For the definition of the variables $\lambda$ and $A$ refer to the caption of Figure 1. NDS is defined as a non-dimensional span number, NDS=$L_c/L_y$ (Venditti et al. 2005), where $L_c$ is the crestline length and $L_y$ is the linear distance between the crest endpoints. Wall units are defined based on the local wall-shear velocity, $u_\tau$, and the kinematic viscosity, $\nu$.

<table>
<thead>
<tr>
<th>Case No.</th>
<th>$\lambda/h$</th>
<th>$A/h$</th>
<th>NDS</th>
<th>$\Delta n_{\text{avg}}^+$</th>
<th>$\Delta z_{\text{avg}}^+$</th>
<th>Alignment</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>8.0</td>
<td>1.0</td>
<td>1.14</td>
<td>15.0</td>
<td>0.7</td>
<td>13.5 in-phase</td>
</tr>
<tr>
<td>9</td>
<td>4.0</td>
<td>1.0</td>
<td>1.46</td>
<td>22.4</td>
<td>0.7</td>
<td>25.9 in-phase</td>
</tr>
<tr>
<td>11</td>
<td>8.0</td>
<td>1.0</td>
<td>1.14</td>
<td>17.9</td>
<td>0.7</td>
<td>15.1 staggered</td>
</tr>
</tbody>
</table>

Figure 2. Contours of mean streamwise vorticity, $\Omega_x h/U_h$, for (a) Case 5 and (b) Case 11 on crossplanes at $x/h = 2.0, 7.0, 12.0, 17.0, 22.0, 27.0,$ and $32.0$. Arrows show the mean secondary flows. “L” represents the lobe and “S” represents the saddle.

new simulation; its mean-flow characteristics are similar to Case 10 in Omidyeganeh & Piomelli (2013), which had, however, a smaller wavelength.

The number of grid points per dune in Case 5 is $384 \times 128 \times 384$ and in Case 11 is $320 \times 128 \times 320$; these numbers are higher than those used in our previous simulation of 3D dunes (Omidyeganeh & Piomelli 2013), to obtain higher resolution for the visualization of coherent structures. In Case 9, the same grid used in Omidyeganeh & Piomelli (2013) is employed, with $256 \times 96 \times 256$ points. The average grid spacings for each case are also included in Table 1, illustrating very good resolution for a typical LES. Validation of the numerical model and grid-convergence of the results are discussed in Omidyeganeh &
Piomelli (2013). Note that the computational domain for Case 11 has two dunes in series in the streamwise direction with 180° phase shift in the cosine function of the crestline.

The equations were integrated for $500h/U_b$ time units to remove transient effects. Then, statistics were accumulated over $1200h/U_b$ time units, equivalent of 60 flow-through times. To increase the sample size, averaging was also performed over the symmetric points in the spanwise direction. To verify the adequacy of the sample, we compared statistics obtained using only half of the sample with those obtained using the complete sample, and found that the mean velocities differed by less than 1%, and the root-mean-square (rms) intensities by less than 5%.

3. Results

It is useful to recall here that the mean secondary flow induced by the crestline curvature significantly alters the characteristics of the separated shear-layer at the crest (Omidyeganeh & Piomelli 2013); low-momentum fluid, near the bed, moves towards the lobe plane over the stoss side of the dune (Figure 2); the alignment of the crestlines does not affect this feature. However, the bulk flow is affected by both the crestline curvature and its alignment: if the crestline are in-phase, high-momentum fluid converges towards the saddle plane and sweeps towards the bed; in the staggered alignment, high-momentum fluid converges to a line between the saddle and the lobe planes (Figure 2(b)). The wavelength of the crestline also affects the secondary flow characteristics; Case 11, which has half the wavelength of Case 10, has weaker streamwise vortices around the saddle plane of the downstream dune; Case 9 with the smallest wavelength has no streamwise vortices in the bulk flow (Figures 8 and 18 in Omidyeganeh & Piomelli (2013)).

Figure 3 shows instantaneous coherent structures in Case 5, visualized by isosurfaces of $p'$ and $Q$, the second invariant of the velocity-gradient tensor (Chong et al. 1990),

$$ Q = \frac{1}{2} \frac{\partial u_i}{\partial x_j} \frac{\partial u_j}{\partial x_i} $$

and coloured by distance from the bed. $Q$ isosurfaces are shown hereafter to illustrate population of structures in the separated-shear layer and the internal boundary layer. Some features of large-scale vortical structures (shown by $p'$ isosurfaces) are similar to those in the flow over 2D dunes (Omidyeganeh & Piomelli 2011). The separated shear-layer rolls up and generates a spanwise-oriented structure, a roller (Region 1 in Figure 3), which may undergo a three-dimensional instability, interact with surrounding vortices and deform to a horseshoe-like structure like the one in Region 2. After the reattachment of the flow, on the stoss side, structures generally lose their energy and coherence; population of structures over the stoss side significantly drops in the figure. This is also shown by small-scale wall turbulence structures, highlighted by $Q$ isosurfaces in Figure 3 (Region 3). We rarely observe strong coherent structures close to the surface; however, there is a weak signature of such a vortex in Region 4. In the next sections we will discuss these flow features in depth, and quantify their characteristics.

Coherent structures in the flow over low wavelength crestline curvatures, e.g. Case 9 (Figure 4), have similar shape and length scales as Case 11 at larger crestline wavelengths than the flow depth. The regions encircled in black show two large vortices in the separated shear layer, which have scales comparable to the flow depth and the crestline wavelength; they appear at random spanwise locations and not over the lobe, as is characteristic in Cases 5 and 11 (will be discussed later). Coherent structures rarely rise and reach the free surface; the region encircled by white in Figure 4 is an example of such an event. In general, sinusoidal crestlines reported in nature have wavelengths
Figure 3. Instantaneous flow structures for the in-phase crestline alignment, Case 5. Isosurfaces of pressure fluctuations $p'/\rho U_b^2 = -0.061$ are coloured by the distance from the bed with rainbow colormap and isosurfaces of the second invariant of the velocity tensor, $Qh^2/U_b^2 = 5.29$, are coloured by the distance from the bed with grayscale colormap.

larger than the flow depth (Allen 1968; Gabel 1993); for this reason in the following we will concentrate on Cases 5 and 11, and mention Case 9 only when necessary.

3.1. Near-wall turbulence

Streamwise velocity fluctuations, $u'$, in a plane located $0.05h$ above the bed (the distance to the bed in wall units is $n^+ \approx 15$), are shown in Figure 5. After flow separation at the crestline, over the lee side, low values of $u'$ are observed because of the separation and the bed inclination ($u'$ is nearly normal to the wall here); in the recirculation zone, the contours of $u'$ are mostly oriented in the spanwise direction, due to the separated eddies in the shear layer leaving their footprints on the wall turbulence. Flow reattachment occurs on the stoss side around the solid line, which represents the mean reattachment line. Further downstream the internal boundary layer develops, and longitudinal high- and low-speed streaks are observed; the flow acceleration resulting from the favourable pressure gradient over the stoss side elongates the streaks.

High- and low-speed streaks are not uniformly distributed over the wall; clumps of several high-speed streaks can be observed, alternating with clumps of low-speed ones. In 2D dunes this preferential concentration was due to the presence of Görtler-like vortices generated on the stoss side, which is concave (Omidyeganeh & Piomelli 2011). A similar mechanism originates it in this case. Figure 6 shows the secondary-flow streamlines and vertical velocity fluctuations; the secondary velocity was averaged over a short time, approximately $20h/U_b$, to visualize better the large vortices, which tend to meander. Note that three pairs of vortices are observed both for the staggered and the in-phase crestline alignments, giving a wavelength of approximately $5h$ (a result confirmed by the spanwise

Figure 4. Instantaneous flow structures for the in-phase crestline alignment, Case 9. Isosurfaces of pressure fluctuations \( p' / \rho U_b^2 = -0.061 \) are coloured by the distance from the bed with rainbow colormap and isosurfaces of the second invariant of the velocity tensor, \( Qh^2 / U_b^2 = 5.29 \), are coloured by the distance from the bed with grayscale colormap.

two-point correlations of velocity, not shown). In Figure 5 we also show the regions of upwash due to the presence of streamwise vortices, generated by the spanwise pressure gradient at the wall and discussed in Omidyeganeh & Piomelli (2013). We note very little correlation between the upwash regions and the concentrations of low-speed streaks, and only a slight one between the downwash (located immediately next to the upwash region) and the high-speed streaks. This indicates that the preferential concentration of streaks is not due to the large secondary motions, but to the Görtler vortices.

To quantify the dimensions and features of the structures near the bed, we examined the auto-correlation coefficients of the streamwise velocity fluctuations, \( u' \), at several points on the plane shown in Figure 5(a). The correlation is defined as

\[
R_{uu}(x, z; \Delta x, \Delta z) = \frac{\langle u'(x, z)u'(x + \Delta x, z + \Delta z) \rangle}{\langle u'(x, z)u'(x, z) \rangle},
\]

where the averaging is performed in time and over symmetric points.

The 2D spatial correlation coefficients and the mean-flow streamlines tangential to the plane are shown in Figure 7 for Case 5. Immediately after flow separation, the eddies are more elongated in the direction normal to the mean streamlines (Figures 7(a,d,g)); the vortices are strongly correlated and narrower in the lobe plane than in the node and the saddle planes. The dominant structures over the lobe and the saddle are symmetric and parallel to the crestline (as expected). In the node plane (Figure 7(d)), the structures are more elongated towards the saddle plane, i.e., in the direction opposite to the lee-side slope; the spanwise gradient of the streamwise velocity is responsible for tilting the eddies forward on the side of the saddle, where the fluid is faster. Close to the mean reattachment
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Figure 5. Instantaneous streamwise-velocity fluctuations, $u'$, on a plane 0.05$h$ above the bed; (a) Case 5; (b) Case 11; (c) Case 9. Solid lines are contours of $\langle u \rangle = 0.0$ representing the mean separation and reattachment lines. The ovals highlight regions in which the streamwise vortices cause upwash.

Figure 6. Secondary-flow streamlines in the $yz$-plane at $x = 15h$, superposed on the contours of short time-averaged wall-normal velocity fluctuations for (a) Case 5 and (b) Case 11. The lobe planes are at $z/h = 2.0$ and 10.0, while the saddle planes are located at $z/h = 6$ and 14.

line, Figures 7(b,e,h), contours of the correlation become small and rounded, showing no directional preference; structures in this zone may be advected from the separated shear layer, or originate from wall turbulence. This behaviour is characteristic of reattachment regions, as also shown by Le et al. (1997) in their backward-facing step calculations. On the stoss side and in the internal boundary layer (Figures 7(c,f,i)) the correlations have the characteristics of attached boundary layers: the eddies are elongated in the direction

Figure 7. Contours of spatial auto-correlation coefficient of streamwise velocity fluctuations in the plane 0.05$h$ above the bed. Case 5. Contour levels are 0.3, 0.5, and 0.7; the position of the center of the correlation is shown in Figure 5(a). Streamlines show the flow direction tangential to the plane. (a,d,g) at $(x - x_s)/h \approx 1.75$, (b) at $(x - x_s)/h = 5.0$, (e,h) at $(x - x_s)/h \approx 4.5$, and (c,f,i) at $(x - x_s)/h \approx 10.0$.

of the mean flow streamlines; in the node plane (Figure 7(f)) they are inclined (the tip is tilted towards the lobe plane) following the mean-flow streamlines.

Figure 8 shows contours of the joint probability density functions of $u'$ and $v'$ for Case 5. The dashed lines represent the inclination of the bed, and the direction normal to it (the dashed lines do not appear normal to each other because the $u'$ and $v'$ scales are different) and separate transport towards the wall (below and to the left of the line) from that away from it. Thus, events with $v' > 0$ may actually represent wall-ward fluctuations. The quadrant partition relative to the bed is indicated in Figure 8(a) for the lee-side (where the flow is directed upwards and to the left, causing the quadrant ordering to be opposite to the usual one) and stoss-side locations. Over the lee side, bed-parallel events are dominant (Figures 8(a,d,g)), with a predominance of wall-ward transport (the events below and to the left of the dashed line in the figure). This, taken together with the correlation data in Figures 7(a,d,g), indicates that the rollers (Region 1 in Figure 3) generated at the crest leave their footprints on the lee side of the dune.

The rollers are stronger in the lobe region; this is shown by the wider range of bed-
parallel fluctuations observed in this region (Figure 8(g)). Over the lee side of the saddle plane (Figure 8(c)) turbulence events are well organized but weak. In all cases Q4 events are dominant, as is the case near the wall in boundary layers. Despite the fact that the flow is separated over the lee side, the vigorous recirculation that results in upward flow over the lee side of the dune resembles in many ways a standard, attached wall-bounded flow.

In the reattachment region (Figures 8(b,e,h)), the bedward Q3 and Q4 events are dominant, reflecting the flow impingement. Stronger sweeps occur over the node plane. Although the mean wall-shear stress is small at the reattachment region, the turbulence may affect the sediment transport significantly: Q1 events may be responsible for initiating sediment transport (McLean et al. 1994), and Q4 events (sweeps) for bedload sediment transport (Nelson et al. 1993). Q4 events are particularly significant in this region. Note that the data provided by LES could be beneficial for the development of sediment transport models that take into account the turbulence structure in addition to the mean wall-shear stress (Nelson et al. 1993; McLean et al. 1994).

On the stoss side of the dune (Figures 8(c,f,i)) we observe a dominance of Q2 and, especially, Q4 events, typical of attached boundary layers (Ong & Wallace 1998). These
characteristics of the near-bed events are consistent for all the cases studied; the near-wall turbulence appears to be primarily affected by the crestline shape, and rather insensitive to the alignment.

The frequency spectra of the pressure fluctuations in the lobe and the saddle planes of Cases 5 and 11 are illustrated in Figure 9. The Strouhal number is defined as $St = f h / U_b$ ($U_b$ is the bulk velocity at the streamwise location where the channel height is equal to the mean channel height). Time series of pressure fluctuations are also shown in Figures 9(a,c). The spectra in the saddle plane have a low-frequency peak due to the flapping of the separated shear-layer, typical of the reattachment region of flows with separation, such as backward facing steps (Eaton & Johnston 1982; Driver et al. 1987; Dejoan & Leschziner 2004; Aider & Danet 2006); $St = 0.011$ for the in-phase alignment, 0.021 for the staggered case. The state of the boundary layer approaching the crest may play a role in this difference, in that in the staggered case, the boundary layer approaching the saddle plane is coming from the upstream lobe. However, in the lobe region, turbulence is more vigorous than in the saddle area, and also the peaks are farther away from the wall (Omidyeganeh & Piomelli 2013). Aider & Danet (2006) observed that the flapping frequency at the reattachment region in backward-facing step simulations was lower when the flow approaching the step was less perturbed. In the lobe region, the peak occurs at a higher frequency ($St = 0.079$ for the in-phase alignment and $St = 0.072$ for the staggered one), less sensitive to the crestline alignment. The time-scale of this event is indicated by $TL1$ and $TL2$ in the corresponding time-series (Figures 9(a,c)). These events are correlated with the passage of large-scale vortices advected from the separated shear-layer; we will discuss this later. Second peaks in the spectra near the saddle are weaker and have smaller frequency than the corresponding ones near the lobe; their time-scales are $TS2$ and $TS4$ in the figure.
We also note that in the lobe region the flapping frequency is absent (Figures 9(b,d)). This may be due to the near-bed behaviour of the flow there: low-momentum fluid converges on the lobe plane from the sides and inhibits reattachment on the bed; this phenomenon results into a focal saddle point of separation on the bed over the lobe plane and discussed in Omidyeganeh & Piomelli (2013). The effective isolation of the near bed region from the separated shear layer thus may be the reason why the flapping frequency is not observed at the wall here.

The shedding frequencies in the current simulations are close to those reported in the literature. In the backward-facing step, for instance, the dominant frequency was between $St \approx 0.06$ (Le et al. 1997) and $0.066 < St < 0.08$ (Eaton & Johnston 1982). Aider & Danet (2006) found the flapping frequency as well as the shedding frequency at $St = 0.064$ and $0.102$, respectively. In the simulations over the two-dimensional dunes, similar shedding frequencies have been observed ($St = 0.078$ by Grigoriadis et al. (2009), and $St = 0.065$ by Omidyeganeh & Piomelli (2011)). The shedding frequency is also in the range of the measurements by Venditti & Bauer (2005) as well as the range proposed by Jackson (1976), $St = 0.04 - 0.11$.

Coherent structures are shown in Figure 10 for the in-phase crestline alignment, Case 5, and in Figure 11 for the staggered crestline alignment, Case 11. Only half of the
channel width is shown in the figures. Four instants from the time-series in Figures 9(a,c) are chosen to discuss the features of energetic events observed in the pressure spectra in Figures 9(b,d). In both alignments, rollers are generated at the crest of the lobe plane; they extend from one node to the next; their width is, therefore, comparable to the channel depth. Rollers with comparable scale and strength (negative pressure fluctuation) rarely appear in the shear layer near the saddle. This may be due to the approaching flow at the crest of the saddle plane which has much smaller deceleration (Figure 12 in Omidyeganeh & Piomelli (2013)) than in the lobe plane; low-speed fluid over the lobe with higher deceleration enhances the generation of large-scale rollers. Note that isosurfaces of Q show small-scale rollers over the saddle in Figures 10 and 11.

The mean flow induced by the streamwise vortices in the lobe plane lifts the structures towards the free surface. Negative peaks in the time series of pressure fluctuations at the reattachment region of the lobe plane (Figures 9(a,c)) correspond to the passage of the large-scale rollers shown in Figures 10(a,b) and 11(a,b), while the energetic events that occur in the saddle plane (Figures 9(a,c)) correspond to the passage of large-scale rollers generated over the lobe, rather than the saddle. Both realizations in Figures 10(c,d) and 11(c,d)) show rollers advected downstream of the lobe plane for the in-phase and the staggered crestline alignments. The vortex shedding over the saddle caused by the events
over the lobe results in a lower shedding frequency of structures ($S_2$ and $S_4$ in Figures 9(b,d)).

3.2. Separated shear-layer turbulence

In the previous section, we examined the characteristics of wall turbulence and connected the events in the reattachment region to the large-scale separated vortices at the crest. As discussed in the context of Figures 10 and 11, rollers are generated at the crest due to the Kelvin-Helmholtz instability of the separated shear-layer; near the lobe they are more coherent, as shown by the $p'$ isosurfaces; these structures are advected downstream, undergo instability and rise up over the lobe. Near the saddle, the separated vortices do not appear as spatially coherent, but can still be visualized by the $Q$ isosurfaces; they are advected downstream and towards the bed to the reattachment region. Large-scale rollers over the lobe affect the separation bubble over the saddle; we observed a peak in the frequency spectrum of the pressure fluctuations over the saddle corresponding to the events over the lobe.

The main source of turbulent energy is the separated shear-layer, with its inflectional
velocity profile, which is instrumental in generating large-scale vortical structures due to the Kelvin-Helmholtz instability; these eddies are then advected towards the bed, or rise towards the free surface, while undergoing complex interactions with surrounding structures and with the mean flow. The importance of these coherent structures in the transport of sediment has been discussed in the literature (Schmeeckle et al. 1999; Venditti & Bennett 2000; Best 2005a). However the instantaneous characteristics of these eddies have not been studied yet.

The mean upwash and downwash caused by the streamwise vortices over the lobe and the saddle planes affect the dynamics of coherent structures in the bulk flow significantly. The separated shear-layer in the lobe plane (Figures 12(a,b)) affects the whole channel depth and the structures generated in this layer reach the free surface; in the saddle plane, on the other hand, (Figures 12(c,d)) the wake region behind the shear layer stays close to the bed and rarely a large-scale structure reaches the free-surface. The downwash of the mean streamwise vortices on the saddle plane (especially strong in the in-phase alignment), inhibits generation of large-scale rollers (refer to Figures 10 and 11) and prevents their upwards motion, advecting them towards the bed instead. The upwash generated in the lobe plane, on the other hand, advects structures toward the free surface. Since, in the staggered alignment, each saddle is followed by a lobe, eddies advected from the upstream lobe plane appear close the free surface even in the plane of the saddle (Figure 12(d)). In the in-phase alignment, on the other hand, the streamwise vortices are amplified as they extend from one dune to the next. For this reason, we rarely observe strong events at the surface in their downwash region.

The significant difference between the dynamics of coherent structures in the lobe and the saddle planes can be quantified by considering the probability-density function of spanwise eddies, using the technique proposed by Kida & Miura (1998) to identify spanwise vortices. This technique extracts the low-pressure vortices with swirling motion and demarcates the core region around the central axis of vortices. With the added condition that the pressure fluctuation is also negative, these criteria help to identify the centre of the large vortical structures in the shear layer. Figure 13 shows that most of the structures appear in the separated shear-layer, and have negative vorticity (clockwise rotation). In the lobe plane (Figures 13(a,b)) the most probable path of structures in the separated shear-layer is toward the free surface, while in the saddle plane (Figures 13(c,d)) the eddies remain close to the bed and do not reach the free surface. This is consistent with the observations based on instantaneous flow fields above, and justified by the effect of the large streamwise vortices. A significant difference between in-phase and staggered alignments is that when the crestlines are aligned, once the large eddies reach the surface, they persist for long times. In the staggered arrangement, on the other hand, they are more quickly dissipated as the upwash region due to the streamwise vortices is replaced by a downwash one. Compared with the 2D dune case, the crestline curvature primarily directs high-energy vortical structures generated at the crest of the lobe planes toward the free surface; alignment of the crestline, on the other hand, affects the distribution of the structures in the flow and at the surface.

3.3. Boil events

The evolution of vortical structures and their impact at the free surface is shown in Figures 14 through 16. Since the strongest rollers are generated over the lobe plane and the most probable path to the free surface is on this plane (Figure 13) these figures highlight the neighbourhood of the lobe for clarity. An equispaced series of visualizations is shown, starting from the time in which a vortex loop is passing the separation bubble. The roller deforms into a horseshoe like structure (Figures 14(a-c)) and is advected
downstream and toward the free surface. The horseshoe vortex loses energy, as shown by the fact that the pressure fluctuation decreases in magnitude (Figure 14). The $Q$ isosurfaces show a distribution of smaller structures near the horseshoe vortex.

Figure 15 shows the further evolution of the structure; the levels of pressure fluctuation and $Q$ are decreased to follow the later stages of the development, and the field of view concentrates on the stoss side. The vortex is stretched in the streamwise direction whilst is being advected downstream due to the mean-flow acceleration over the stoss side, and it is tilted towards to an inclined position by the mean velocity-gradient. The horseshoe vortex reach the surface near the crestline of the downstream dune (Figure 15(h)). The entire flow field at this time is shown in Figure 16, together with a detail illustrating of the flow field induced by this vortex at the surface. The strong ejection that occurs behind the horseshoe head and between its legs causes the impingement of a nearly circular jet on the surface, made visible by the divergence of velocity-fluctuation vectors, similar to what was observed for 2D dunes (Omidyeganeh & Piomelli 2011). This impingement causes...

Figure 14. Instantaneous flow visualization around the lobe plane \( (0.0 \leq z/h \leq 4.0) \) for Case 5 (in-phase crestline alignment) at 8 instants in time between (a) \( tU_b/h = 156 \) and (h) \( tU_b/h = 164 \). Isosurfaces of pressure fluctuations \( p'/pU_b^2 = -0.076 \) are coloured by the distance from the bed with rainbow colormap and isosurfaces of the second invariant of the velocity tensor, \( Qh^2/U_b^2 = 7.6 \), are coloured by the distance from the bed with grayscale colormap.

The upwelling of the surface known as a "boil" (Matthes 1947; Jackson 1976; M"uller & Gyr 1986; Nezu & Nakagawa 1993; Babakaiff & Hickin 1996; Kadota & Nezu 1999; Best et al. 2001; Best 2005a,b).

Figure 17 shows the probability of boil events occurring at the surface, selected by requiring that the planar divergence

\[
\nabla_s \cdot \mathbf{u}' = \frac{\partial u'}{\partial x} + \frac{\partial w'}{\partial z}
\]

be greater than \( 2.0U_b/h \) while the pressure fluctuations are positive. The first noticeable feature is the fact that the probability of horseshoe occurrence is much higher for 3D dunes than in the 2D case. This is due to a more frequent generation of boil-producing eddies in the separated shear-layer; the upwash in the lobe plane transports them towards the free surface. For the in-phase crestline alignment, the probability of strong boils occurring in the lobe plane is much higher than in the saddle plane, and is more uniform than in the 2D case. This may be due to the fact that, in the 2D case, the mean velocity in the region \( 5.0 \leq (x - x_s)/h \leq 10.0 \) is directed downwards, whereas in the lobe region of the 3D dune the upwash of the streamwise vortices tends to advect vortices towards the surface. The staggered alignment of the crestlines alters the distribution of boils; the characteristics of the approaching boundary layer, in particular, affect the boil probability very strongly. Thus, over the crest the probability of boils is higher in the saddle than in the lobe plane; this behaviour is opposite to that of the in-phase alignment, and is due to the fact that the vortices being convected over the saddle were generated near the lobe of the previous dune. Thus, the initial behaviour is reversed between saddle and lobe.
Figure 15. Instantaneous flow visualization around the lobe plane \((0.0 \leq z/h \leq 4.0)\) and over the stoss side \((7.9 \leq (x-x_s)/h \leq 20.0)\) for Case 5 (in-phase crestline alignment) at 8 instants in time between (a) \(tU_b/h = 164\) and (b) 172. Isosurfaces of pressure fluctuations \(p'/\rho U_b^2 = -0.038\) for (a-d) and \(p'/\rho U_b^2 = -0.03\) for (e-h) are coloured by the distance from the bed with rainbow colormap and isosurfaces of the second invariant of the velocity tensor, \(Qh^2/U_b^2 = 3.78\), are coloured by the distance from the bed with grayscle colormap.

(a)

(b)

Figure 16. Instantaneous flow visualization at \(tU_b/h = 172.1\). Isosurfaces of pressure fluctuations \(p'/\rho U_b^2 = -0.03\) are coloured by the distance from the bed with rainbow colormap and isosurfaces of the second invariant of the velocity tensor, \(Qh^2/U_b^2 = 3.8\), are coloured by the distance from the bed with grayscle colormap. (a) Entire flow field; (b) enlargement of the vortex impinging on the surface, and tangent velocity fluctuation vectors at the surface.
since upstream effects are significant. Over the stoss side, on the other hand, the local behaviour becomes dominant, and the probabilities over lobe and saddle approach the behaviour observed in the in-phase case.

4. Conclusions
We performed a study of dunes with sinusoidal crestline shapes. In a previous paper we discussed the mean flow characteristics of such geometries. Here, we concentrate on the effect of geometric three-dimensionality on the turbulent structures. In particular, we examine the near-wall structures, the eddies generated in the separated shear-layer, and the large horseshoe-shaped vortices responsible for the generation of boils (large upwellings at the surface).

The main feature of the mean flow that affects the turbulent structure in 3D dunes, and is responsible for many of the differences between those and 2D dunes, is the presence of large, streamwise vortices. These vortices are generated by the spanwise gradient of the wall pressure, which is directed from the saddle to the lobe, and causes the secondary motion. For crestline wavelengths larger than the channel depth, the secondary motions take the form of a pair of longitudinal counter-rotating vortices, that straddle the lobe plane, causing upwash of slow fluid in the lobe plane, and downwash of high-speed fluid over the saddle plane. The crestline alignments does not change the generation mechanism of the mean secondary motions, but when the crests are aligned the position of the vortices is stabilized, while if they are staggered, in addition to the vortices that straddle the lobe, the remains of the vortex pair generated at the previous dune are still present, although weaker, and straddle the saddle.

Most of the coherent-structure dynamics observed here are very similar to those in 2D geometries. The main effect of crestline three-dimensionality appears as a preferential generation and distribution of the vortical structures, and a different development depending on whether the eddies are in the downwash field of the longitudinal vortices, or in the upwash region. Thus, the main role of the crestline alignment is to either amplify or dampen the development of the eddies through the advection field of the mean longitudinal vortices.

Wall turbulence is primarily affected by the curvature of the crestline rather than by its alignment. Over the lee side, the spanwise oriented rollers generated at the crest are
advected downstream and leave their footprints on the bed; the rollers are more highly correlated in the lobe plane; the spanwise gradient of the streamwise velocity tilt the rollers in the node plane forward on the saddle side. Around the reattachment region, a highly intermittent interaction of separated vortices at the crest with the bed is observed; sweeps are dominant and are stronger over the node plane. An internal boundary layer develops on the stoss side; low- and high-speed streaks appear near the bed and, due to the flow acceleration, become elongated in the streamwise direction. As in the 2D case we observe preferential concentration of low- and high-speed streaks, which appears to be due to the generation of Görtler-like streamwise vortices (and not to the mean secondary motions).

The curvature of the crestline significantly affects the characteristics of the separated vortices and their evolution through the secondary motions; the rollers are stronger over the lobe plane, and have sizes comparable to the channel height. Shedding of the rollers over the lobe occurs at higher frequency than over the saddle plane; the staggered alignment of the crestlines decrease this frequency. The flapping of the separated shear layer results in a peak of the wall-pressure spectrum at a frequency much lower than the shedding frequency, which also depends on the state of the boundary layer approaching the crest: the vigorous turbulence originating in the lobe area results in higher-frequency flapping. In the staggered case, this results in a higher frequency in the saddle plane, since the approaching flow comes from the lobe. Since the mean flow does not reattach on the bed over the lobe plane, the wall is effectively sheltered from the shear layer there, and the flapping behaviour of the separated shear-layer is not observed in the pressure spectra around the reattachment point.

Because of the upwash of the longitudinal vortices, in the lobe plane the separated shear-layer disturbs the whole channel depth; turbulent eddies advected downstream rise towards the surface. In the saddle plane, on the other hand, the coherent structures remain close to the bed as they are advected downstream. The staggered alignment of the crestlines only changes the distribution of the structures in the bulk flow; downstream of a lobe, structures reach the free surface and are dissipated as they approach the saddle plane of the downstream dune. Hence, in the staggered alignment we observe less persistent surface events than in the in-phase one.

The large-scale rollers generated near the lobes undergo 3D instability while being advected downstream and rise up toward the free surface; they become horseshoe-like vortices similar to those observed over 2D dunes. The flow acceleration over the stoss side elongates them, and the mean-velocity gradient tilts them to an inclined orientation with respect to the horizontal direction. When the tip of such a vortex loop reaches the free surface, the ejection of the flow between the horseshoe legs and behind its head causes boil events. The curvature of the crestline increases the appearance of boil events at the surface of the lobe plane, compared with 2D dunes, and decreases the appearance of these events at the surface of the saddle plane. The staggered alignment changes the distribution of their occurrence over the crest of the dune, which follows the characteristic of the upstream dune. Over the saddle plane, boil events over the crest are highly probable as they come from the upstream lobe plane; on the stoss side of the saddle plane, on the other hand, boils advected from the upstream dune are dissipated and new ones are rarely produced.

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